Department of Mechanical Engineering Massachusetts Institute of Technology 2.010 Modeling, Dynamics and Control III Spring 2002

READING Chapter 2 2.1 - 2.7

Problem Set #2 **DUE** Thursday, February 21, 2002

Problem 1

Using the Laplace Transform, obtain the time response for each of the following systems subject to the input and initial conditions specified below:

a)

$$\frac{d^{3}y}{dt^{3}} + 3\frac{d^{2}y}{dt^{2}} + 2\frac{dy}{dt} = 2\frac{du}{dt} + 3u$$

$$u = \begin{cases} 1 & t > 0 \\ 0 & t \le 0 \end{cases}$$

$$y(0) = 1 \qquad \dot{y}(0) = -1 \qquad \ddot{y}(0) = 2$$
b)

$$\frac{d^{2}y}{dt^{2}} + 2\frac{dy}{dt} + 10y = -3\frac{du}{dt} + u$$

$$u = \begin{cases} t^{2} & t > 0 \\ 0 & t \le 0 \end{cases}$$

Problem 2

Nise Problem 2-27

Problem 3

Nise Problem 2-46: Solve the problem as shown in the book. The following diagram is aimed at clarifying the parameters specified for the motor.

 $y(0) = \dot{y}(0) = 0$

