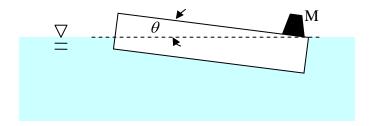


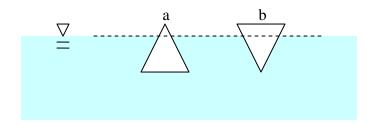
13.012 Marine Hydrodynamics for Ocean Engineers Fall 2004 Quiz #1

Ocean		Student name:			
Γhis is a	a closed book	examination. Yo	ou are allowed 1 shee	t of 8.5" x 11" paper with no	tes.
space.				icated by, or tc), circle all the options (all,	
		water density:	nerwise specified: $\begin{aligned} \rho_w &= 1000 \text{ kg/m}^3 \\ \text{y: } \rho_w &= 1025 \text{ kg/m}^3 \\ \rho_a &= 1 \text{ kg/m}^3 \end{aligned}$	kinematic viscosity: v_w = kinematic viscosity: v_{sw} = kinematic viscosity: v_a =	$= 1 \times 10^{-6} \text{ m}^2/\text{s}$
			less otherwise defined All numerical answer	d. ers MUST have the proper ur	nits attached.
Part A	(30%):				
1)	A 1 m ³ block of aluminum, specific gravity 2.7, is tethered to a piece of cork, specific gravity 0.24.				
	The volume of cork required to keep the block neutrally buoyant in seawater is				
	and the volume required in fresh water is Assume both the aluminum and				
	cork are full	y submerged and	that the weight of the	e tether is negligible.	
2)	The velocity field $\vec{V} = 4xy \hat{i} + 10y^2 \hat{j} + Czy \hat{k}$ is valid for $C = $ The vorticity				
	in this flow field is $\omega =$ This flow field is [irrotational][rotational].				
3)	The two <i>linearized</i> boundary conditions at the free surface for linear progressive free-surface				
	gravity wave	es are	and	(give mat	hematically).
4)	The linear fr	ee surface disper	rsion relationship is gi	ven by $\omega^2 =$	This
	relationship holds for [shallow] [intermediate] [deep] [all of the above] waves. The shallow water				
	form of the o	lispersion relatio	n is $\omega^2 =$	This holds for H	/ λ [greater
	than] [less	than]	·		

5) When a M=5kg weight is placed at the end of a uniform density floating wooden beam (3 m long, with a $10cm \times 10 cm$ cross section), the beam tilts at an angle θ such that the upper right corner of the beam is exactly at the surface of the water (as shown below). The angle θ = ______ and the specific gravity of the log is ______.

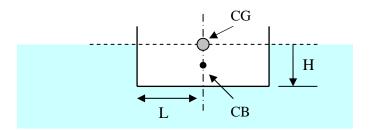


- 6) A progressive linear free surface gravity wave train is propagating in a tank from left to right. This wave train is generated by a wave paddle at one end. The deep water wave has frequency $\omega = 1 \, rad \, / \, s$. The time it takes for the front edge of the wave packet to reach the far end of the tank, 100 meters away, is _______ seconds.
- 7) When floating in water ($\rho = 1000 kg / m^3$), an equilateral triangular body (SG = 0.9) with a long length into the board is more stable in position [a] [b].

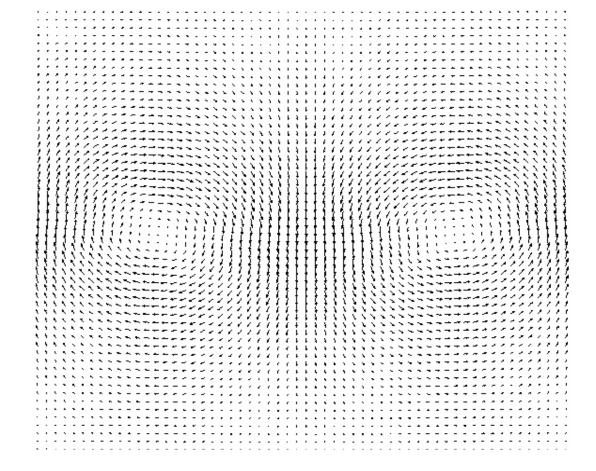


8) A deep water wave train with amplitude a=0.5m is propagating from left to right in a tank. The tank depth is 15 meters, and the wave frequency is 0.25 Hz. These waves are [linear] [non-linear][cannot determine] water waves. The appropriate dispersion relationship is given by $\omega^2 =$ ______. The wavelength $\lambda =$ ______. Phase speed $V_p =$ ______.

9) For the rectangular barge with width 2L and vertical draft H shown below, the Metacentric Height $\overline{GM} = \underline{\hspace{1cm}}$ for small tilt angles (in terms of L and H). This barge can only be stable if $\underline{\hspace{1cm}}$ > $\underline{\hspace{1cm}}$.



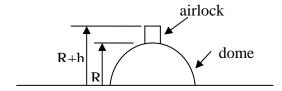
- 10) The conservation of mass equation depends on the assumption(s) of [constant density] [irrotationality] [inviscid fluid] [incompressibility] [Newtonian fluid] [matter cannot be created]. For incompressible flow, the density ρ satisfies the equation _______.
- 11) BONUS (5pts) Sketch ten streamlines on the plot below. Vectors represent the flow velocity.



FOR PART B PROBLEMS: BE SURE TO SKETCH THE PROBLEM, STATE YOUR ASSUMPTIONS AND SHOW YOUR WORK! USE THE PROVIDED EXAM BOOKLET. DON'T FORGET TO CHECK UNITS!

Problem B.1: (35%)

A highly skilled diver is to be sent on a mission to repair a broken cable that supplies electricity to an underwater habitat. The cable has come un-plugged and is tangled about a nearby rock formation. The habitat is located 100m under the water, and is shaped as a hemispherical dome (radius R=15m) with a cylindrical airlock chamber (height h=5m, radius r=h/2) at the very top of the dome.

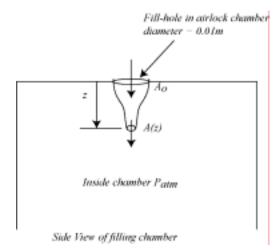


- a) To release the diver into the water the airlock must be filled with water and pressurized to ambient ocean pressure at the depth of the hatch on top of the airlock. Determine the magnitude of pressurization required inside the airlock to release a diver into the water from the underwater habitat.
- b) If the airlock chamber did not pressurize to ambient ocean pressure, but stayed at atmospheric pressure, what is the force that would be required to open the hatch (upwards in to the ocean)? The hatch has the same radius as the airlock cylindrical chamber.

The airlock fill valve is a simple circular hole in the top of the airlock, as shown below. When the fill valve is open water pours into the airlock. At some depth, z, below the fill the water spout has area A(z).

- c) Determine area A(z) of the incoming water spout at some depth below the opening.
- d) Calculate how long it will take (time in seconds) the airlock chamber to completely fill

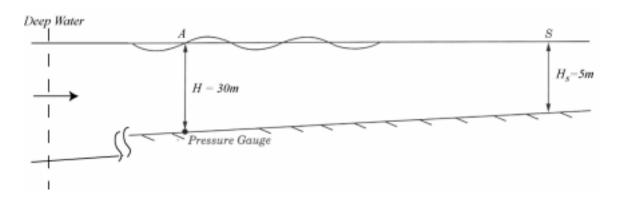
Assume that the chamber is kept at atmospheric pressure while it fills and the air is released as the water comes in so that the air does not compress. The diameter of the fill hole is $D_o = 0.01m$. The flow at the inlet and across A(z) is uniform.



Hint: Bernoulli's equation will come in *very* handy here. Consider a streamline along the middle of the spout and a reference point where the vertical velocity is zero.

PROBLEM B.2: (35%)

A plane progressive LINEAR wave travels from deep water towards shallow depth over a gently sloping bottom. To record the wave characteristics, a pressure gage is positioned on the bottom at station A where the depth is H = 30 m.



The difference between maximum and minimum pressure measured is $6000 \ N/m^2$. Measurements had a period of $10 \ seconds$. The bottom slope is very gradual, and can be taken locally as constant, such that reflections and energy dissipation can be neglected and the wave period remains constant. For simplicity use $\rho = 1000 m^3 / kg$; $g = 10 m/s^2$.

- a) Determine the wavelength, λ , amplitude, a, group velocity, V_g , at point A and point S.
- b) Out in deep water the wave period and amplitude can be assumed to be the same as at point A.
 Determine the energy flux 3 across a vertical plane in deep water.
- c) Calculate the mean volume (mass) transport per unit width through the same vertical plane in deep water.
- d) Calculate the maximum instantaneous horizontal volume flux at this point. (ie. depth integrated velocity).
- e) Sketch the particle orbits at the two positions A and S.