## Matlab, Introduction

## Resources:

1. Matlab Guide D.J.Higan,N.J.Higan, SIAM, 2000.

Intro to Matlab 6.0.
2. Matlab Primer, See web page of course18.354: old Matlab 3, but short and clear introduction.
3. Matlab on Athena (MIT computer services web page).
4. www.mathworks.com, Matlab online documentation:
answers most of the questions.
5. Mastering Matlab 6, D.Hanselman, B.Littlefield,

Prentice Hall 2001, comprehensive tutorial \& reference, good after one of $1,2,3$.
6. Lecture notes: 10.001 web page.

## Main Features of Matlab

$¥$ Matlab = matrix laboratory, matrix oriented.
$¥$ Any variable is an array by default, thus almost no declarations. All variables are by default double.
¥ High level language: (i) quick and easy coding
(ii) lots of tools (Spectral Analysis, Image

Processing, Signal Processing, Financial, Symbolic Math etc.)
(iii) relatively slow
$¥$ All Matlab functions are precompiled.
$¥$ One may add extra functions by creating M-files.

## Main Features of Matlab

$¥$ Translator - interpreter: line after line, no exe files, does not reevaluate old variables (example)

$$
\begin{aligned}
& \gg a=2 \\
& \mathrm{a}= \\
& 2 \\
& \gg b=3 * a \\
& \mathrm{~b}= \\
& \gg a=4 \\
& \text { a = } \\
& 4 \\
& \gg \mathrm{~b} \\
& \mathrm{~b}= \\
& 6 \\
& \text { b } \\
& 6
\end{aligned}
$$

a has been changed, but to has not been reevaluated!

## Comparison with C.

$¥$ Syntax is similar
$¥$ Language structure is similar to C :
-MATLAB supports variables, arrays, structures, subroutines, files
-MATLAB does NOT support pointers and does not require variable declarations

## Matlab, Getting Started

1. Accessing Matlab on Athena:
add matlab
matlab \&
2. Log out: quit or exit

Useful hints and commands:
¥ input: variable_name ->
output: variable_value
$¥$ semicolon atthe end will suppress the output

## Useful Hints \& Commands

$¥$ command history: upper \& lower arrows, also command name guess:
(i) type abc
(ii) hit upp er arrow key -> get th e last command starting from abc
$¥$ format compact - no blank lines in the output format loose - back to default
$¥$ help commandname - info on commmandname

## Workspace Maintenance

```
¥clear all-clears all the memory (workspace)
    clear xyz - removes xyz from the memory
# who - lists all the variables from the workspace
whos - also gives the details
>> who
Your variables are:
ans c1 c2
>> whos
Name Size Bytes Class
ans 1x1 8 double array
c1 1x1
16
c2 2x2
6
\begin{tabular}{lccl} 
Name & Size & Bytes & Class \\
ans & \(1 \times 1\) & 8 & double array \\
c1 & \(1 \times 1\) & 16 & double array (complex) \\
c2 & \(2 x 2\) & 64 & double array (complex)
\end{tabular}
```


## Workspace Maintenance

$¥$ save saves all workspace variables on disk in file matlab.mat
$¥$ save filename x y z - x, y, z are saved in file filename.mat
$¥$ load filename - loads contents of the filename.mat to the workspace
¥ load filename x y z-loads only $\mathrm{x}, \mathrm{y}, \mathrm{z}$ from filename.mat to the workspace
$¥$ Each array requires a continuous chunk of memory; use pack for memory defragmentation.

## Dealing with Matrices

Entering matrices by explicit list of elements:

$$
\left.\begin{array}{lll}
A==\left[\begin{array}{lll}
1 & 2 & 3
\end{array}\right] & A=[1 ; 2 ; 3
\end{array}\right]
$$

$$
A=\left[\begin{array}{lllllllll}
1 & 2 & 3 ; & 5 & 6 ; & 8 & 9
\end{array}\right]
$$

or

$$
A=\left[\begin{array}{llll}
1 & 2 & 3 & \\
& 4 & 5 & 6 \\
& 7 & 8 & 9
\end{array}\right]
$$

Spaces separate the elements, semicolons and new line symbols separate the rows.

## Dealing with Matrices

Complex matrices:
either $A=[12 ; 34]+i *[56 ; 7$ 8]
or $A=[1+5 i$ 2+6i; 3+7i 4+8i]
No blank spaces, i or j stands for imaginary one .
Matrix and array operations.
$\left.\begin{array}{l}+ \\ - \\ \star \\ \star\end{array}\right\}$ element-wise (array operation $\begin{aligned} & \text { array or matrix operations }\end{aligned}$ conjugate transpose
\ left division
/ right division
only matrix operations

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## Dealing with Matrices, Examples

```
> \(C=A+B ;\)
\(C(k, l)=A(k, l)+B(k, l)\)
>> C = A*B;
\(C(k, l)=A(k, m) * B(m, l)\)
>> \(\mathrm{C}=\mathrm{A} . * \mathrm{~B}\)
\(C(k, l)=A(k, l) * B(k, l) \quad\) Element-wise (array)
operation
>> C = A^alpha;
>> C = A.^alpha;
\(C(k, l)=A(k, l)^{\wedge} a l p h a\)
```

Matrix multiplication, summation over the repeating index is implied.

Element-wise (array) operation

## Dealing with Matrices

Conjugate transpose: swaps the indices and changes the sign of imaginary part of each element.
$\mathrm{C}=\mathrm{A}$
$C(i, j)=\operatorname{real}(A(j, i))-i * \operatorname{imag}(A(j, i))$
$\mathrm{x}=\mathrm{A} \backslash \mathrm{b}$ (left) $\mathrm{A} * \mathrm{x}=\mathrm{b} \quad \mathrm{A}$-square matrix, b -column vector
$\mathrm{x}=\mathrm{b} / \mathrm{A}$ (right) $\mathrm{x} * \mathrm{~A}=\mathrm{b}$
Colon notation: used to construct vectors of equally spaced elements:

$$
\begin{aligned}
& \gg a=1: 6 \\
& a= \\
& 123456
\end{aligned}
$$

$$
\begin{aligned}
& \gg b=1: 2: 7 \\
& b= \\
& 1357
\end{aligned}
$$

## Dealing with Matrices

Submatrices:
A (1:4,3) - column vector, first 4 elements of the 3-d column of A. A $(:, 3)$ - the 3-d column of A
A $\left.\left(:, \begin{array}{ll}2 & 4\end{array}\right]\right)-2$ columns of A: 2 -d \& 4-th.

Standard math. functions of matrices operate in array sense: $\exp (A), \sin (A), \operatorname{sqrt}(A)=A .{ }^{\wedge} 0.5$
>> $\mathrm{B}=\exp (\mathrm{A})$
$B(i, j)=\exp (A(i, j))$

## Relational \& Logical Operators \& Functions

True: non-zero, false: zero.
Relational: <, <=, >, >=, ==, ~=.
Operate on matrices in elementwise fashion:
>> $A=1: 9, B=9-A$
$\mathrm{A}=1 \begin{array}{llllllll}1 & 2 & 4 & 5 & 6 & 7 & 9\end{array}$
$B=\begin{array}{lllllllll}7 & 6 & 5 & 4 & 3 & 2 & 1 & 0\end{array}$
>> $\mathrm{tf}=\mathrm{A}>4$
$t f=0 \quad 0 \quad 0 \quad 0 \quad 1 \quad 111111$
>> $t f=(A==B)$
000000000

## Relational \& Logical Operators \& Functions

Logical: \& AND; | OR; ~ NOT.
>>tf $=\sim(A>4)$
$t f=111100000$
$\gg t f=(A>2) \&(A<6)$
$t f=0011110000$
Functions: $x$ or $(x, y)$ - exclusive OR, true if either $x$ or $y$ is non-zero, false of both are true or false.
isempty - true for empty matrix
isreal, isequal, isfinite,...

## Flow of Control

For loops. Syntax:
for $\mathrm{x}=$ array
(commands)
end
Example:
>> for $n=1: 10$

$$
\mathrm{x}(\mathrm{n})=\sin (\mathrm{n} * \mathrm{pi} / 10) ;
$$

end

## Flow of Control

Nested loops, decrement loop.
>> for $\mathrm{n}=1: 5$
for $m=5:-1: 1$
$A(n, m)=n^{\wedge} 2+m^{\wedge} 2$;
end
end
Alternative: vectorized solution, much faster: assigns memory for $x$ only once.

$$
\begin{aligned}
& \gg \mathrm{n}=1: 10 ; \\
& \gg \mathrm{x}=\sin (\mathrm{n} * \mathrm{pi} / 10)
\end{aligned}
$$

## Flow of Control

## While loops. Syntax:

while expression
(commands)
end
(commands) will be executed as long as all the elements of expression are true.

Example: search for the smallest number EPS which if added to 1 will give the result greater than 1.

## Flow of Control

>> num $=0 ;$ EPS = 1;
>> while (1+EPS) >1

$$
\begin{aligned}
& \qquad \begin{array}{l}
\mathrm{EPS}=\mathrm{EPS} / 2 ; \\
\text { num }=\text { num }+1 ;
\end{array} \\
& \text { end }
\end{aligned}
$$

>> num
num $=53$
>> EPS = 2*EPS
$\operatorname{EPS}=2.2204 \mathrm{e}-16$

## Flow of Control

If-Else-End constructions. Syntax:
if expression1
(commands1: if expr-n1 is true)
elseif expression2
(commands2: if expr-n2 is true)
elseif expression3
(commands3: if expr-n3 is true)
else
(commands: if $1,2, \ldots, n$ are false)
end
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## Flow of Control

> Breaking out of the loop:
> $\gg \operatorname{EPS}=1 ;$
> $\gg$ for num $=1: 1000$
> $\operatorname{EPS}=\operatorname{EPS} / 2 ;$
> $\operatorname{if}(1+\mathrm{EPS})<+1$
> $\operatorname{EPS}=\operatorname{EPS} * 2$
> break
> end
$E P S=2.2204 e-16$

## M-files

Script files \& Function files
Script files: contain a set of Matlab commands - programs. To execute the file: enter the file name.

```
% script M-file example.m
erasers = 4; pads = 6; tape = 2;
items = erasers + pads + tape
cost = erasers*25 + pads*52 + tape*99
average_cost = cost/items
>>example
items = 12
cost = 610
average_cost = 50.833
```


## M-files

Interpreter actions while processing example statement:

1. Is example a current Matlab variable?
2. Is example a built-in Matlab command?
3. Is Example an M-file?
4. Opens the file and evaluates commands as if they were entered from the command line.

Thus: (i) all workspace variables are accessible to the commands form the M-file.
(ii) all variables created by M-file become a part of the work space.

## M-files

## Function files

$¥$ Analogous to functions in C.
$¥$ Communicate with the workspace only through variables passed to it and the output variables it creates. All internal variables are invisible to the workspace.
$¥ \mathrm{M}$-files name $=$ functions name.
$¥$ The first line - function-declaration line


## Function M-files

function $s=\operatorname{area}(a, b, a l p h a)$
\%AREA calculates triangles area given 2 side $\mathrm{s} \&$ angle between them $\%$ AREA reads in two sides of thel riangle and the angle between them $\%$ (in radians) and returns the area of the triangle.
if $a<0 \mid b<0$

error(a and b ca n not be negative.) end
$\mathrm{s}=\mathrm{a}$ * ${ }^{*} \sin ($ alpha) $/ 2$;
searched and displayed by the help command

## Function M-files

$¥$ Function M-files may call script files, the script file being evaluated in the workspace.
$¥$ F. M-files can have zero input and output arguments.
$¥$ Functions may share variables. The variable must be declared as global in each desired workspace.
$¥$

