

## Types of Variables

| Key measures Describing data |  |  |
| :---: | :---: | :---: |
|  | Moment | Non-mean based measure |
| Center | Mean | Mode, median |
| Spread | Varia <br> (standard deviation) | Range <br> Interquartile range |
| Skew | Skewness | -- |
| Peaked | Kurtosis | - |

## Key distinction

Population vs. Sample Notation

| Population | vs. | Sample |
| :--- | :--- | :--- |
| Greeks |  | Romans |
| $\mu, \sigma, \beta$ |  | $\mathrm{s}, \mathrm{b}$ |
|  |  |  |



Variance, Standard Deviation

$$
\begin{aligned}
& \sum_{i=1}^{n} \frac{\left(x_{i}-\mu\right)^{2}}{n} \equiv \sigma^{2} \\
& \sqrt{\sum_{i=1}^{n} \frac{\left(x_{i}-\mu\right)^{2}}{n}} \equiv \sigma
\end{aligned}
$$




## Commands in STATA for getting univariate statistics

- summarize varname
- summarize varname, detail
- histogram varname, bin() start() width() density/fraction/frequency normal
- graph box varnames
- tabulate [NB: compare to table]

Normal distribution


$$
f(x)=\frac{1}{\sigma \sqrt{2 \pi}} e^{-(x-\mu) / 2 \sigma^{2}}
$$

- Skewness = 0
- Kurtosis = 3

The $z$-score
or the
"standardized score"

$$
Z=\frac{x-\bar{x}}{\sigma_{x}}
$$

## Example of Sophomore Test

 Scores- High School and Beyond, 1980: A Longitudinal Survey of Students in the United States (ICPSR Study 7896)
- totalscore $=\%$ of questions answered correctly minus penalty for guessing
- recodedtype $=$ (1=public school, 2=religious private, 3 = non-sectarian private)



## Graph totalscore



## Main issues with histograms

- Proper level of aggregation
- Non-regular data categories


## A note about histograms with unnatural categories

From the Current Population Survey (2000), Voter and Registration Survey
How long (have you/has name) lived at this address?
-9 No Response
-3 Refused
-2 Don't know
-1 Not in universe
1 Less than 1 month
1-6 months
3 7-11 months
4 1-2 years
5 3-4 years
65 years or longer

## Solution, Step 1

Map artificial category onto "natural" midpoint
-9 No Response $\rightarrow$ missing
-3 Refused $\rightarrow$ missing
-2 Don't know $\rightarrow$ missing
-1 Not in universe $\rightarrow$ missing
1 Less than 1 month $\rightarrow 1 / 24=0.042$
2 1-6 months $\rightarrow 3.5 / 12=0.29$
3 7-11 months $\rightarrow 9 / 12=0.75$
4 1-2 years $\rightarrow 1.5$
5 3-4 years $\rightarrow 3.5$
65 years or longer $\rightarrow 10$ (arbitrary)



## So, what's wrong with them

- For non-time series data, hard to get a comparison among groups; the eye is very bad in judging relative size of circle slices
- For time series, data, hard to grasp crosstime comparisons

Draw the box plots for the different types of schools
graph box totalscore, by(recodedtype)


## Three words about pie charts: don't use them



Some words about graphical presentation

- Aspects of graphical integrity (following Edward Tufte, Visual Display of Quantitative Information)
$\square$ Represent number in direct proportion to numerical quantities presented
$\square$ Write clear labels on the graph
$\square$ Show data variation, not design variation
$\square$ Deflate and standardize money in time series

