

Problem Set No. 2

Out: Wednesday, September 10, 2014

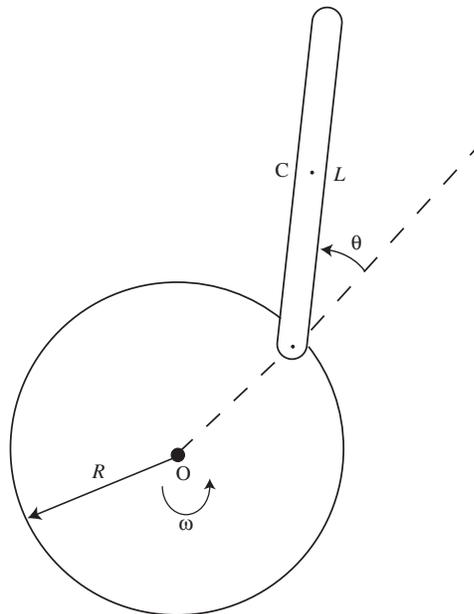
The homework problems are for practice only. Solutions are posted in a separate file. Please work on the problems and be prepared to ask questions related to this homework in the recitation of September 16, 2014 (4:00–5:30pm in Room 5-233).

Problem 1

A pendulum consists of a rod of length L with a frictionless pivot at one end. The pendulum is suspended from a flywheel of radius R which rotates with fixed angular velocity ω , as shown below.

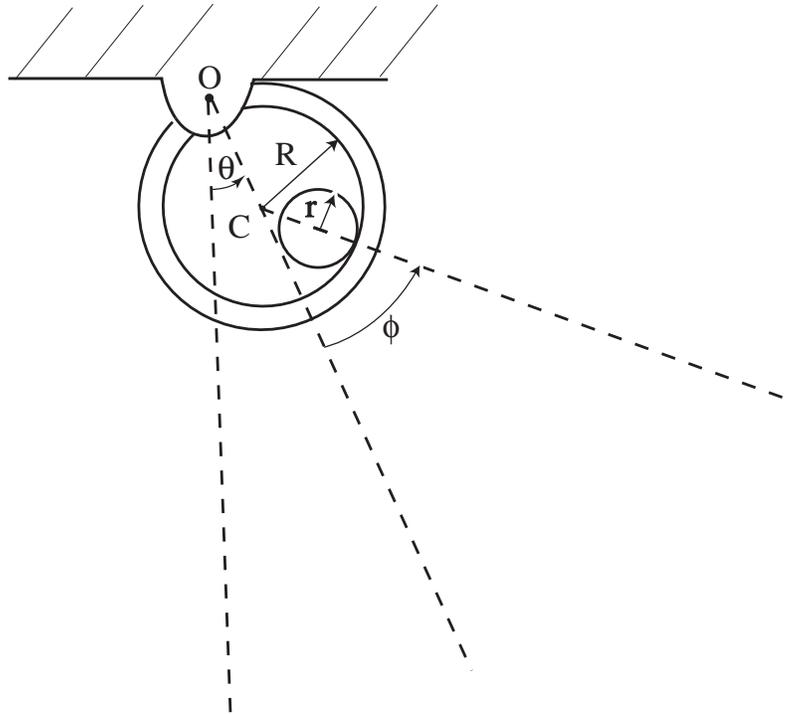
(a) Determine the angular velocity of the rod in terms of ω and the generalized coordinate θ indicated in the sketch

(b) Calculate the velocity of the mid point C of the rod



Problem 2

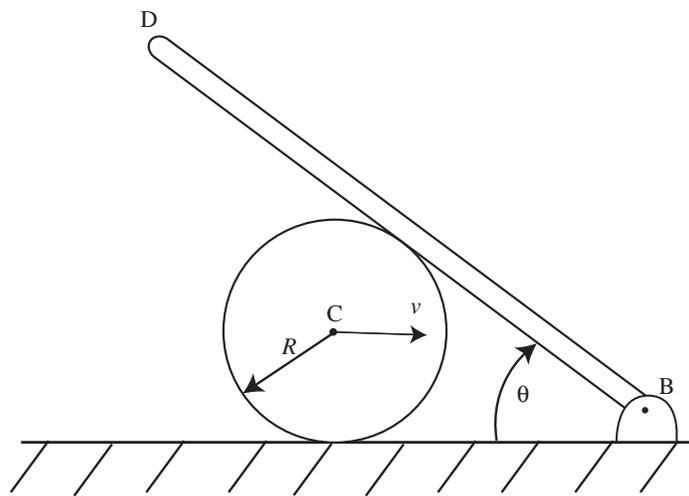
A ring of radius R is pivoted without friction at O . A disk of radius r rolls without slipping inside the ring, as shown below. Determine the angular velocities of the ring and the disk in terms of the generalized coordinates θ , ϕ indicated.



Problem 3 (adapted from Doctoral Qualifying Exam 2002)

In the system sketched below, the rigid cylinder of radius R is moving to the right such that its center C has velocity v . There is no slipping between the cylinder and the bar BD , but there is slipping between the cylinder and the ground. In the position shown,

- (a) Determine the angular velocity of the bar BD
- (b) Determine the velocity of the cylinder at the point where it contacts the ground.



Problem 4 (adapted from Ginsberg, 3-22)

The disk rotates at ω_1 about its axis, and the rotation rate of the forked shaft is ω_2 . Both rates are constant. Determine the velocity and acceleration of an arbitrarily selected point B on the perimeter. Describe the results in terms of components relative to the xyz axes in the sketch.

