## Multi-dimensional Arrays 3/16/01 Lecture \#16 16.070

- Review:
> An array is set of elements that all have same data type
$>$ Array elements stored sequentially in memory and accessed using integer index
$>$ First element has index of 0
- Arrays can be of multiple dimensions: 1-D, 2-D, 3-D, etc.
$>$ Arrays can be declared in which each element is itself an array


## Visualizing Multi-dimensional Arrays

- Draw a One-Dimensional Array of 8 elements


## Visualizing Multi-dimensional Arrays - cont.

- Draw a Two-Dimensional Array of 8 elements, each containing 5 elements


## Visualizing Multi-dimensional Arrays - cont.

- Draw a Three-Dimensional Array of 8 elements, each contain 5 elements, and each of those contain 3 elements


## Visualizing Multi-dimensional Arrays

- Draw a Four-Dimensional Array of 8 elements, each contain 5 elements, each of those contain 3 elements, each of those contain 2 elements


## Declaring Multi-Dimensional Arrays

- Multi-dimensional arrays must be declared, just like variables and onedimensional arrays
- Each dimension is represented by a subscript: [ ], [ ][ ], [ ][ ][ ], etc.
- For a 2-D array, first subscript defines the Row Number, second subscript defines the Column Number
- Format for declaring a 2-D array
<type> <array_name> [<\#_of_rows>][<\#_of_columns>];
- Example declaration
int grades [students] [exams];


## Multiple Dimensional Arrays - Example

- Create a 2-D array to represent the torque of 4 reaction wheels. Each wheel has a force component in each s/c axis (roll, pitch, yaw)

```
float wheels [4][3] ; /* 4 wheels x 3 axes */
```

Index for each element in wheels array

| RowlCol | 1: Roll | 2: Pitch | 3: Yaw |
| :---: | :---: | :---: | :---: |
| 1: RW1 | $[0][0]$ | $[0][1]$ | $[0][2]$ |
| 2: RW2 | $[1][0]$ | $[1][1]$ | $[1][2]$ |
| 3: RW3 | $[2][0]$ | $[2][1]$ | $[2][2]$ |
| 4: RW4 | $[3][0]$ | $[3][1]$ | $[3][2]$ |

- Two dimensional array is a convenient way of visualizing the data
- However, internally the data are stored sequentially, by rows.

| $[0][0]$ | $[0][1]$ | $[0][2]$ | $[1][0]$ | $[1][1]$ | $[1][2]$ | $\ldots$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Initializing Multiple Dimensional Arrays

- Like variables and single-dimensional arrays, multi-dimensional arrays can be initialized at compile time or at run time
$>$ At compile time, enclose each row in braces, and enclose all rows by one outer set of braces (for 2-D arrays)

```
float wheels [4][3] = {
    {0.0, 0.0, 0.0},
    {0.0, 0.0, 0.0},
    {0.0, 0.0, 0.0},
    {0.0, 0.0, 0.0}
};
```

$>$ At run time, loop over each index: use nested for loops

```
for (i = 0; i < 3; i++)
    for (j = 0; j < 2; j++)
        wheels[i][j] = 0.0;
```

$>$ Generalize to higher dimensions: to initialize values in an N-dimensional array at run time, iterate over each index, usually right-most index first

- Like variables, un-initialized arrays contain garbage!


## Manipulating Multi-Dimensional Arrays - Examples

- Declare a 3x2 array

```
const int rows = 3;
const int cols = 2;
int matrix [rows][cols] = {
```

                                    \(\{5,7\}\),
                                    \(\{2,8\}\),
                                    \(\{10,4\}\),
    \};
$>$ Sum up rows:

```
for (i = 0; i < rows; i++)
{
        sum = 0;
        for (j = 0; j < cols; j++)
            sum = sum + matrix[i,j];
        printf ("Sum for row %d is %d\n", i, sum);
}
```

$>$ Sum up columns:

## Manipulating Multi-Dimensional Arrays - Example

- Calculate total rainfall for each of 5 years, based on monthly averages

```
#include <stdio.h>
#define MONTHS 12 /* number of months in year */
#define YRS 3 /* number of years of data */
int main(void)
{ /* initialize rainfall data for 1998-2000 */
float rain[YRS][MONTHS] = {
    {10.2, 8.1, 6.8, 4.2, 2.1, 1.8, 0.2, 0.3, 1.1, 2.1, 6.1, 7.4},
    {9.2, 9.8, 4.4, 3.3, 2.2, 0.8, 0.4, 0.0, 0.1, 1.2, 2.5, 5.3},
    {8.6, 5.6, 1.3, 1.5, 2.5, 2.0, 0.5, 0.4, 0.9, 0.3, 2.1, 3.5}
    };
int year = 0, month = 0;
float subtot = 0.0, total = 0.0;
printf (" YEAR RAINFALL (inches)\n");
for (year = 0; year < YRS; year++)
{ /*for each year, sum rainfall over all months */
            for (month = 0; month < MONTHS; month++)
                subtot = subtot + rain[year][month];
            printf ("%d %f\n", 1998 + year, subtot);
            total = total + subtot; /* total for all years */
}
printf ("\nTotal rainfall for all years was %f inches.\n", total);
return 0;
}
```


## Passing 1-D Arrays to Functions

- Name of array is the address of the first element in array
$>$ For one-D arrays, name of array points to an element which is the zero index entry of the array

```
const int axes = 3;
float sc_torque [axes] = {0.0, 0.1, 0.2};
    sc_torque }->\quad\begin{array}{l}{0.0}\\{\hline1.0}\\{\hline2.0}
```

$>$ In calling statement, name of array is passed without subscript

```
total_torque = calc_torque (sc_torque, axes)
```

$>$ In function definition, declare formal argument as a pointer to initial element of array

```
float calc_torque (float torques[], int num_axes)
```


## Passing 2-D Arrays to Functions

- For two-D arrays, name of array points to the zero index entry, which is the first row of the 2-D array

$$
\begin{aligned}
& \text { float wheels [4][3] = } \\
& \text { \{ } \\
& \{0.0,0.1,0.2\} \text {, } \\
& \{1.0,1.1,1.2\} \text {, } \\
& \{2.0,2.1,2.2\} \text {, } \\
& \{3.0,3.1,3.2\} \\
& \text { \}; } \\
& \text { wheels } \rightarrow \quad \begin{array}{|}
\hline 0.0,0.1,0.2 \\
\hline 1.1,1.1,1.2 \\
\hline 2.2,2.1,2.2
\end{array}
\end{aligned}
$$

## Passing 2-D Arrays to Functions - cont.

$>$ In calling statement, name of array is passed without subscript

$$
\text { rates }=\text { calc_rates (wheels, 4) }
$$

$>$ In function definition, must declare second subscript of formal parameter

```
float calc_rates (float wheels[][3], int num_wheels);
                                    /*prototype*/
```

- Compiler needs to know size of each element (i.e., size of each row for a 2-D)
- You may omit size of array being passed, but must specify size of each element
- In general, may omit only the first size specification, but must specify other sizes


## Passing 2-D Arrays to Functions - Example

- Examine the following example

```
float two_axes_gyro_bias [3][2] = {
                                    {0.01, 0.02},
                                    {0.03, 0.02},
                                    {0.01, 0.03},
                                    };
/*xy, yz, xz gyro biases*/
two_axes_gyro_bias == ? address of array of 2 floats = &t_a_g_b[0]
two_axes_gyro_bias[0] == ? address of a float = &t_a_g_b[0][0]
```

$>$ Same value?

```
two_axes_gyro_bias + 1 == ? refers to 2 float object
two_axes_gyro_bias[0] + 1 == ? refers to a float
```

$>$ Same value?
two_axes_gyro_bias[0][0] == ? 0.01

## Protecting Array Contents

- When passing information to a function, pass by value or pass by reference (pointer)
$>$ Pass by value preserves contents of original variable since value is copied into a local variable
$>$ Pass by pointer allows function to have access to original variable. Integrity of constant may be compromised
$>$ Arrays are passed to functions by pointer (more efficient)
$>$ Array can be declared constant inside function to prevent function from modifying contents, even if array is not declared constant outside of function

```
float total_torque (const float wheels[][num_axes],
    int num_wheels);
```

- If program attempts to modify contents of constant array, compiler will identify error


## Constant Arrays

- Like variables, arrays can be declared as constant
$>$ Constant arrays are a good way to represent look-up tables

```
const float wheels[4][3] = {
    {0.90, 0.05, 0.02},
    {0.03, 0.90, 0.01},
    {0.02, 0.02, 0.90},
    {0.34, 0.32, 0.32}
};
```

$>$ Compiler will guard against the value of a constant array being changed

- Attempts to alter array contents will generate syntax error
- Compiler probably will not guard against mis-handled pointers
- Compiler probably will not prevent another array, whose limits are incorrectly defined, from overwriting a neighboring constant (array or otherwise)


## Review

- Multi-dimensional arrays are useful for storing/manipulating multivectored data of the same type (e.g., monthly rainfall over n years)
- Have care when iterating over subscripts -- order is important!
- Read Sections C11.8-11.10 to solidify these concepts
- Extra help session offered Sunday, 3/18. Consider starting homework prior to this session and bring questions
- Incentive proposal for exams: going once, going twice...?
- I have Exam \#1 exams that have not been picked up yet. Come see me after class

