

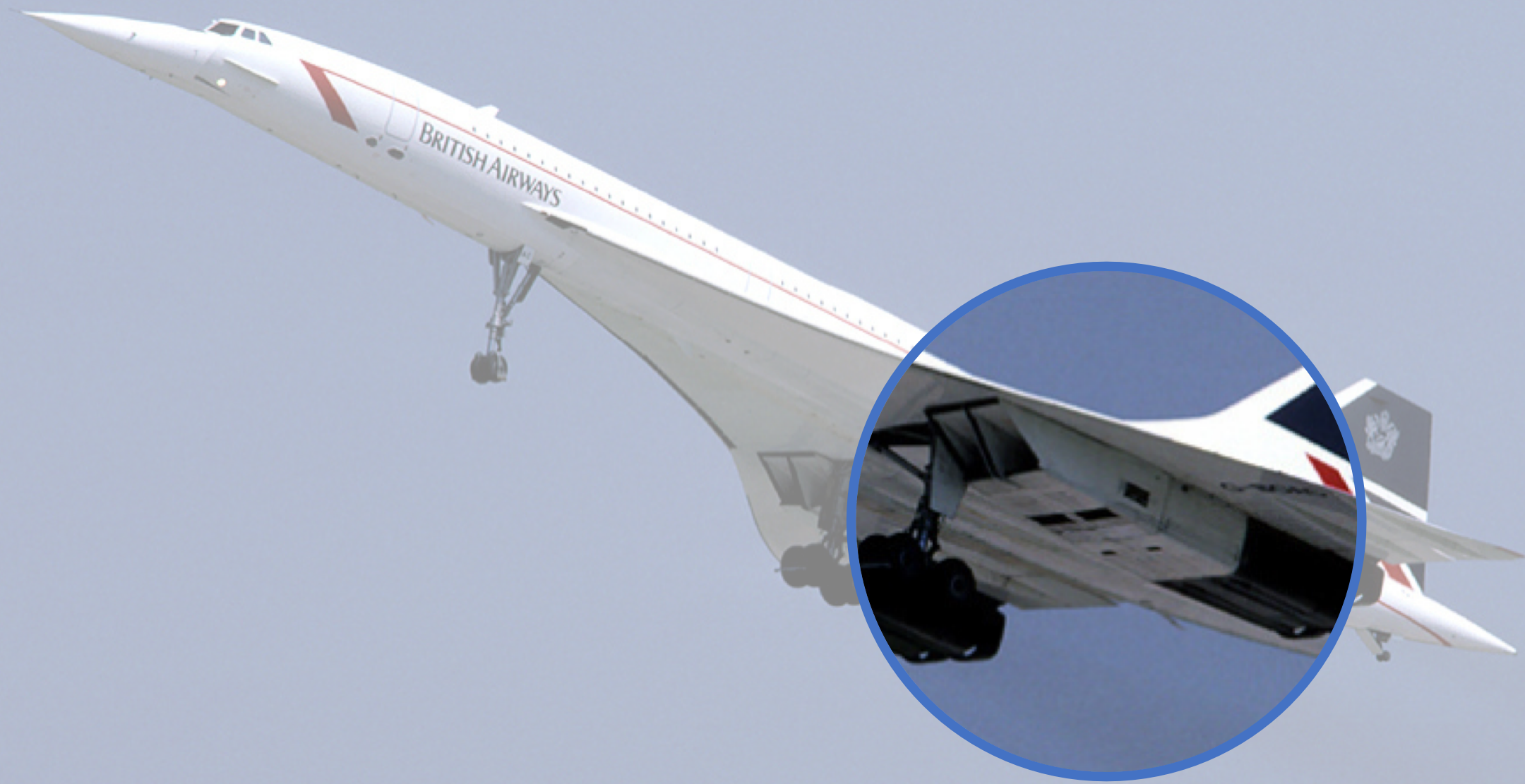


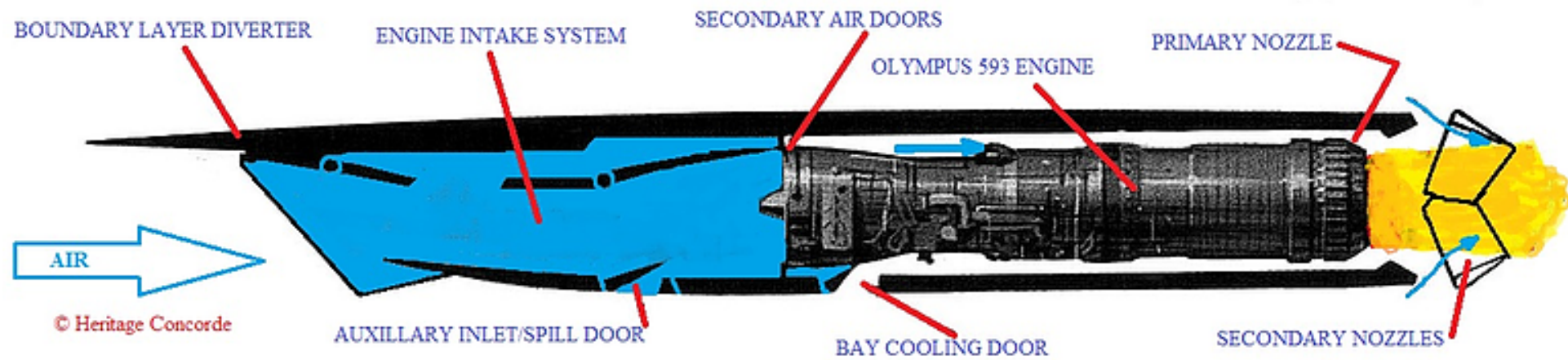
A 2D finite-volume compressible Navier-Stokes solver to simulate inlets of supersonic engines

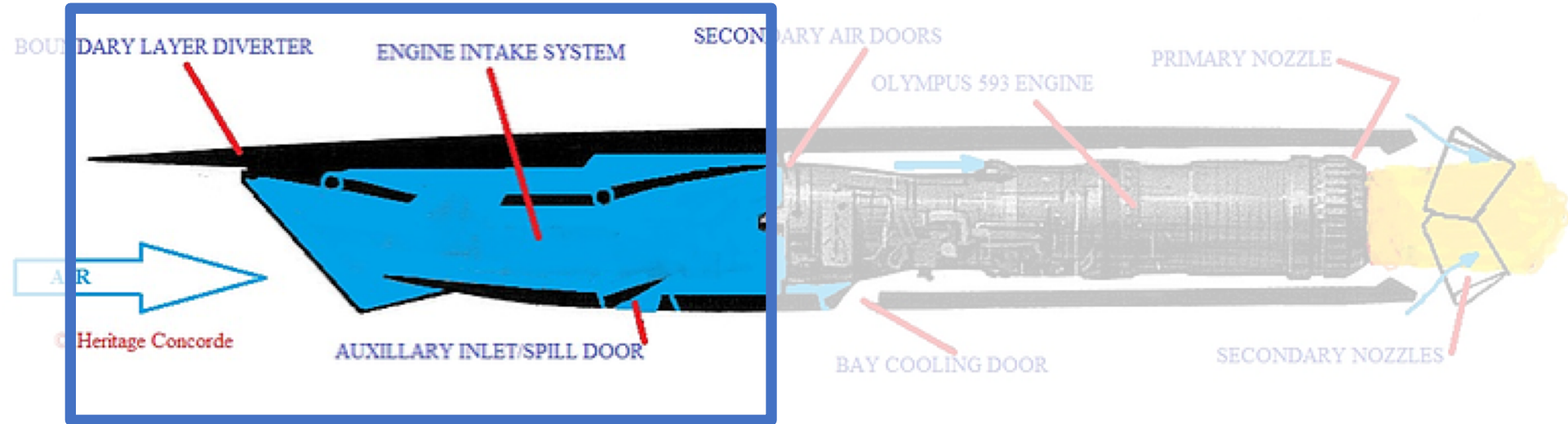
Thursday May 16, 2019

Laurens Voet



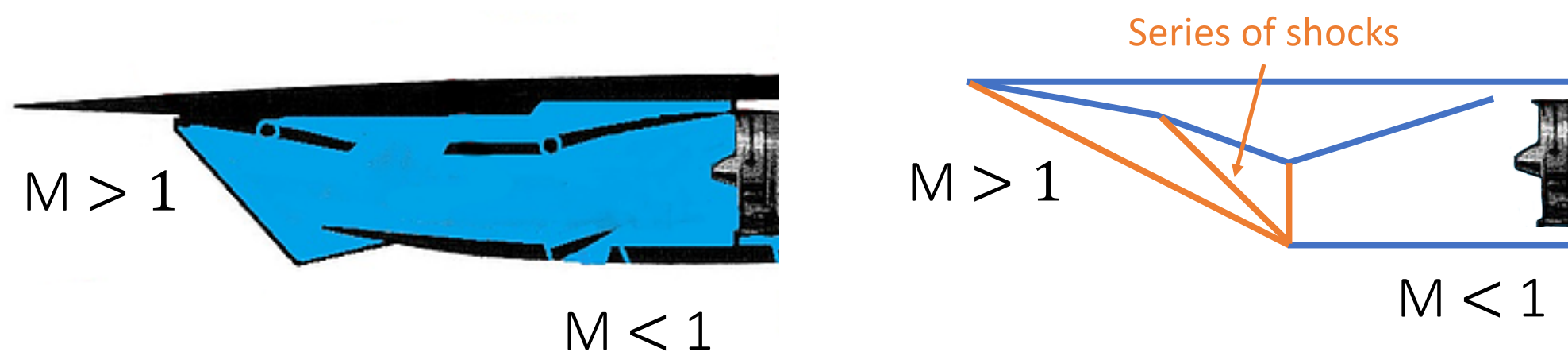






Motivation

- Inlet design of engine for supersonic airplanes \approx wedge flow



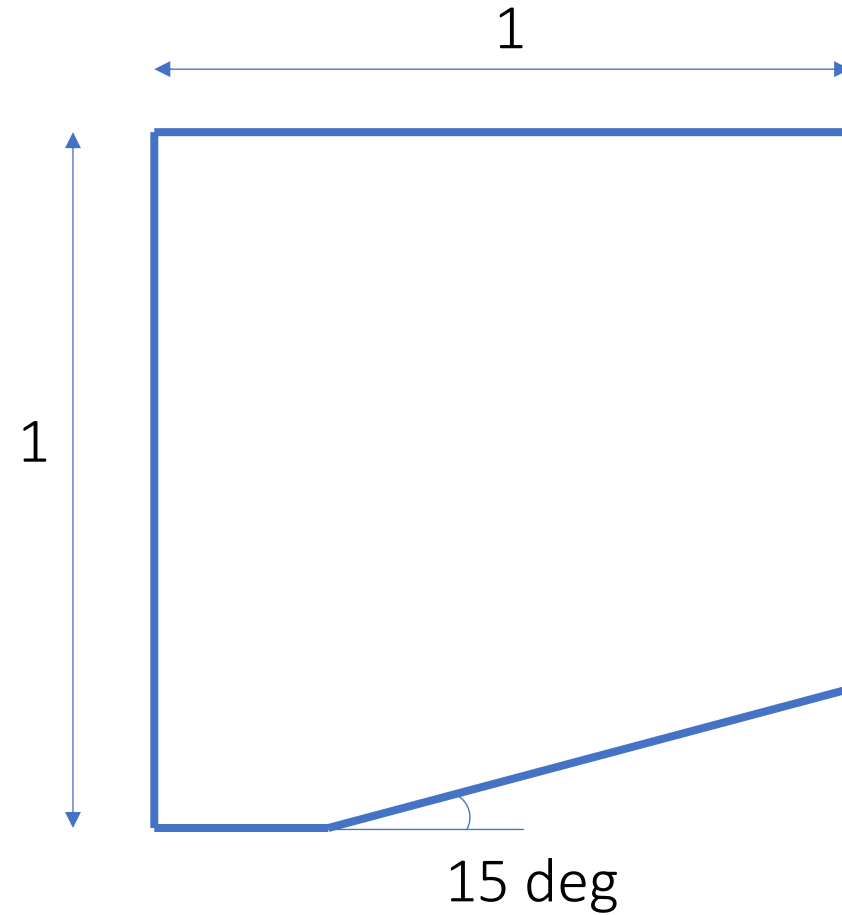
- Objective: minimize total pressure loss for optimal performance

FV solver setup

- Geometry
- Mesh
- IC and BC
- Flux reconstruction
- Time integration
- Results

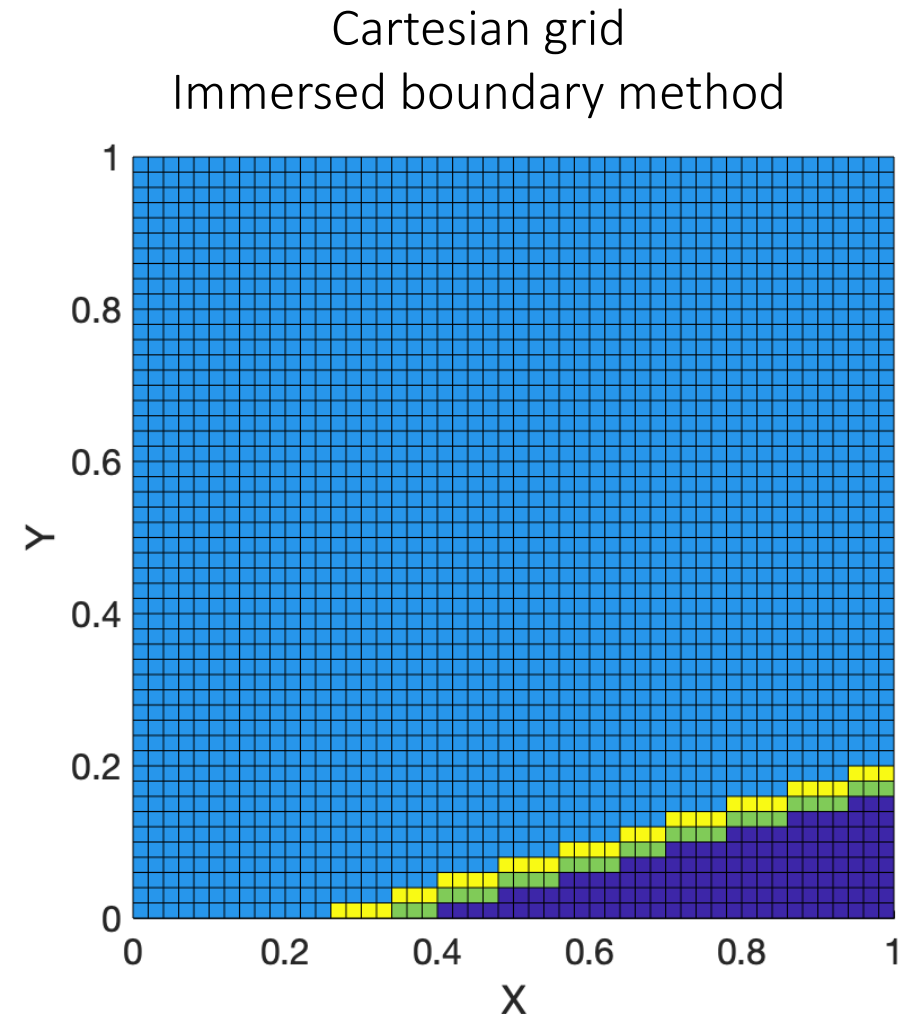
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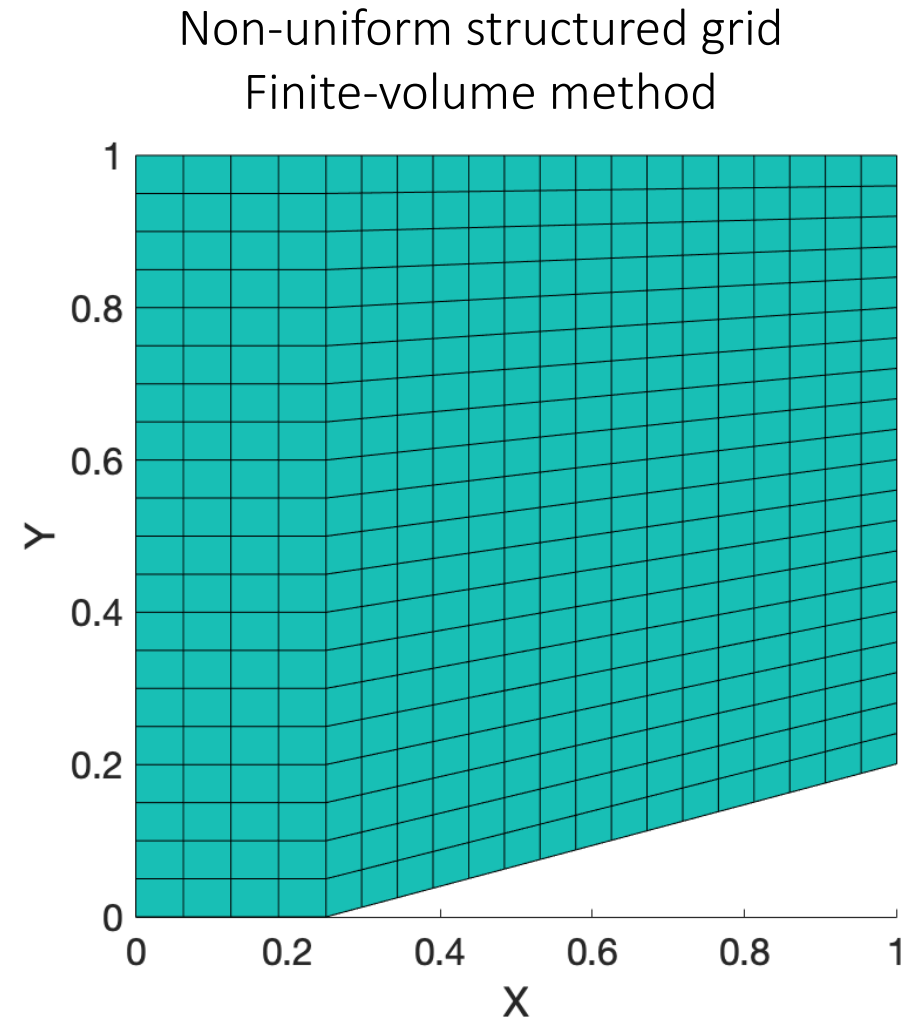
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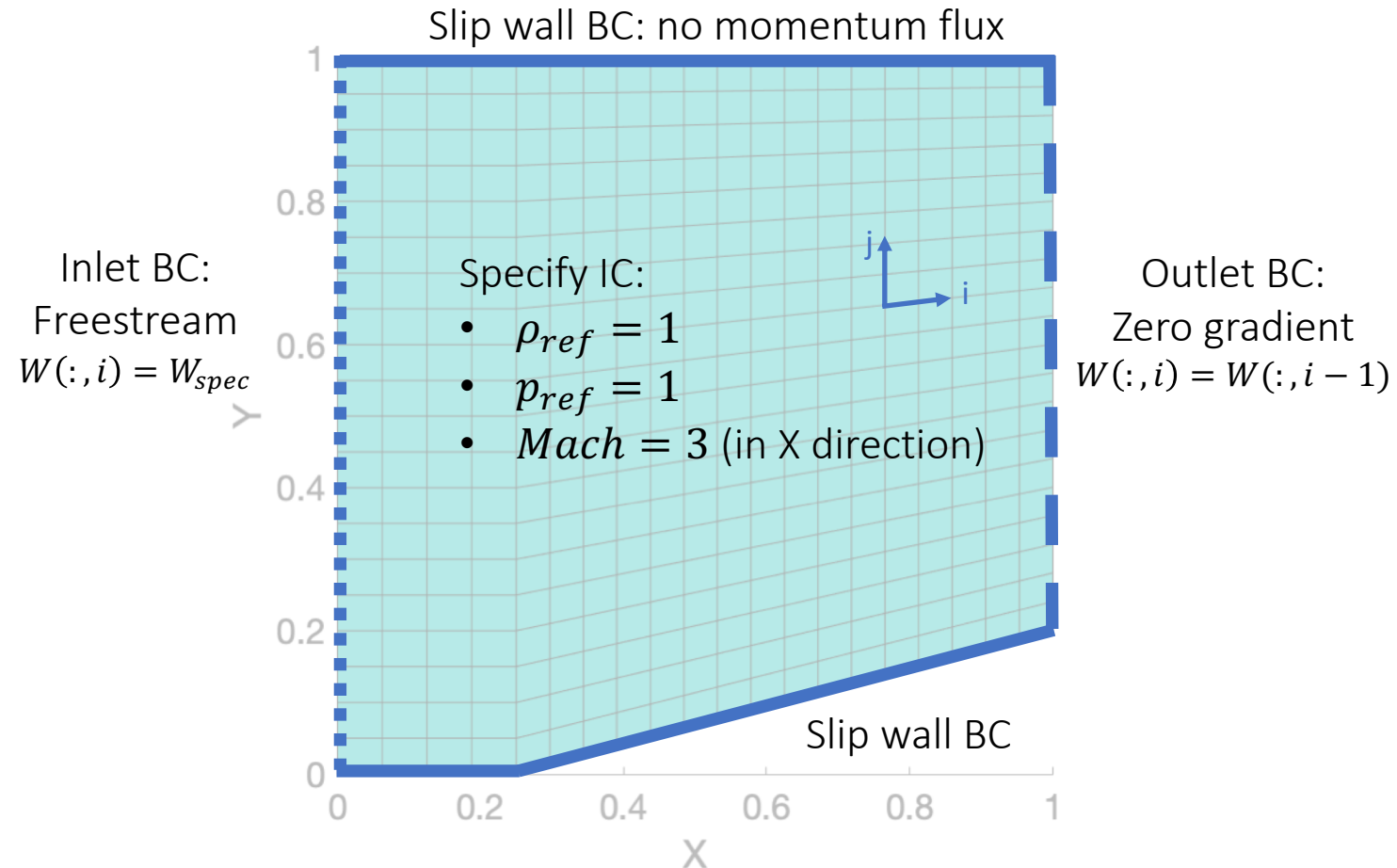
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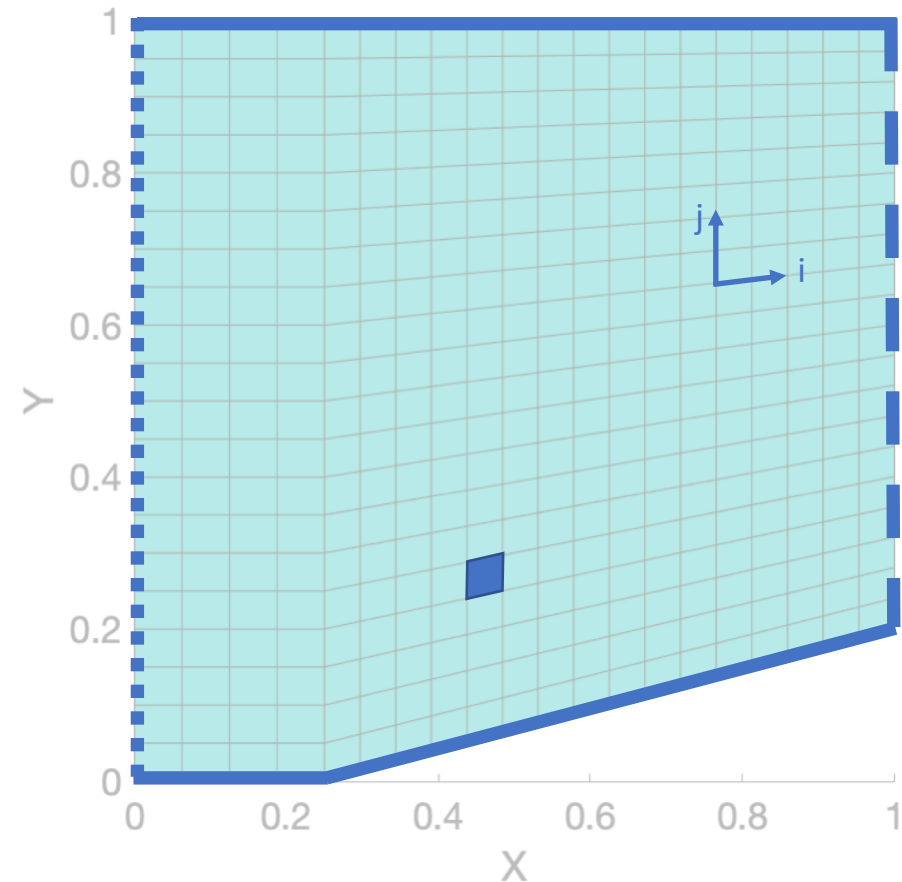
Solver setup

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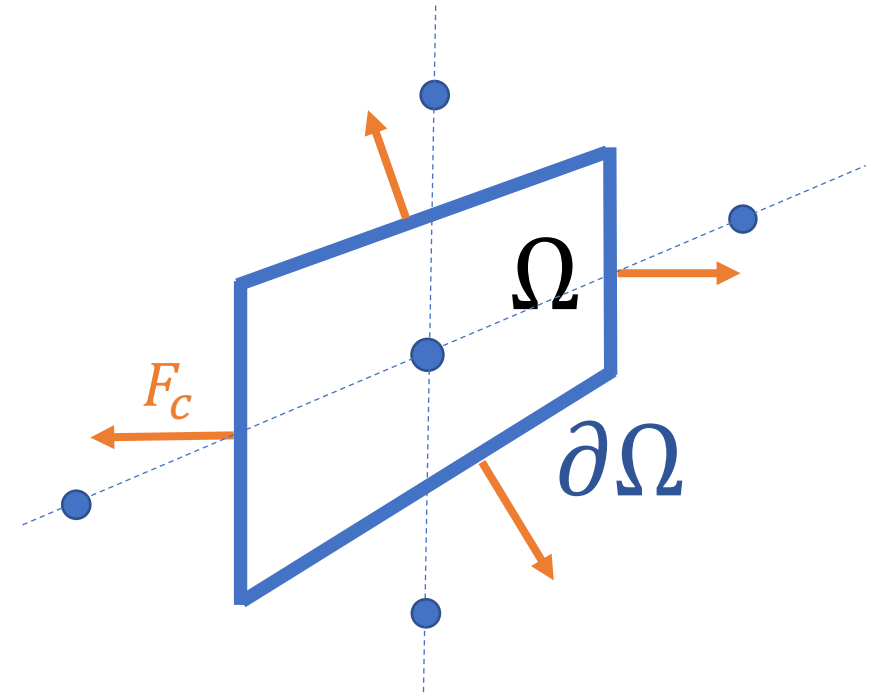


Flux reconstruction

- Equation of motion: Euler equations

$$\frac{\partial}{\partial t} \int_{\Omega} \bar{W} d\Omega + \oint_{\partial\Omega} \bar{F}_c \cdot \bar{n} dS = 0$$

$$\bar{W} = \begin{bmatrix} \rho \\ \rho u \\ \rho v \\ \rho e \end{bmatrix} \quad \text{and} \quad \bar{F}_c = \begin{bmatrix} \rho V \\ \rho u V + p e_x \\ \rho v V + p e_y \\ \rho(e + p/\rho)V \end{bmatrix} \quad \text{with} \quad V = \begin{bmatrix} u \\ v \end{bmatrix} \cdot \begin{bmatrix} n_x \\ n_y \end{bmatrix}$$



- Flux calculation at face:

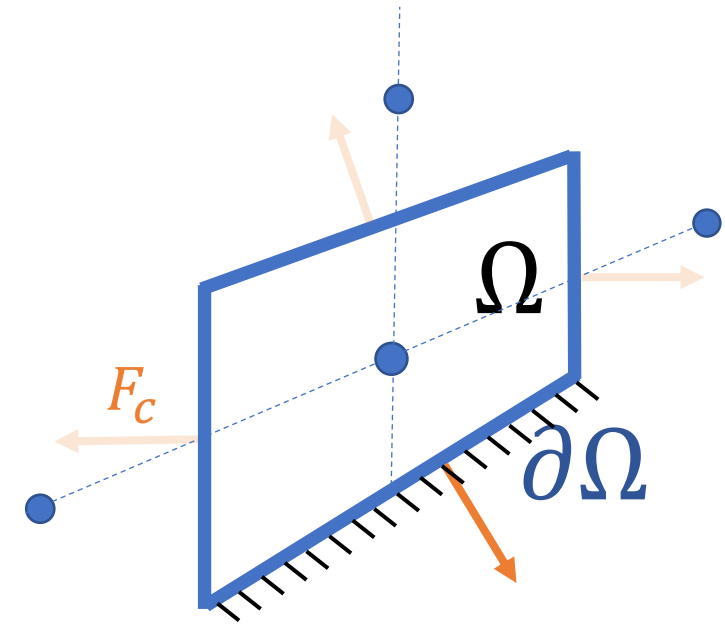
$$F_{\phi} = \left(\frac{u_{up} - u_{down}}{2} \right) \left[\left(\frac{1}{2} + \epsilon \right) \cdot \phi_{up} + \left(\frac{1}{2} - \epsilon \right) \cdot \phi_{down} \right] \quad \begin{cases} \epsilon \in [0, 0.5] & \text{if } \frac{u_{up} - u_{down}}{2} \geq 0 \\ \epsilon \in [-0.5, 0] & \text{if } \frac{u_{up} - u_{down}}{2} < 0 \end{cases}$$

- Upwind ($\epsilon = 0.5$) \approx smoothing due to 2nd order derivative in truncation error

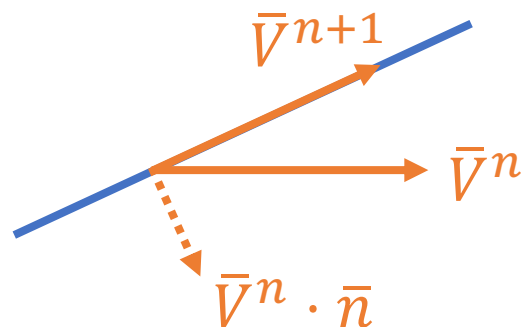
Flux reconstruction

- Flux reconstruction at slip wall boundary

$$\bar{W} = \begin{bmatrix} \rho \\ \rho u \\ \rho v \\ \rho e \end{bmatrix} \quad \text{and} \quad \bar{F}_c = \begin{bmatrix} \cancel{\rho v} \\ \cancel{\rho u v} + p e_x \\ \cancel{\rho v v} + p e_y \\ \cancel{\rho (e + p/\rho) v} \end{bmatrix} \quad \text{with} \quad V = \begin{bmatrix} u \\ v \end{bmatrix} \cdot \begin{bmatrix} n_x \\ n_y \end{bmatrix}$$



- After update $\bar{W}^n \rightarrow \bar{W}^{n+1}$: take out any normal component of velocity at the wall



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Steady solver: 3 step Runge-Kutta method (AERK3J) with pseudo time step

- 1st order accurate

$$\bar{W}_i^{(1)} = \bar{W}_i^{(n)} - 0.1481 \frac{\Delta t}{\Omega_i} \sum_{n=1}^{NF} (\bar{F}_n S_n)$$

$$\bar{W}_i^{(2)} = \bar{W}_i^{(n)} - 0.4 \frac{\Delta t}{\Omega_i} \sum_{n=1}^{NF} (\bar{F}_n S_n)$$

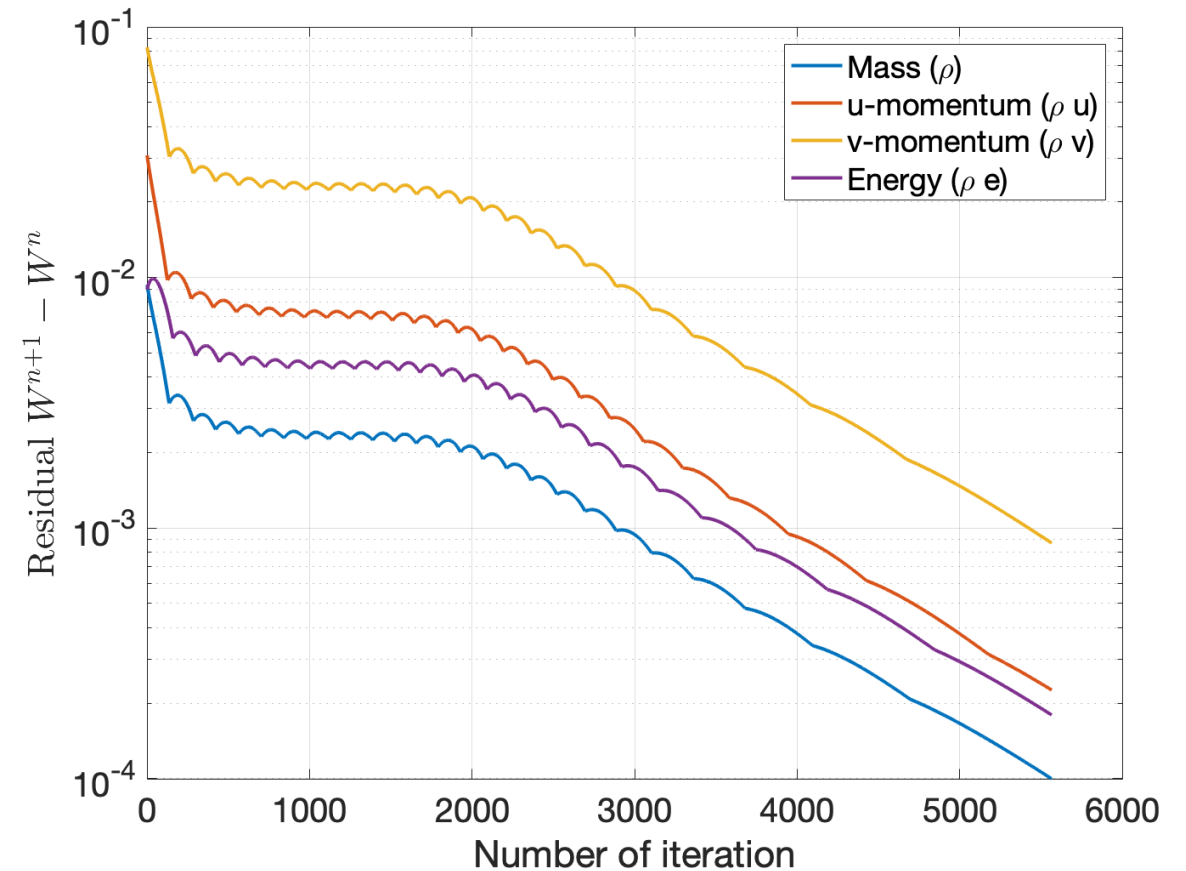
$$\bar{W}_i^{(n+1)} = \bar{W}_i^{(n)} - 1.0 \frac{\Delta t}{\Omega_i} \sum_{n=1}^{NF} (\bar{F}_n S_n)$$

- Stopping criterium: residuals

$$\bar{W}^{n+1} - \bar{W}^n < tol \quad with \quad tol = 10^{-3}$$

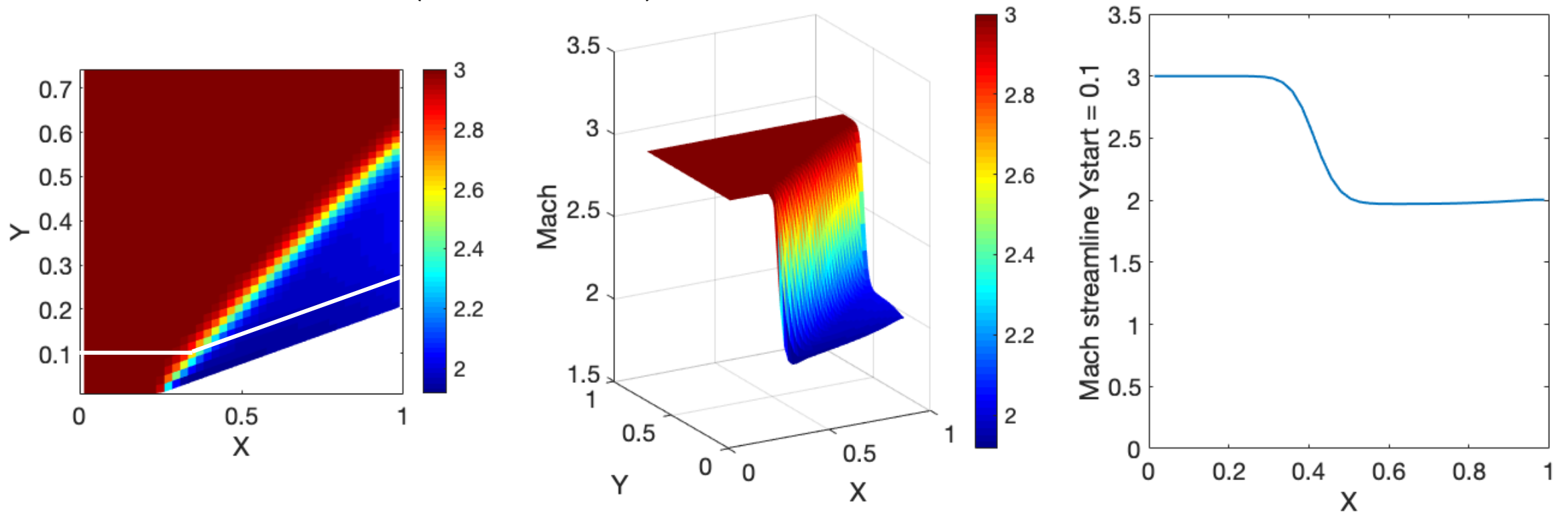
Results

Rate of convergence of the solver
(mesh: 40x40)



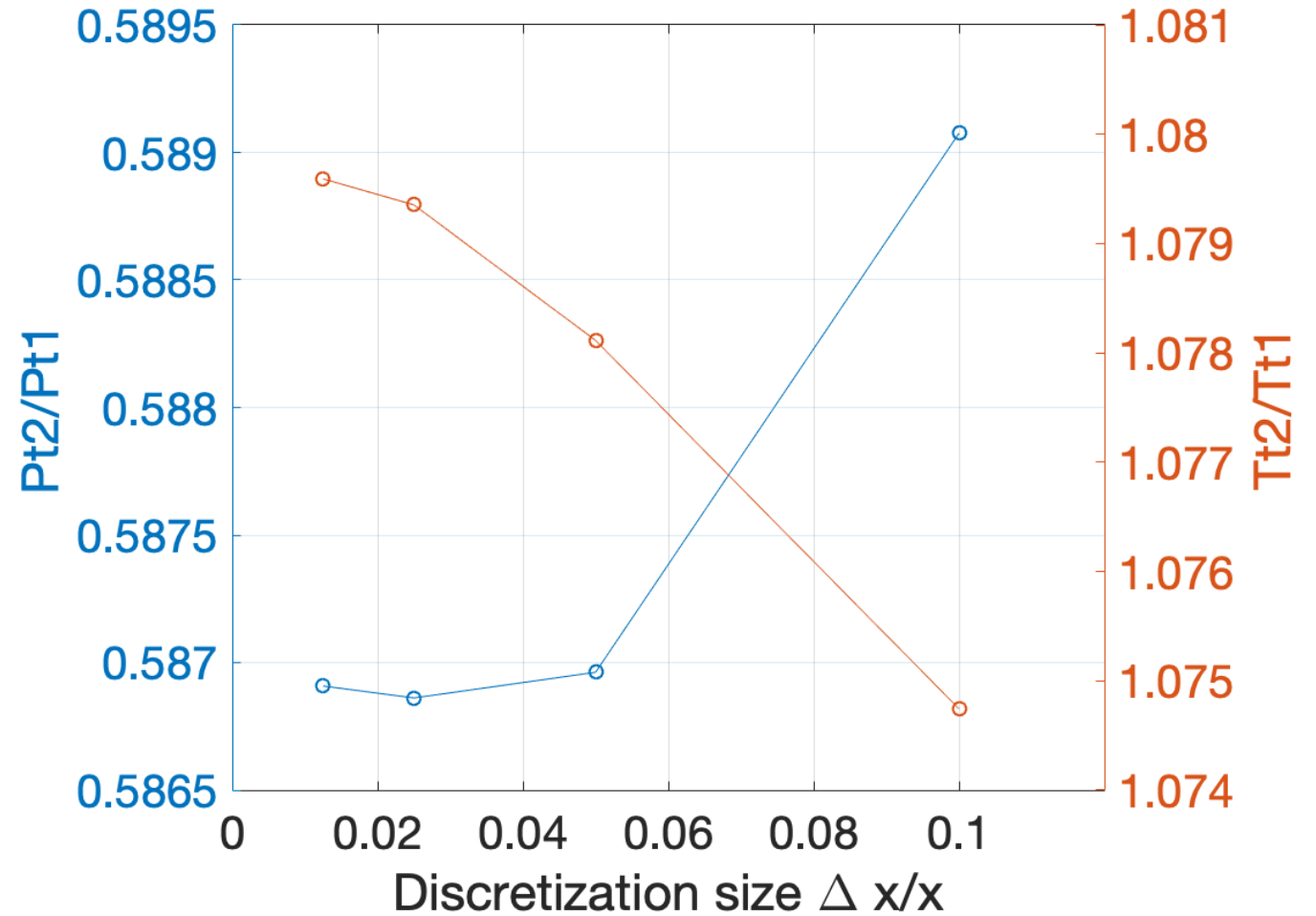
Results

Mach in fluid domain (mesh: 40x40)

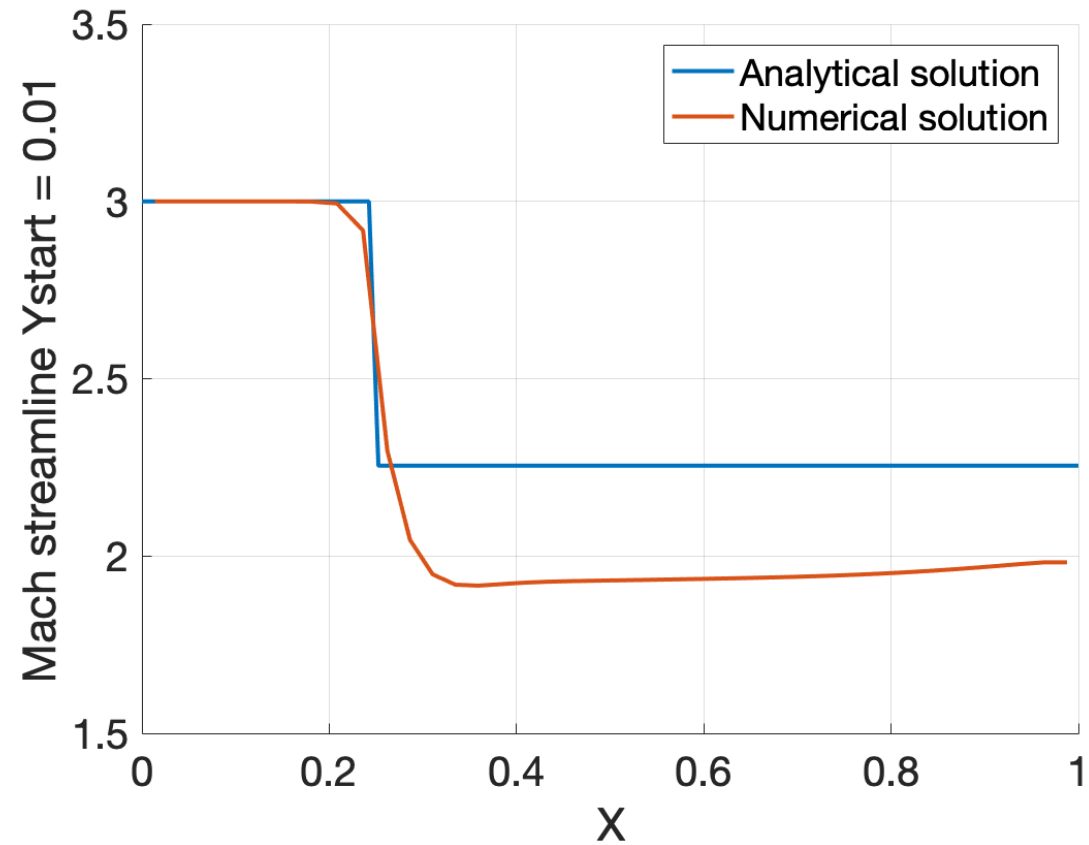


Results

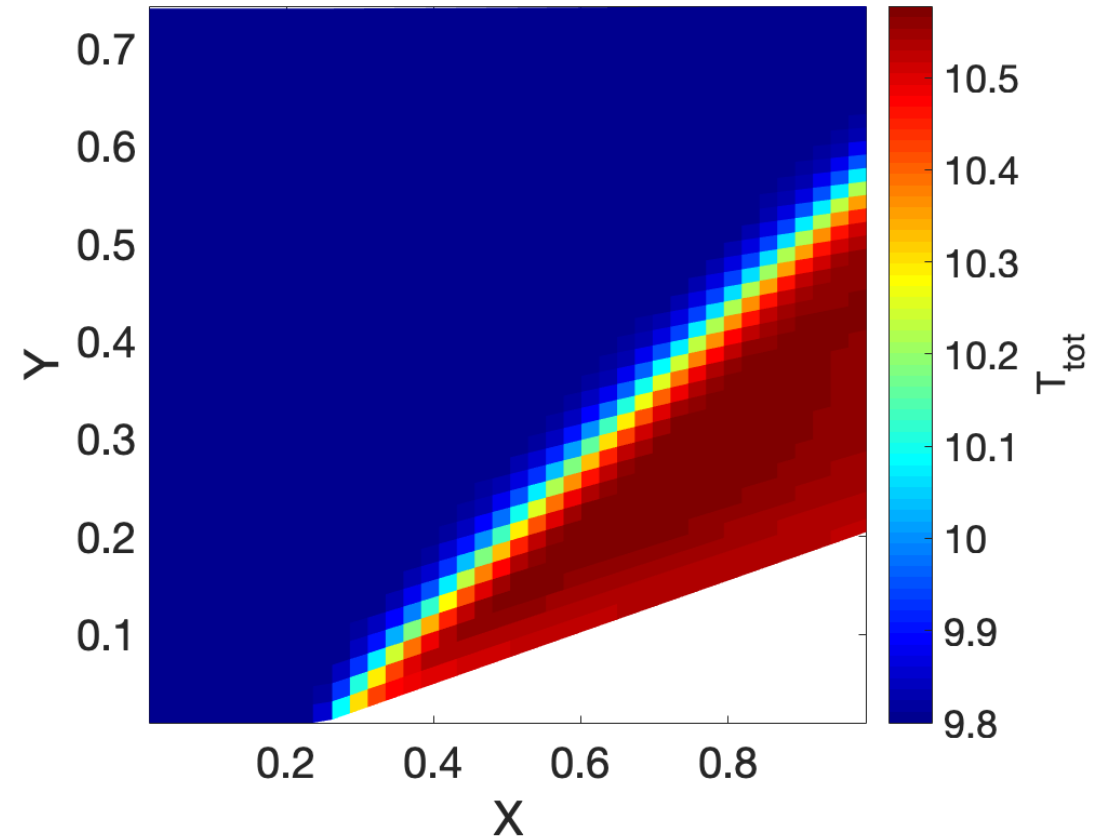
Mesh convergence



Results



$$\frac{T_{t2}}{T_{t1}} \leq 1.08$$



Future work

Debug the code to get closer to analytical solution

Model Prandtl-Meyer expansion fan

Calculate engine inlet geometry

Optimize geometry for total pressure loss

Questions

