

a) Shock relations for  $M_1 = 2.6$ :  $\frac{P_2}{P_1} = 7.72$ ,  $\frac{\rho_2}{\rho_1} = 3.449$ ,  $\frac{T_2}{T_1} = 2.238$ ,  $\frac{P_{02}}{P_1} = 9.181$ ,  $M_2 = 0.5039$

$$\therefore P_2 = P_1 \cdot \frac{P_2}{P_1} = 7.72 \text{ atm}$$

$$T_2 = T_1 \cdot \frac{T_2}{T_1} = 288 \text{ K} \cdot \frac{T_2}{T_1} = 644.54 \text{ K}$$

$$\rho_1 = \frac{p_1}{RT_1} = \frac{1.013 \cdot 10^5 \text{ Pa}}{287 \text{ J/kg} \cdot \text{K} \cdot 288 \text{ K}} = 1.226 \text{ kg/m}^3, \quad \rho_2 = \rho_1 \cdot \frac{\rho_2}{\rho_1} = 4.227 \text{ kg/m}^3$$

$$P_{02} = P_1 \cdot \frac{P_{02}}{P_1} = 9.181 \text{ atm}$$

$$T_{02} = T_{01} = T_1 \left[ 1 + \frac{\gamma-1}{2} M_1^2 \right] = 288 \text{ K} \left[ 1 + \frac{\gamma-1}{2} 2.6^2 \right] = 677.4 \text{ K}$$

b) Given:  $\frac{P_2}{P_1} = \frac{10.33 \text{ atm}}{1 \text{ atm}} = 10.33$ . From shock  $\frac{P_2}{P_1}(M_1)$  function, this gives  $M_1 = 3.0$

Also given:  $T_2 = 1390^\circ \text{R}$ , and  $\frac{T_2}{T_1}(M_1=3.0) = 2.679$ ,  $\therefore T_1 = T_2 \frac{1}{T_2/T_1} = 518.85^\circ \text{R}$

$$T_{02} = T_{01} = T_1 \left[ 1 + \frac{\gamma-1}{2} M_1^2 \right] = 1452.8^\circ \text{R}$$

$$\frac{P_{02}}{P_1}(M_1=3) = 12.06, \quad P_{02} = P_1 \cdot \frac{P_{02}}{P_1} = 12.06 \text{ atm}$$

c) Given  $\frac{P_{02}}{P_1} = \frac{7712.8 \text{ lb/ft}^2}{2116 \text{ lb/ft}^2} = 3.645$  this is on the shock table, for  $M_1 = 1.56$

For  $T_{11} = 519^\circ \text{R} = 288^\circ \text{K}$ ,  $a_1 = \sqrt{\gamma RT_1} = 340.4 \text{ m/s}$ ,  $V_1 = M_1 a_1 = 531 \text{ m/s} = 1742 \text{ ft/s}$

d)  $V_1 = 2112 \text{ mi/h} = 943.9 \text{ m/s}$ , At altitude 80000 ft:  $T_\infty = 390^\circ \text{R} = 216.7^\circ \text{K}$   
 $P_\infty = 5.8125 \text{ lb/ft}^2 = 278.3 \text{ Pa}$

Ahead of bow shock, we have  $T_1 = T_\infty = 216.7^\circ \text{K}$   
 $P_1 = P_\infty = 278.3 \text{ Pa}$ ,  $a_1 = \sqrt{\gamma RT_1} = 295 \text{ m/s}$

$$M_1 = \frac{V_1}{a_1} = 3.2 \rightarrow T_{01} = T_1 \left[ 1 + \frac{\gamma-1}{2} M_1^2 \right] = 660.5^\circ \text{K} = 1189^\circ \text{R} = T_{02}$$

$$\text{For } M_1 = 3.2: \frac{P_{02}}{P_1} = 13.66, \quad P_{02} = P_1 \cdot \frac{P_{02}}{P_1} = 3801.6 \text{ Pa}$$