Unit M4.8 Final Notes on 1-D Structural Members

Readings:

_ _ _

16.003/004 -- "Unified Engineering" Department of Aeronautics and Astronautics Massachusetts Institute of Technology Spring, 2009

FINAL BLOCK M4 OBJECTIVES via M4.8

Through participation in the lectures, recitations, and work associated with Block M4 as emphasized in Unit M4.8, it is intended that you will be able to.....

-describe the key aspects composing the models of the one-dimensional structures of a rod, a beam, a shaft, and a column, and recognize their similarities
-identify the limitations associated with these models
-apply the basic equations of elasticity to derive the solutions for the general cases of various onedimensional structures
-apply these models to examine the behavior of various structural configurations

Remember that all we have done are <u>models</u> of actual structural configurations (which are, by nature, always three-dimensional). The <u>key</u> is in the assumptions and resulting limitations and <u>how good</u> an answer is needed

It is useful to look at the forms of the relations for the models we considered:

One-dimensional Model	Rod	Beam	Shaft
Equilibrium Equation(s)	$\frac{dP}{dx_1} = -p_x$	$\frac{dS}{dx} = q$ $\frac{dM}{dx} = S$	$\frac{dT}{dx_1} = -t$
Stress	$\sigma_{11} = \frac{P}{A}$	$\sigma_{xx} = -\frac{Mz}{I}$ $\sigma_{xz} = -\frac{SQ}{Ib}$	$\sigma_{13} = \frac{Tx_2}{J}$ $\sigma_{12} = -\frac{Tx_3}{J}$ $\tau_{res} = \frac{Tr}{J}$
Deflection	$\frac{du_1}{dx_1} = \frac{P}{EA}$	$\frac{d^2 w}{dx^2} = \frac{M}{EI}$	$\frac{d\phi}{dx_1} = \frac{T}{GJ}$



--> What can we now do?

Make simple models of real structure by <u>superposing</u> our simple one-dimensional models



Model as a constant cantilevered cross-section beam with distributed loads and moments:

