

## Unified Quiz M5

April 29, 2009

# M - PORTION

- Put your name on each page of the exam.
- Read all questions carefully.
- Do all work on that question on the page(s) provided. Use back of the page(s) if necessary.
- Show all your work, especially intermediate results. Partial credit cannot be given without intermediate results.
- Show the logical path of your work. Explain clearly your reasoning and what you are doing. *In some cases, the reasoning is worth as much (or more) than the final answers.*
- Please be neat. It will be easier to identify correct or partially correct responses when the response is neat.
- Be sure to show the appropriate units throughout. Answers are not correct without the units.
- Report significant digits only.
- Box your final answers.
- **Calculators are allowed.**
- **Print-outs of all M&S Handouts, particularly "HO-M-15", along with 2 sides of pages of handwritten material are allowed.**

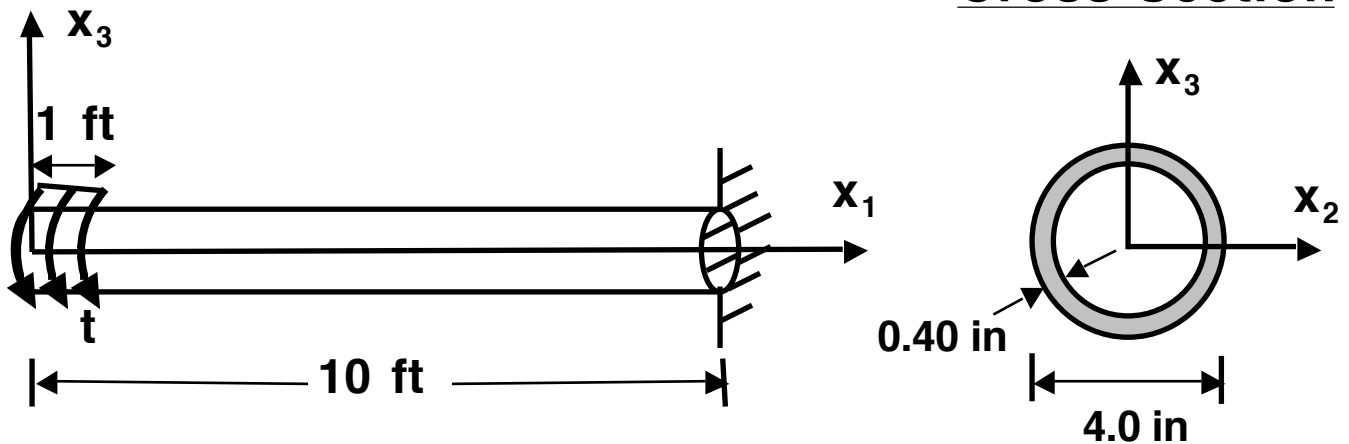
### EXAM SCORING

#1M (1/3)	
#2M (1/3)	
#3M (1/3)	
FINAL SCORE	

**PROBLEM #1M (1/3)**

A shaft configuration has been designed as a means to transmit a constant distributed torque applied over 1 foot at a free end, to a device at the other end. This device can be represented as a clamped support. The shaft is 10 feet long and is a tube with an outer diameter of 4 inches and a wall thickness of 0.40 inches. Two materials are being considered for use. The first is steel which has a Young's modulus of 30 Msi, a Poisson's ratio of 0.30, and a yield stress of 50 ksi. The second is titanium which has a Young's modulus of 15 Msi, a Poisson's ratio of 0.30, and a yield stress of 210 ksi.

**Cross-Section**



- (a) A critical consideration in the design is the rotation of the free end at the critical applied torque. Determine the ratio of that rotation for the two materials being considered.

Unified Quiz M5 - Materials and Structures Portion  
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Name \_\_\_\_\_

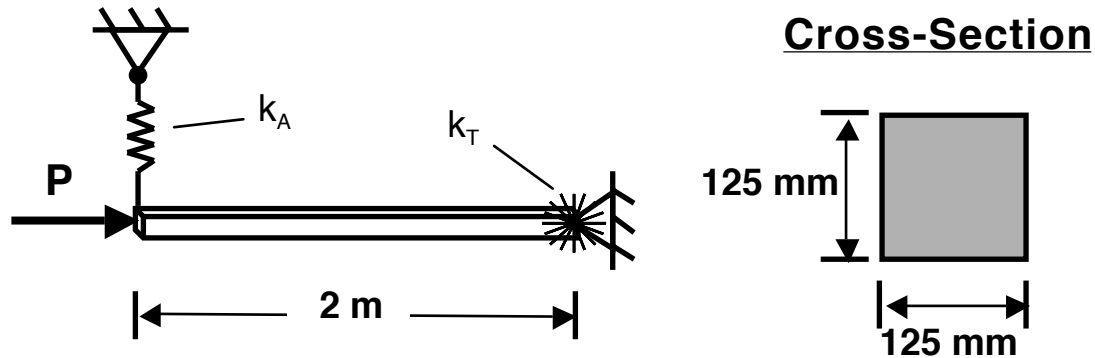
**PROBLEM #1M (continued)**

**PROBLEM #1M (continued)**

- (b) The maximum shear stress in the shaft is also an important consideration in the design. Determine the ratio of that for the two materials being considered.

**PROBLEM #2M (1/3)**

A component of a load transfer device in an industrial machinery system has a square cross-section of 125 mm to a side and is 2 meters long. This piece can be modeled as a component that is attached to a pin support via a torsional spring of stiffness  $k_T$  at one end, and has a compressive load applied at the other end with a linear spring of stiffness  $k_A$  providing transverse support. The component is made of machinery-grade steel with a modulus of 200 GPa and an ultimate stress of 400 MPa.



Set up the equation(s) needed to determine the maximum load of this component assuming that manufacturing, alignment, and loading are “perfect”. This includes contributions due to **any** deformation prior to instability. Describe how you would use the resulting equation(s) to determine the response but **DO NOT SOLVE**. Use figures if/as appropriate.

**PROBLEM #2M (continued)**

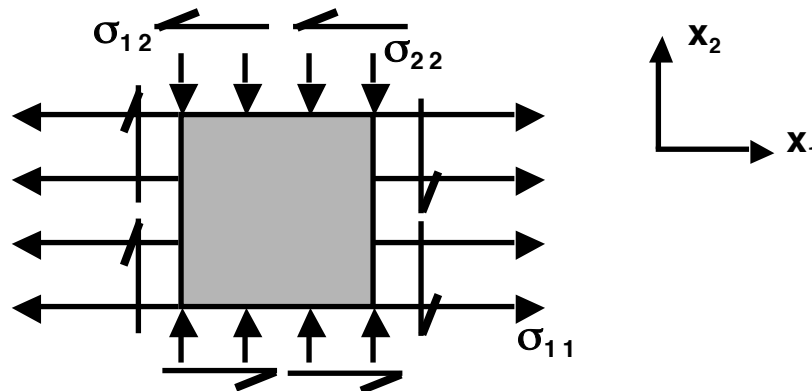
**PROBLEM #2M (continued)**

**PROBLEM #2M (continued)**



**PROBLEM #3M (1/3)**

A joint structure is to be designed to withstand in-plane stresses using either the basic strength approach or the damage tolerance approach. The loading is such that the stresses along each axis have one in tension and one in compression, with a ratio in magnitude of 3:1, tension to compression. There is also a negative shear stress with the shear stress being half in magnitude to the tensile stress. Aluminum and steel are being considered for this piece. The particular aluminum has a modulus of 70 GPa, a Poisson's ratio of 0.30, a value of the tensile yield stress of 200 MPa, a value of the tensile ultimate strength of 350 MPa, and a value of fracture toughness of  $30.0 \text{ MPa(m)}^{1/2}$ . The particular steel has a modulus of 200 GPa, a Poisson's ratio of 0.31, a value of the tensile yield stress of 350 MPa, a value of the tensile ultimate strength of 500 MPa, and a value of fracture toughness of  $50.0 \text{ MPa(m)}^{1/2}$ .



The objective of the design is to minimize weight. The density of the aluminum is  $2.7 \text{ Mg/m}^3$ , that of the steel is  $8.0 \text{ Mg/m}^3$ .

- (a) Using the von Mises criterion and the tensile ultimate strength as the failure criterion, the necessary thickness for the aluminum is determined to be 10 mm for the critical loading. Determine which of the two materials better fulfills the design objective using this failure criterion. Explain carefully using equations as needed.

**PROBLEM #3M (continued)**

**PROBLEM #3M (continued)**

- (b) Using the damage tolerance approach for Mode I considerations and using only the stress normal to a critical crack size of 16.0 mm as the failure criterion, the necessary thickness for the aluminum is determined to be 8.0 mm for the critical loading. Determine which of the two materials better fulfills the design objective using this failure criterion. Explain carefully using equations as needed.

**PROBLEM #3M (continued)**