

Department of Mechanical Engineering
Massachusetts Institute of Technology
2.14 Analysis and Design of Feedback Control Systems
Fall 2004
Assignment #7
Distributed Friday October 29
Due: **Wednesday, November 3** by 5pm in 35-231 Drop Box

Reading: Reading: Nise Chapter 10

Problem 1

We are given the forward loop transfer function:

$$G(s) = \frac{K}{s^2 + 0.5s + 1} \quad \text{and the feedback transfer function } H(s) = 1:$$

- a) Sketch an asymptotic bode diagram for the case of $K=1$ and then fare-in the region around the resonance.
- b) On that plot indicate the unity gain line for three loop gain values $K = 0.1, 3$ and 10 :
- c) For each case what is:
 - The frequency range of region I?
 - The frequency range of region III?
 - The crossover frequency?
- d) Based on c) sketch the approximate closed-loop bode diagram using $|T(s)| \cong \frac{|G(s)|}{1 + |G(s)|}$ as discussed in class. You can put all three sketches on the same axes, but please delineate each clearly.
- e) Looking at each closed-loop plot, how does it coincide with what you expect from a root locus plot of this system?
- e) Compare that approximation to the exact plot for each gain produced by using MATLAB.
- f) Comment on why the approximation deviated from the actual, and see if you can develop a “rule” for using this approximation.

Problem 2

Nise Problem 10-1

Problem 3

Nise Problem 10-3

Problem 4

Nise Problem 10-5