Distributed Constraint Satisfaction Problems: 2 Asynchronous Algorithms

Thomas Léauté 16.412J - Cognitive Robotics April 7, 2004

Presentation Outline

- 1. Introduction to CSPs and DCSPs
- 2. The Asynchronous Backtracking Algorithm
- 3. The Asynchronous Weak-Commitment Search Algorithm
- 4. Conclusion and Introduction to the Task Allocation Problem

M. Yokoo, E. Durfee, T. Ishida and K. Kuwabara, *Distributed Constraint Satisfaction Problem: Formalization and Algorithms*, IEEE Transactions on Knowledge and Data Engineering, VOL. 10, NO. 5, Sept/Oct 1998



• A solution to the problem is an assignment to the variables that satisfies all the constraints

1. Introduction to CSPs and DCSPs

- Many AI problems can be formulated as CSPs
- Example of a multi-agent scheduling problem*: to do to do



* K. Sycara, S. Roth, N. Nadeh and M. Fox, *Distributed Constrained Heuristic Search*, IEEE Transactions on Systems, Man, and Cybernetics, VOL. 21, NO. 6, Nov/Dec 1991

1. Introduction to CSPs and DCSPs

• Split the problem in coupled sub-problems: distribute the variables AND the constraints among the agents



* K. Sycara, S. Roth, N. Nadeh and M. Fox, *Distributed Constrained Heuristic Search*, IEEE Transactions on Systems, Man, and Cybernetics, VOL. 21, NO. 6, Nov/Dec 1991





- Prohibitive cost of collecting information
- Security/Privacy reasons
- Not computationally efficient

1. Introduction to CSPs and DCSPs

• Synchronous Backtracking method:





- 2. Asynchronous Backtracking
 - Assumptions:
 - Given priority order on the agents
 - An agent must be able to send messages to any other agent
 - Each agent has exactly ONE single variable
 - Key ideas:
 - Agents work concurrently (= "asynchronously"), exchanging messages to collect required information
 - Conflict-directed search

2. Asynchronous Backtracking



The agent selects a value for its variable satisfying the constraints whose enforcement it is responsible for



If there is at least one value satisfying the constraints, the agent picks one and changes the assignment to its variable

















NAME	VALUE	DOMAIN			
VIEW	CHILDREN	PARENTS			
	KNOWN CONFLICTS				
_	CONSTRAINTS TO ENFORCE				

2. Asynchronous Backtracking: The Graph Coloring Example

2. Asynchronous Backtracking: The Graph Coloring Example





Each agent chooses an assignment to its variable









































Weaknesses of the Asynchronous Backtracking Algorithm

- How to better choose the assignments?
 →Use a heuristic to make better choices
- The authors prove the algorithm always reaches a stable state within a finite number of steps, BUT it still lacks a termination procedure

→Use a "Distributed Snapshot" external procedure

K. M. Chandy and L. Lamport, *Distributed Snapshots: Determining Global States of Distributed Systems*, ACM Transactions on Computer Systems, 1985

Weaknesses of the Asynchronous Backtracking Algorithm (cont.)

- Need of a judicious priority ordering among the agents
 - →Do it beforehand? (might be difficult + need of a centralizing agent...)
 - →Dynamic priority ordering: let the agents come up with a judicious ordering themselves, as they encounter conflicts

Weaknesses of the Asynchronous Backtracking Algorithm (cont.)

- How to extract conflicts?
 - \rightarrow Open to all conflict extraction policies
 - →There is a trade off between taking the time to extract minimal conflicts, and trying to speed up the algorithm by using the agent's view as a super-conflict but wasting time by backtracking more often



3. The Asynchronous Weak-Commitment Search Algorithm

- Use a local min-conflict heuristic to guide the choices of assignments
- Judiciously change the priority ordering every time the search needs to backtrack

3. The Asynchronous Weak-Commitment Search Algorithm (cont.)

- "Weak-Commitment" Search:
 - A partial assignment to the variables is constructed step by step by extending it to variables with lower priority
 - The group of agents "weakly commits" itself to the partial assignment because the partial assignment is abandoned as soon as the algorithm needs to backtrack
 - The priority ordering is then modified so that the agent which failed to find a value to its variable consistent with the constraints "promotes itself" (i.e. it changes its priority value to locally become the agent with the highest priority)

3. The Asynchronous Weak-Commitment Search Algorithm (cont.)

- ATTENTION! Tricky point:
 - Every time an agent discovers a known conflict in its view, it will abandon the partial solution
 - However, if, due to message delays, the agent's view is obsolete, it will abandon the partial assignment too early and perform an unnecessary change in its priority value
 - To avoid reacting to such unstable situations, the agent records the conflicts it has already sent, and it will temporarily ignore a conflict if it has already sent it before





















3. Weak-Commitment Search: The Graph Coloring Example

























M. Yokoo, E. Durfee, T. Ishida and K. Kuwabara, *Distributed Constraint Satisfaction Problem: Formalization and Algorithms*, IEEE Transactions on Knowledge and Data Engineering, VOL. 10, NO. 5, Sept/Oct 1998

4. Conclusion

TABLE 1 COMPARISON BETWEEN ASYNCHRONOUS BACKTRACKING AND ASYNCHRONOUS WEAK-COMMITMENT SEARCH (DISTRIBUTED N-QUEENS)

	asynchronous		asynchronous		asynchronous	
	backtracking		backtracking with		weak-commitment	
			min-conflict heuristic			
n	ratio	cycles	ratio	cycles	ratio	cycles
10	100%	105.4	100%	102.6	100%	41.5
50	50%	325.4	56%	326.8	100%	59.1
100	14%	510.0	30%	504.3	100%	50.8
1000	0%		16%	323.8	100%	29.6

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4. Conclusion

- Perform much better than the trivial algorithms
- Single-variable agents => Task Allocation Problem

W.-M. Shen and B. Salemi, *Distributed and Dynamic Task Reallocation in Robot Organizations*

References

- M. Yokoo, E. Durfee, T. Ishida and K. Kuwabara, *Distributed Constraint Satisfaction Problem: Formalization and Algorithms*, IEEE Transactions on Knowledge and Data Engineering, VOL. 10, NO. 5, Sept/Oct 1998
- K. Sycara, S. Roth, N. Nadeh and M. Fox, *Distributed Constrained Heuristic Search*, IEEE Transactions on Systems, Man, and Cybernetics, VOL. 21, NO. 6, Nov/Dec 1991
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