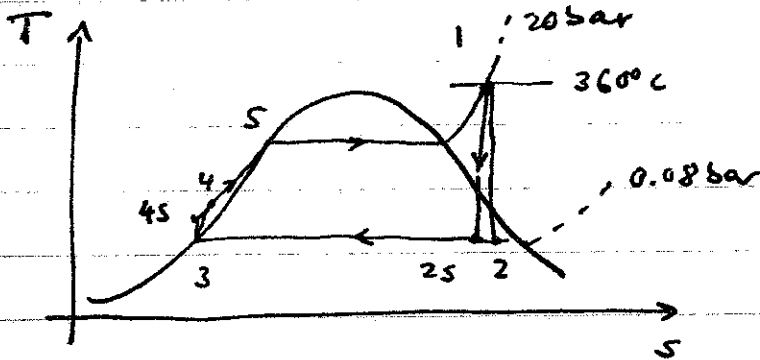


T12

16. Unified Sp09  
25



Concepts:

- 2 phase-media
- ad. component efficiencies
- Rankine cycles

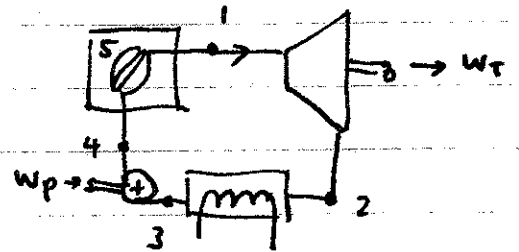
a) state 1:  $h_1 = 3159.1 \text{ kJ/kg}$   
 $s_1 = 6.9904 \text{ kJ/kg-K}$

state 2s:  $s_1 = s_{2s} = x_{2s} s_g + (1-x_{2s}) s_f$

$\rightarrow x_{2s} = \frac{s_1 - s_f}{s_g - s_f} = \frac{6.9904 - 0.5909}{8.2312 - 0.5909} = 0.837$

$h_{2s} = 2185 \text{ kJ/kg}$  ;  $h_g = 2576.8 \text{ kJ/kg}$  ,  $h_f = 173.4 \text{ kJ/kg}$

$v_3 = 0.001 \text{ m}^3/\text{kg}$



$w_T^s = h_1 - h_{2s} = 974 \text{ kJ/kg}$  ;  $w_P^s = v_3 (P_1 - P_3) = 1.99 \text{ kJ/kg}$

$q_R^s = h_{2s} - h_f = 2011.6 \text{ kJ/kg}$  ;  $q_A^s = w_T^s - w_P^s + q_R^s = 2983.6 \text{ kJ/kg}$

$w_{net}^s = w_T^s - w_P^s = 972 \text{ kJ/kg}$  ;  $\eta_{th}^s = \frac{w_{net}^s}{q_A^s} = 0.326$

b)  $\eta_P = \frac{h_{4s} - h_3}{h_4 - h_3} \rightarrow w_P = \frac{1}{\eta_P} w_P^s = 2.49 \text{ kJ/kg}$

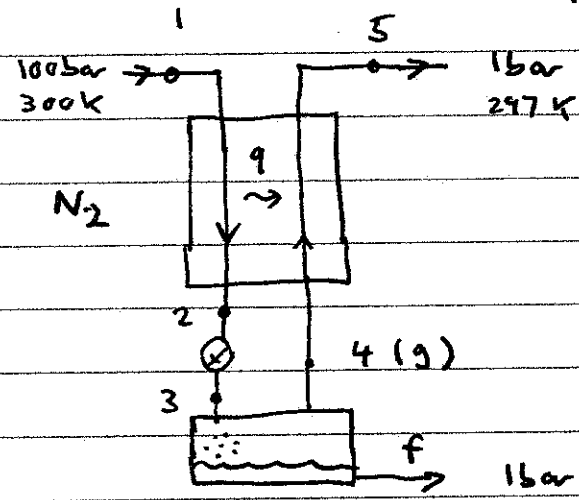
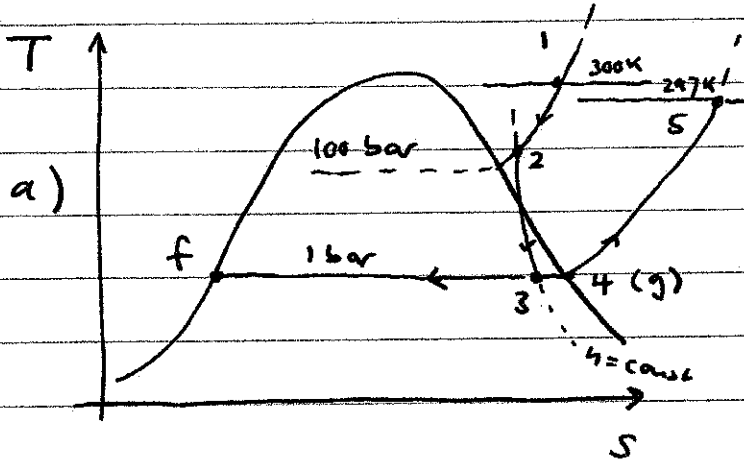
$\eta_T = \frac{h_1 - h_2}{h_1 - h_{2s}} \rightarrow w_T = \eta_T w_T^s = 779.2 \text{ kJ/kg}$

$w_{net} = w_T - w_P = 776.5 \text{ kJ/kg}$  ;  $q_R = h_2 - h_f = 2206.5 \text{ kJ/kg}$

$q_A = w_{net} + q_R = 2983 \text{ kJ/kg}$

$\eta_{th} = \frac{w_{net}}{q_A} = 0.26$

$\frac{\Delta w_{net}}{w_{net}^s} = 20\%$  ;  $\frac{\Delta \eta_{th}}{\eta_{th}^s} = 20\%$



$\dot{V}_3 = 0.167 \text{ m}^3/\text{s}$       $\dot{m}_3 = \frac{1}{v_3} \dot{V}_3$   
 $\dot{m}_1 = \dot{m}_3$      cons. mass

from tables:
$h_1 = 291.9 \text{ kJ/kg}$
$h_5 = 308 \text{ kJ/kg}$
$h_g = h_4 = 76.7 \text{ kJ/kg}$
$h_f = -122 \text{ kJ/kg}$
$v_g = 0.21639 \text{ m}^3/\text{kg}$
$v_f = 0.00124 \text{ m}^3/\text{kg}$

1→2: 1st law  $h_1 - h_2 = q$   
 2→3: 1st law  $h_3 = h_2$  (note  $T_2 \neq T_3$ !)  
 (two-phases: no heat, no work)  
 4→5: 1st law  $\dot{m}_4 (h_5 - h_4) = \dot{m}_3 q$

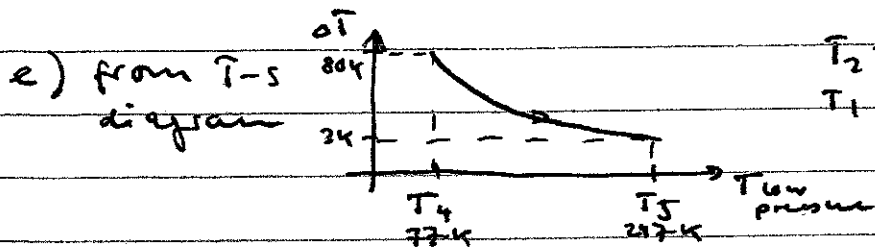
quality:  $\dot{m}_4 = \dot{m}_3 \rightarrow \frac{\dot{m}_4}{\dot{m}_3} = x_3$  ,  $h_3 = h_g x_3 + h_f (1-x_3)$

combine  $h_1 - h_3 = q = x_3 (h_5 - h_g) \rightarrow x_3 = \frac{h_1 - h_f}{h_5 - h_f}$       $x_3 = 0.962$

b) mass flow:  $\dot{V}_3 = x_3 v_g + (1-x_3) v_f = 0.2082 \text{ m}^3/\text{kg} \rightarrow \dot{m}_3 = 0.8 \text{ kg/s}$

c) heat transfer:  $h_3 = x_3 h_g + (1-x_3) h_f = 69.1 \text{ kJ/kg} \rightarrow \dot{Q} = \dot{m}_3 (h_1 - h_3)$   
 $\dot{Q} = 178.2 \text{ kW}$

d) liquid  $N_2$  rate:  $\dot{m}_f = (1-x_3) \dot{m}_3$  ,  $\dot{m}_f = 0.03 \text{ kg/s}$



$T_2 = 157\text{K} \rightarrow \Delta T(T_4) = 80\text{K}$   
 $T_1 = 300\text{K} \rightarrow \Delta T(T_5) = 3\text{K}$   
 irreversible heat transfer  
 due to finite temp. difference