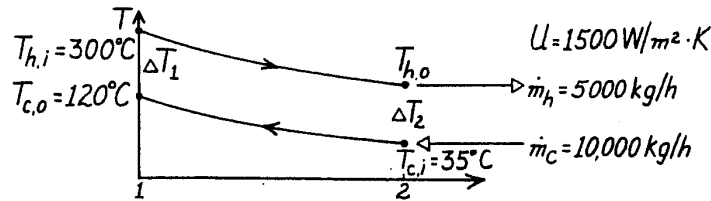


PROBLEM 11.10

KNOWN: A shell and tube HXer (two shells, four tube passes) heats 10,000 kg/h of pressurized water from 35 °C to 120 °C with 5,000 kg/h water entering at 300 °C.

FIND: Required heat transfer area, A_s .

SCHEMATIC:



ASSUMPTIONS: (1) Negligible heat loss to surroundings, (2) Negligible kinetic and potential energy changes, (3) Constant properties.

PROPERTIES: Table A-6, Water ($\bar{T}_c = 350\text{K}$): $c_p = 4195 \text{ J/kg}\cdot\text{K}$; Table A-6, Water (Assume $T_{h,o} \approx 150^\circ\text{C}$, $\bar{T}_h \approx 500\text{K}$): $c_p = 4660 \text{ J/kg}\cdot\text{K}$.

ANALYSIS: The rate equation, Eq. 11.14, can be written in the form

$$A_s = q/U \Delta T_{\ell m} \quad (1)$$

and from Eq. 11.18,

$$\Delta T_{\ell m} = F \Delta T_{\ell m, CF} \quad \text{where} \quad \Delta T_{\ell m, CF} = \frac{\Delta T_1 - \Delta T_2}{\ln \Delta T_1 / \Delta T_2} \quad (2,3)$$

From an energy balance on the cold fluid, the heat rate is

$$q = \dot{m}_c c_{p,c} (T_{c,o} - T_{c,i}) = \frac{10,000 \text{ kg/h}}{3600 \text{ s/h}} \times 4195 \frac{\text{J}}{\text{kg}\cdot\text{K}} (120 - 35)\text{K} = 9.905 \times 10^5 \text{ W}.$$

From an energy balance on the hot fluid, the outlet temperature is

$$T_{h,o} = T_{h,i} - q/\dot{m}_h c_{p,h} = 300^\circ\text{C} - 9.905 \times 10^5 \text{ W} / \left(\frac{5000 \text{ kg}}{3600 \text{ s}} \times 4660 \frac{\text{J}}{\text{kg}\cdot\text{K}} \right) = 147^\circ\text{C}.$$

From Fig. 11.11, determine F from values of P and R where $P = (120 - 35)^\circ\text{C} / (300 - 35)^\circ\text{C} = 0.32$, $R = (300 - 147)^\circ\text{C} / (120 - 35)^\circ\text{C} = 1.8$ giving $F \approx 0.97$. The log mean temperature based upon CF arrangement follows from Eq. (3); find

$$\Delta T_{\ell m} = [(300 - 120) - (147 - 35)]\text{K} / \ln \frac{(300 - 120)}{(147 - 35)} = 143.3\text{K}.$$

$$A_s = 9.905 \times 10^5 \text{ W} / 1500 \text{ W/m}^2\cdot\text{K} \times 0.97 \times 143.3\text{K} = 4.75 \text{ m}^2. \quad \triangleleft$$

COMMENTS: (1) Check $\bar{T}_h \approx 500\text{K}$ used in property determination; $\bar{T}_h = (300 + 147)^\circ\text{C} / 2 = 497\text{K}$. (2) Using the NTU- ϵ method, determine first the capacity rate ratio, $C_{\min}/C_{\max} = 0.56$. Then

$$\epsilon \equiv \frac{q}{q_{\max}} = \frac{C_{\max} (T_{c,o} - T_{c,i})}{C_{\min} (T_{h,i} - T_{c,i})} = \frac{1}{0.56} \times \frac{(120 - 35)^\circ\text{C}}{(300 - 35)^\circ\text{C}} = 0.57.$$

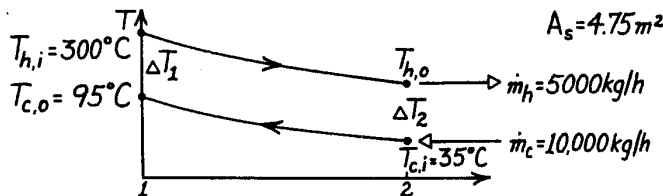
From Fig. 11.17, find that $\text{NTU} = AU/C_{\min} \approx 1.1$ giving $A_s = 4.7 \text{ m}^2$.

PROBLEM 11.11

KNOWN: The shell and tube HXer (two shells, four tube passes) of Problem 11.10, known to have an area 4.75m^2 , provides 95°C water at the cold outlet (rather than 120°C) after several years of operation. Flow rates and inlet temperatures of the fluids remain the same.

FIND: The fouling factor, R_f .

SCHEMATIC:



ASSUMPTIONS: (1) Negligible heat loss to surroundings, (2) Negligible kinetic and potential energy changes, (3) Constant properties, (4) Thermal resistance for the clean condition is $R_f'' = (1500\text{W}/\text{m}^2\cdot\text{K})^{-1}$.

PROPERTIES: Table A-6, Water ($\bar{T}_c \approx 338\text{K}$): $c_p = 4187\text{J}/\text{kg}\cdot\text{K}$; Table A-6, Water (Assume $T_{h,o} \approx 190^\circ\text{C}$, $\bar{T}_h \approx 520\text{K}$): $c_p = 4840\text{J}/\text{kg}\cdot\text{K}$.

ANALYSIS: The overall heat transfer coefficient can be expressed as

$$U = 1/(R_f'' + R_f'') \quad \text{or} \quad R_f'' = 1/U - R_f'' \quad (1)$$

where R_f'' is the thermal resistance for the clean condition and R_f'' , the fouling factor, represents the additional resistance due to fouling of the surface. The rate equation, Eq. 11.14 with Eq. 11.18, has the form,

$$U = q/A_s F \Delta T_{m,CF} \quad \Delta T_{m,CF} = (\Delta T_1 - \Delta T_2)/\ln(\Delta T_1/\Delta T_2). \quad (2)$$

From energy balances on the cold and hot fluids, find

$$q = \dot{m}_c c_{p,c} (T_{c,o} - T_{c,i}) = (10,000/3600\text{ kg/s}) 4187\text{ J/kg}\cdot\text{K} (95 - 35)\text{K} = 6.978 \times 10^5\text{ W}$$

$$T_{h,o} = T_{h,i} - q/\dot{m}_h c_{p,h} = 300^\circ\text{C} - 6.978 \times 10^5\text{ W} / (5000/3600\text{ kg/s} \times 4840\text{ J/kg}\cdot\text{K}) = 196.2^\circ\text{C}.$$

The factor, F , follows from values of P and R as given by Fig. 11.11 with

$$P = (95 - 35)/(300 - 35) = 0.23 \quad R = (300 - 196)/(120 - 35) = 1.22$$

giving $F \approx 1$. Based upon CF arrangement,

$$\Delta T_{m,CF} = [(300 - 95) - (196 - 35)]^\circ\text{C} / \ln[(300 - 95)/(196 - 35)] = 182\text{K}.$$

Using Eq. (2), find now the overall heat transfer coefficient as

$$U = 6.978 \times 10^5\text{ W} / 4.75\text{m}^2 \times 1 \times 182\text{K} = 806\text{ W}/\text{m}^2\cdot\text{K}.$$

From Eq. (1), the fouling factor is

$$R_f'' = \frac{1}{806\text{ W}/\text{m}^2\cdot\text{K}} - \frac{1}{1500\text{ W}/\text{m}^2\cdot\text{K}} = 5.74 \times 10^{-4}\text{ m}^2\cdot\text{K}/\text{W}.$$

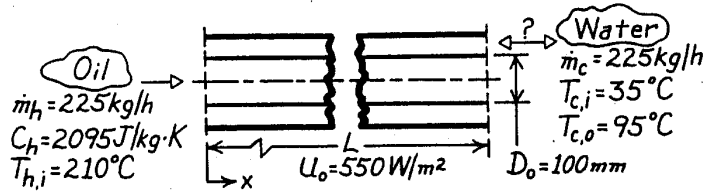
COMMENTS: Note that the effect of fouling is to nearly double ($U_{\text{clean}}/U_{\text{fouled}} = 1500/806 \approx 1.9$) the resistance to heat transfer. Note also the assumption for $T_{h,o}$ used for property evaluation is satisfactory.

PROBLEM 11.29

KNOWN: Concentric tube heat exchanger.

FIND: Length of the exchanger.

SCHEMATIC:



ASSUMPTIONS: (1) Negligible heat loss to surroundings, (2) Negligible kinetic and potential energy changes, (3) Constant properties.

PROPERTIES: Table A-6, Water ($\bar{T}_c = (35+95)^\circ\text{C}/2 = 338\text{K}$): $c_{p,c} = 4188\text{ J/kg}\cdot\text{K}$.

ANALYSIS: From the rate equation, Eq. 11.14, with $A_o = \pi D_o L$,

$$L = q / U_o \pi D_o \Delta T_{\ell m}.$$

The heat rate, q , can be evaluated from an energy balance on the cold fluid,

$$q = \dot{m}_c c_c (T_{c,o} - T_{c,i}) = \frac{225\text{ kg/h}}{3600\text{ s/h}} \times 4188\text{ J/kg}\cdot\text{K} (95 - 35)\text{K} = 15,705\text{ W}.$$

In order to evaluate $\Delta T_{\ell m}$, we need to know whether the exchanger is operating in CF or PF. From an energy balance on the hot fluid, find

$$T_{h,o} = T_{h,i} - q / \dot{m}_h c_h = 210^\circ\text{C} - 15,705\text{ W} / \frac{225\text{ kg/h}}{3600\text{ s/h}} \times 2095 \frac{\text{J}}{\text{kg}\cdot\text{K}} = 90.1^\circ\text{C}.$$

Since $T_{h,o} < T_{c,o}$ it follows that HXer operation must be CF. From Eq. 11.15,

$$\Delta T_{\ell m, CF} = \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1 / \Delta T_2)} = \frac{(210 - 95) - (90.1 - 35)}{\ln(115 / 55.1)}^\circ\text{C} = 81.4^\circ\text{C}.$$

Substituting numerical values, the HXer length is

$$L = 15,705\text{ W} / 550\text{ W/m}^2 \cdot \text{K} \pi (0.10\text{ m}) \times 81.4\text{ K} = 1.12\text{ m}.$$

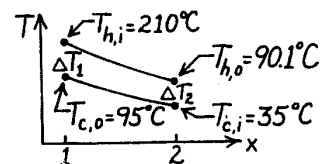
COMMENTS: The ϵ -NTU method could also be used. It would be necessary to perform the hot fluid energy balance to determine CF operation existed. The capacity rate ratio is $C_{\min} / C_{\max} = 0.50$. From Eqs. 11.19 and 11.20 with q evaluated from an energy balance on the hot fluid,

$$\epsilon = \frac{T_{h,i} - T_{h,o}}{T_{h,i} - T_{c,i}} = \frac{210 - 90.1}{210 - 35} = 0.69.$$

From Fig. 11.15, find $\text{NTU} \approx 1.5$ giving

$$L = \text{NTU} \cdot C_{\min} / U_o \pi D_o \approx 1.5 \times 130.94 \frac{\text{W}}{\text{K}} / 550 \frac{\text{W}}{\text{m}^2 \cdot \text{K}} \cdot \pi (0.10\text{ m}) \approx 1.14\text{ m}.$$

Note the good agreement by both methods.

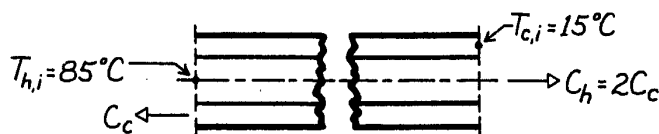


PROBLEM 11.31

KNOWN: A very long, concentric tube heat exchanger having hot and cold water inlet temperatures, 85°C and 15°C , respectively; flow rate of hot water is twice that of the cold water.

FIND: Outlet temperatures for counterflow and parallel flow operation.

SCHEMATIC:



ASSUMPTIONS: (1) Equivalent hot and cold water specific heats, (2) Negligible kinetic and potential energy changes, (3) No heat loss to surroundings.

ANALYSIS: The heat rate for a concentric tube heat exchanger with very large surface area operating in the counterflow mode is

$$q = q_{\max} = C_{\min} (T_{h,i} - T_{c,i})$$

where $C_{\min} = C_c$. From an energy balance on the hot fluid,

$$q = C_h (T_{h,i} - T_{h,o})$$

Combining the above relation and rearranging, find

$$T_{h,o} = -\frac{C_{\min}}{C_h} (T_{h,i} - T_{c,i}) + T_{h,i} = -\frac{C_c}{C_h} (T_{h,i} - T_{c,i}) + T_{h,i}$$

Substituting numerical values,

$$T_{h,o} = -\frac{1}{2} (85 - 15)^\circ\text{C} + 85^\circ\text{C} = 50^\circ\text{C}$$

For parallel flow operation, the hot and cold outlet temperatures will be equal; that is, $T_{c,o} = T_{h,o}$. Hence,

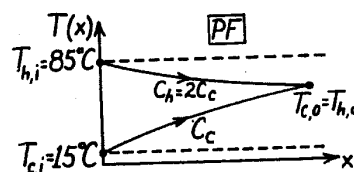
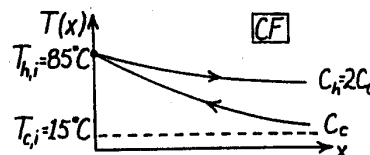
$$C_c (T_{c,o} - T_{c,i}) = C_h (T_{h,i} - T_{h,o})$$

Setting $T_{c,o} = T_{h,o}$ and rearranging,

$$T_{h,o} = \left[T_{h,i} + \frac{C_c}{C_h} T_{c,i} \right] / \left[1 + \frac{C_c}{C_h} \right]$$

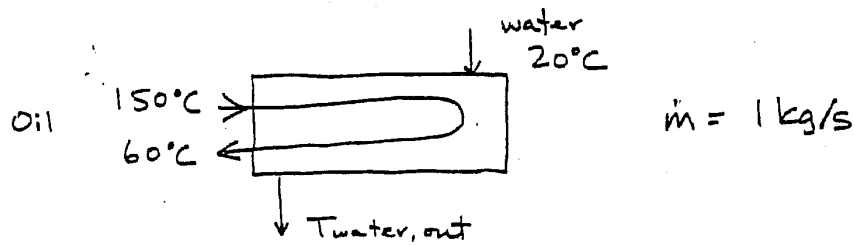
$$T_{h,o} = \left[85 + \frac{1}{2} \times 15 \right]^\circ\text{C} / \left[1 + \frac{1}{2} \right] = 61.7^\circ\text{C}$$

COMMENTS: Note that while $\epsilon = 1$ for CF operation, for PF operation find $\epsilon = q/q_{\max} = 0.67$.



Part C

a)



Calculate $T_{\text{water, out}}$ by overall energy balance

$$(\dot{m} C_p)_{\text{oil}} (T_{\text{oil, in}} - T_{\text{oil, out}}) = (\dot{m} C_p)_{\text{water}} (T_{\text{water, out}} - T_{\text{water, in}})$$

$$\frac{2120 \text{ J/kg} \cdot \text{K} (150^\circ\text{C} - 60^\circ\text{C})}{4190 \text{ J/kg} \cdot \text{K}} + 20^\circ\text{C} = T_{\text{water, out}} = \underline{65.5}$$

Calculate overall heat transfer coefficient based on outside area (U_o)

$$\frac{1}{U_o A_o} = \frac{1}{h_o A_o} + \frac{\ln D_o/D_i}{2\pi K L} + \frac{1}{h_i A_i}$$

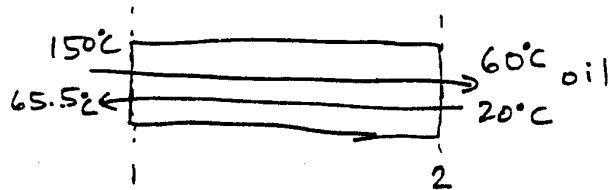
$$U_o = \left(\frac{1}{h_o} + \frac{D_o \ln D_o/D_i}{2k} + \frac{D_o}{h_i D_i} \right)^{-1}$$

$$\underbrace{1 \times 10^{-3}}_{\text{can neglect}} \quad \underbrace{\frac{D_o \ln D_o/D_i}{2k}}_{\substack{\text{of stainless steel} \\ \text{tube} \\ -7.2 \times 10^{-5} \\ \text{can neglect}}} \quad \underbrace{3.8 \times 10^{-3}}_{\text{can neglect}}$$

$$\underline{U_o = 203 \text{ W/m}^2\text{K}}$$

by LMTD method,

$$q = UAF\Delta T_{lm} \rightarrow \text{countercurrent}$$



$$\Delta T_1 = 84.5^\circ\text{C}$$

$$\Delta T_2 = 40$$

$$\Delta T_{lm} = \frac{\Delta T_1 - \Delta T_2}{\ln \frac{\Delta T_1}{\Delta T_2}} = 59.5$$

Find F for 1-2 shell tube exchanger using Figure 11.10 in I&D.

$$R = \frac{20 - 65.5^\circ\text{C}}{60 - 150^\circ\text{C}} \approx 0.51 \quad P = \frac{60 - 150^\circ\text{C}}{20 - 150^\circ\text{C}} \approx 0.70$$

$$\rightarrow F \approx 0.75$$

Find Exchanger Area

$$q = \dot{m}C_p\Delta T = U_o A_o F \Delta T_{lm}$$

$$\rightarrow A_o = \frac{\dot{m}C_p\Delta T}{U_o F \Delta T_{lm}}$$

$$\frac{(1 \text{ kg/s})(2120 \text{ J/kg}\cdot\text{K})(90^\circ\text{C})}{(203 \text{ W/m}^2\cdot\text{K})(0.75)(59.5^\circ\text{C})} = \boxed{21 \text{ m}^2 = A_o}$$

or by ϵ -NTU method,

$$\text{Oil is } C_{min} \quad \text{and} \quad C_r = \frac{C_{min}}{C_{max}} = \frac{(1)(2120)}{(1)(4190)} = 0.506$$

$$\epsilon = \frac{C_{oil} \Delta T_{oil}}{C_{oil} (T_{oil,in} - T_{water,in})} = \frac{150 - 60}{150 - 20} = 0.692$$

using Eq 11.31b from Table 11.4,

$$NTU = -(1+C_r^2)^{-1/2} \ln \frac{E-1}{E+1}$$

$$E = \frac{2/\epsilon - (1+C_r)}{(1+C_r^2)^{1/2}} = 1.235$$

$$NTU = 2.01$$

$$NTU = \frac{U_o A_o}{C_{min}} = 2.01 \rightarrow A_o = \frac{(2.01)(2120)(1)}{(203)} = \boxed{21 \text{ m}^2}$$

- b) (15 points)
Goo will change U_o by adding another layer of heat transfer resistance.

$$(*) U_o = \left(\frac{1}{h_o} + \frac{D_o \ln(D_o/D_i)}{2k_{ss}} + \frac{D_o \ln(D_i/D_{goo})}{2k_{goo}} + \frac{D_o}{D_{goo} h_i} \right)^{-1}$$

where D_{goo} is the inner diameter of the tube with goo.

(D_i is the original, clean, inner diameter of tube)

Given the same A_o from a)
by LMTD method,
Need to find new $T_{water, out}$ using overall energy balance

$$\frac{(2120)(150-80)}{4190} + 20 = 55.4^\circ\text{C}$$

$$U_o = \frac{[mC_p \Delta T]_{oil}}{A_o F \Delta T_{lm, countercurrent}}$$

Recalculate $\Delta T_1, \Delta T_2, \Delta T_{lm}, R, P, F$ as in part a)

$$\Delta T_1 = 94.6^\circ\text{C}$$

$$\Delta T_2 = 60^\circ\text{C} \rightarrow \Delta T_{lm, countercurrent} = 76^\circ\text{C}$$

$$R = 0.51$$

$$P = 0.54 \rightarrow F \approx 0.92$$

$$U_o = \frac{(1)(2190)(150-80)}{(21)(0.92)(76)} = \underline{104.4 \text{ W/m}^2\text{K}}$$

by ϵ -NTU method,

$$C_r = 0.506 \text{ as before}$$

$$\epsilon = \frac{150-80}{150-20} = 0.538$$

$$E = 1.970$$

$$NTU \approx 1 = \frac{U_o A_o}{C_{min}}$$

$$U_o = C_{min}/A_o = \frac{2120}{21} = \underline{101.0 \text{ W/m}^2\text{K}}$$

With U_o , use (*) to find D_{goo} , or goo thickness

$$\text{as } \frac{D_i - D_{goo}}{2} = \delta_{goo}$$

Can solve for D_{g00} by iterating Eq (*) or using various simplifications.

- layers are thin relative to diameter so can approximate as planar

$$U_o = \left(\frac{1}{h_o} + \frac{\delta_{ss} A_o}{k_{ss} A_m} + \frac{\delta_{g00} A_o}{k_{g00} A_i} + \frac{1 A_o}{h_i A_i} \right)^{-1}$$

$\downarrow$
 δ_{ss} thickness of stainless steel $\left(\frac{D_o - D_i}{2} \right)$ so $A_{g00} \sim$
 A_m mean of inner and outer area

Assumed thickness of goo same

$$104 = \left(\frac{1}{1000} + \frac{0.001}{15} \left(\frac{15}{14} \right) + \frac{\delta_{g00}}{0.139} \left(\frac{15}{13} \right) + \frac{1}{300} \left(\frac{15}{13} \right) \right)^{-1}$$

$$\begin{aligned} \delta_{g00} &\cong 5.7 \times 10^{-4} \text{ m} \\ &\cong 0.6 \text{ mm} \end{aligned}$$

Seems reasonable

Additional Notes for Problem 1:

- Oil could have been on shell-side rather than tube-side. Only changes R and P , but F and results remain the same.

The overall heat transfer resistance for the "goo" case could have been expressed as

$$\frac{1}{U_{o,new} A_o} = \frac{1}{U_{o,old} A_o} + R_{f,i}''$$

$$\text{where } R_{f,i}'' = \frac{\ln(D_i/D_{goo})}{2\pi k_{goo} L}$$

Part D: (solution 1)

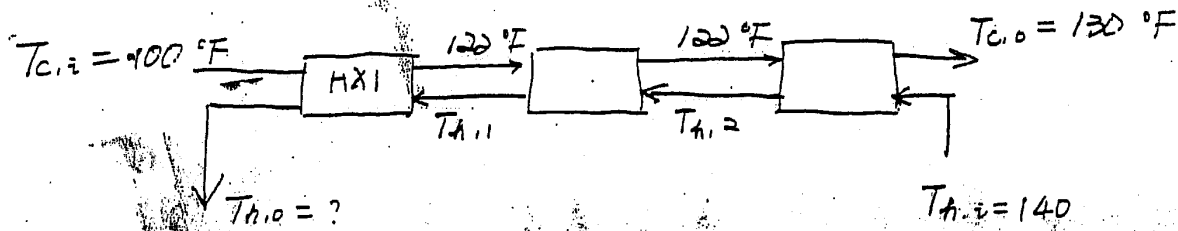
There are several points worth noting in this problem

- i) $T_{c,i} < T_{melt} < T_{c,o}$ for compene, which means we need to divide the HX into three sections. (See figure below)
- ii) Cold stream consists of compene and water. But the solubility in each other is negligible. So the condition leads to:

$$C_{p,c} = x_w C_{p,w} + (1-x_w) C_{p,s}$$

cold stream
water
solid (compene)

- iii) Outlet temperature of hot stream can tell you if CO-CURRENT flow is possible.



(Assume it's counter-current flow for the moment)

Overall energy balance:

$$\begin{aligned} \dot{Q} &= \dot{m}_h C_{p,h} (T_{h,i} - T_{h,o}) = \dot{m}_c C_{p,c,1} (120 - T_{c,i}) \quad \text{HX1} \\ &\quad + \dot{m}_c x_s \Delta H_f \quad \text{HX2} \\ &\quad + \dot{m}_c C_{p,c,3} (T_{c,o} - 120) \quad \text{HX3} \end{aligned}$$

specific heat of cold stream in HX1
Heat of fusion
weight percent of compene

$$C_{p,c1} = C_{p,s} x_s + C_{p,w} x_w = 0.38 \times 0.2 + 1.0 \times 0.8 = 0.876 \text{ Btu/lb. °F}$$

$$C_{p,c3} = 0.44 \times 0.2 + 1.0 \times 0.8 = 0.88 \text{ Btu/lb. °F}$$

From eq. ①, we solve for $T_{h,o}$

$$\text{②} \quad T_{h,o} = T_{h,i} - \frac{\dot{Q}_c}{\dot{m}_h} = 140 - \frac{2.35 \times 10^5}{\dot{m}_h}$$

101) $\dot{m}_h = 9000 \text{ lb/hr}$

$$T_{h,o} = 140 - \frac{2.35 \times 10^5}{9000} = 114^\circ \text{F}$$

Since $T_{h,o} < T_{c,o}$ it is impossible to have co-current flow. Heat cannot be transferred from a colder stream to a hotter one. Only countercurrent flow is OK.

From $q = UA(\text{LMTD})$

$$\Rightarrow A = A_1 + A_2 + A_3 = \frac{1}{U} \left(\frac{q_1}{\text{LMTD}_1} + \frac{q_2}{\text{LMTD}_2} + \frac{q_3}{\text{LMTD}_3} \right)$$

Energy Balance over each HX:

HX1: $q_1 = \dot{m}_h C_{p,h} (T_{h,i} - T_{h,o}) = \dot{m}_c C_{p,c} (122 - T_{c,i}) = 96360 \text{ Btu/hr}$

$$\Rightarrow T_{h,i} = \frac{q_1}{\dot{m}_h C_{p,h}} + T_{h,o}$$

$$= \frac{96360}{9000 \times 1} + 114 = 124.7^\circ \text{F}$$

$$(\text{LMTD})_1 = 6.7^\circ \text{F}$$

HX2: $q_2 = \dot{m}_h C_{p,h} (T_{h,o} - T_{h,i}) = \dot{m}_c X_3 \Delta H_f = 103000 \text{ Btu/hr}$

$$T_{h,o} = \frac{103000}{9000 \times 1} + 124.7 = 136.1^\circ \text{F}$$

$$(\text{LMTD})_2 = 6.9^\circ \text{F}$$

HX3: $q_3 = \dot{m}_c C_{p,c} (136 - 122) = 35040 \text{ Btu/hr}$

$$(\text{LMTD})_3 = 11.9^\circ \text{F}$$

Summarize the above results in a table:

HX	1	2	3
q_i	96360	103000	35040
$(\text{LMTD})_i$	6.7	6.9	11.9
$A_i (\text{ft}^2)$	71.9	74.6	147
A_{total}	161.2		

(2pts)

$$L = \frac{A}{\pi D} = \frac{161.2}{\pi \times 2/12} = 307.9 \text{ ft} \quad (2pts)$$

(b). $\dot{M}_h = 7000 \text{ lb/hr.}$

From eq (2), we can find

(2pts)

$$T_{h,c} = 107^\circ\text{F.}$$

Follow same procedure as in (a), we find

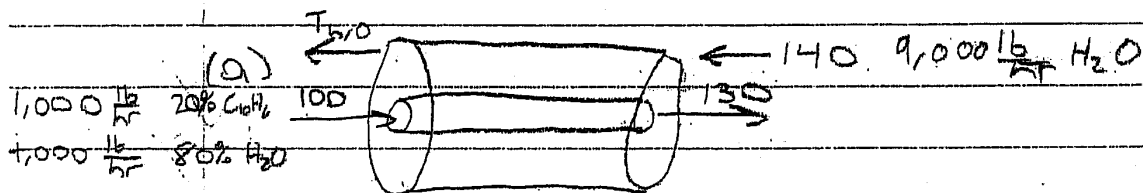
(2pts)

$$T_{h,i} = 121^\circ\text{F} < 122^\circ\text{F}$$

There is a pinch point in HX2; Cannot work.

Part D (Solution 2)

- Assumptions:
- ① Negligible heat loss to the surroundings
 - ② Negligible Potential + Kinetic energy changes
 - ③ Constant properties
 - ④ Fully developed conditions for the H_2O and $C_{10}H_{16}$ (U independent of x)

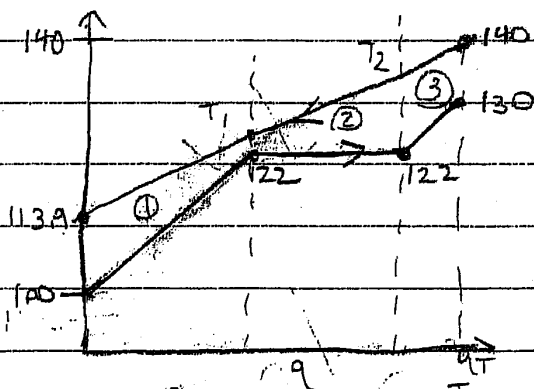


$$q_T = \left[(\dot{m} C_p \Delta T)_{C_{10}H_{16, S}} + (\dot{m} \Delta H_{\text{fusion}})_{C_{10}H_{16}} + (\dot{m} C_p \Delta T)_{C_{10}H_{16, R}} + (\dot{m} C_p \Delta T)_{H_2O} \right] = (\dot{m} C_p \Delta T)_H$$

$$\Rightarrow 1000 (0.38 \times 22 + 103 + 0.8 \times 0.4) + 4,000 (30) = 9,000 (140 - T_{H,O})$$

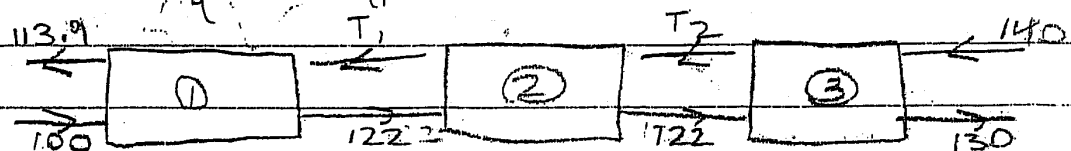
$$\Rightarrow T_{H,O} = 113.9^\circ F$$

$\therefore$ heat exchanger must be counter-current since $T_{H,O} > T_{H,O}$.



To find L , model heat exchanger as 3 separate heat exchangers

$$L = L_1 + L_2 + L_3$$



$$T_1: q_1 = (\dot{m} c_p \Delta T)_{C_{H_2O}} + (\dot{m} c_p \Delta T)_{H_2O} = (\dot{m} c_p \Delta T)_{H_2O}$$

$$= 1000(22 \times 38) + 4000(22) = 9000(T_1 - 113.9)$$

$$\Rightarrow T_1 = 124.6^\circ F$$

$$T_2: q_2 = (\dot{m} \Delta H_{fus}) = (\dot{m} c_p \Delta T)_{H_2O}$$

$$= 1000(103) = 9000(T_2 - 124.6) \Rightarrow T_2 = 136.1^\circ F$$

$$q_1 = UA \Delta T_{lm} \Rightarrow A_1 = \frac{q_1}{U \Delta T_{lm,1}} = A_2 = \frac{q_2}{U \Delta T_{lm,2}} = A_3 = \frac{q_3}{U \Delta T_{lm,3}}$$

$$A_1 = \frac{9000(124.6 - 113.9)}{200 \left[\frac{(124.6 - 122) - (113.9 - 100)}{\ln \frac{124.6 - 100}{113.9 - 122}} \right]} = 70.9 \text{ ft}^2$$

$$A_2 = \frac{103,000}{200 \left[\frac{(136.1 - 122) - (124.6 - 122)}{\ln \frac{136.1 - 122}{124.6 - 122}} \right]} = 75.3 \text{ ft}^2$$

$$A_3 = \frac{9,000(140 - 136.1)}{200 \left[\frac{(140 - 130) - (136.1 - 122)}{\ln \frac{140 - 122}{136.1 - 130}} \right]} = 14.755 \text{ ft}^2$$

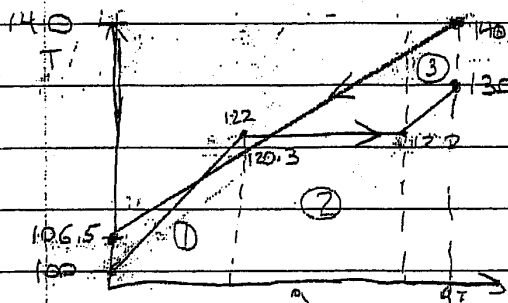
$$A = A_1 + A_2 + A_3 \Rightarrow L = \frac{A}{\pi D} = \frac{160.95}{\pi (6)} = 307.4 \text{ ft}$$

(b) Re-doing calculations for temperatures:

$$1000(38 \times 22 + 103 + 8 \times 0.4) + 4000(30) = 7000(140 - T_{h,o})$$

$$\Rightarrow T_{h,o} = 106.5^\circ F$$

$$1000(22 \times 38) + 4000(22) = 7,000(T_1 - 106.5) \Rightarrow T_1 = 120.3^\circ F$$



We find there is a pinch point
so P can't work.