

3D Optics

2D Optics



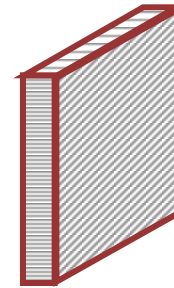
lenses



gratings

Light interacts with medium
on a sequence of
discrete surfaces

3D Optics



GRadiant INdex optics
(GRIN)

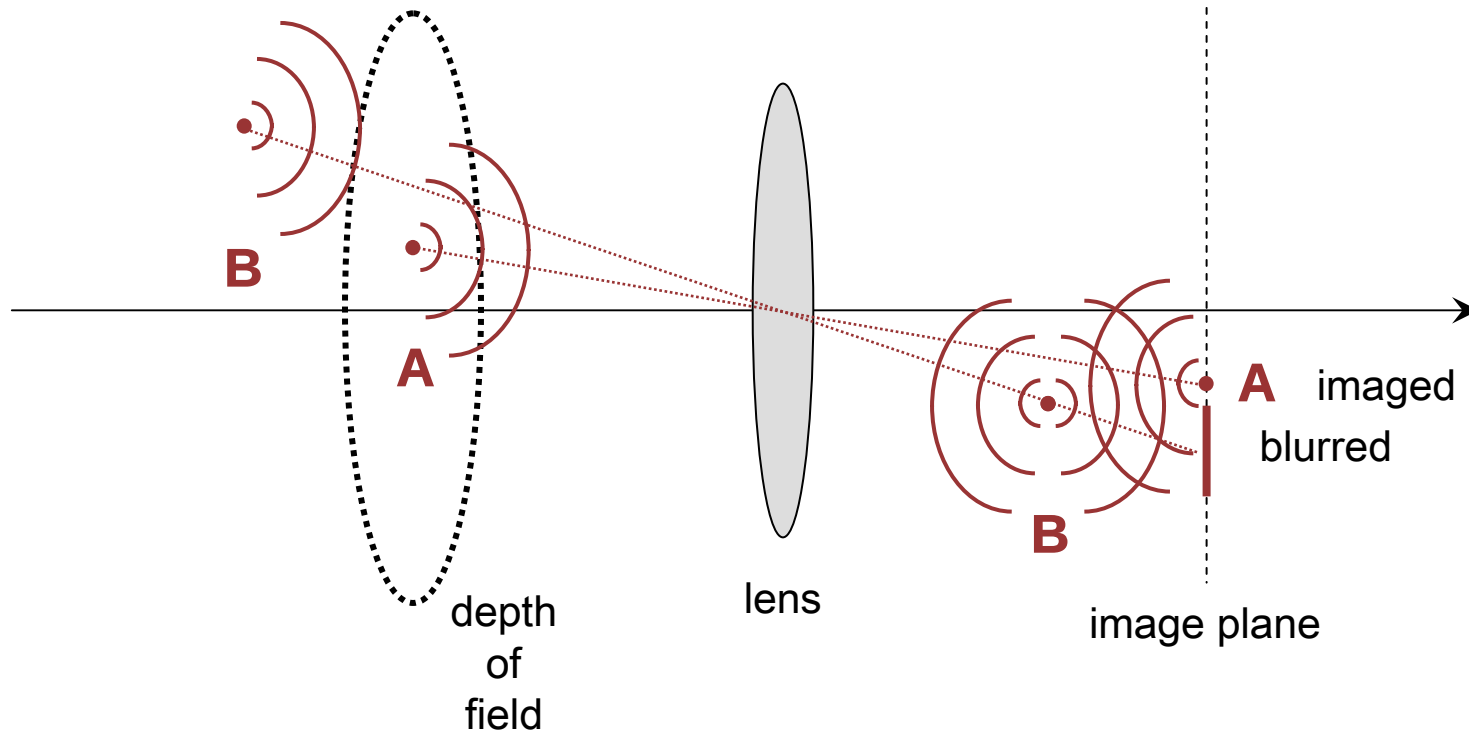
Volume
Holograms

Light interacts with medium
throughout a volume

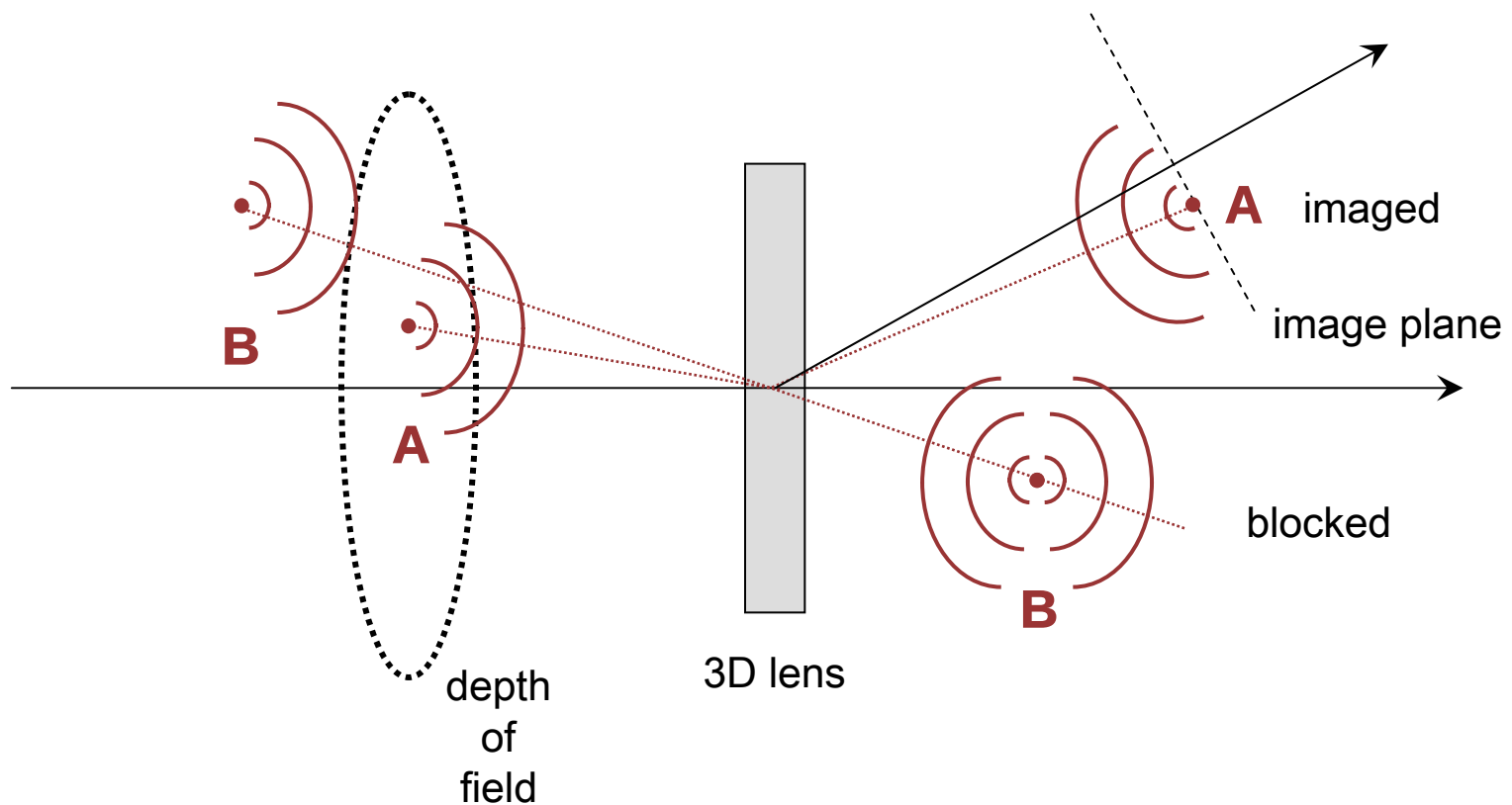




Imaging with traditional lenses

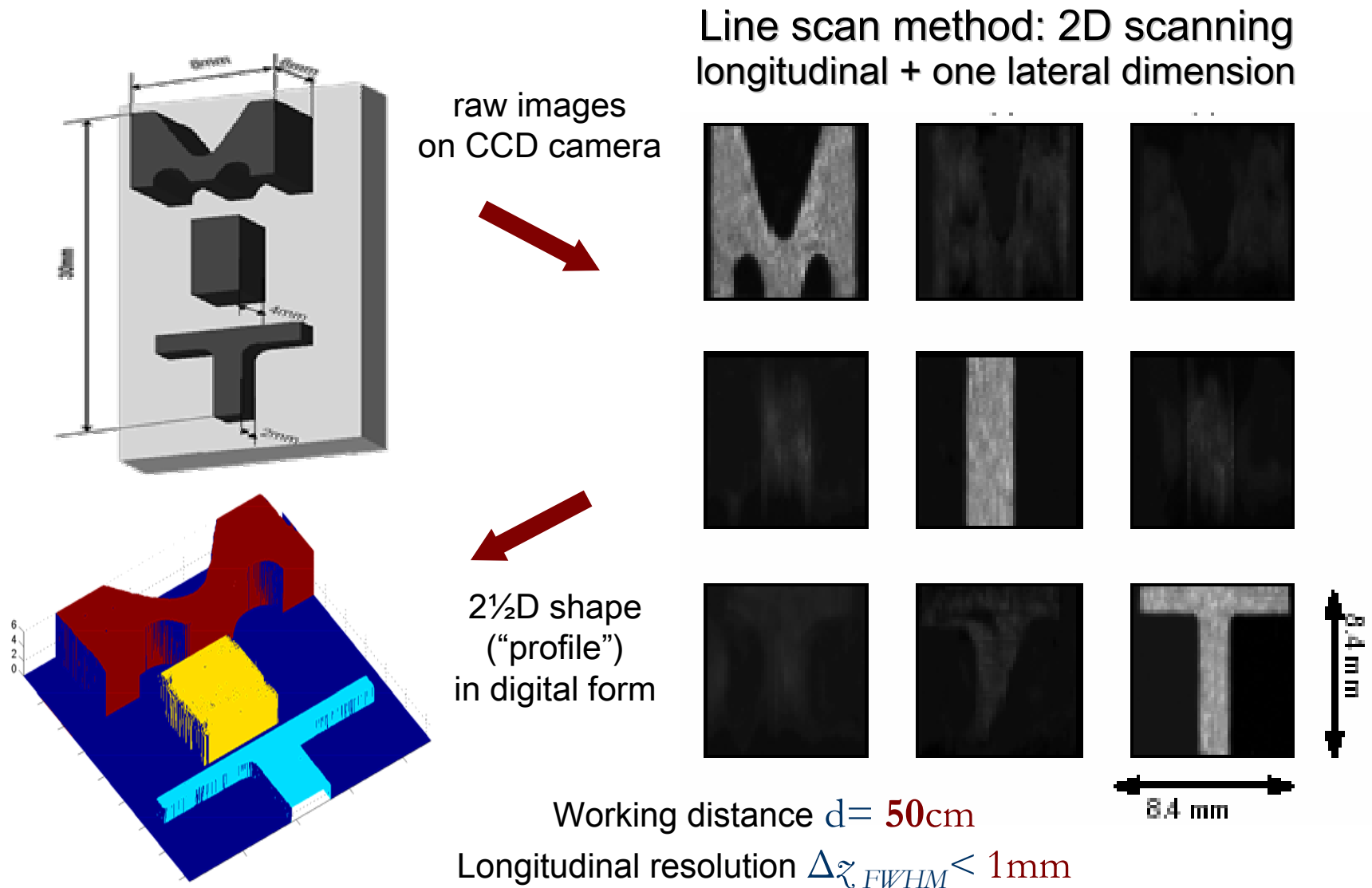


Imaging with 3D lenses



Defocus $\Leftrightarrow$ Contrast

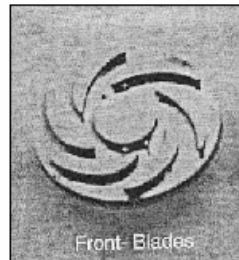
Shape recovery (“profilometry”) with 3D lenses



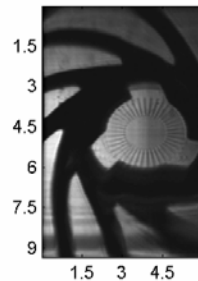
Shape recovery (“profilometry”) with 3D lenses

Arnab Sinha, George Barbastathis
MIT 3D Optical Systems group
Optics Express **11**:3202, 2003

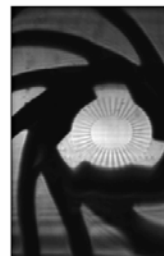
original
object



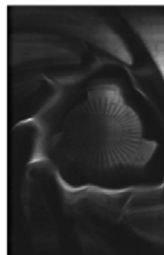
raw images



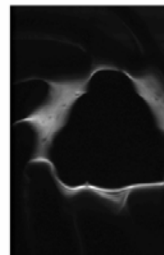
$z=0 \mu\text{m}$



$z=50 \mu\text{m}$



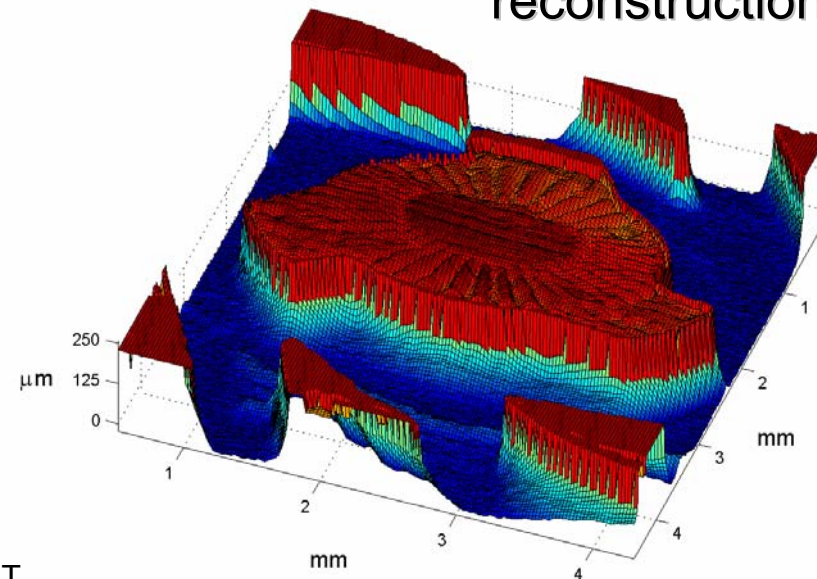
$z=200 \mu\text{m}$



$z=250 \mu\text{m}$

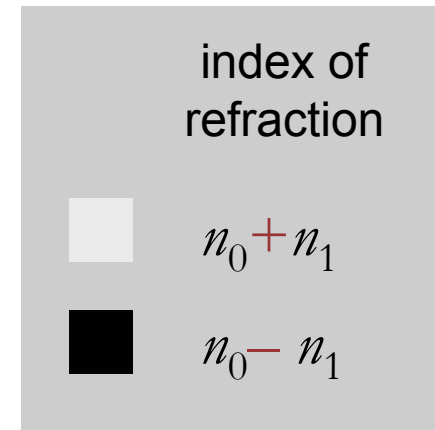
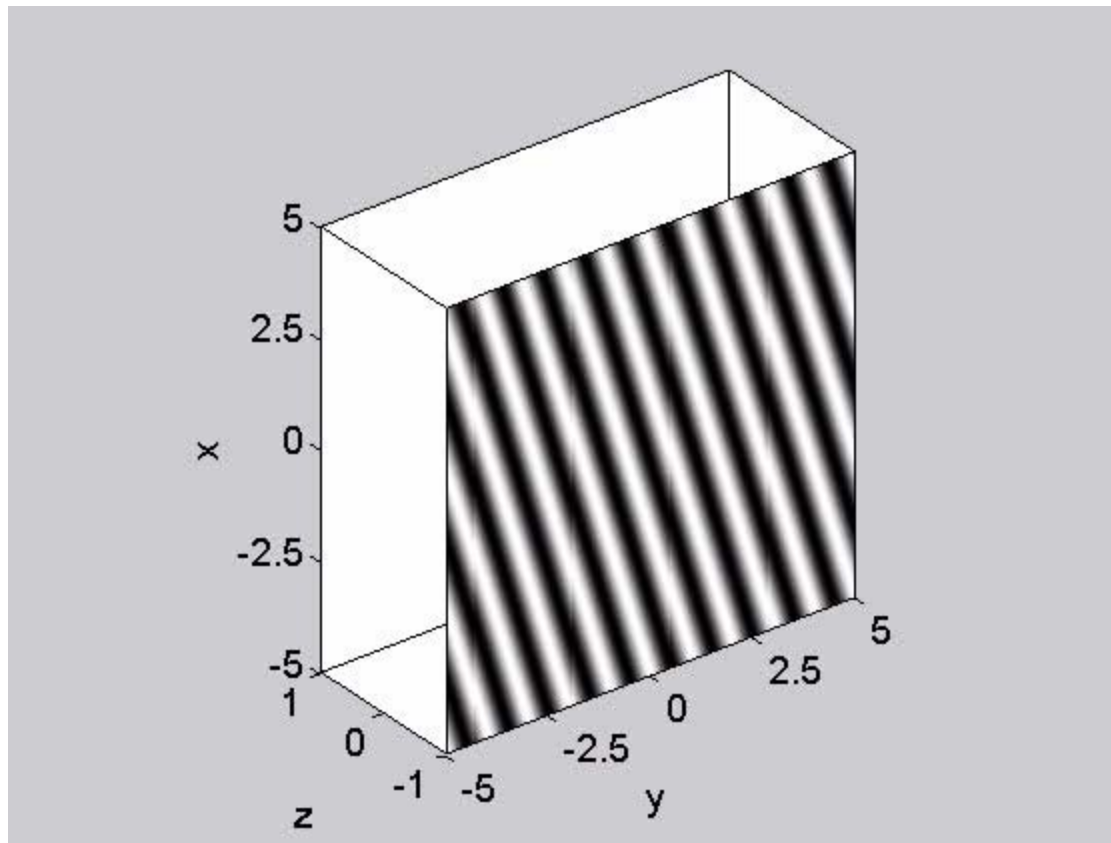
Object Distance = 46 cm
Resolution accomplished $\leq 100 \mu\text{m}$

profile
reconstruction



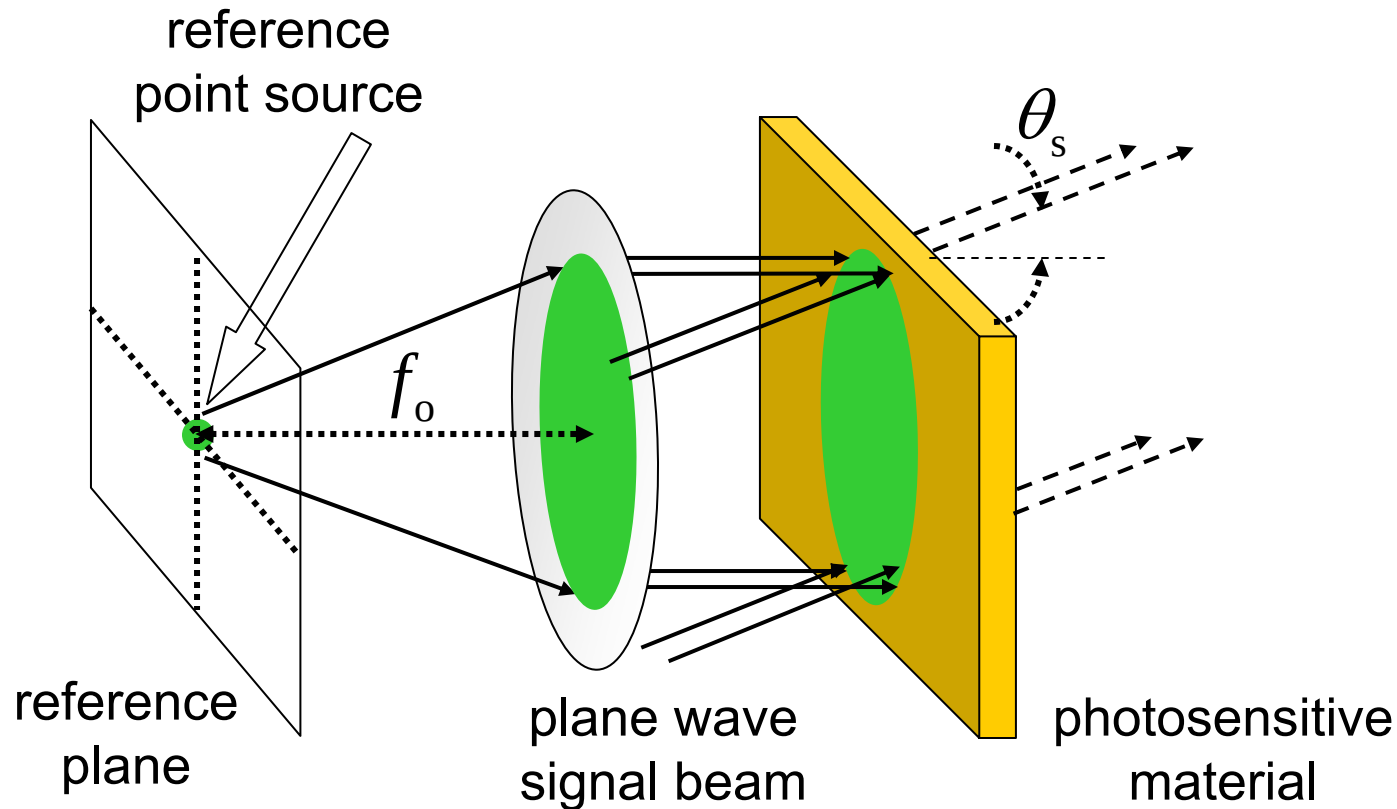
Microturbine provided by Chee Wei Wong, Alan Epstein, MIT

3D lens: plane-to-plane wave volume hologram



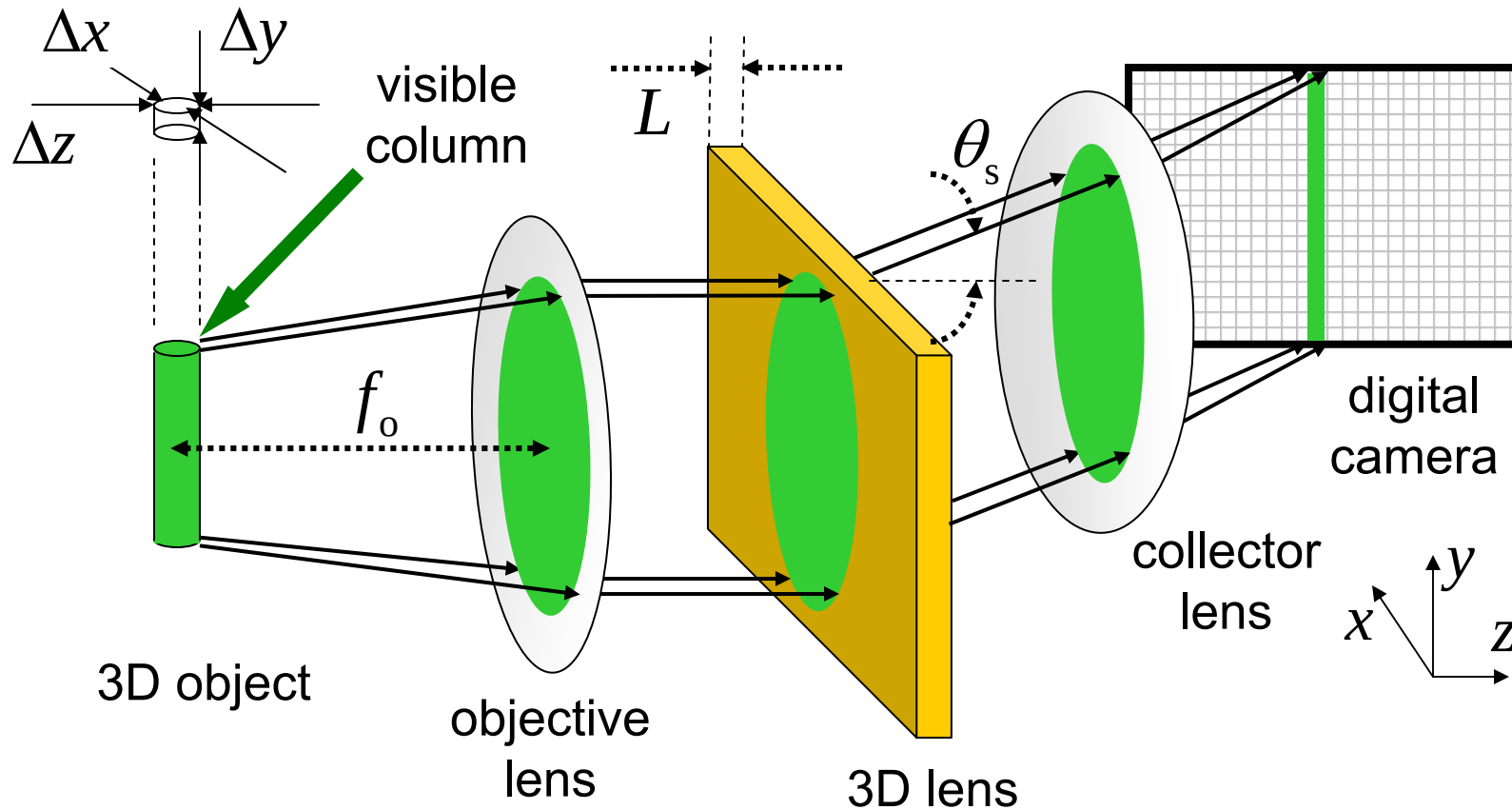
Making the (simplest) 3D lens

after exposure
$$n(\mathbf{r}) = n_0 + n_1 \cos[(\mathbf{k}_s - \mathbf{k}_r) \cdot \mathbf{r}]$$

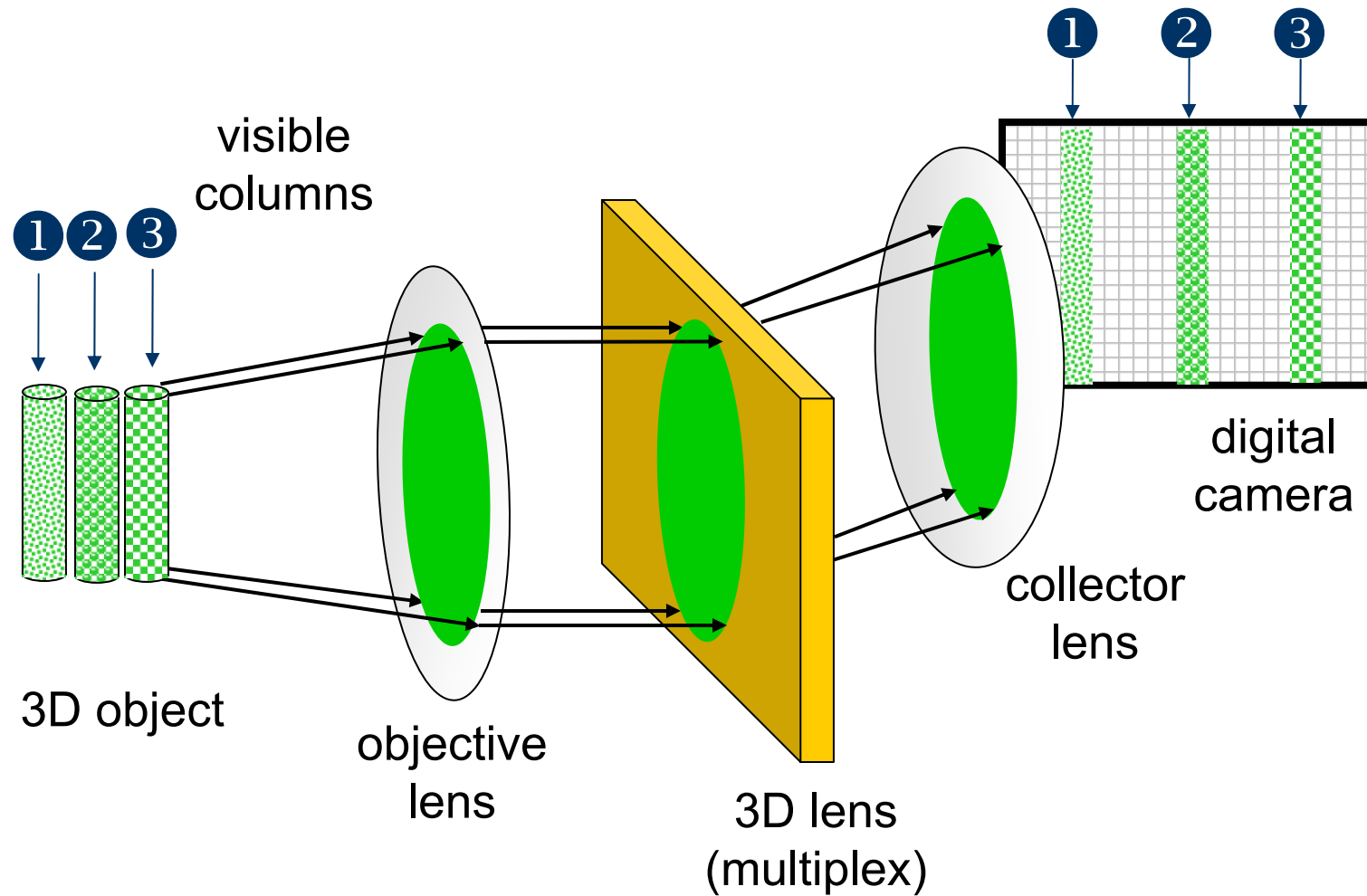


Operating the (simplest) 3D lens

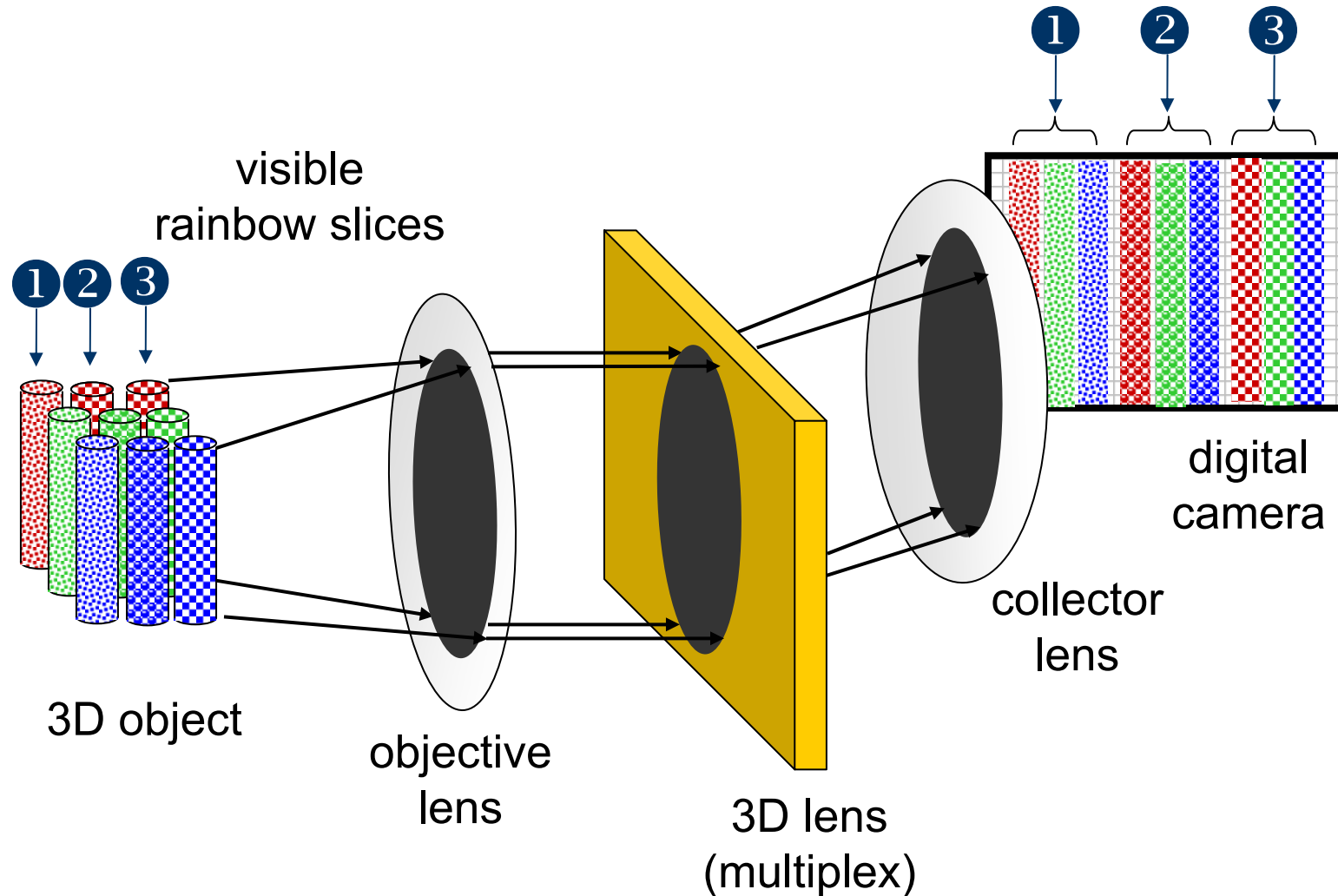
$$L \sim 100\mu\text{m} \div 1\text{mm}$$



Operating a multiplex 3D lens



Operating a hyperspectral multiplex 3D lens

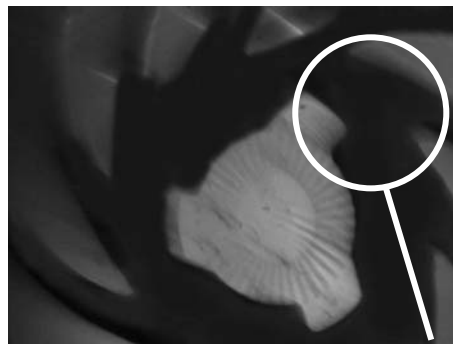


Rainbow volume holographic imaging

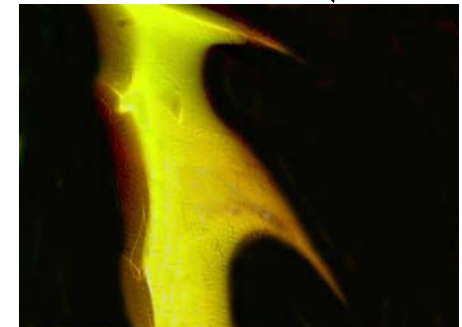
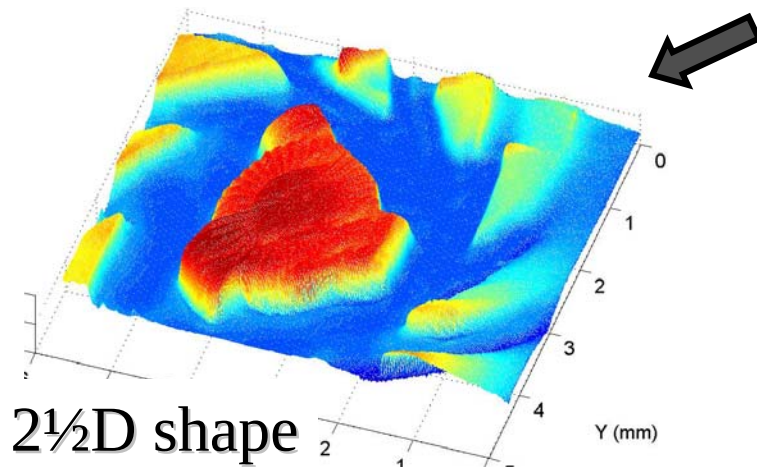
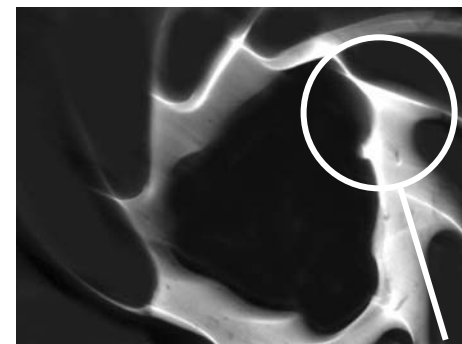
Wenyang Sun, George Barbastathis
MIT 3D Optical Systems group
Optics Letters **30**:976, 2005



slice #1

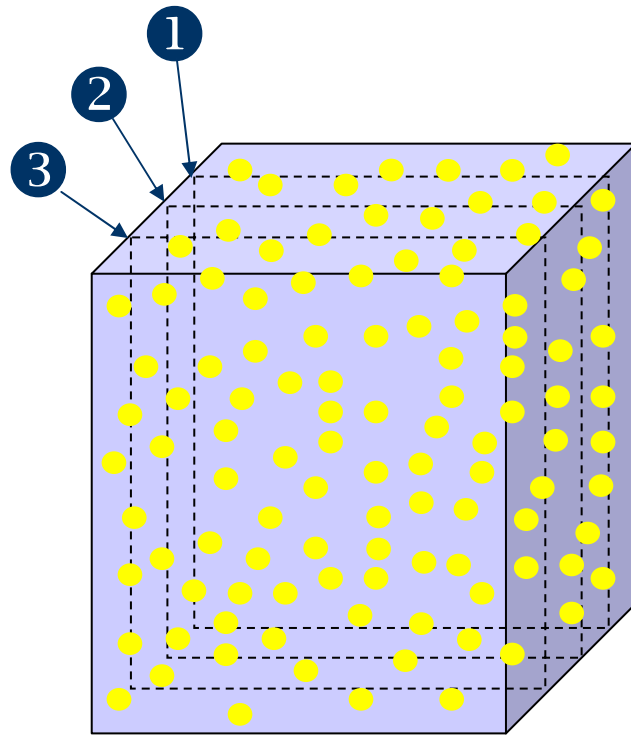


slice #2



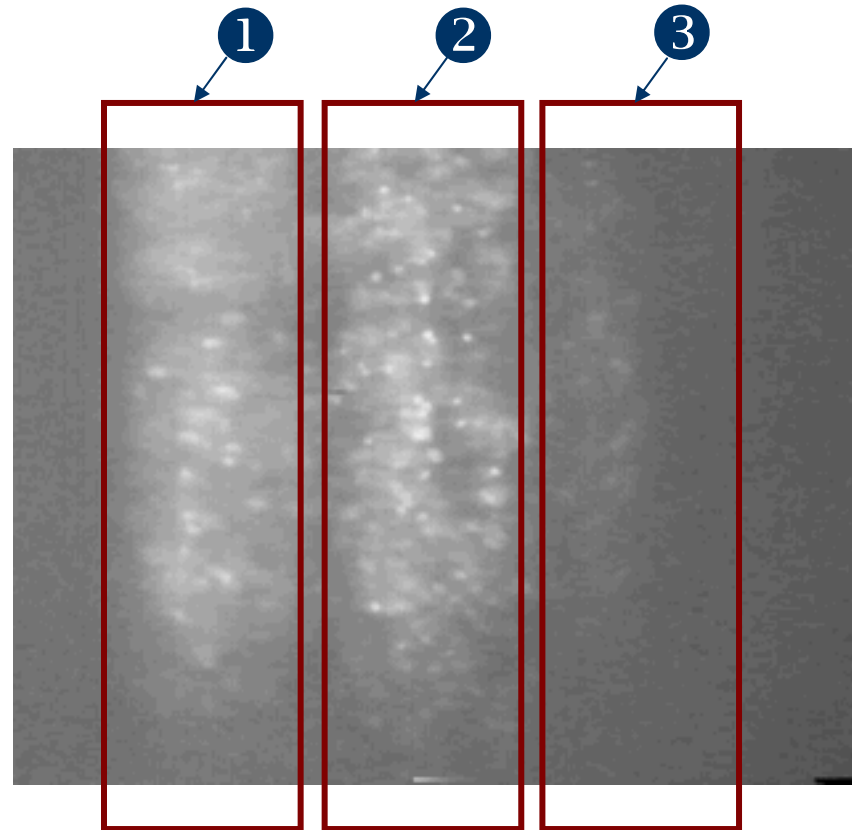
Multiplex imaging of 3D fluorescent object

three “slices” through
fluorescent (3D) object, stacked
along longitudinal direction ...



3D object:
fluorescent beads
in water

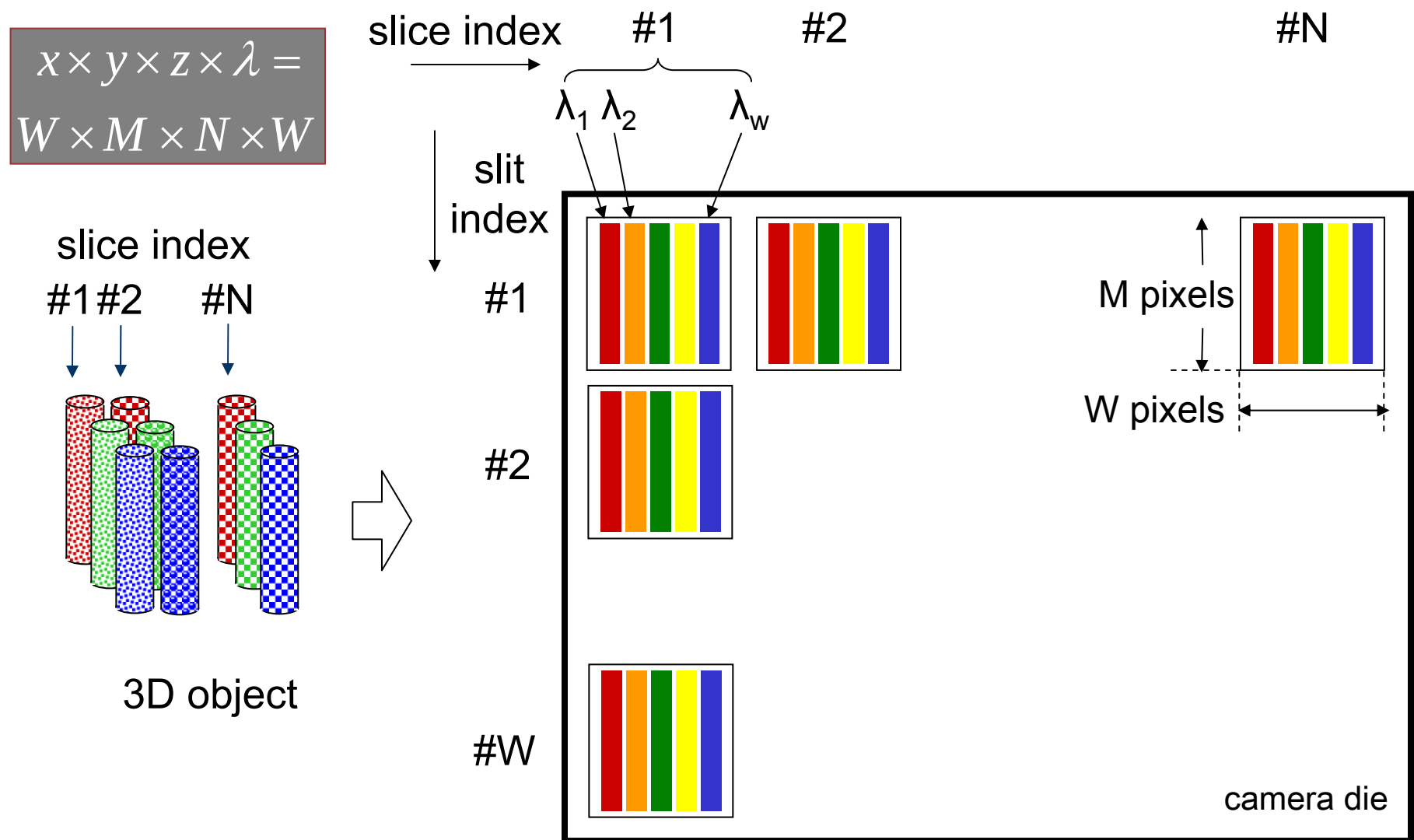
... are viewed **simultaneously** and **side-by-side**
on the digital camera



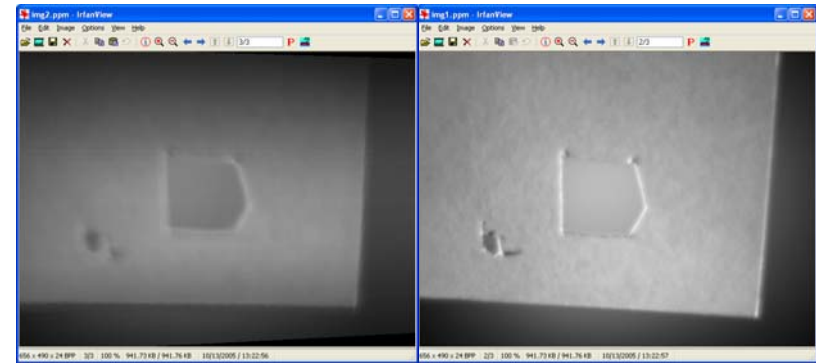
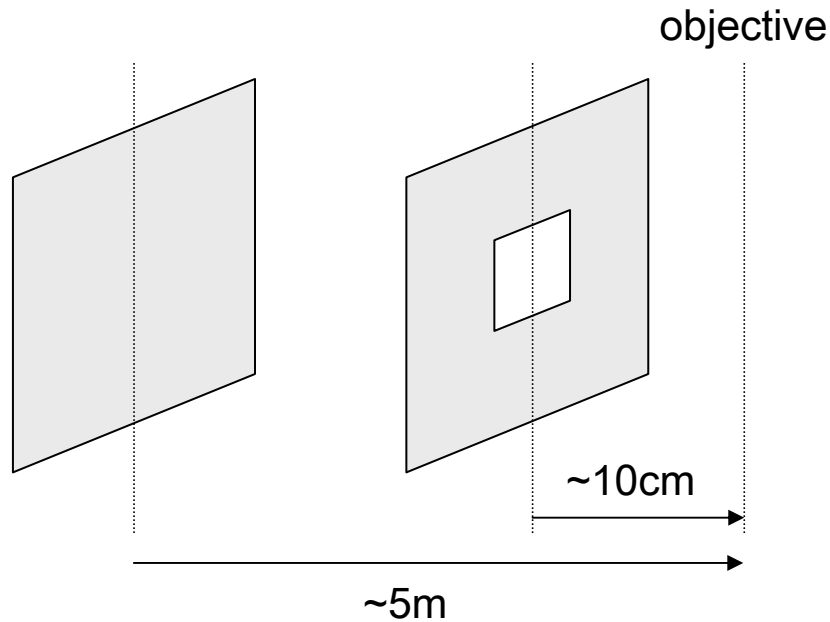
Wenhai Liu,* Demetri Psaltis,* George Barbastathis**

*Caltech Optical Info. Proc. group **MIT 3D Optical Systems group
Optics Letters 27:854, 2002

Camera pixel layout for 4D (3D spatial + spectral) imaging



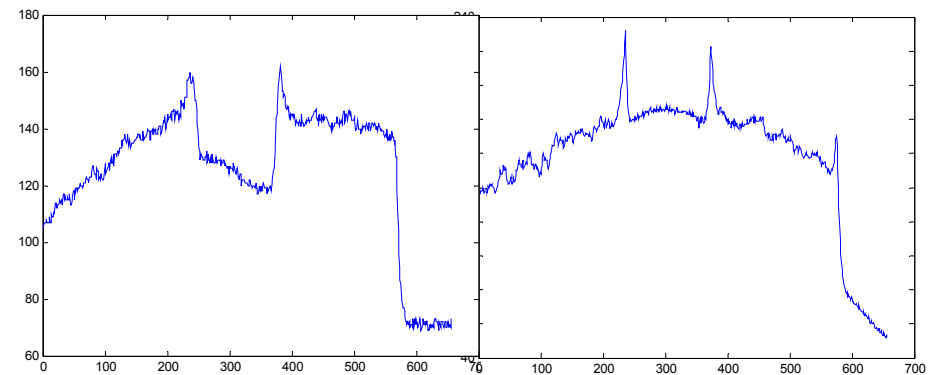
Sun Light (completely passive) illumination



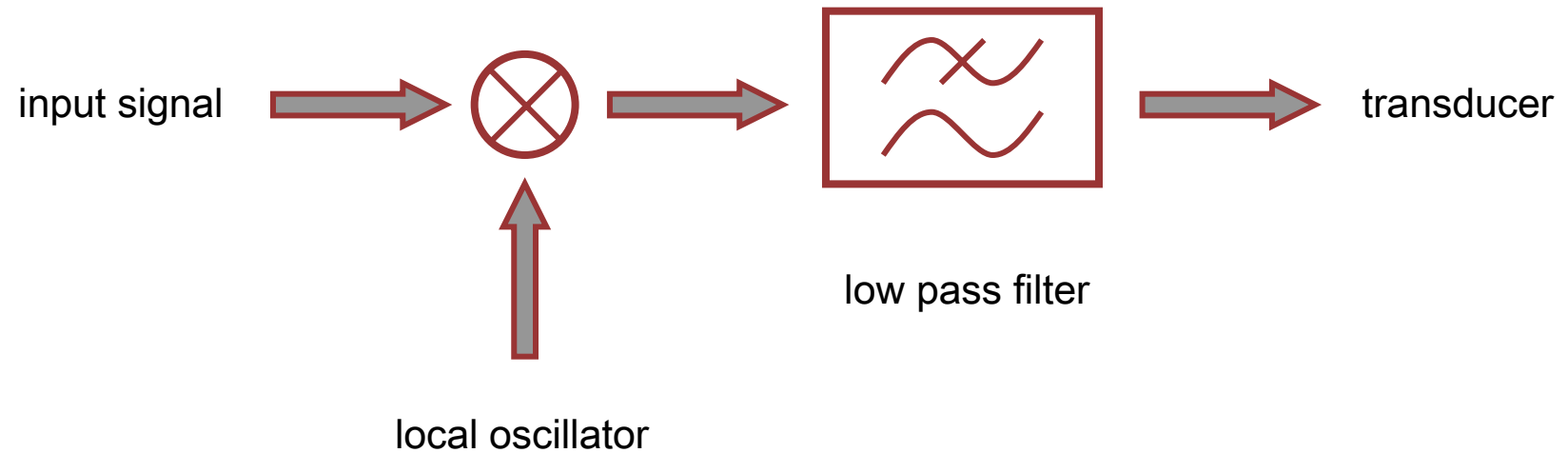
3D optical
image

traditional
camera

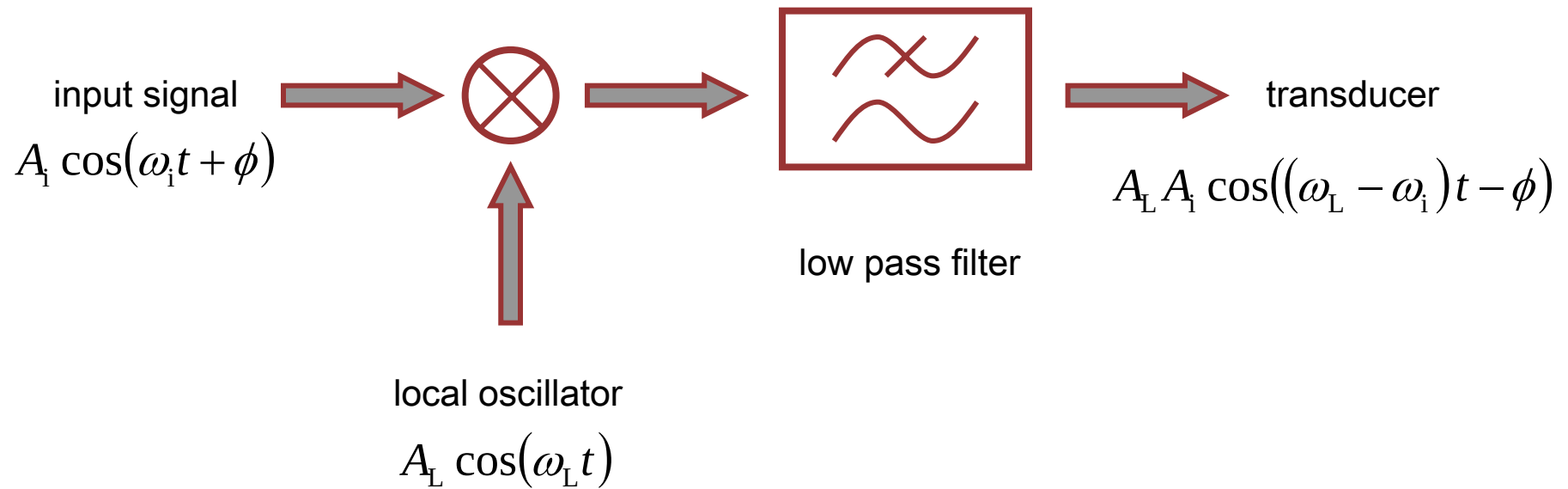
irradiance across
image cross-section



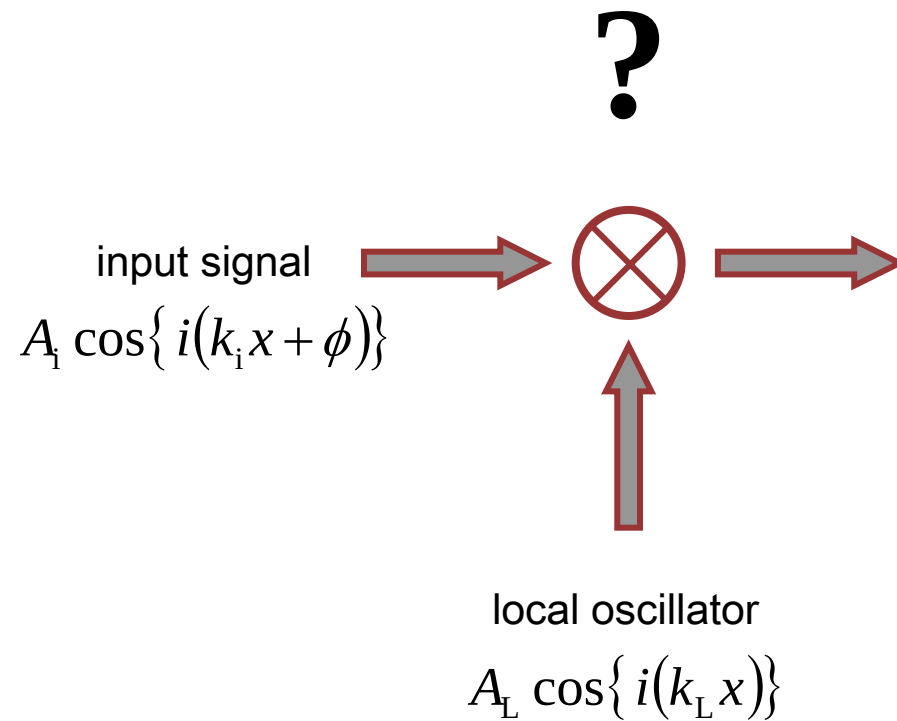
Temporal Heterodyning



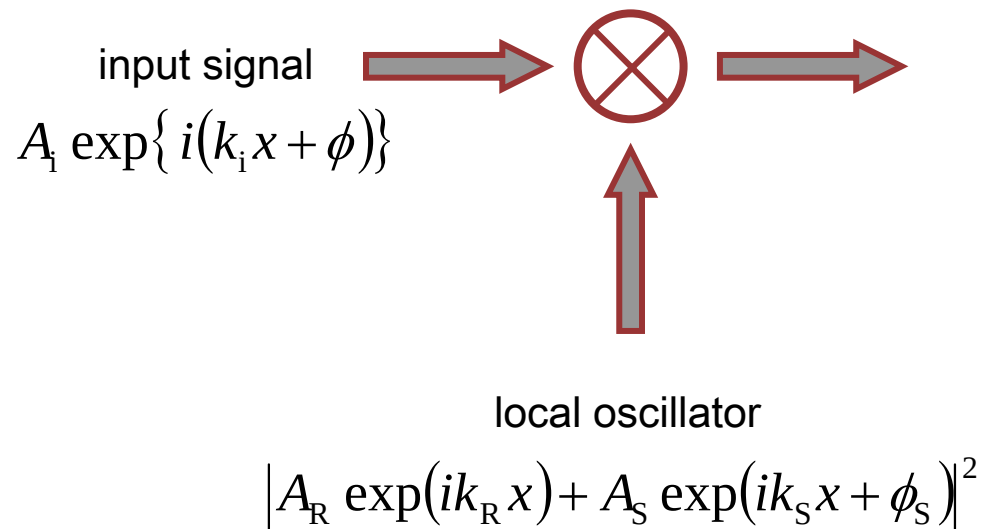
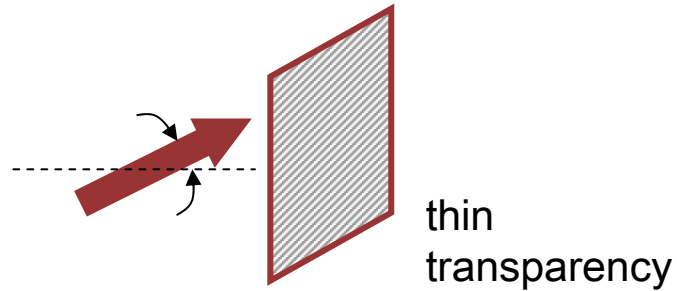
Temporal Heterodyning



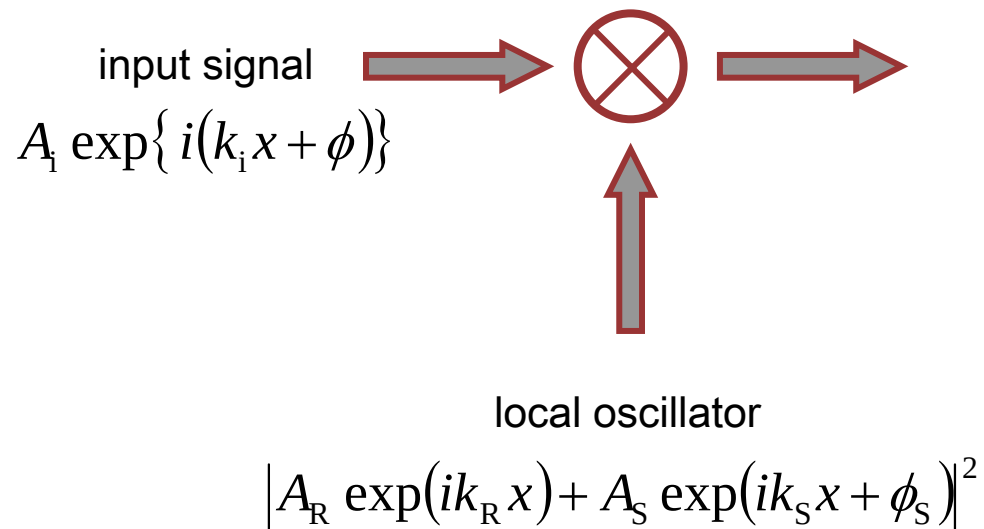
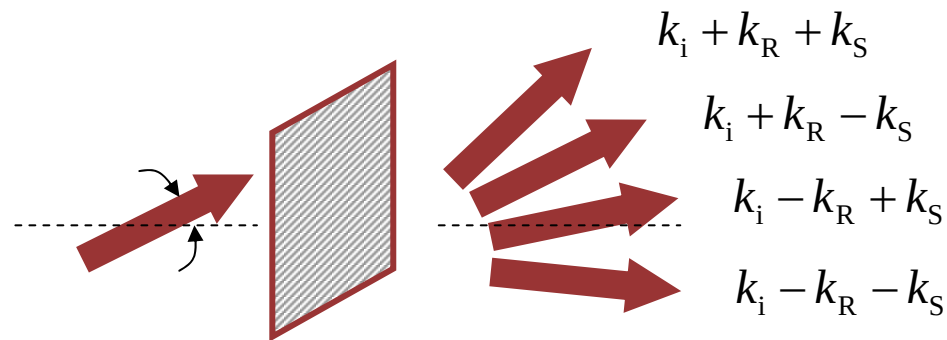
1D Spatial Heterodyning



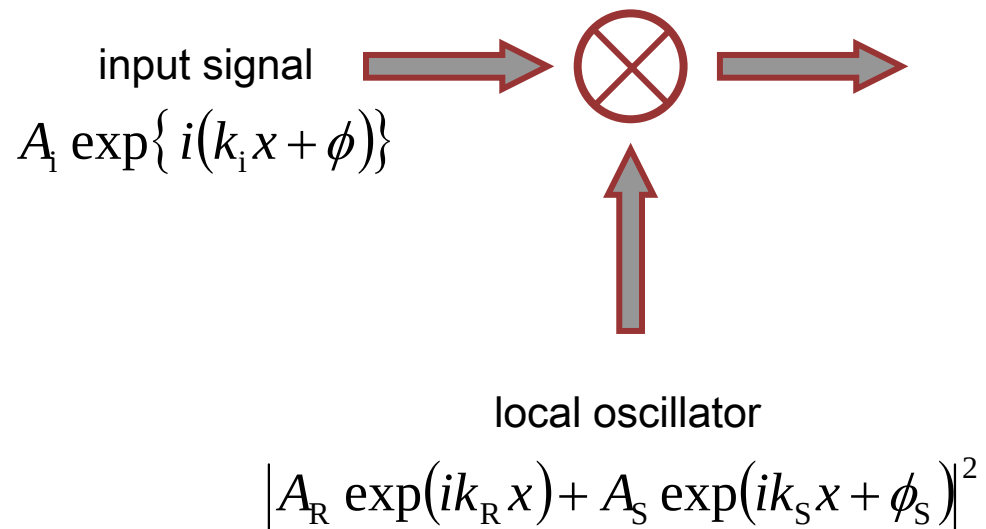
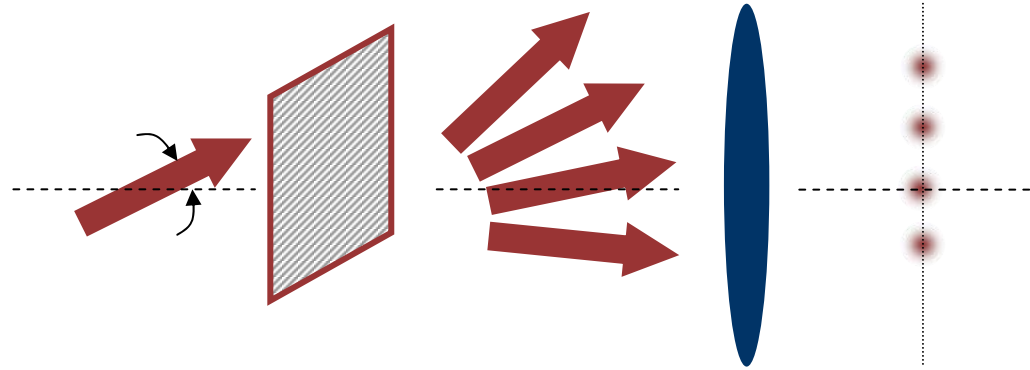
1D Spatial Heterodyning



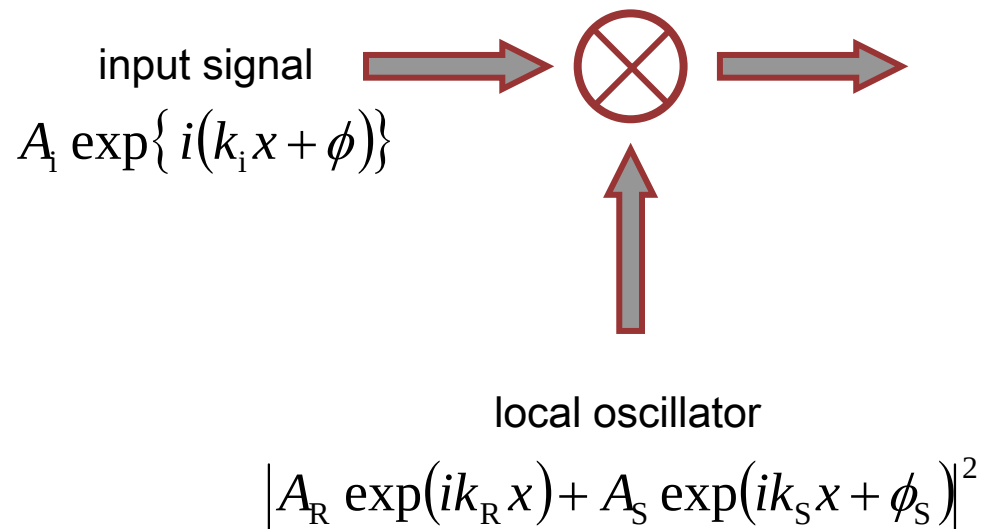
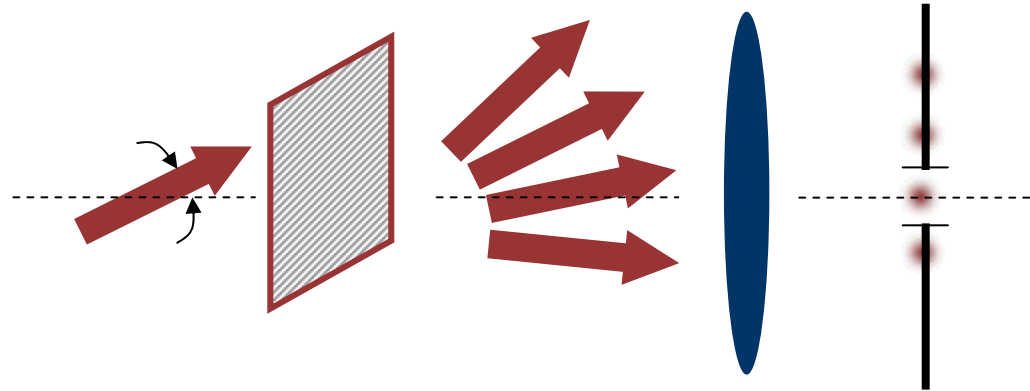
1D Spatial Heterodyning



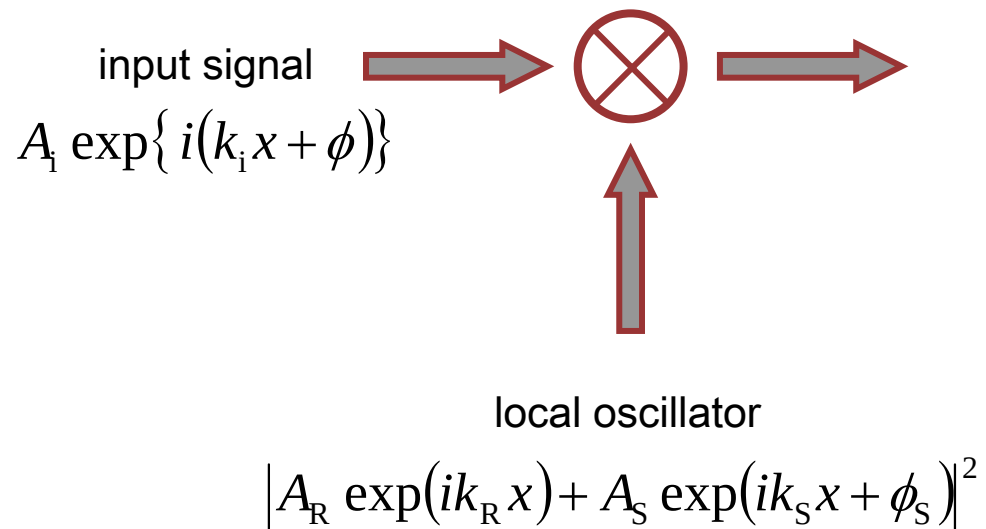
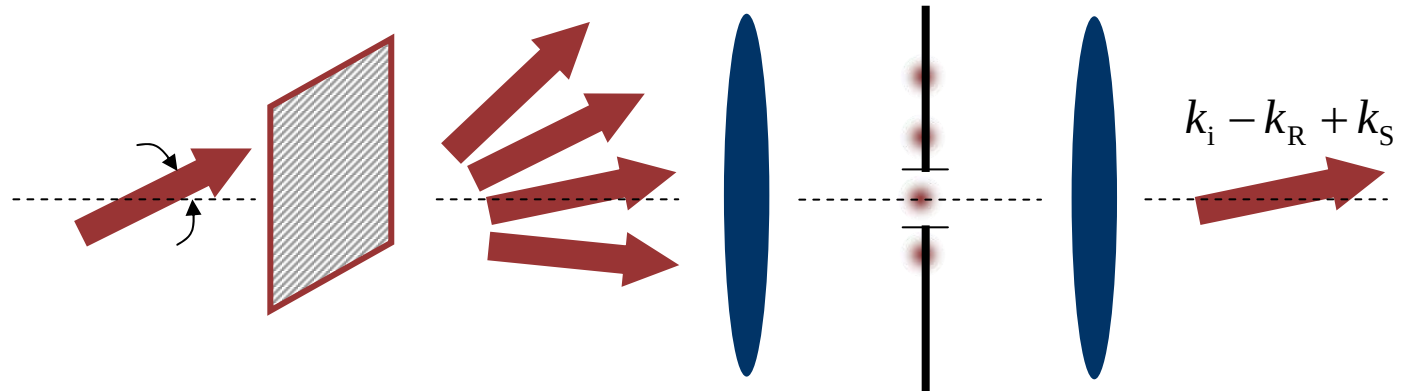
1D Spatial Heterodyning



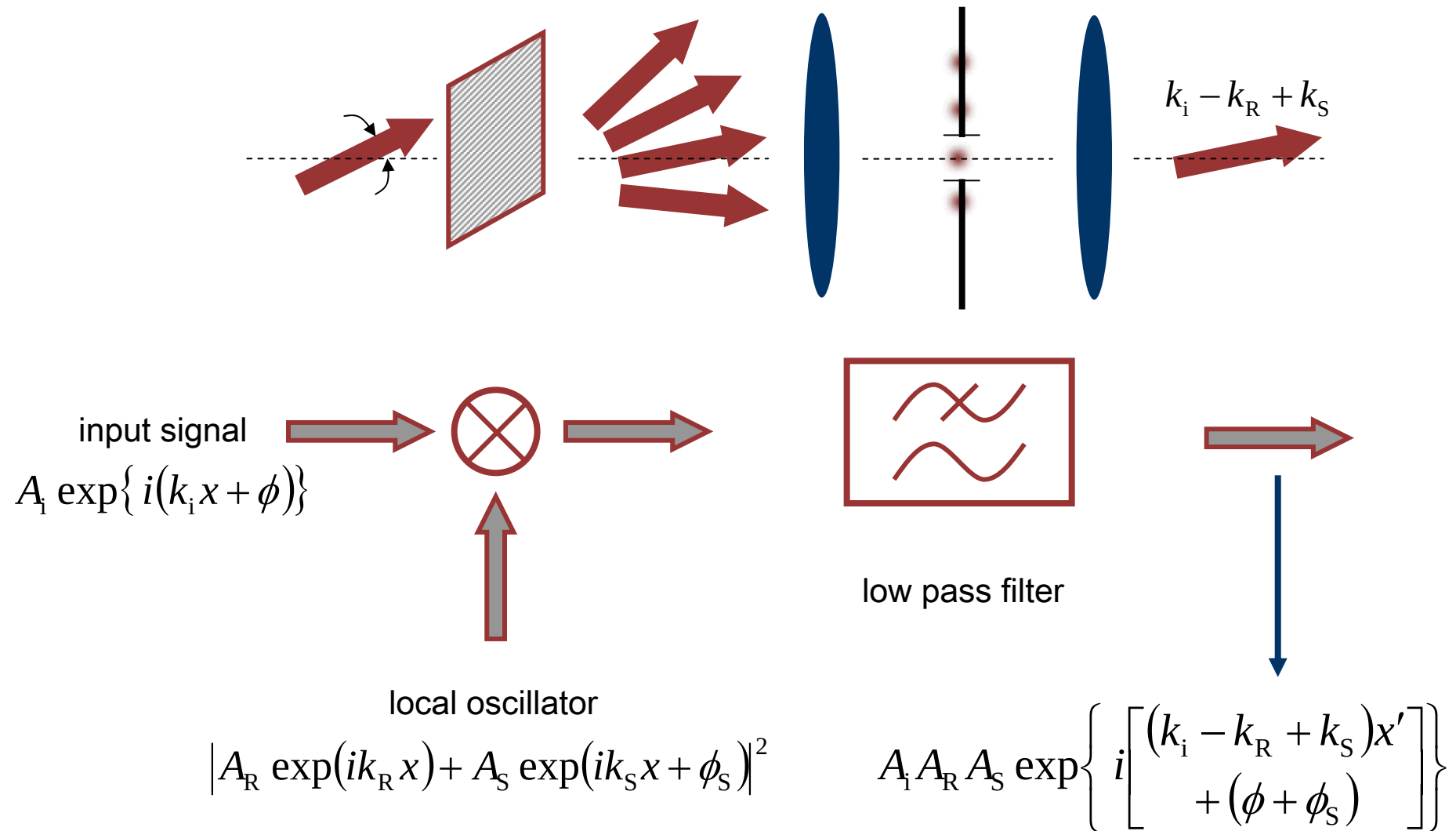
1D Spatial Heterodyning



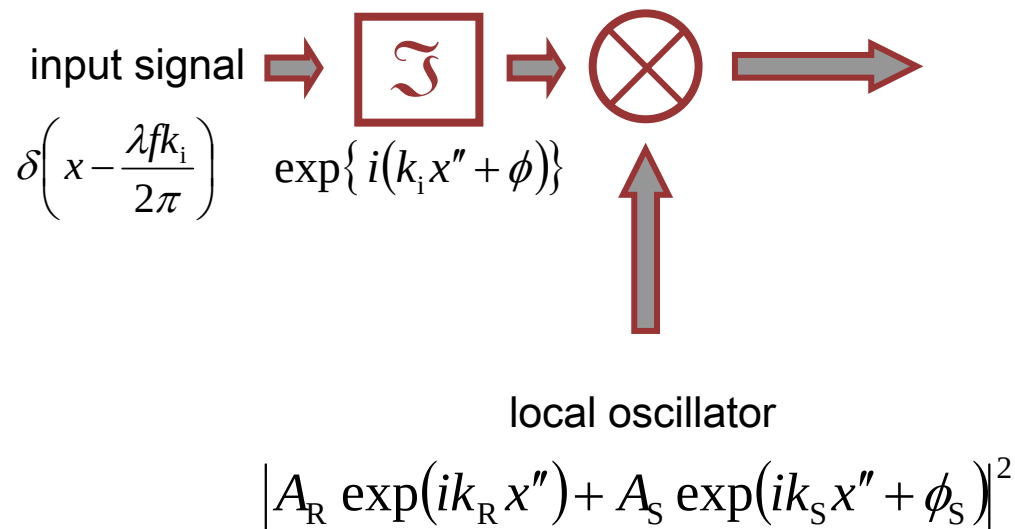
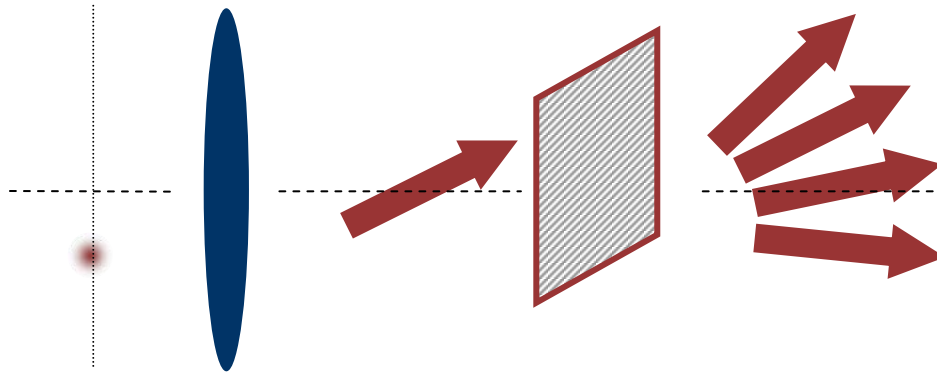
1D Spatial Heterodyning



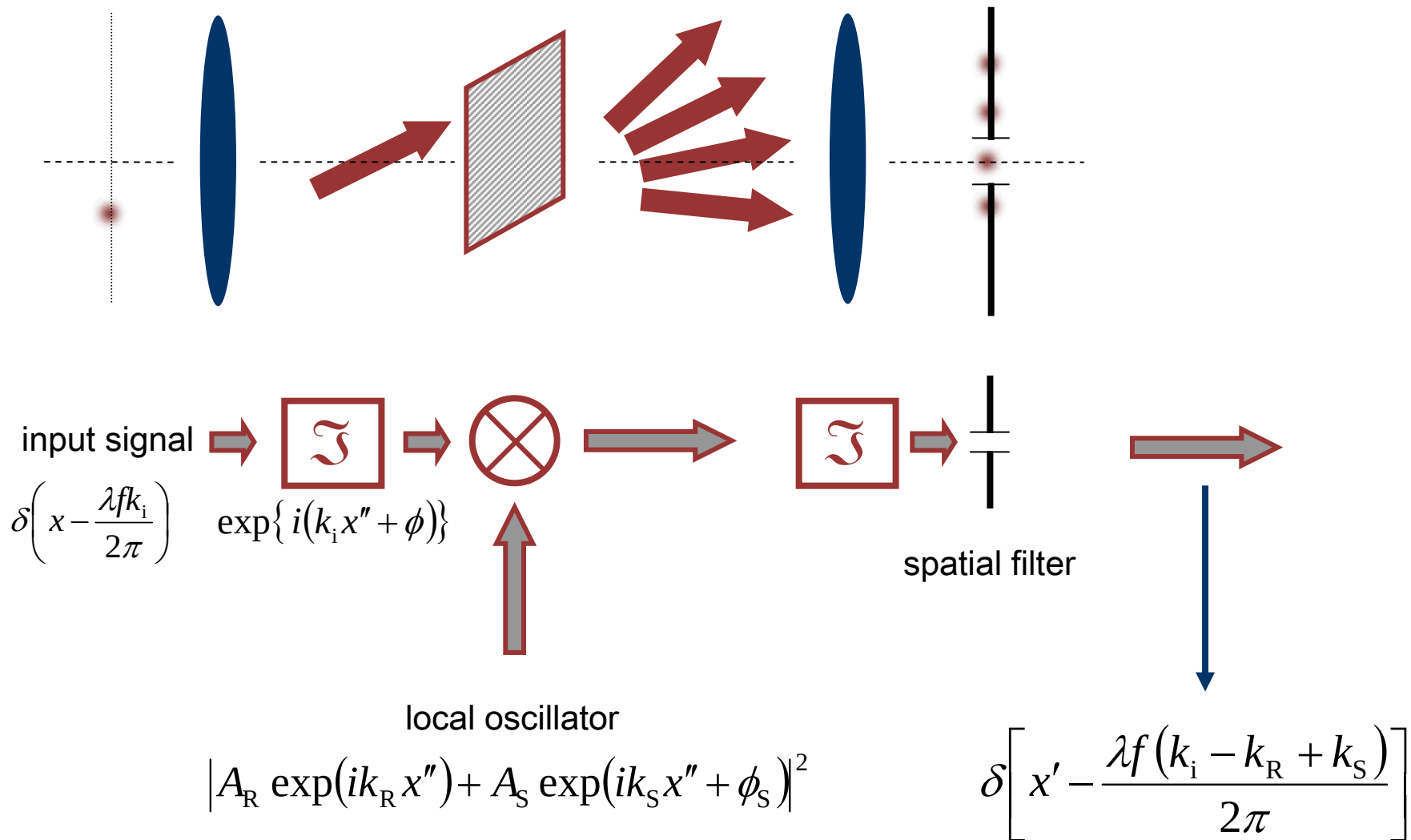
1D Spatial Heterodyning



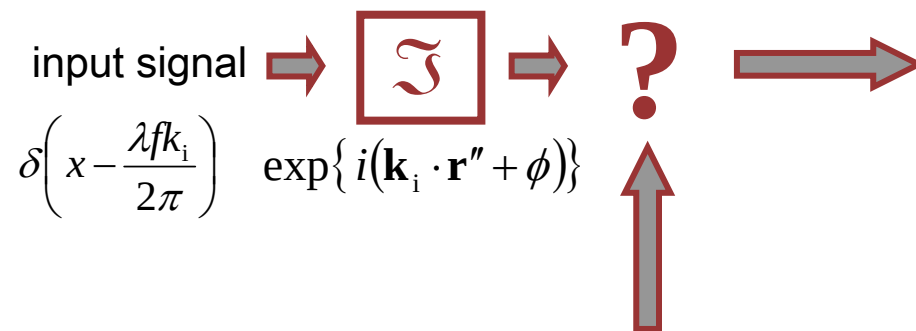
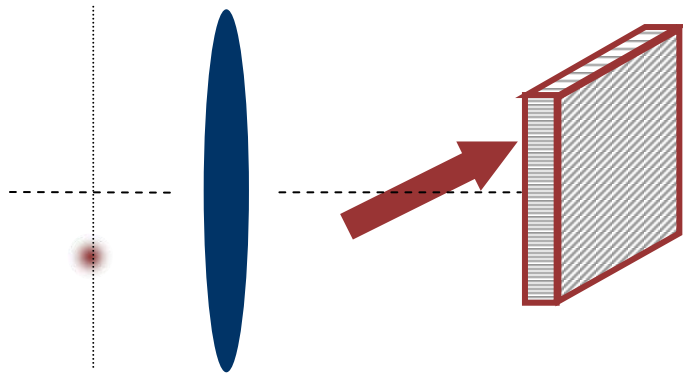
1D Spatial Heterodyning in the Fourier domain



1D Spatial Heterodyning in the Fourier domain



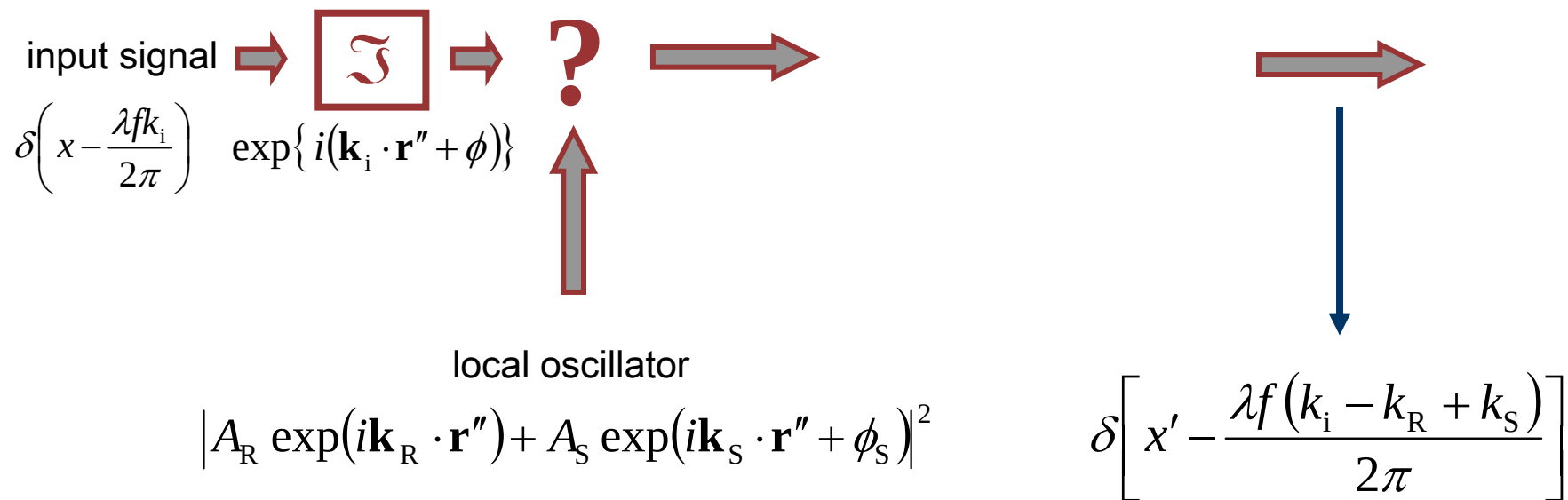
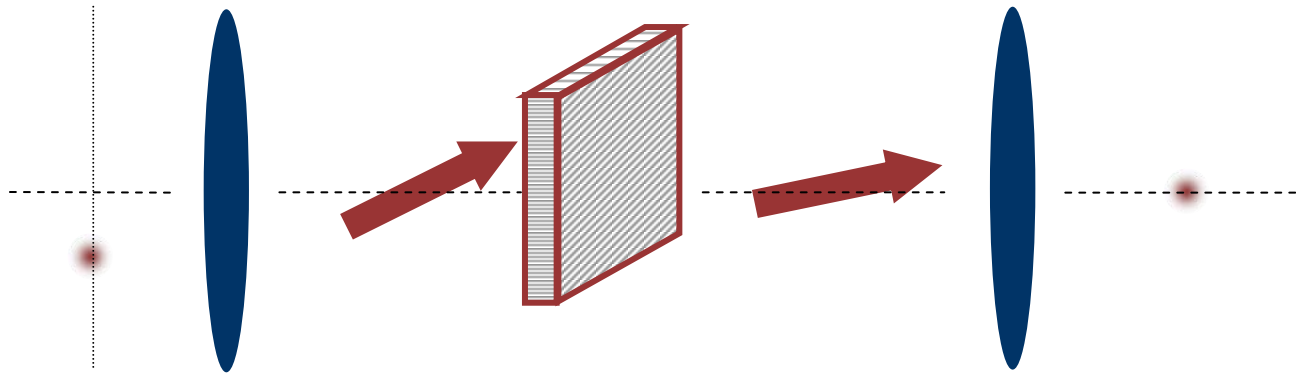
3D Spatial Heterodyning in the Fourier domain



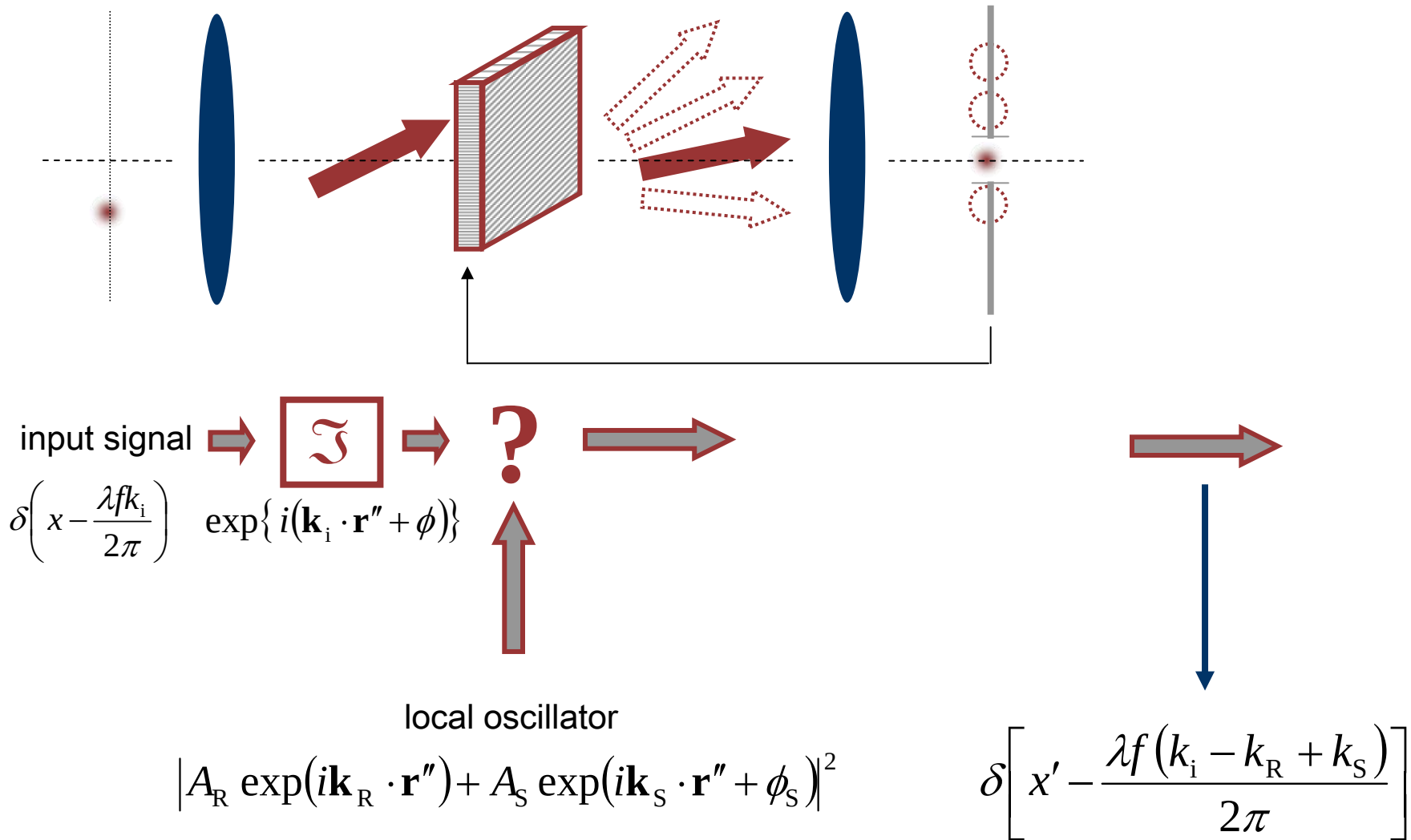
local oscillator

$$\left| A_R \exp(i\mathbf{k}_R \cdot \mathbf{r}'') + A_S \exp(i\mathbf{k}_S \cdot \mathbf{r}'' + \phi_S) \right|^2$$

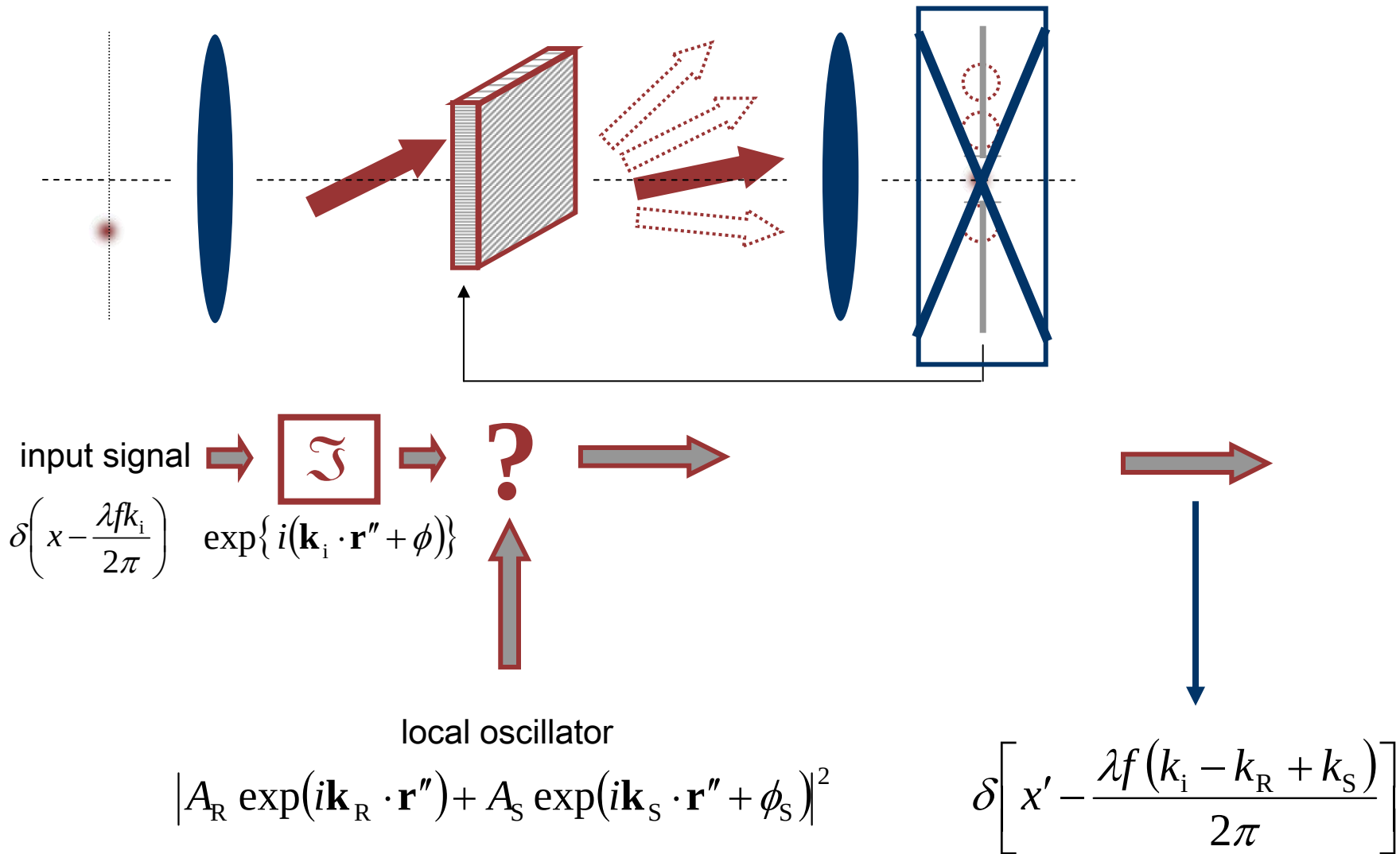
3D Spatial Heterodyning in the Fourier domain



3D Spatial Heterodyning in the Fourier domain

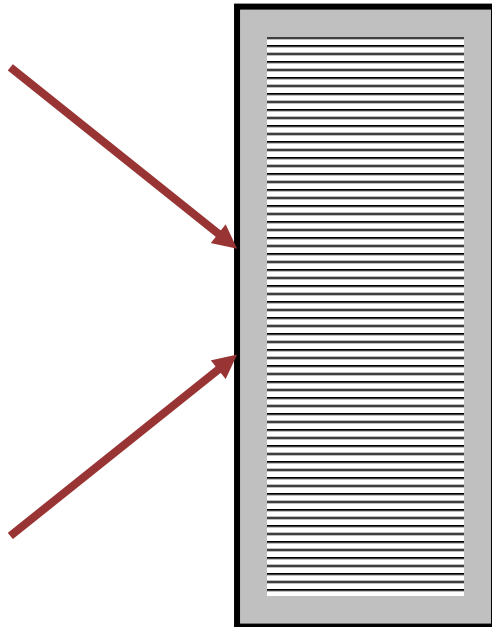


3D Spatial Heterodyning in the Fourier domain

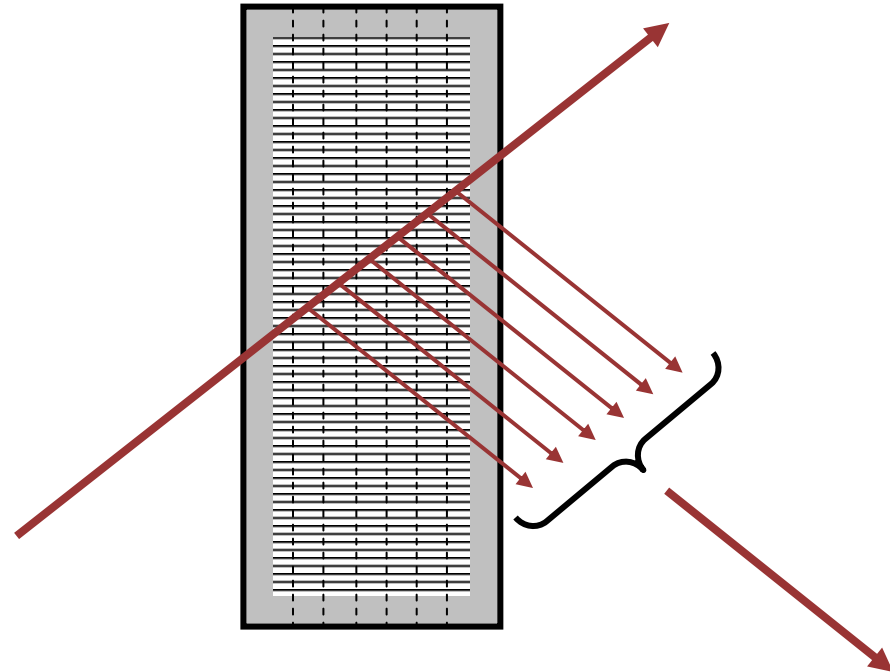


Phase matching as a filter for 3D spatial heterodyning

Recording



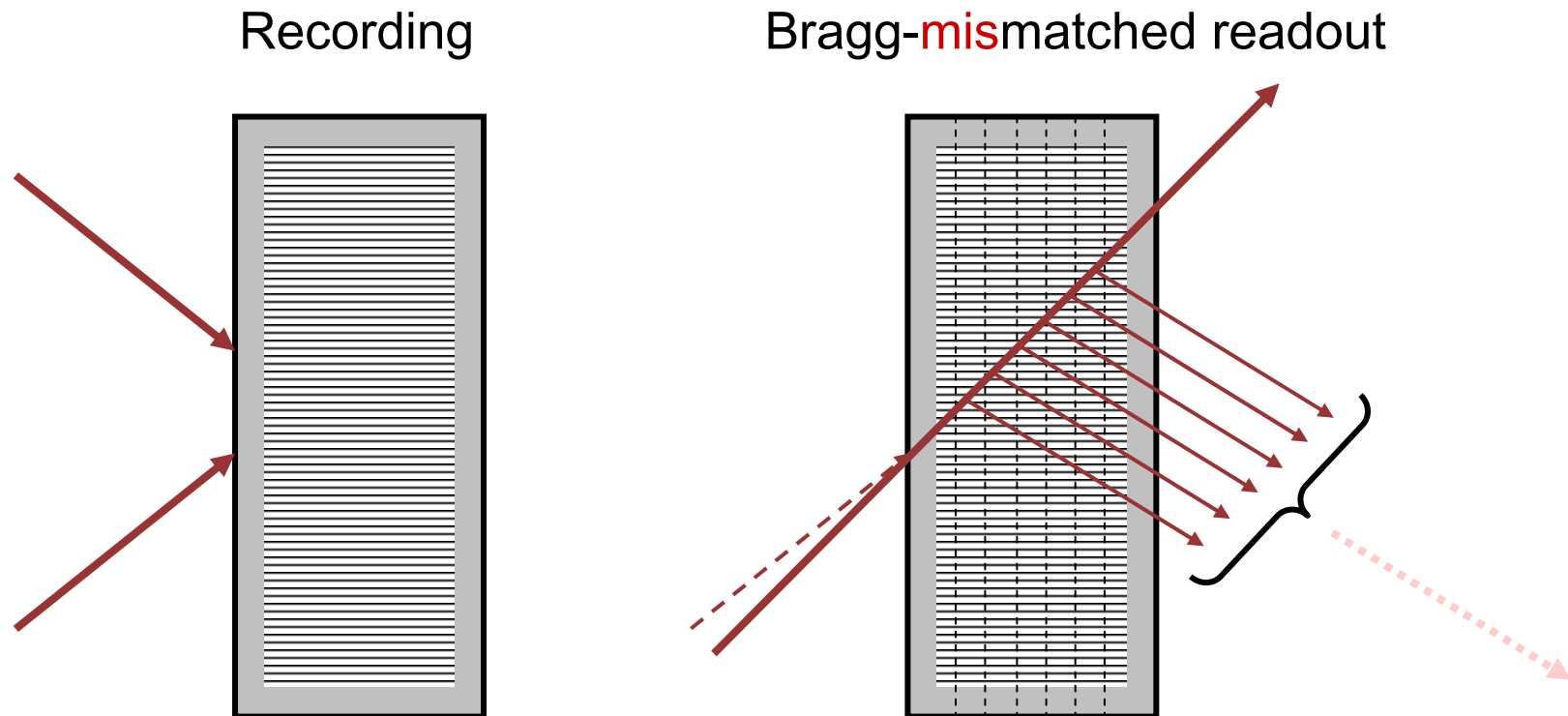
Bragg-matched readout



Diffracted beams from elemental thin slices
are all **in phase** → strong diffraction

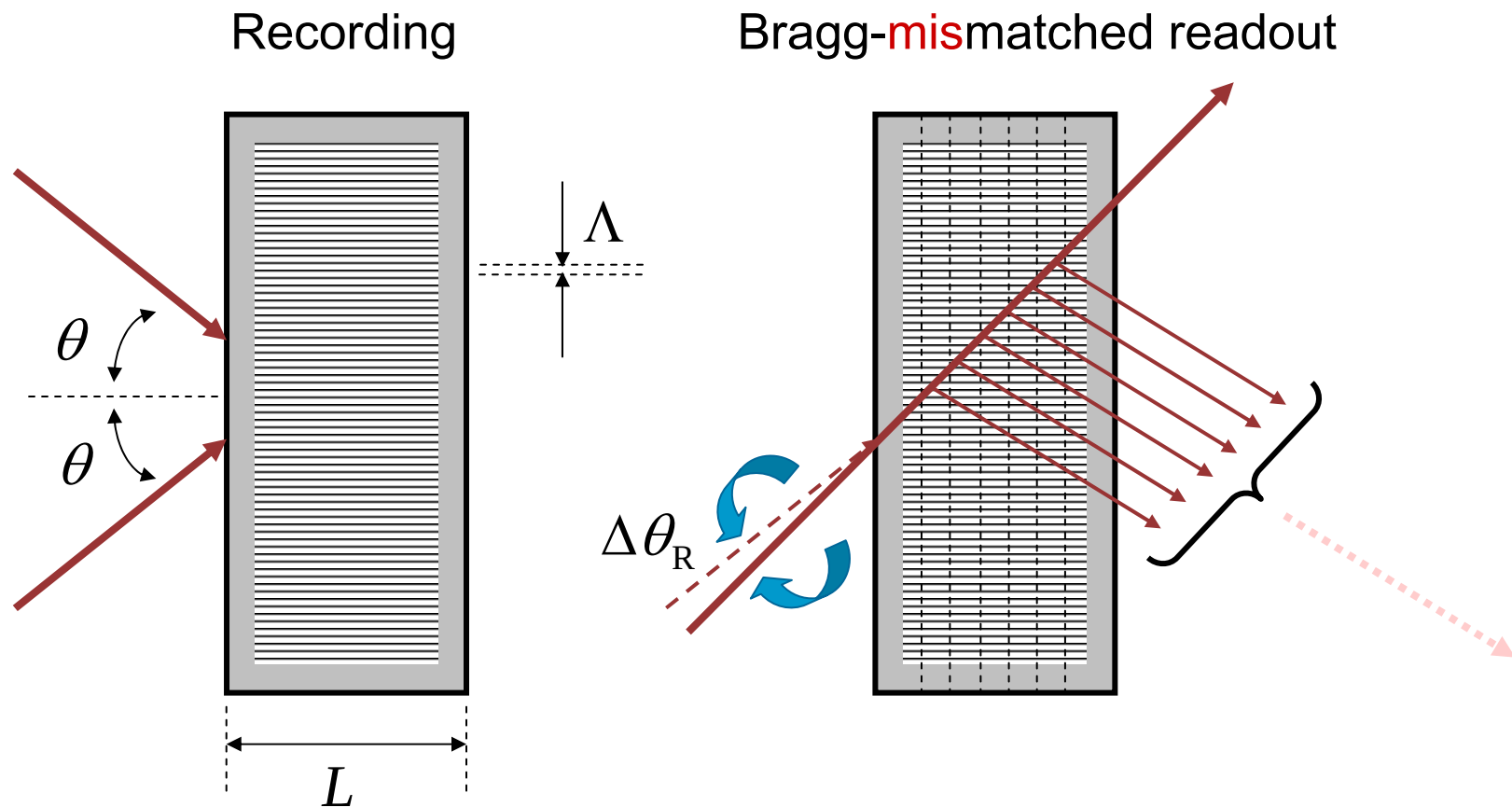


Phase matching as a filter for 3D spatial heterodyning



Diffracted beams from elemental thin slices
are **out of phase** → **no** diffraction

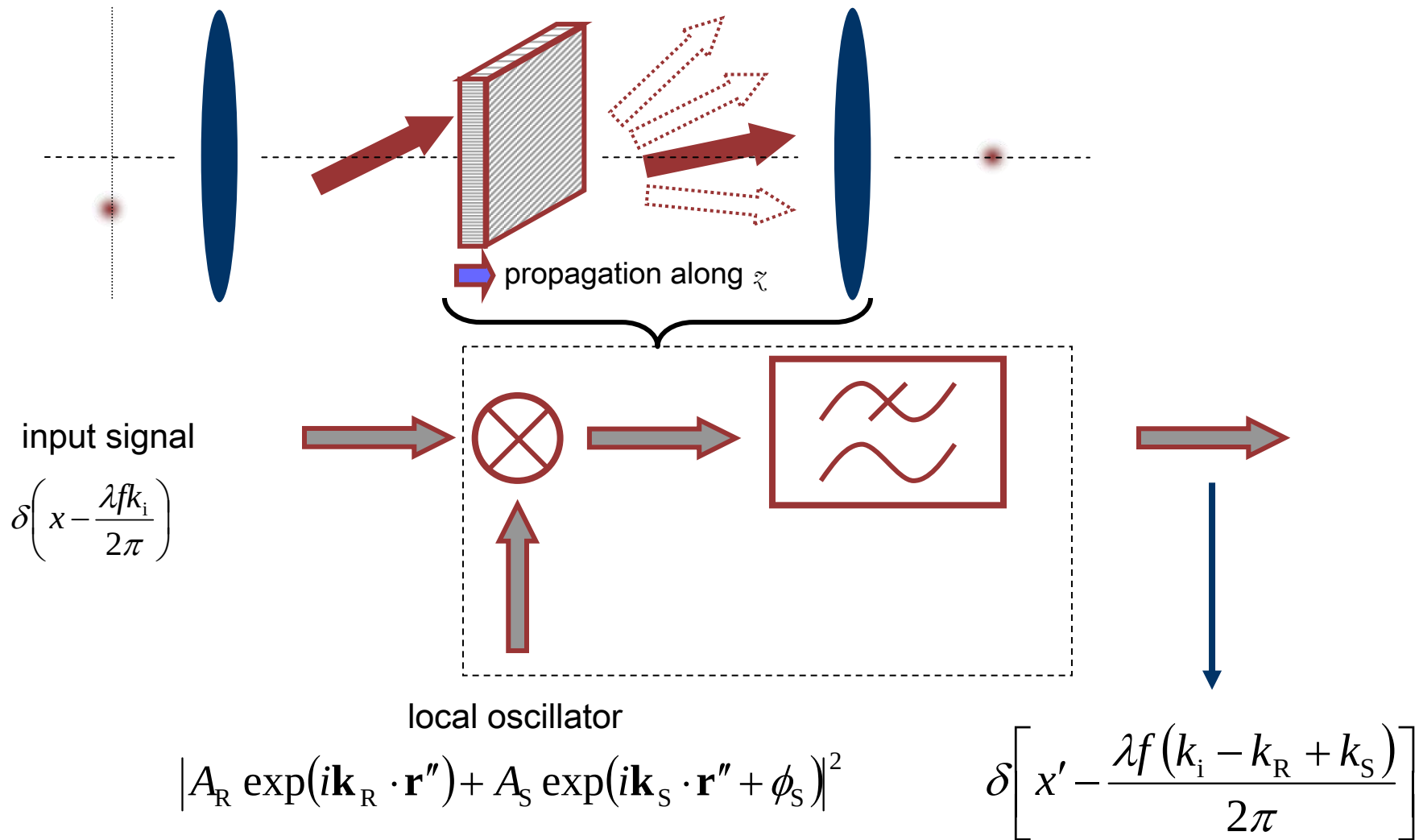
Phase matching as a filter for 3D spatial heterodyning



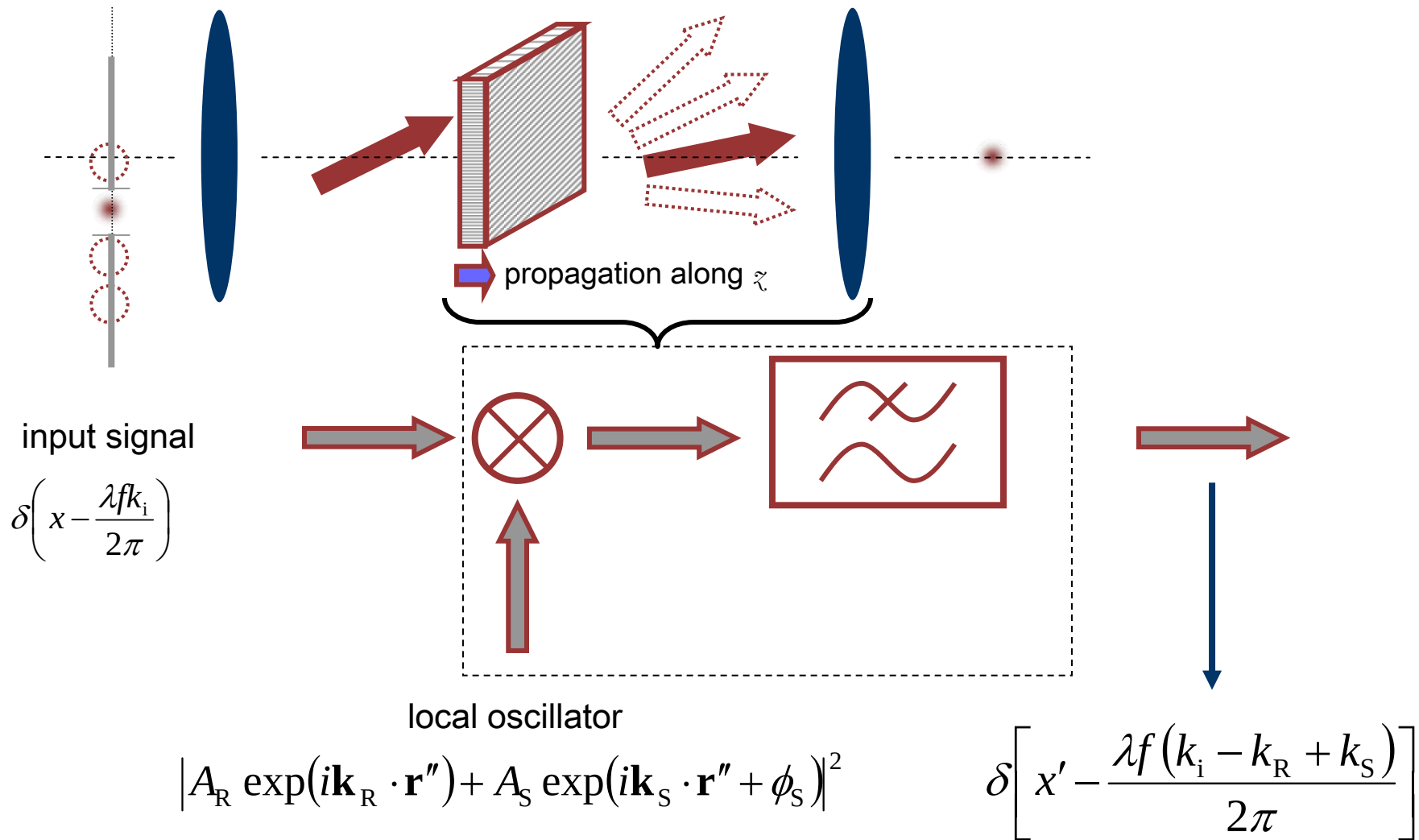
Angle Bragg selectivity $\Delta\theta_R = \frac{\Lambda}{L} = \frac{\lambda}{2L \sin \theta}$



3D Spatial Heterodyning in the Fourier domain

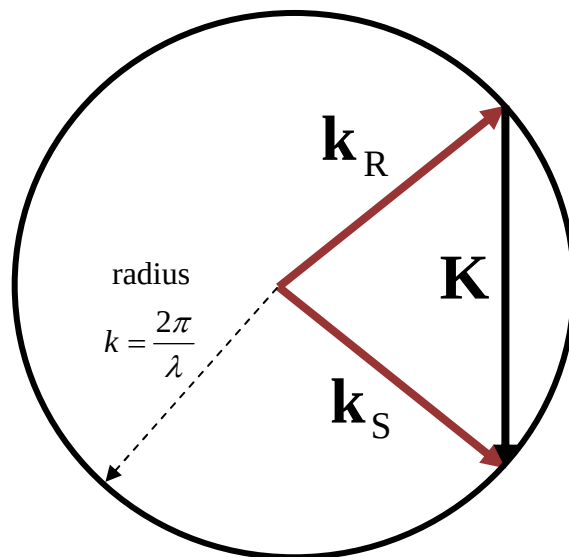


3D Spatial Heterodyning in the Fourier domain



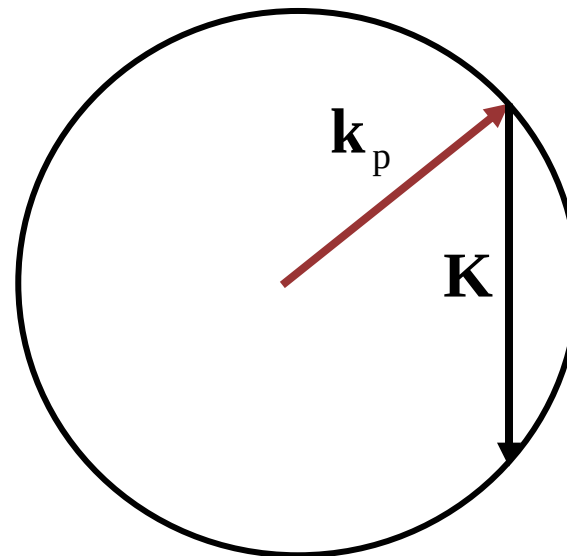
3D Spatial Heterodyning in k -space

Recording



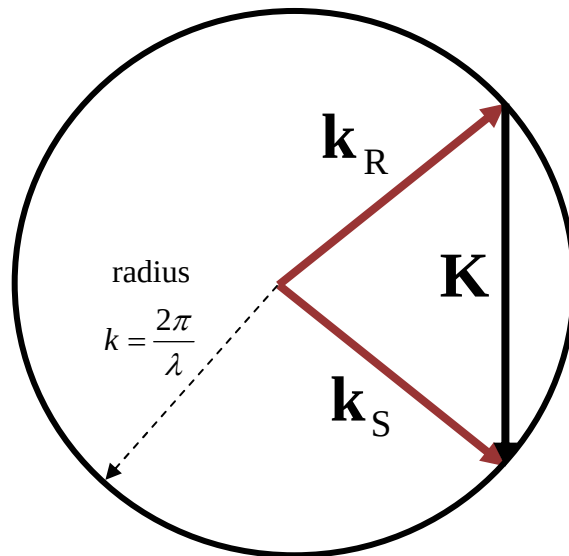
$$\mathbf{K} = \mathbf{k}_S - \mathbf{k}_R$$

Bragg-matched readout



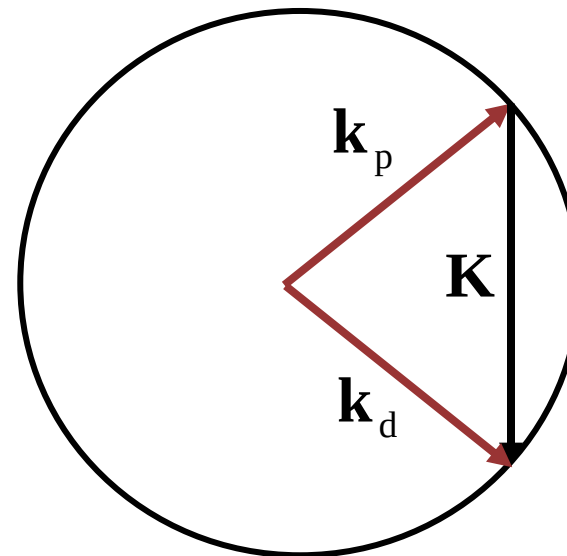
3D Spatial Heterodyning in k -space

Recording



$$\mathbf{K} = \mathbf{k}_S - \mathbf{k}_R$$

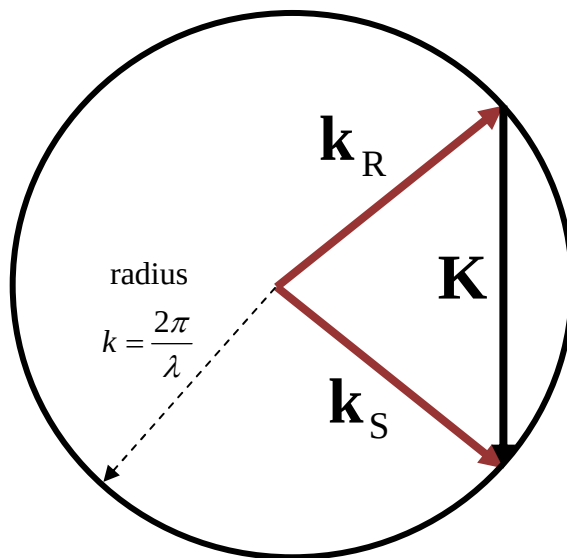
Bragg-matched readout



$$\mathbf{k}_d = \mathbf{k}_R + \mathbf{K}$$

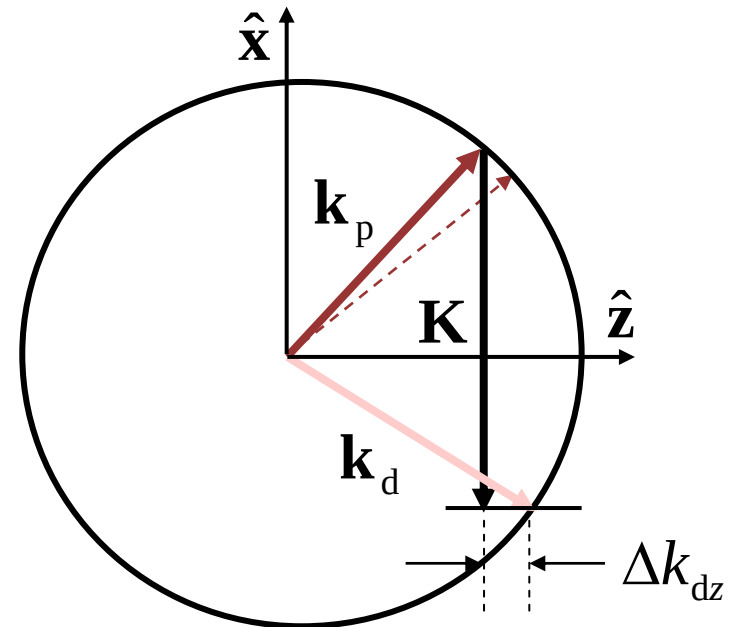
3D Spatial Heterodyning in k -space

Recording



$$\mathbf{K} = \mathbf{k}_S - \mathbf{k}_R$$

Bragg-mismatched readout

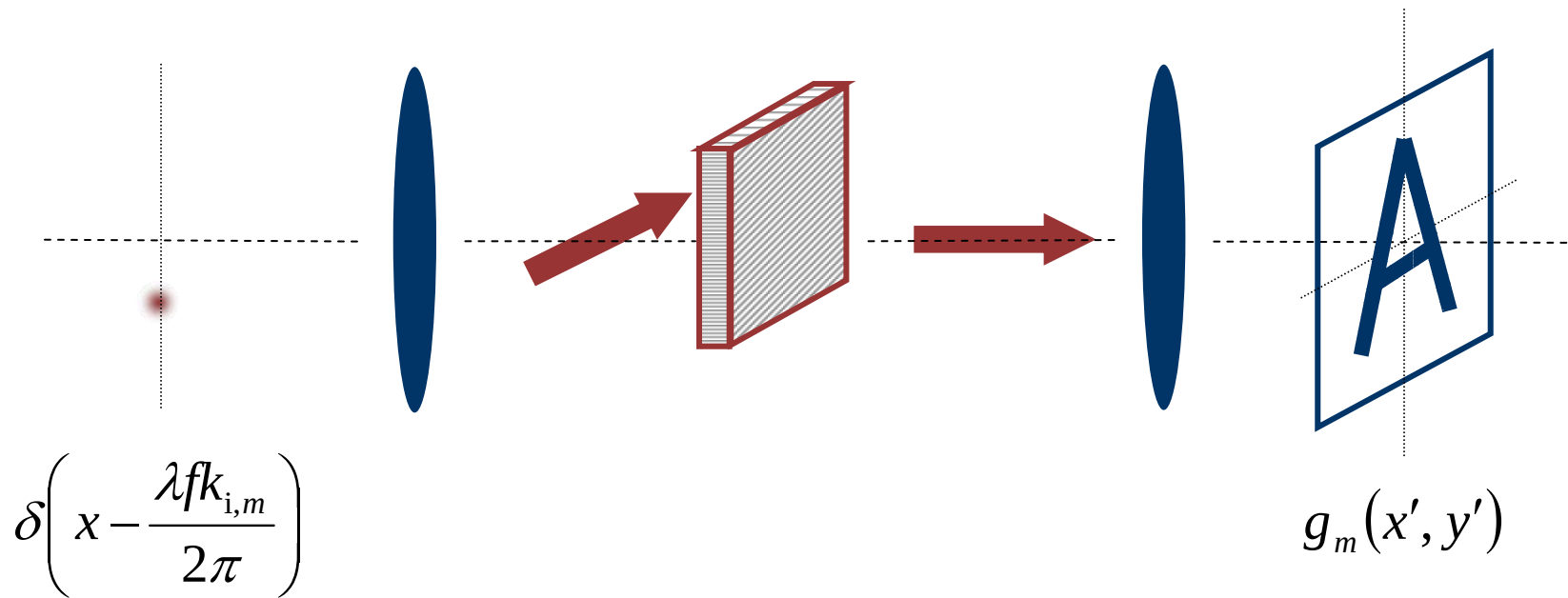


$$\mathbf{k}_d = [(\mathbf{k}_R + \mathbf{K}) \cdot \hat{\mathbf{x}}] \hat{\mathbf{x}} + k_{dz} \hat{\mathbf{z}}$$

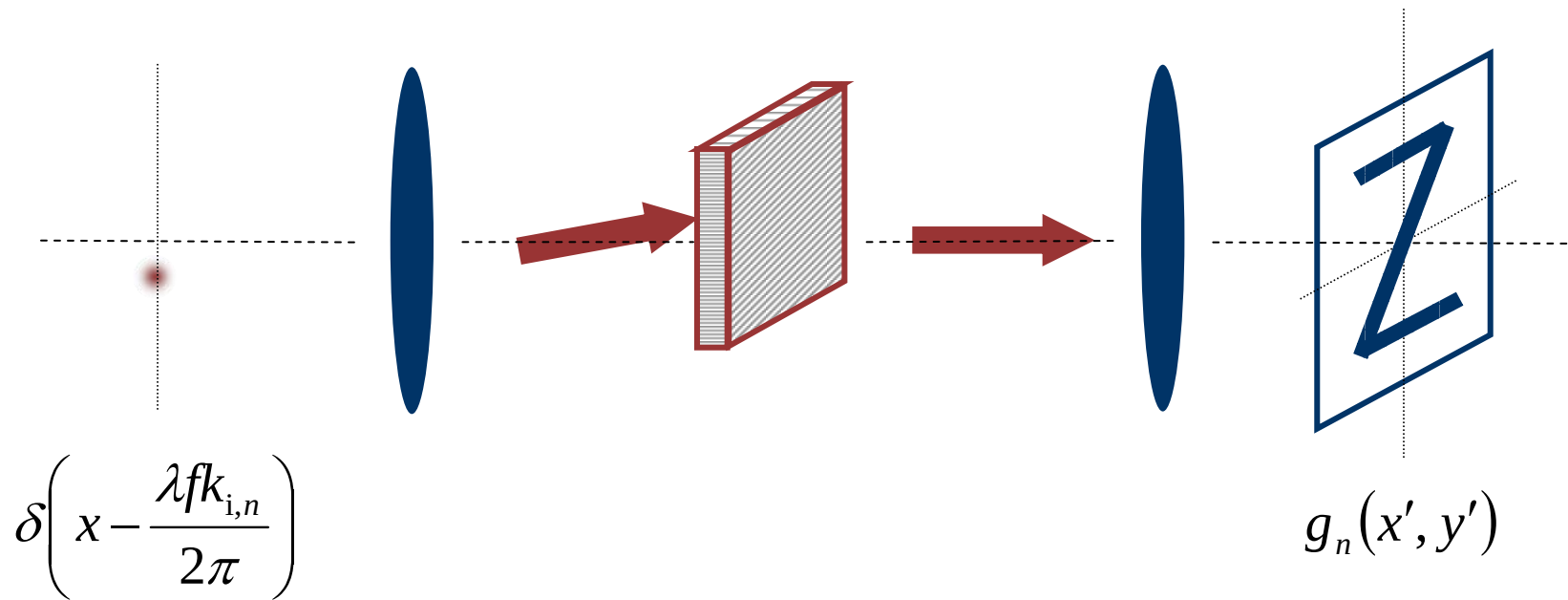
$$\|\mathbf{k}_d\| = k$$

$$I_{\text{diffracted}} = I_{\text{Bragg-matched}} \text{sinc}^2\left(\frac{1}{2} \Delta k_{dz} L\right)$$

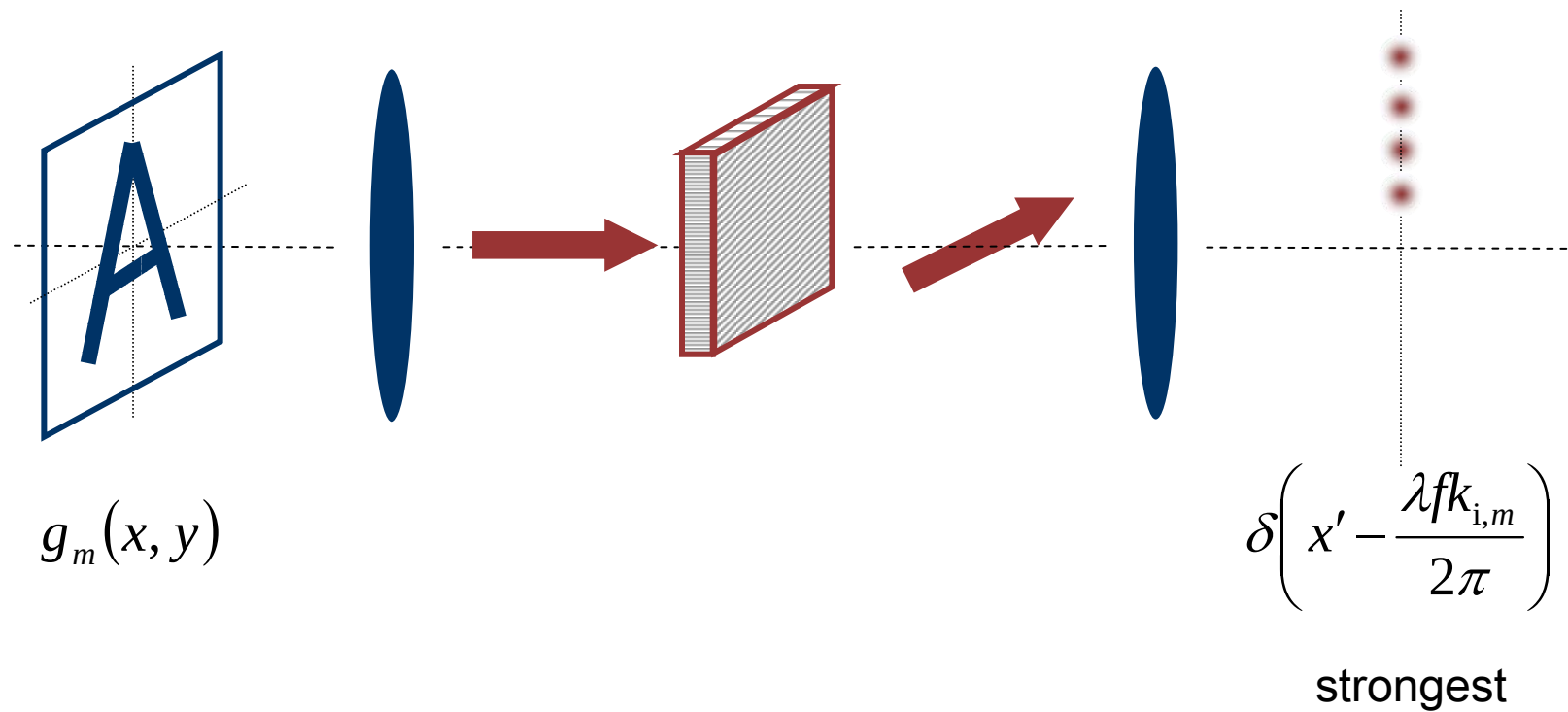
Applications: 3D holographic data storage



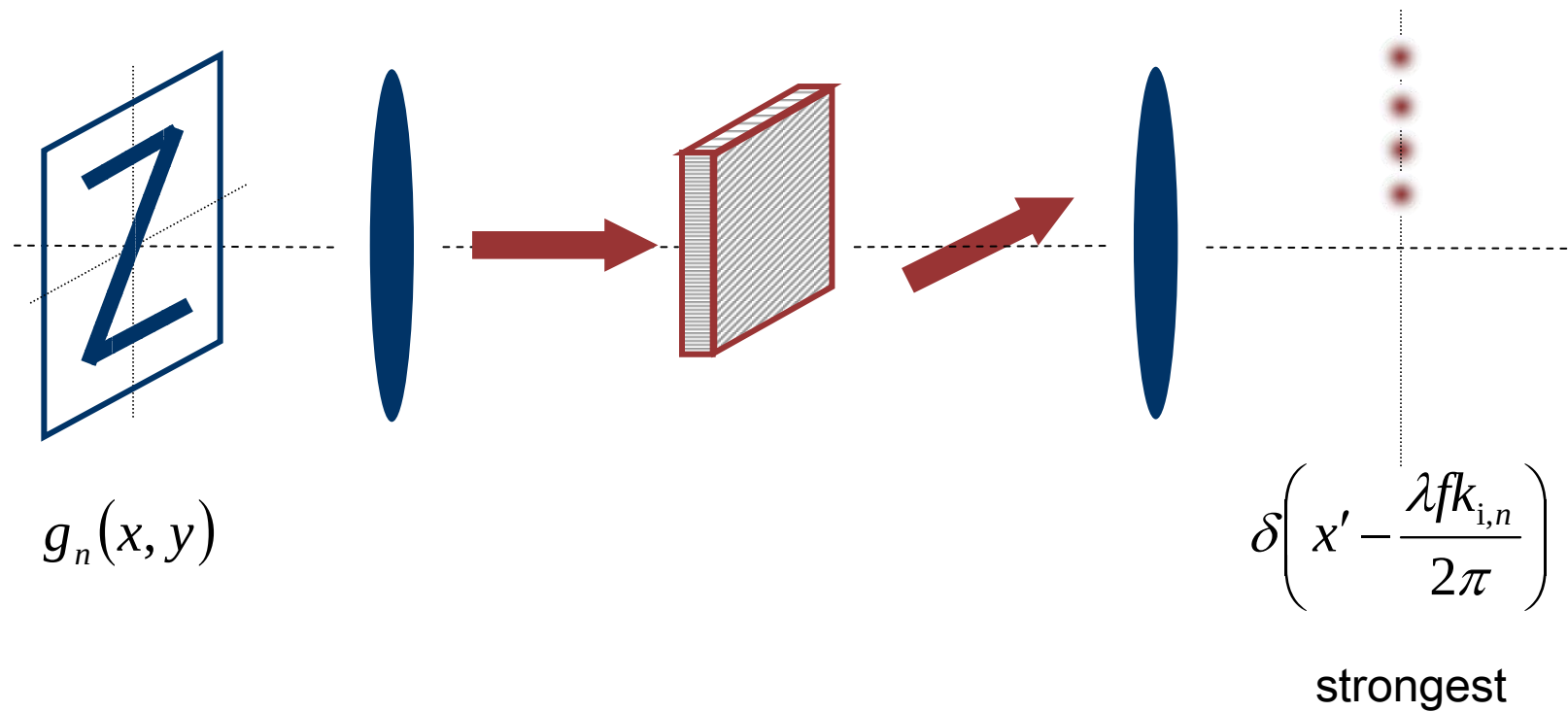
Applications: 3D holographic data storage



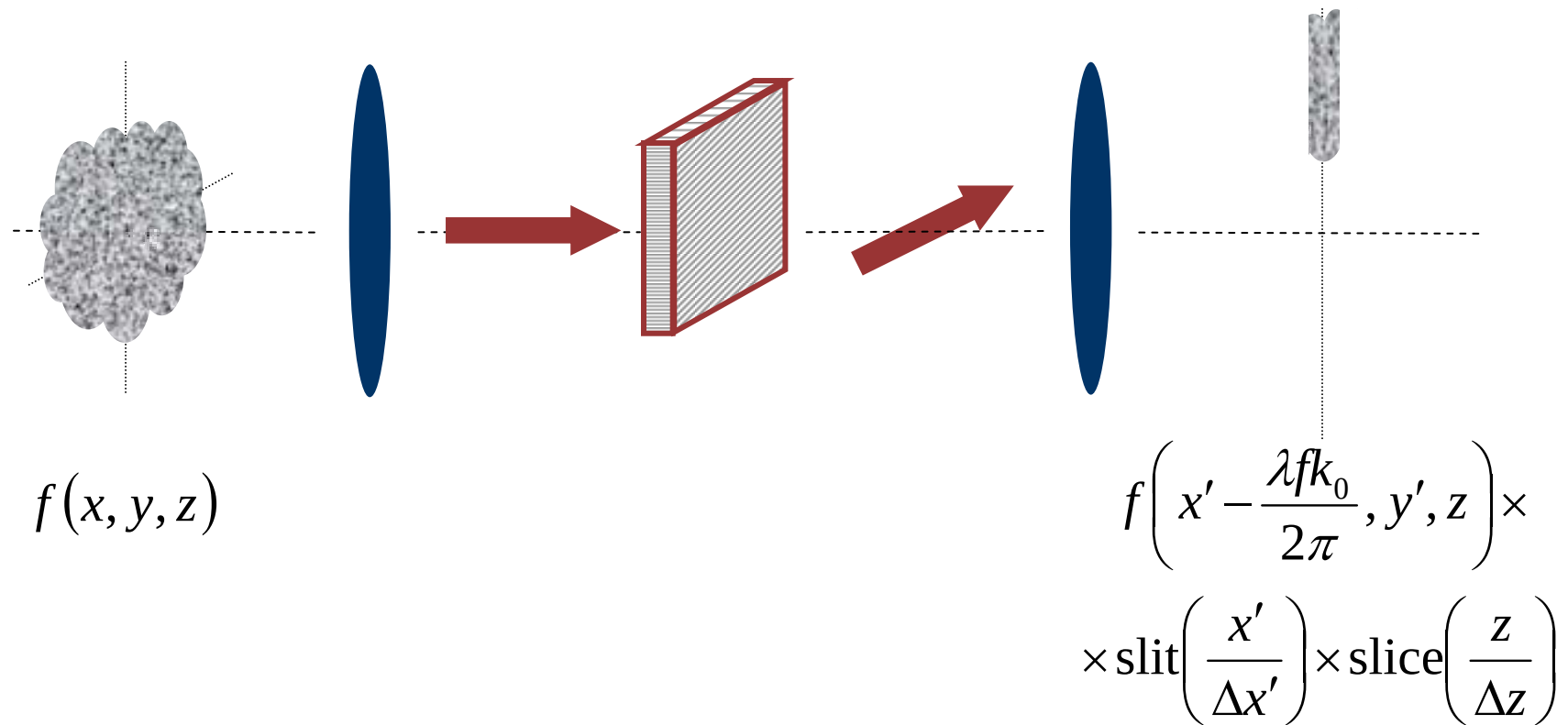
Applications: 3D holographic optical correlators



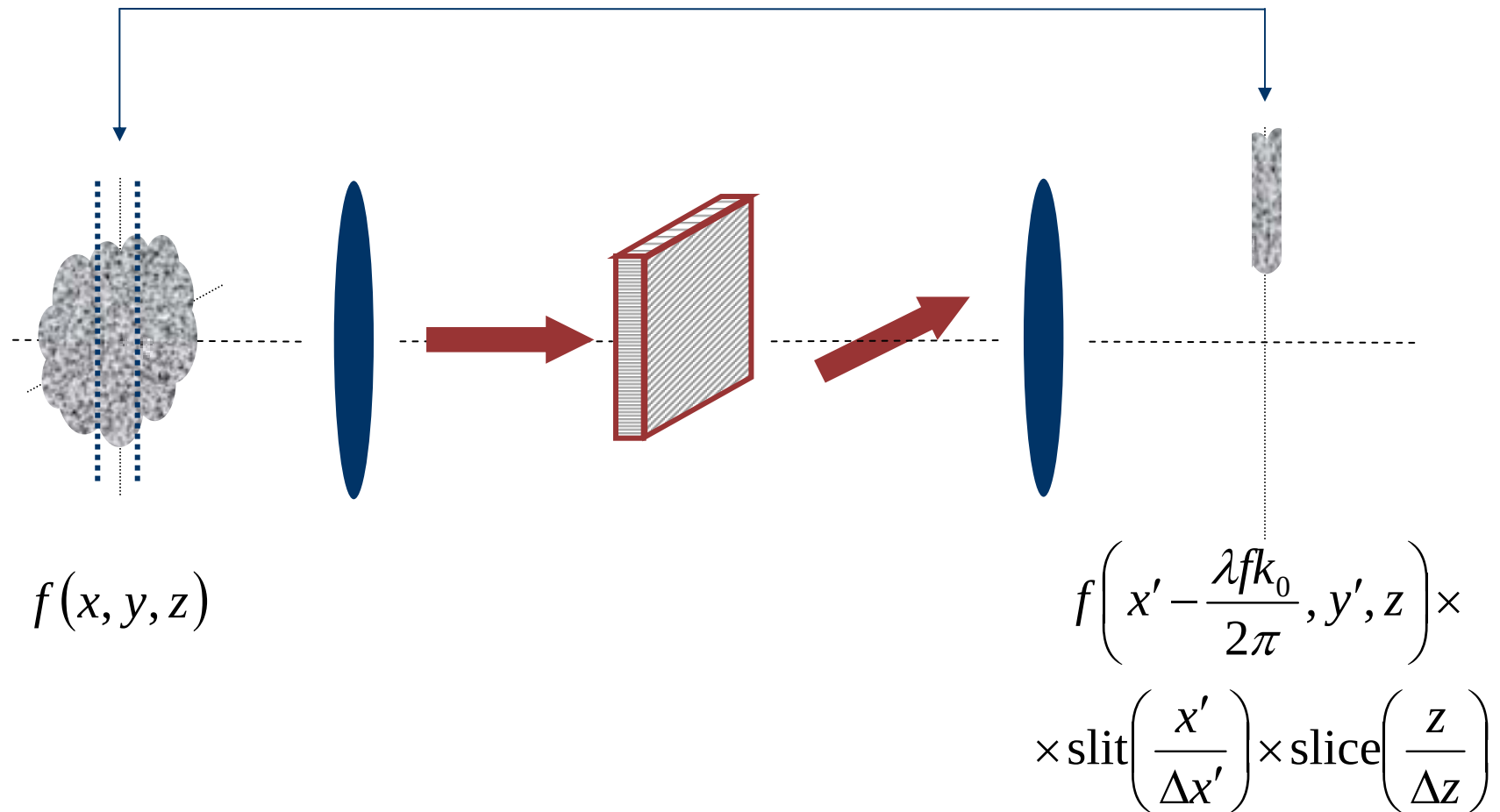
Applications: 3D holographic optical correlators



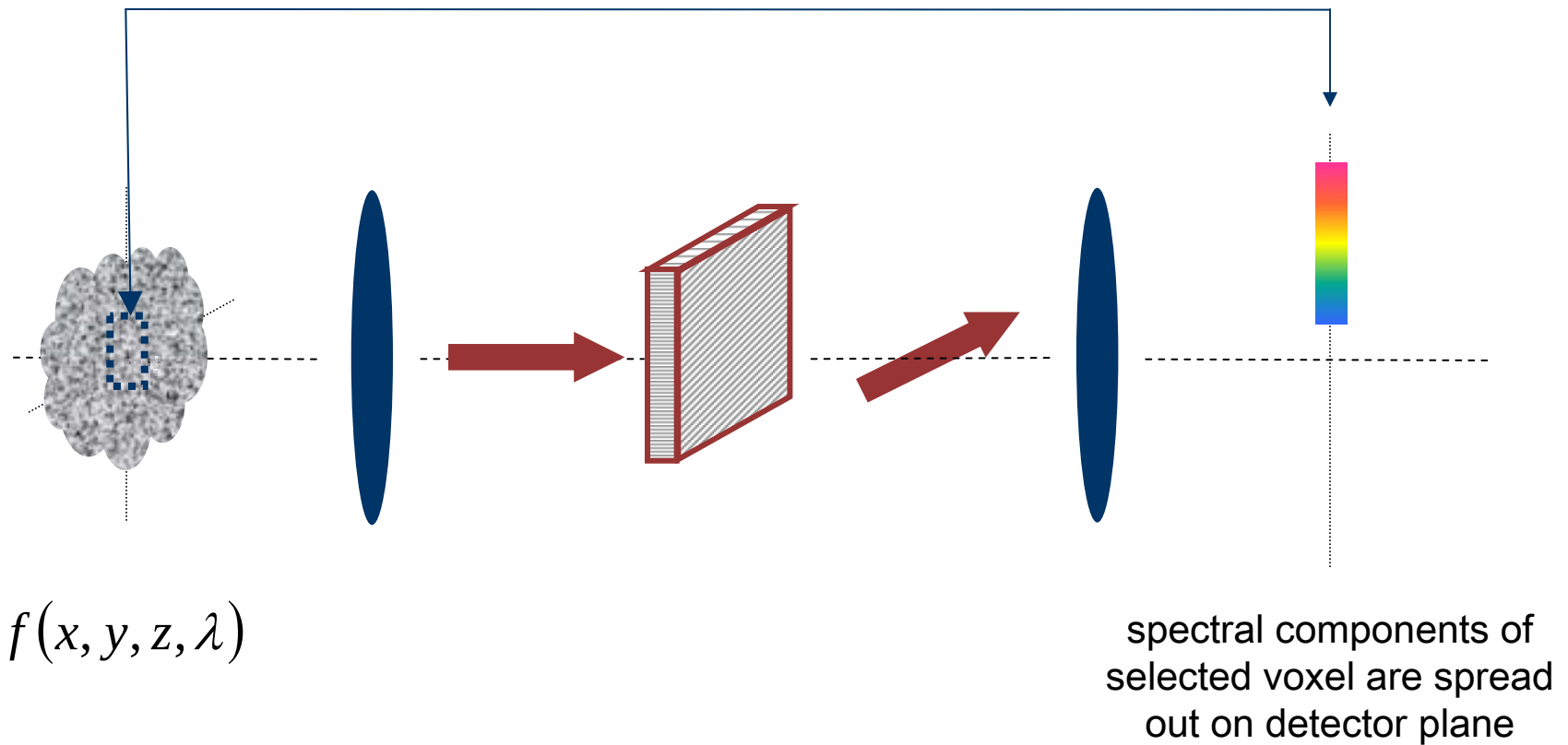
Applications: 3D holographic optical imaging



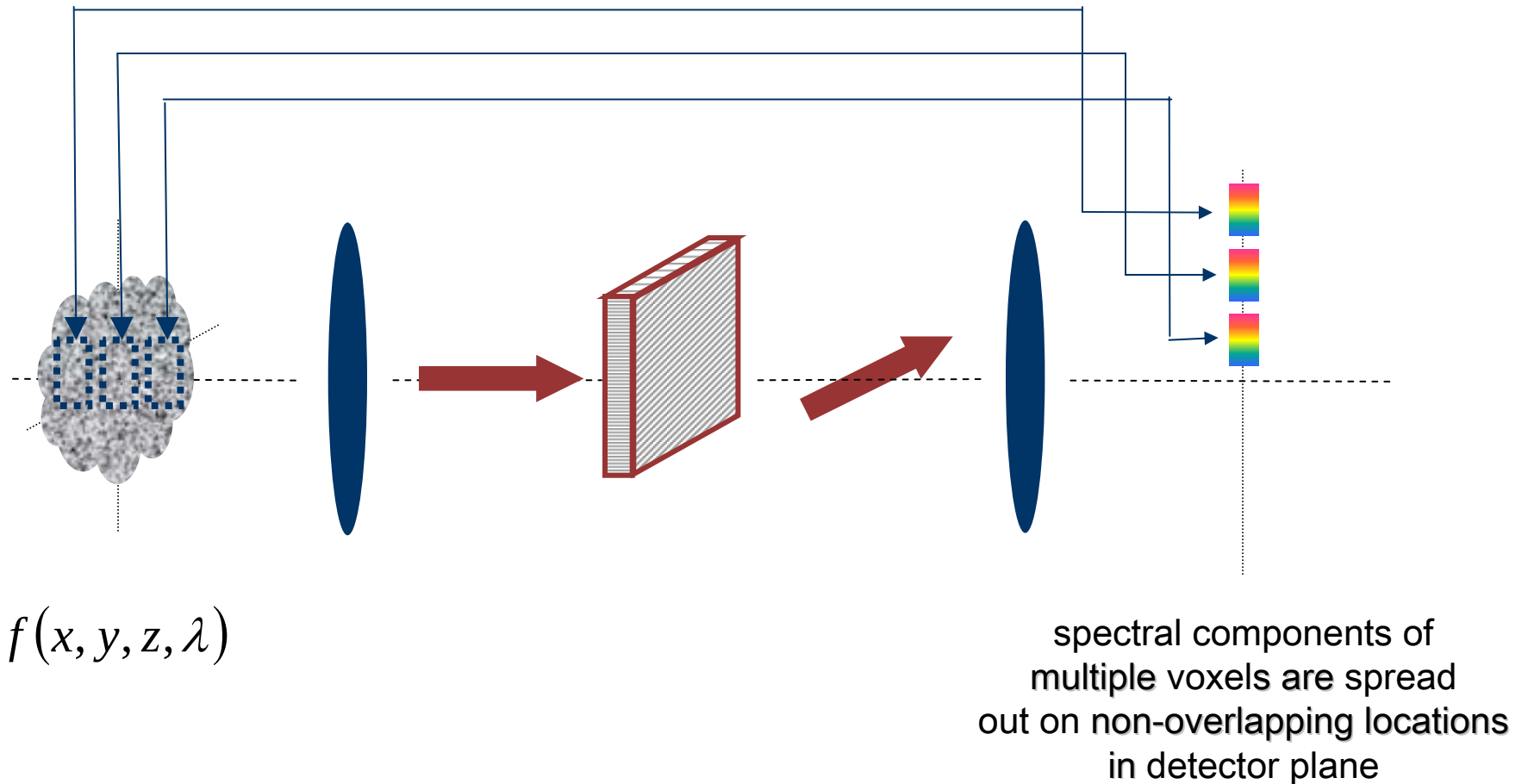
Applications: 3D holographic optical imaging



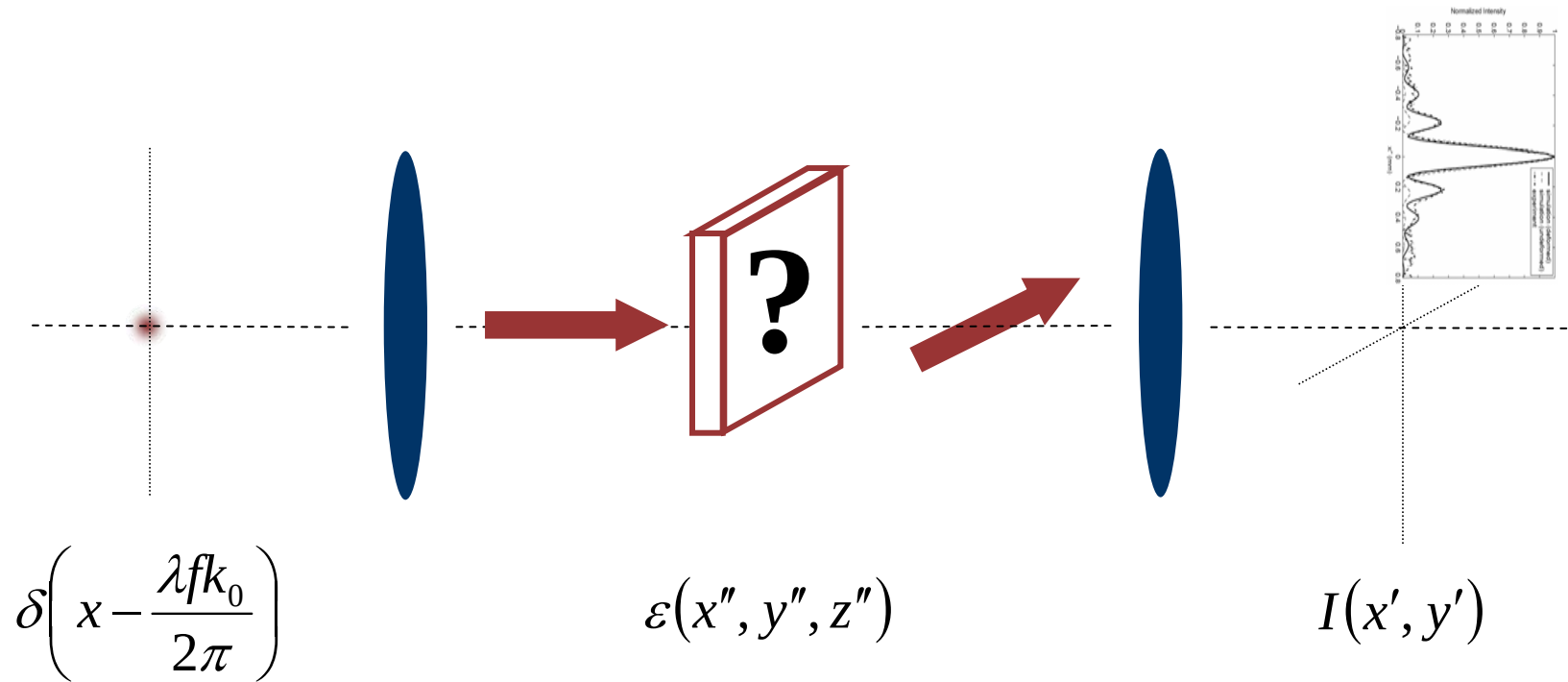
Applications: 3D holographic hyperspectral imaging



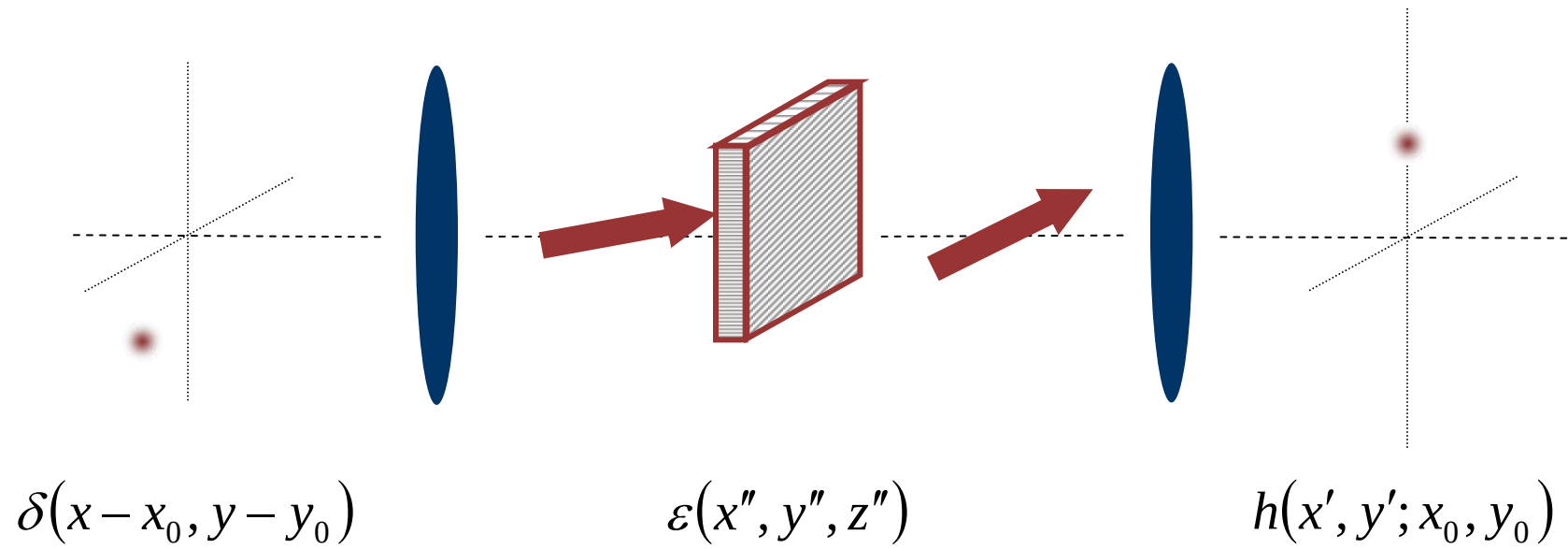
Applications: 3D multiplex hyperspectral imaging



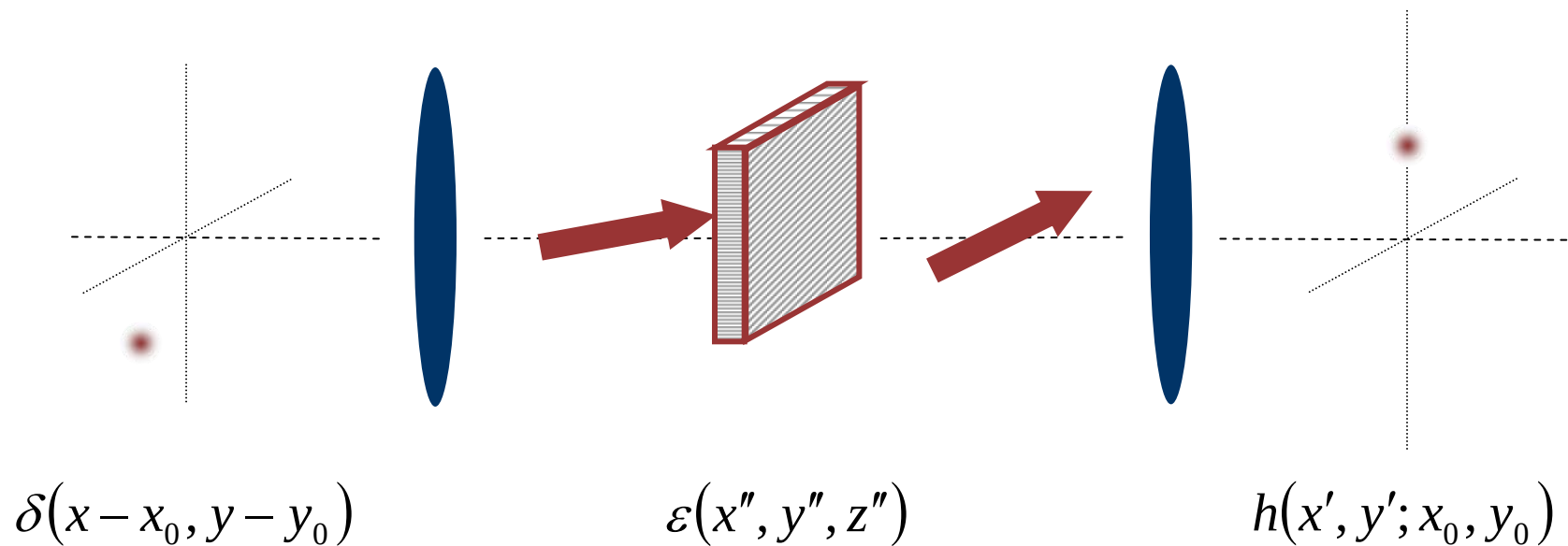
Applications: probing unknown 3D holograms



Optical imaging with 3D pupil

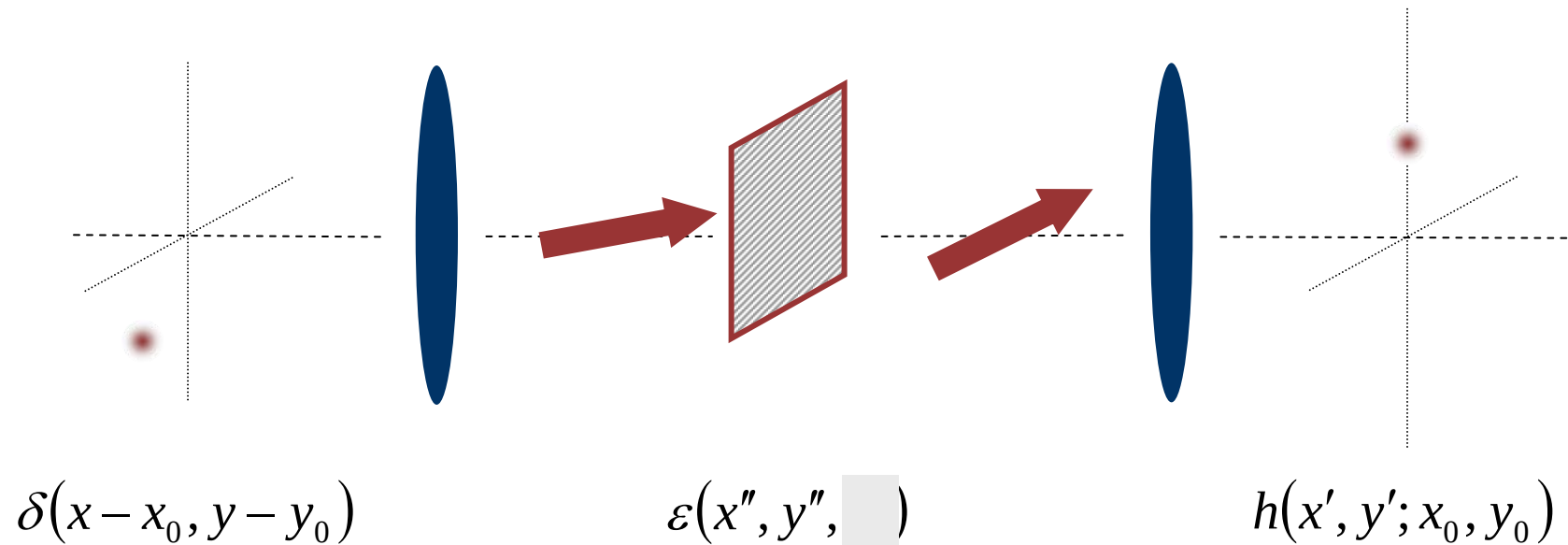


Optical imaging with 3D pupil



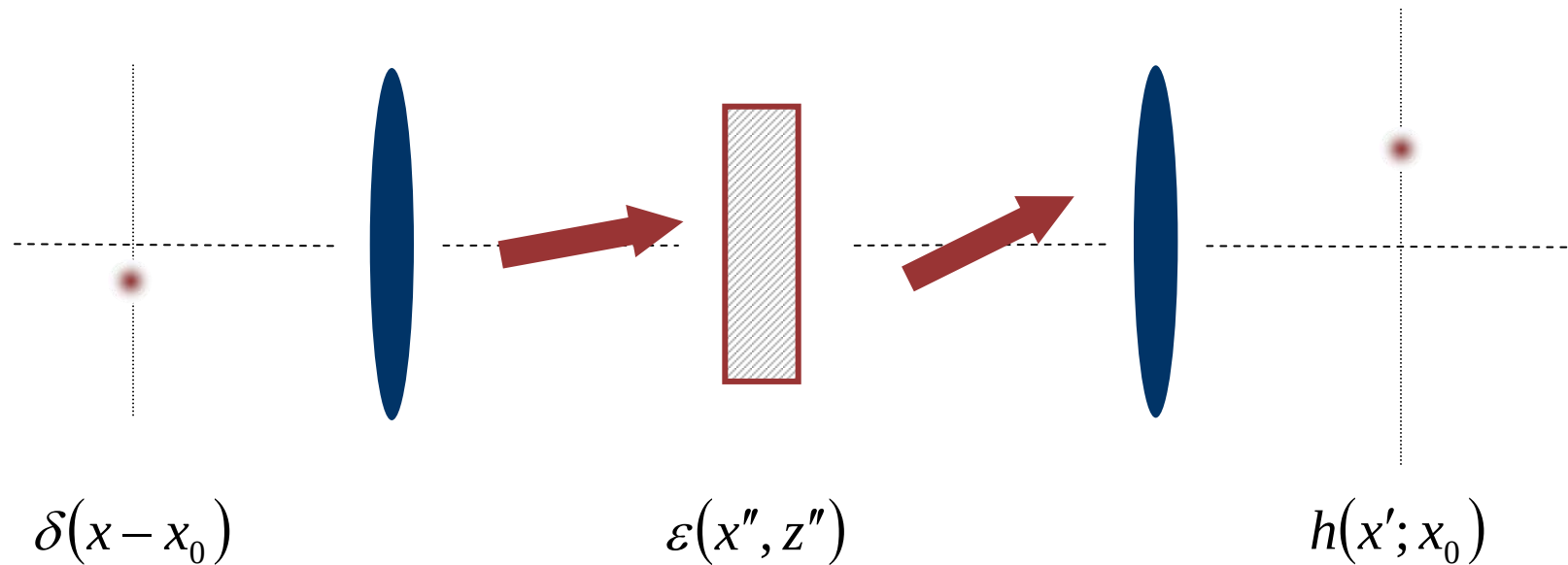
$$h(x', y'; x_0, y_0) = \mathfrak{F}\{\varepsilon\} \left[\frac{1}{\lambda} \left(\frac{x_0}{f_1} + \frac{x'}{f_2} \right), \frac{1}{\lambda} \left(\frac{y_0}{f_1} + \frac{y'}{f_2} \right), \frac{1}{\lambda} \left(\frac{x_0^2 + y_0^2}{2f_1^2} - \frac{x'^2 + y'^2}{2f_2^2} \right) \right]$$

Optical imaging with 2D pupil



$$h(x', y'; x_0, y_0) = \mathfrak{F}\{\varepsilon\} \left[\frac{1}{\lambda} \left(\frac{x_0}{f_1} + \frac{x'}{f_2} \right), \frac{1}{\lambda} \left(\frac{y_0}{f_1} + \frac{y'}{f_2} \right), \text{gray box} \right]$$

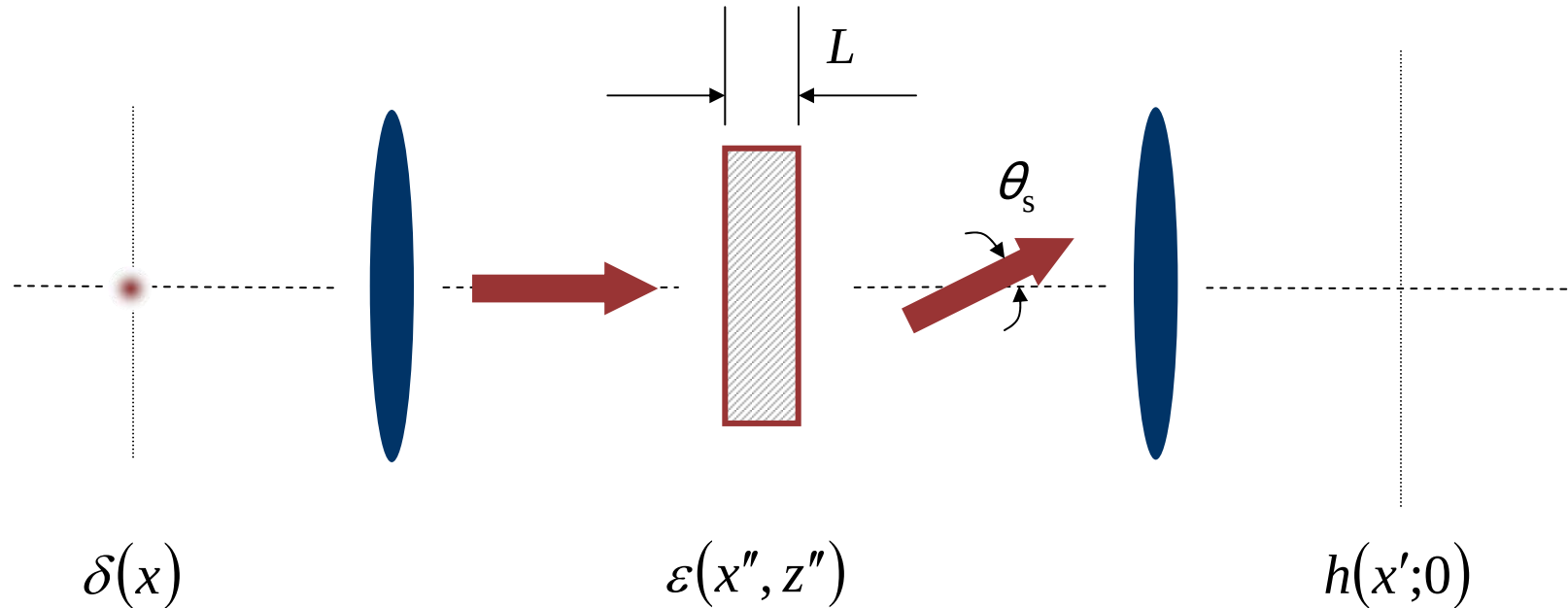
Optical imaging with 3D pupil



$$h(x'; x_0) = \mathfrak{F}\{\varepsilon\} \left[\frac{1}{\lambda} \left(\frac{x_0}{f_1} + \frac{x'}{f_2} \right), \frac{1}{\lambda} \left(\frac{x_0^2}{2f_1^2} - \frac{x'^2}{2f_2^2} \right) \right]$$

simplify to 1D lateral dimension + longitudinal dimension

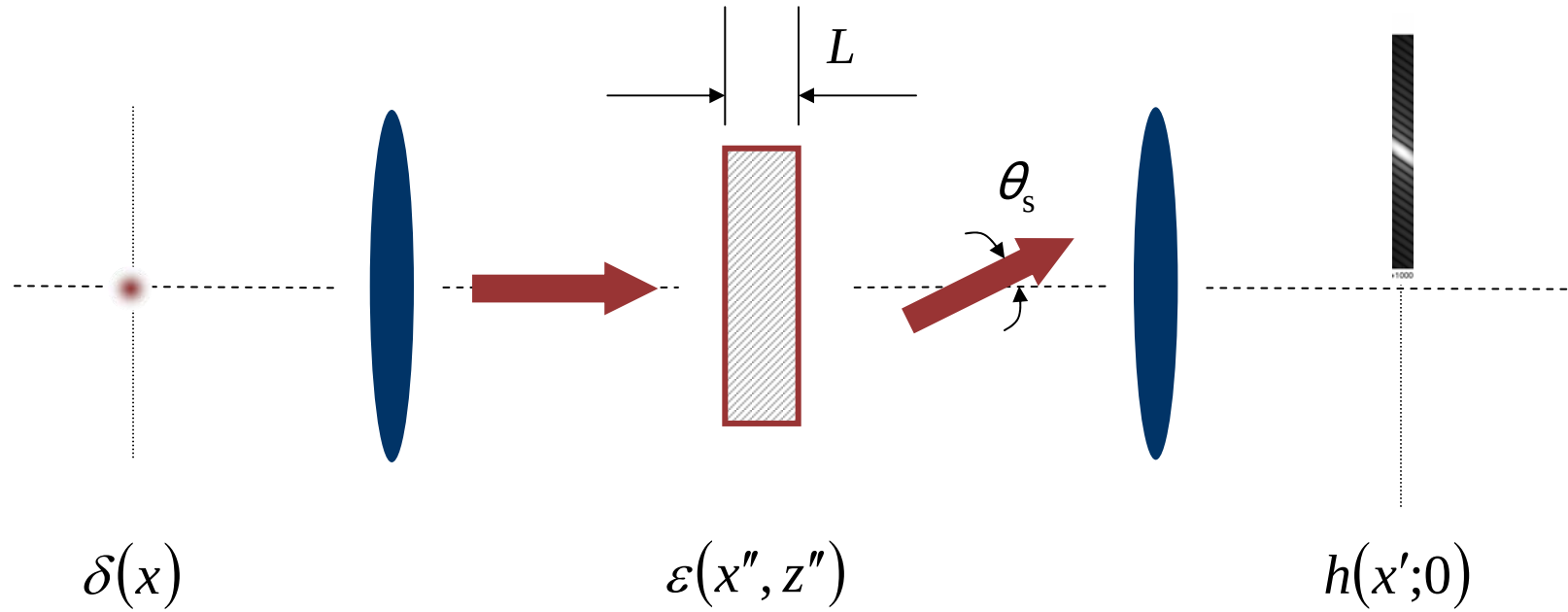
Optical imaging with 3D pupil: building the Hopkins matrix



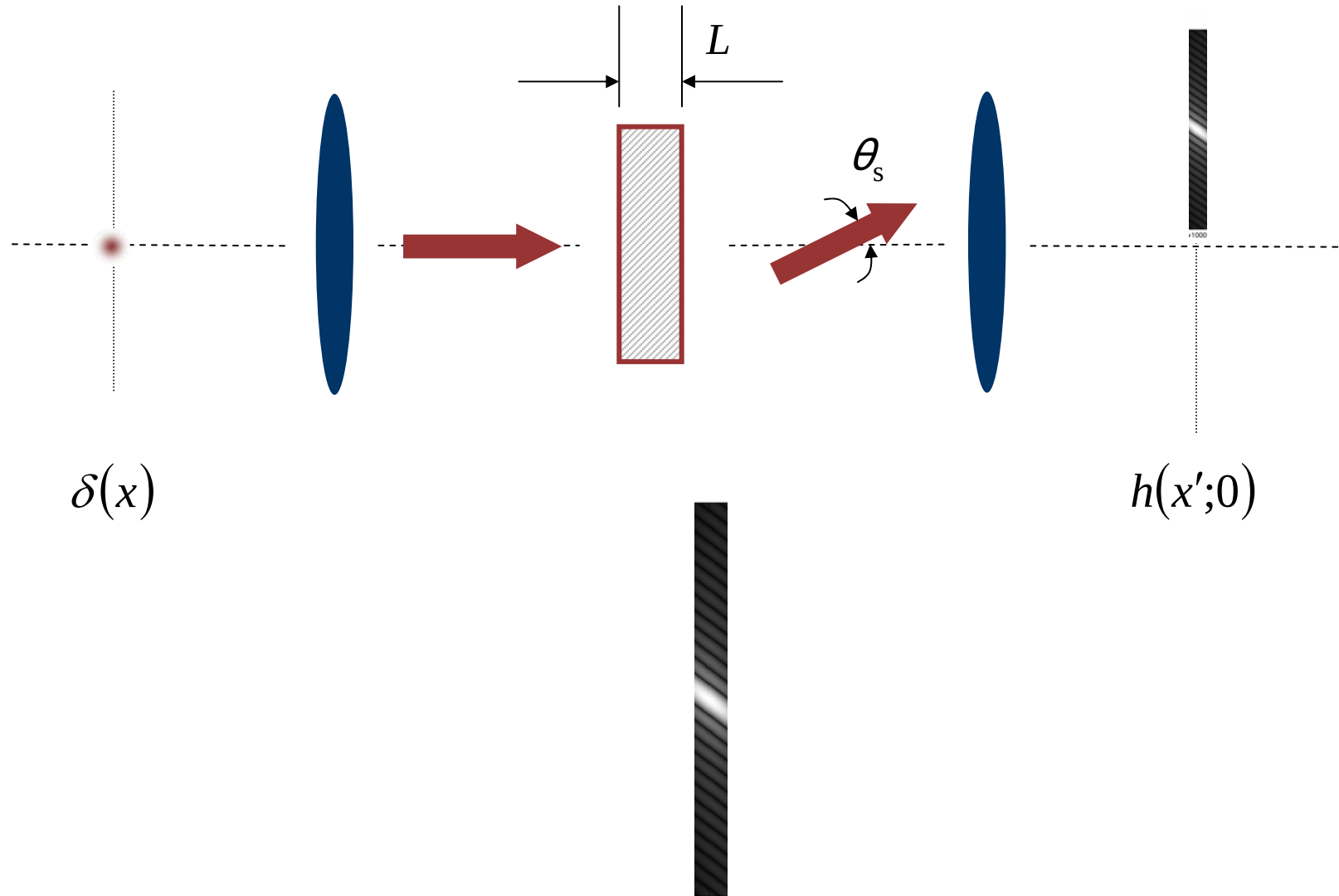
Plane-to-plane wave hologram
On-axis reference

$$\varepsilon(x'', z'') = \left| \exp(ikz) + \exp(ik[x \sin \theta_s + z \cos \theta_s]) \right|^2$$

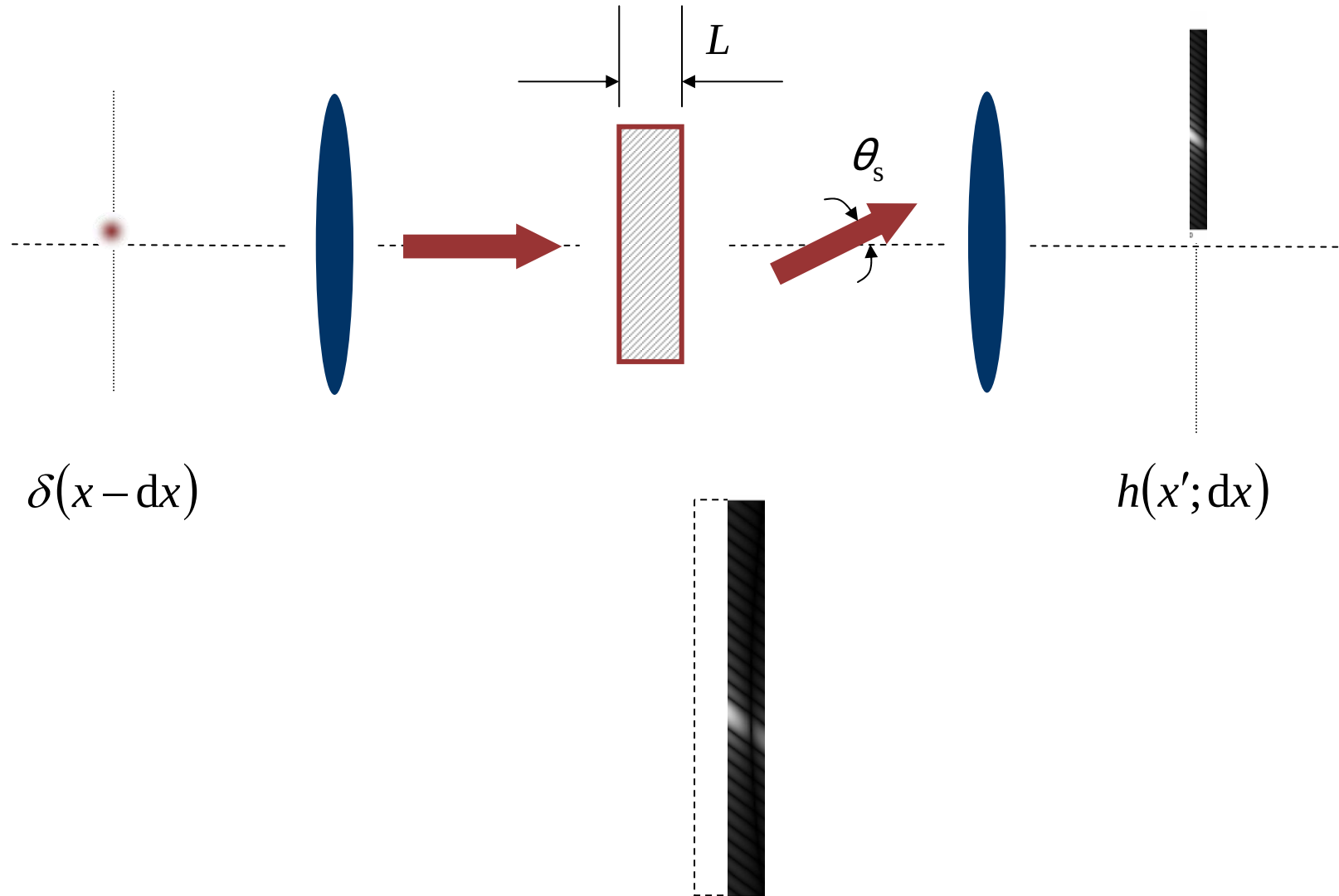
Optical imaging with 3D pupil: building the Hopkins matrix



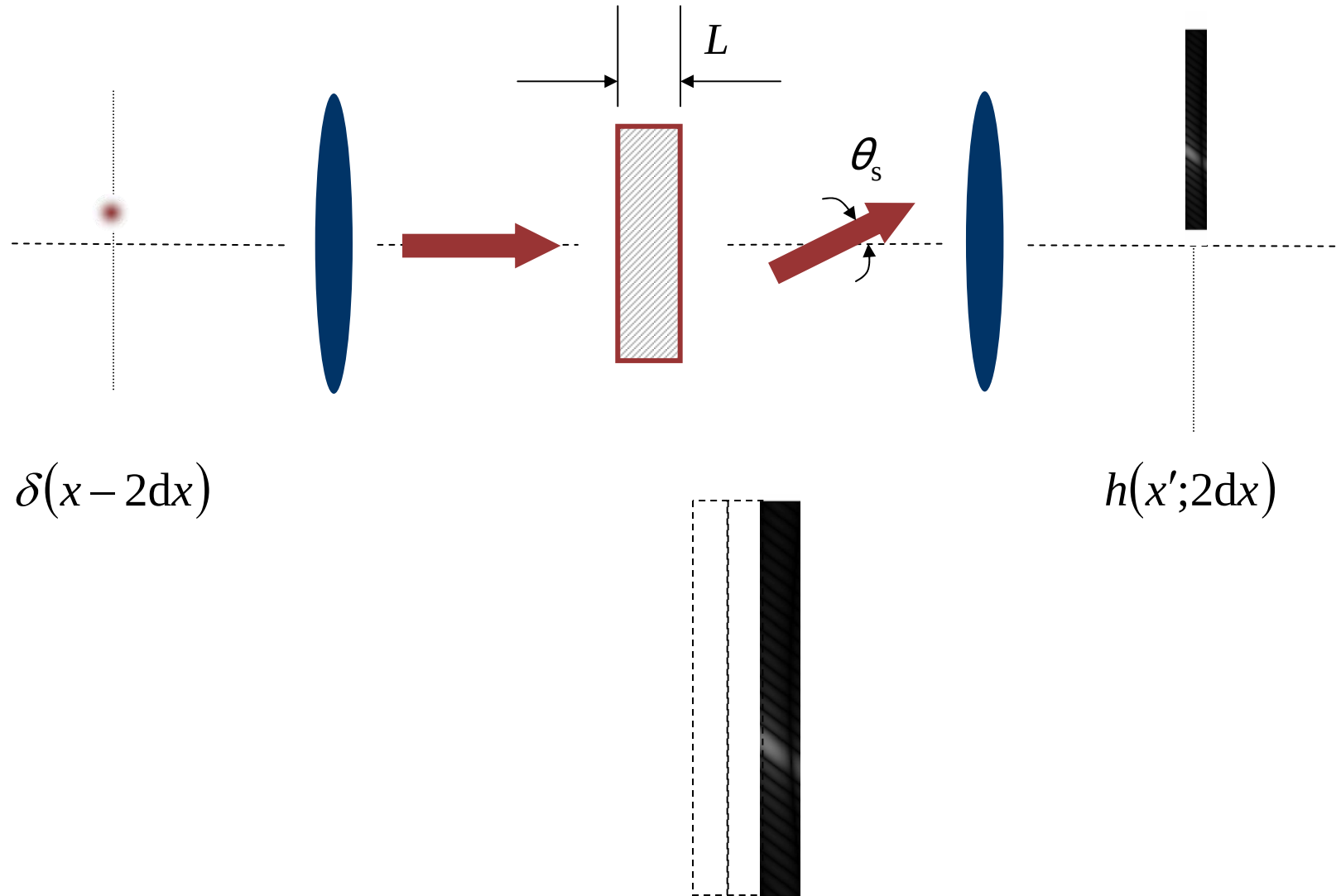
Optical imaging with 3D pupil: building the Hopkins matrix



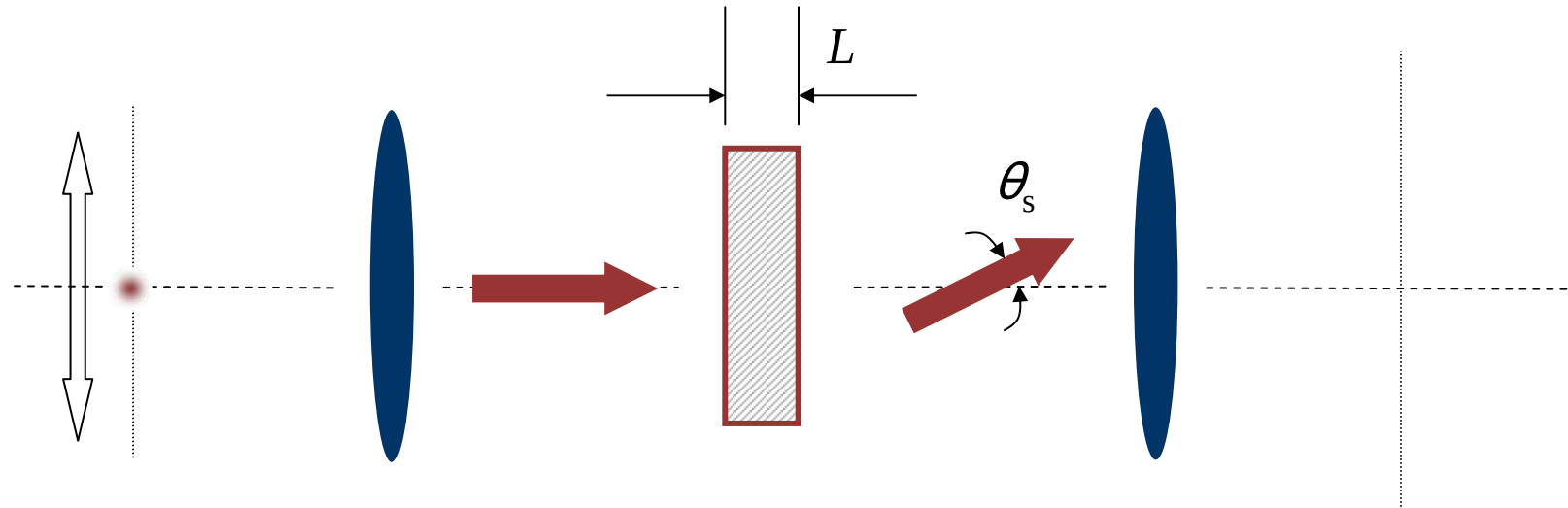
Optical imaging with 3D pupil: building the Hopkins matrix



Optical imaging with 3D pupil: building the Hopkins matrix

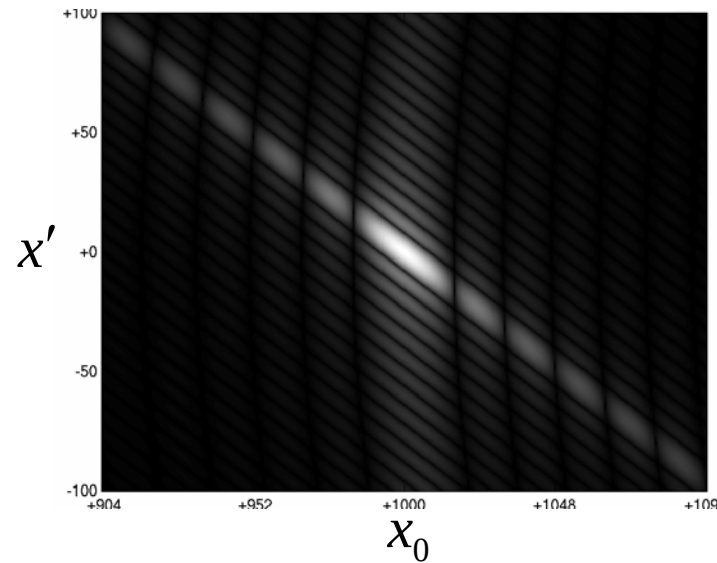


Optical imaging with 3D pupil: building the Hopkins matrix

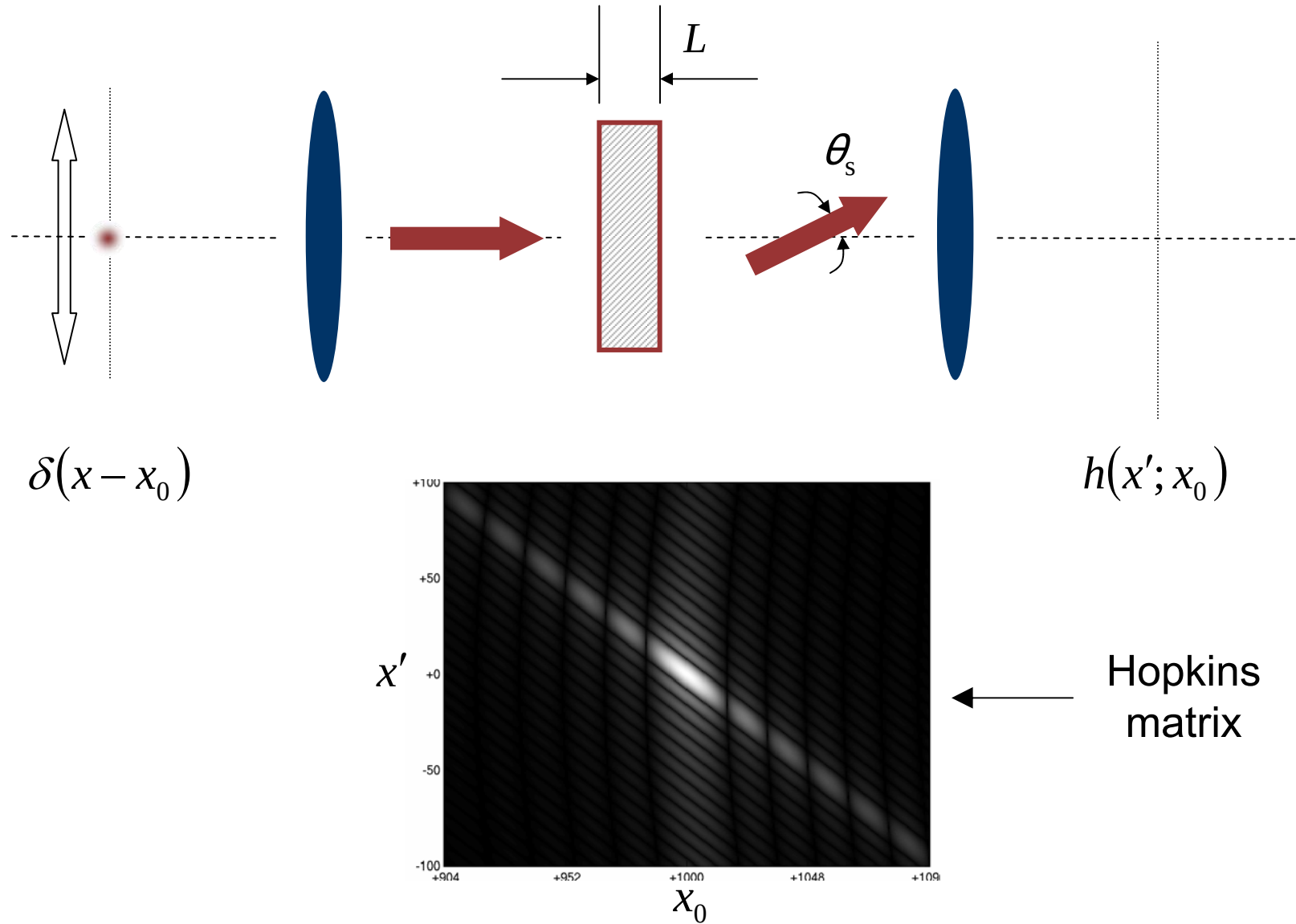


$$\delta(x - x_0)$$

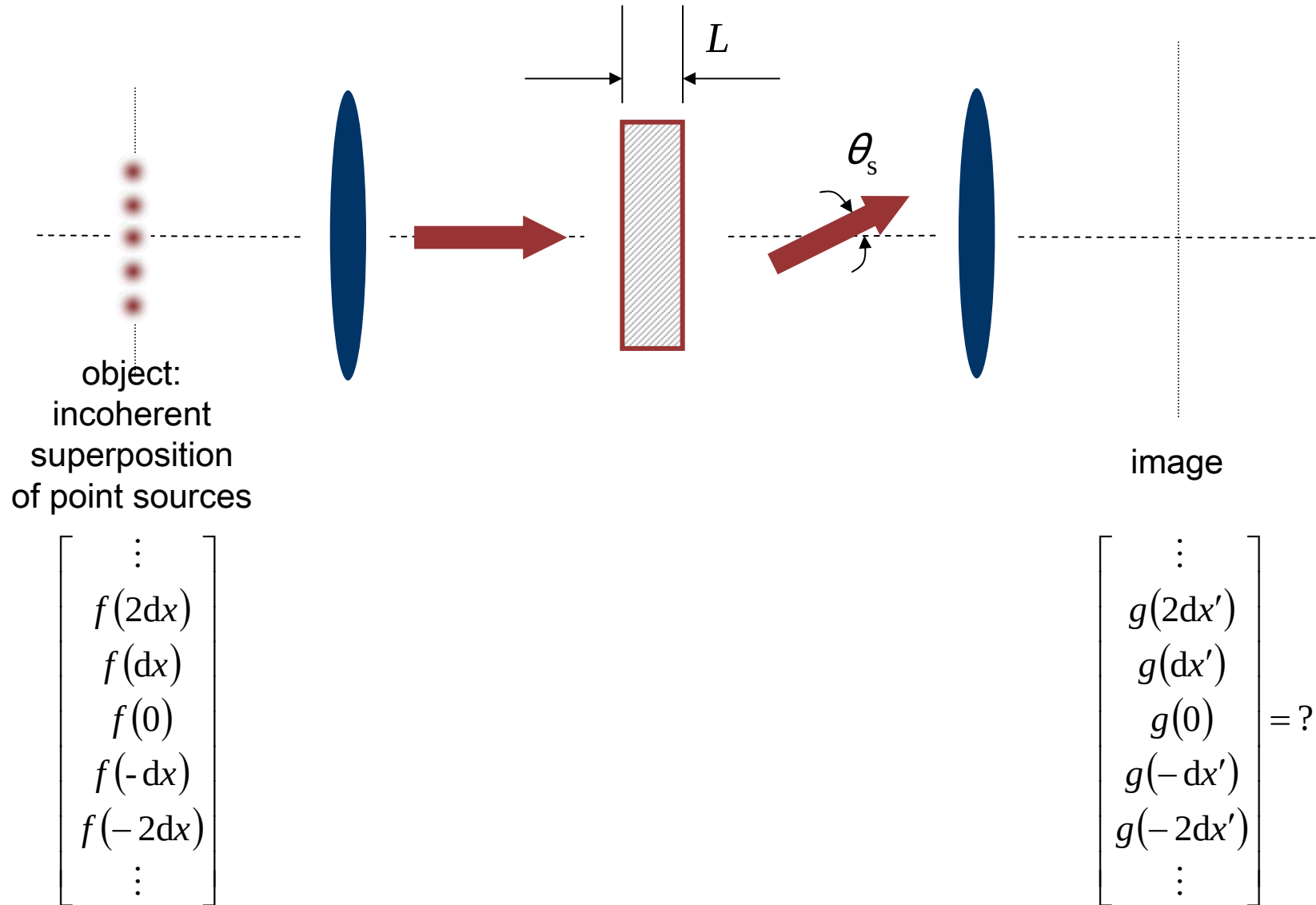
$$h(x'; x_0)$$



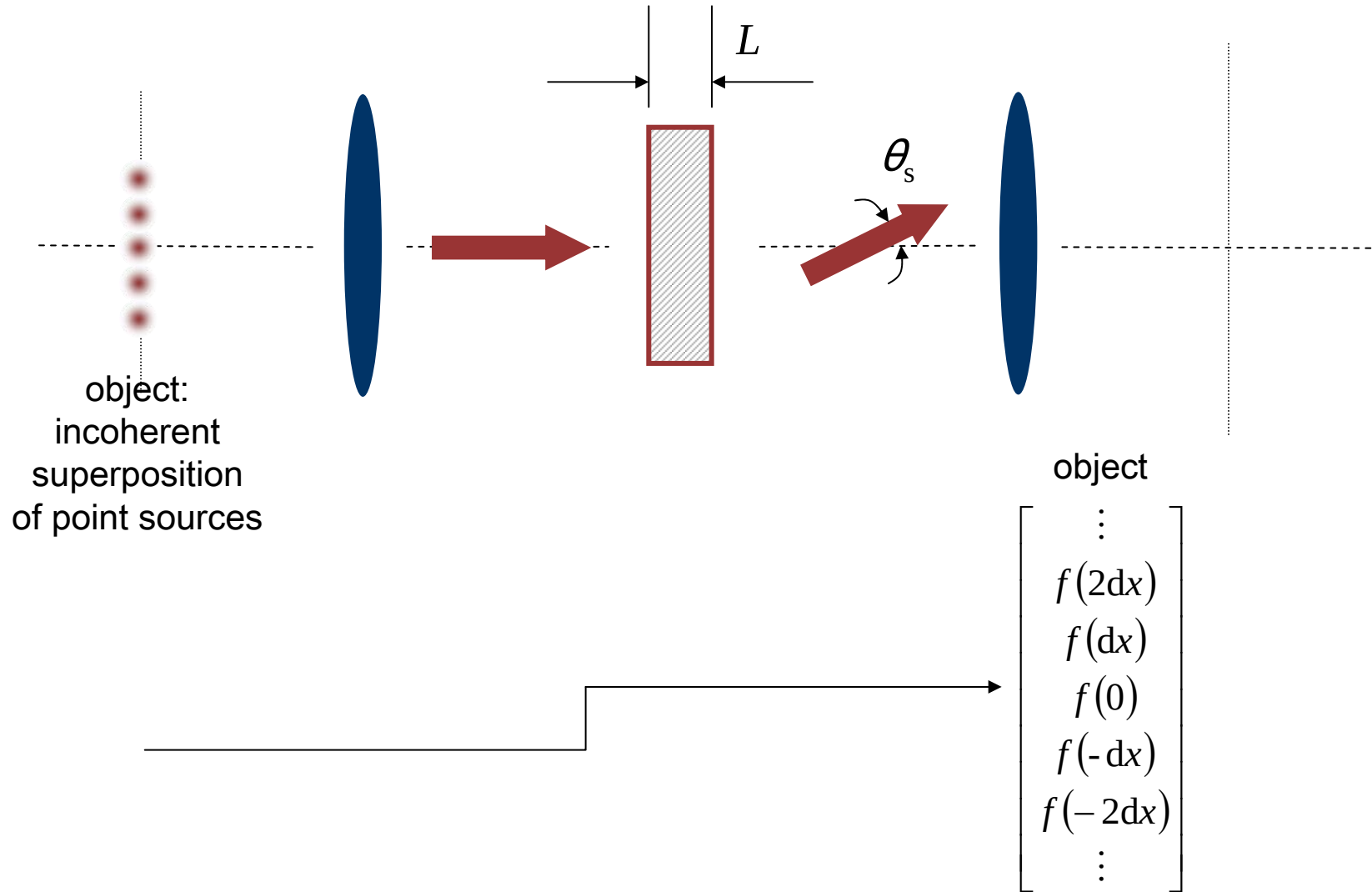
Optical imaging with 3D pupil: building the Hopkins matrix



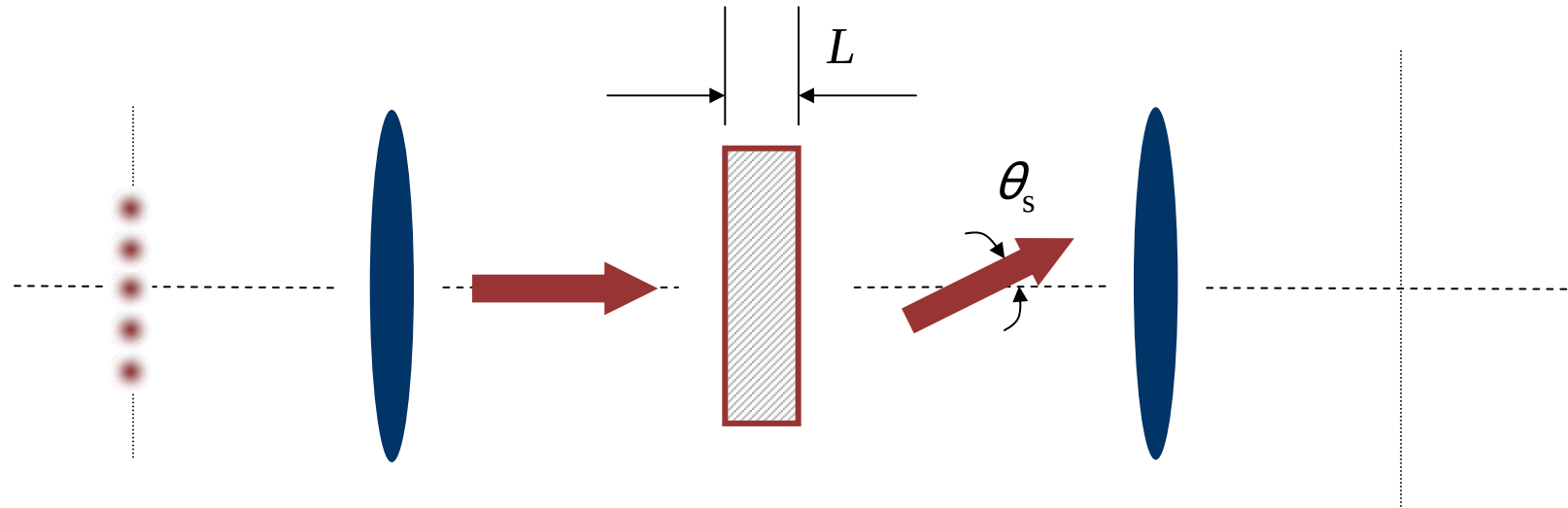
Incoherent imaging with 3D pupil



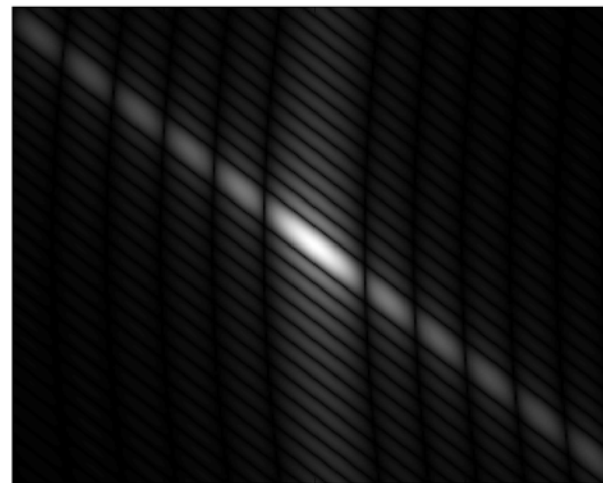
Incoherent imaging with 3D pupil



Incoherent imaging with 3D pupil



Hopkins matrix



object

$$\begin{bmatrix} \vdots \\ f(2dx) \\ f(dx) \\ f(0) \\ f(-dx) \\ f(-2dx) \\ \vdots \end{bmatrix}$$

Incoherent imaging with 3D pupil

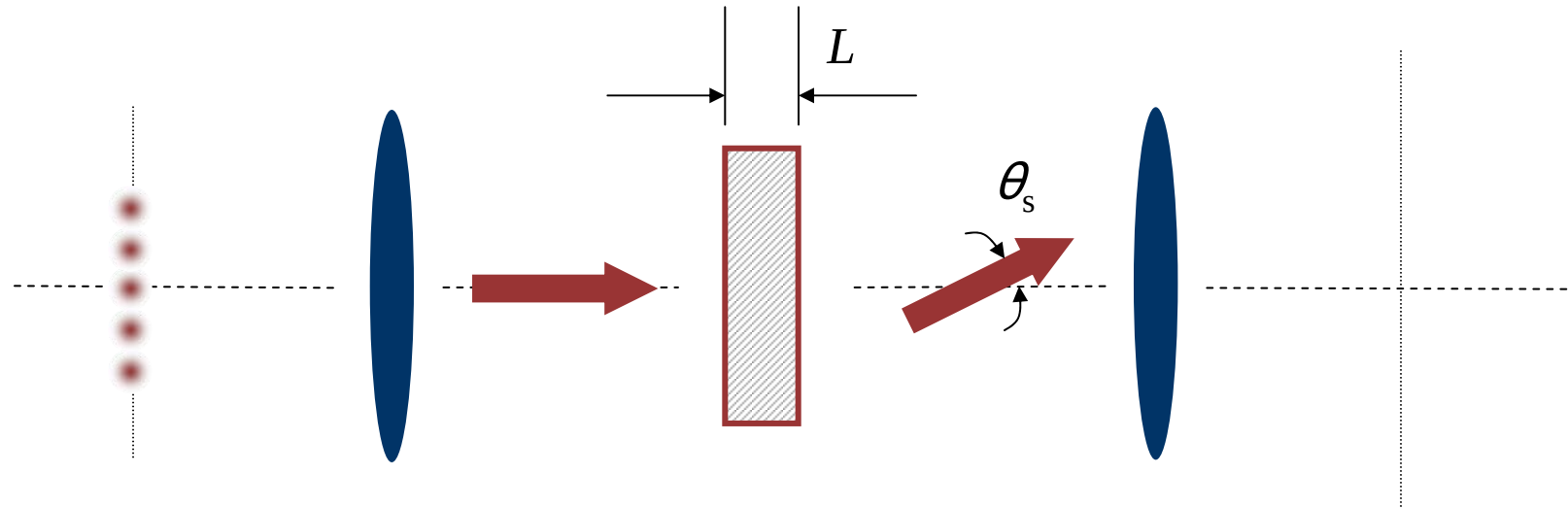
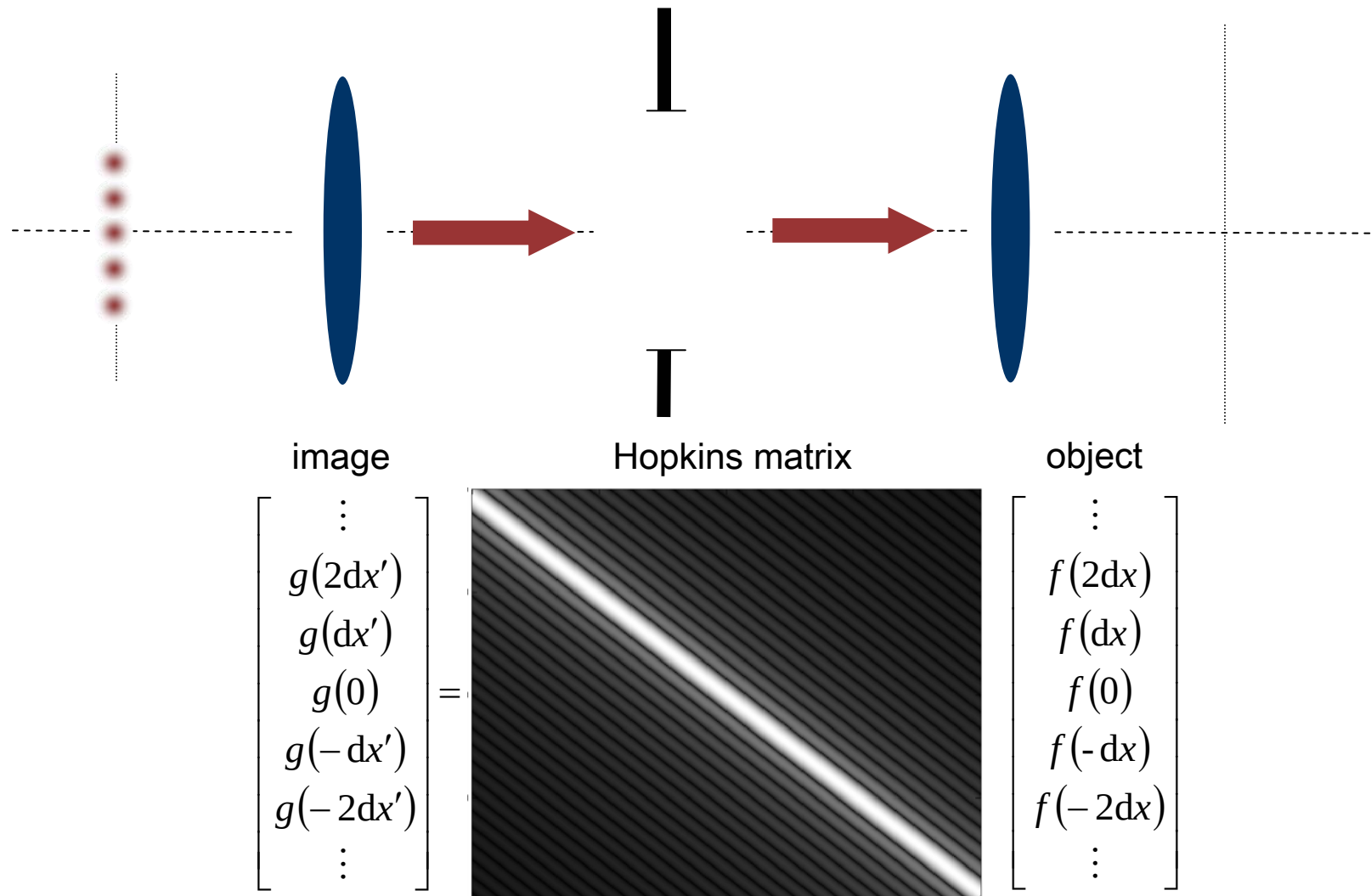
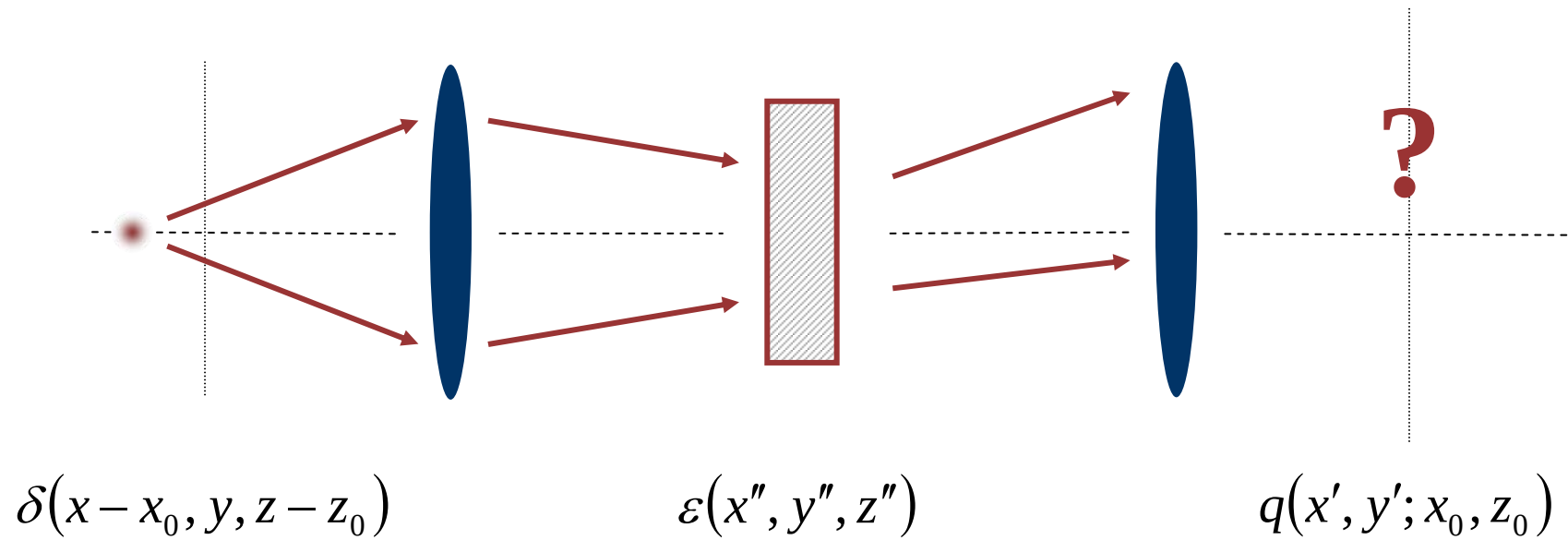


image		Hopkins matrix		object
$\begin{bmatrix} \vdots \\ g(2dx') \\ g(dx') \\ g(0) \\ g(-dx') \\ g(-2dx') \\ \vdots \end{bmatrix}$	=		=	$\begin{bmatrix} \vdots \\ f(2dx) \\ f(dx) \\ f(0) \\ f(-dx) \\ f(-2dx) \\ \vdots \end{bmatrix}$

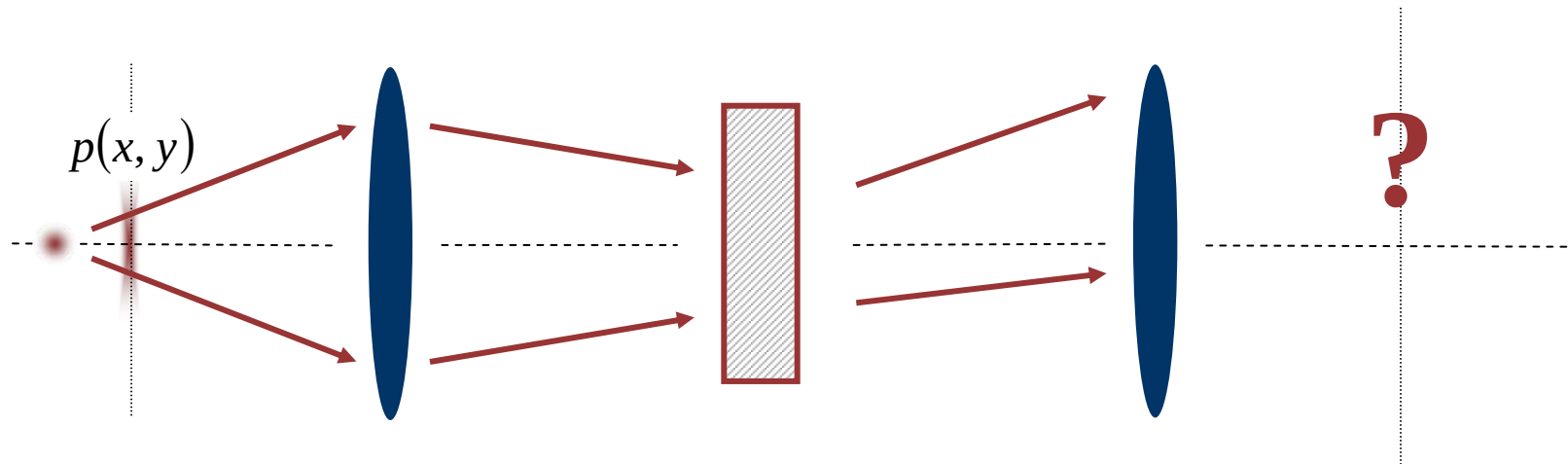
Incoherent imaging with clear (2D) pupil



Defocused response of 3D pupils



Defocused response of 3D pupils



$$\delta(x - x_0, y, z - z_0)$$

$$\varepsilon(x'', y'', z'')$$

$$q(x', y'; x_0, z_0)$$

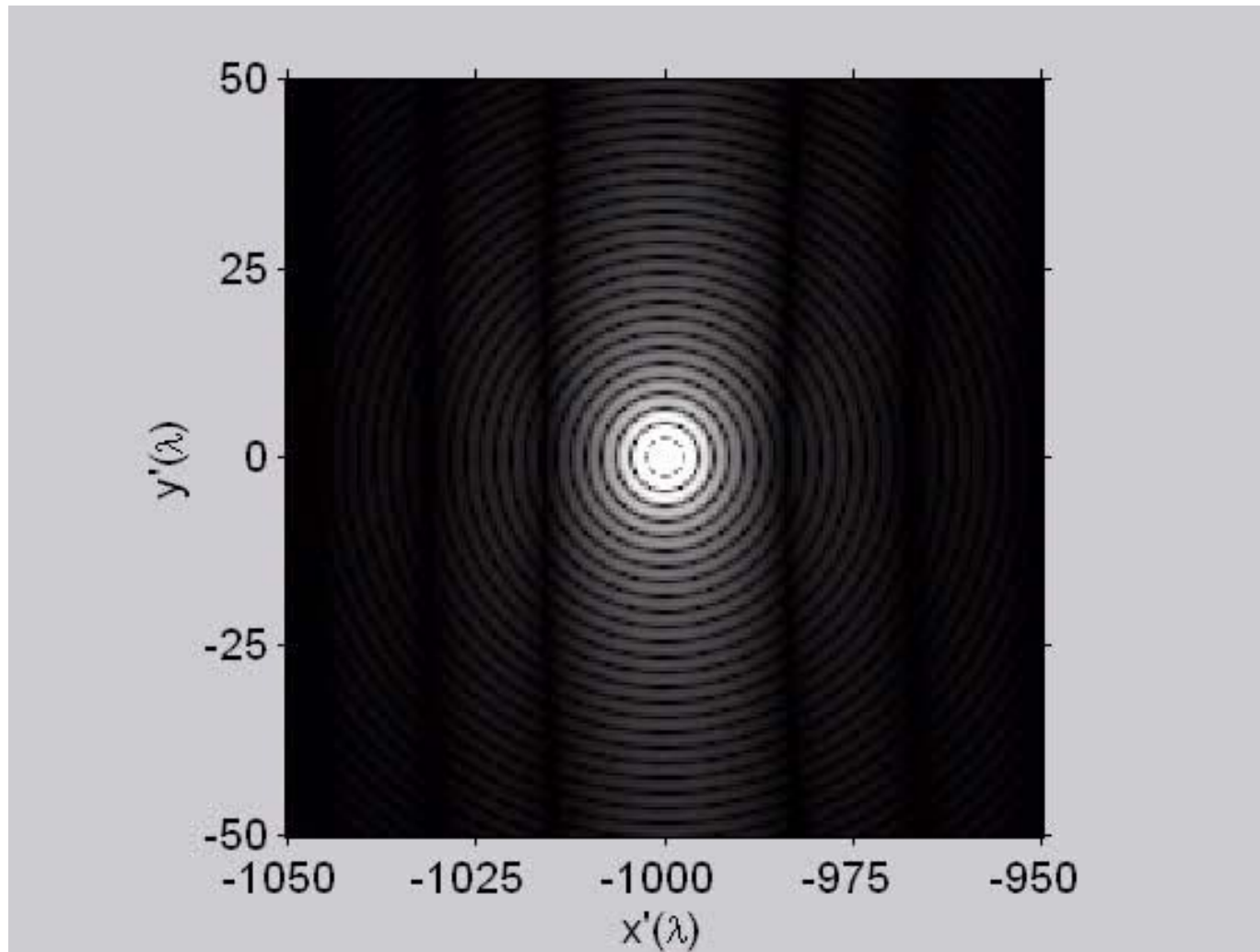
$$p(x, y) = \text{Fresnel}(z_0)$$

$$P(x'', y'', z'') = \exp\left\{i2\pi \frac{z}{\lambda}\right\} \iint dx dy p(x, y) \exp\left\{i2\pi \frac{xx'' + yy''}{\lambda f_1}\right\} \times \exp\left\{-i\pi \frac{(x^2 + y^2)z''}{\lambda f_1^2}\right\}$$

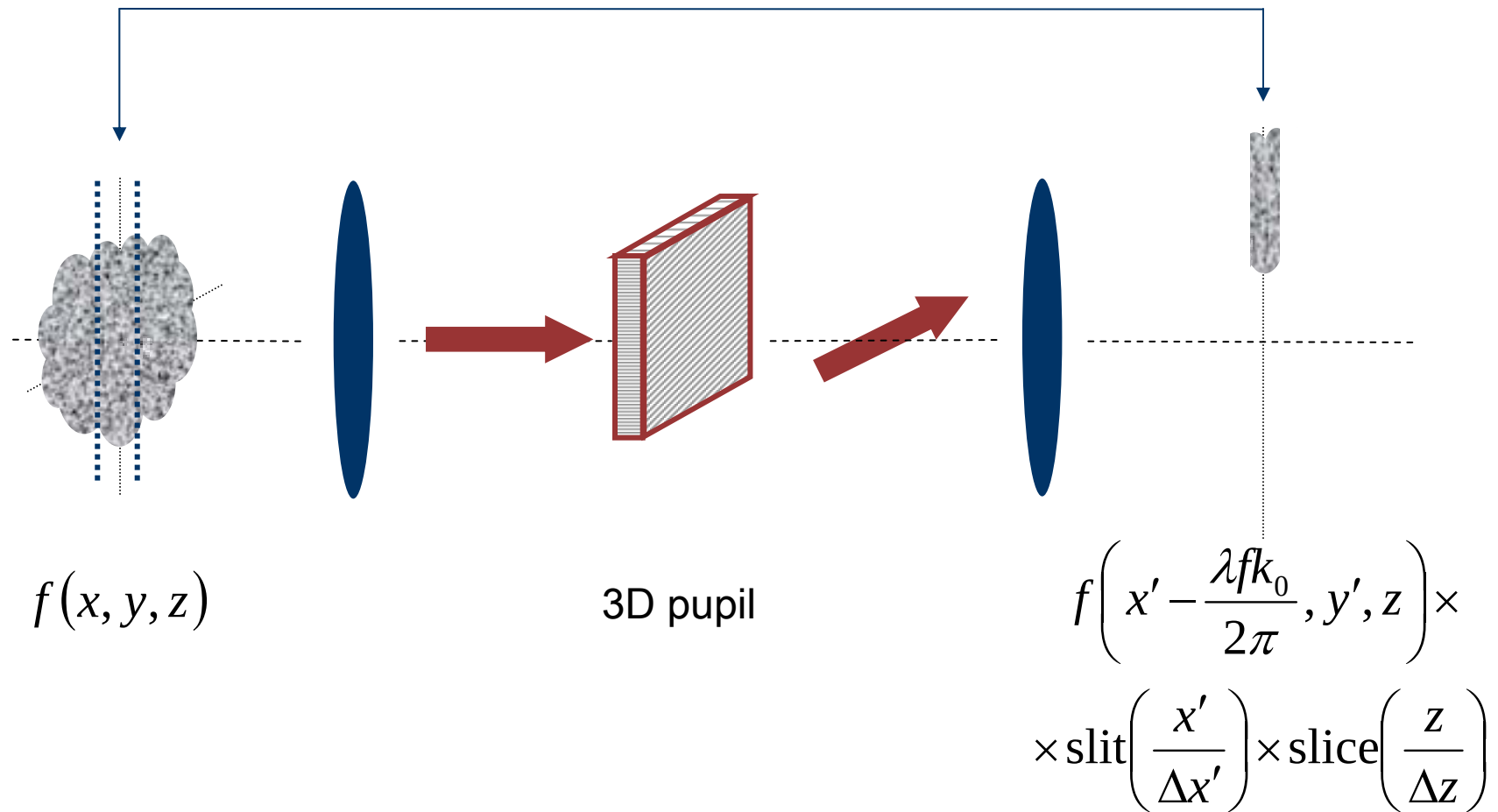
$$g(x'', y'', z'') = \varepsilon(x'', y'', z'') \times P(x'', y'', z'')$$

$$q(x', y') = G\left[\frac{x'}{\lambda f_2}, \frac{y'}{\lambda f_2}, \frac{1}{\lambda} \left(1 - \frac{x'^2 + y'^2}{2f_2^2}\right)\right]$$

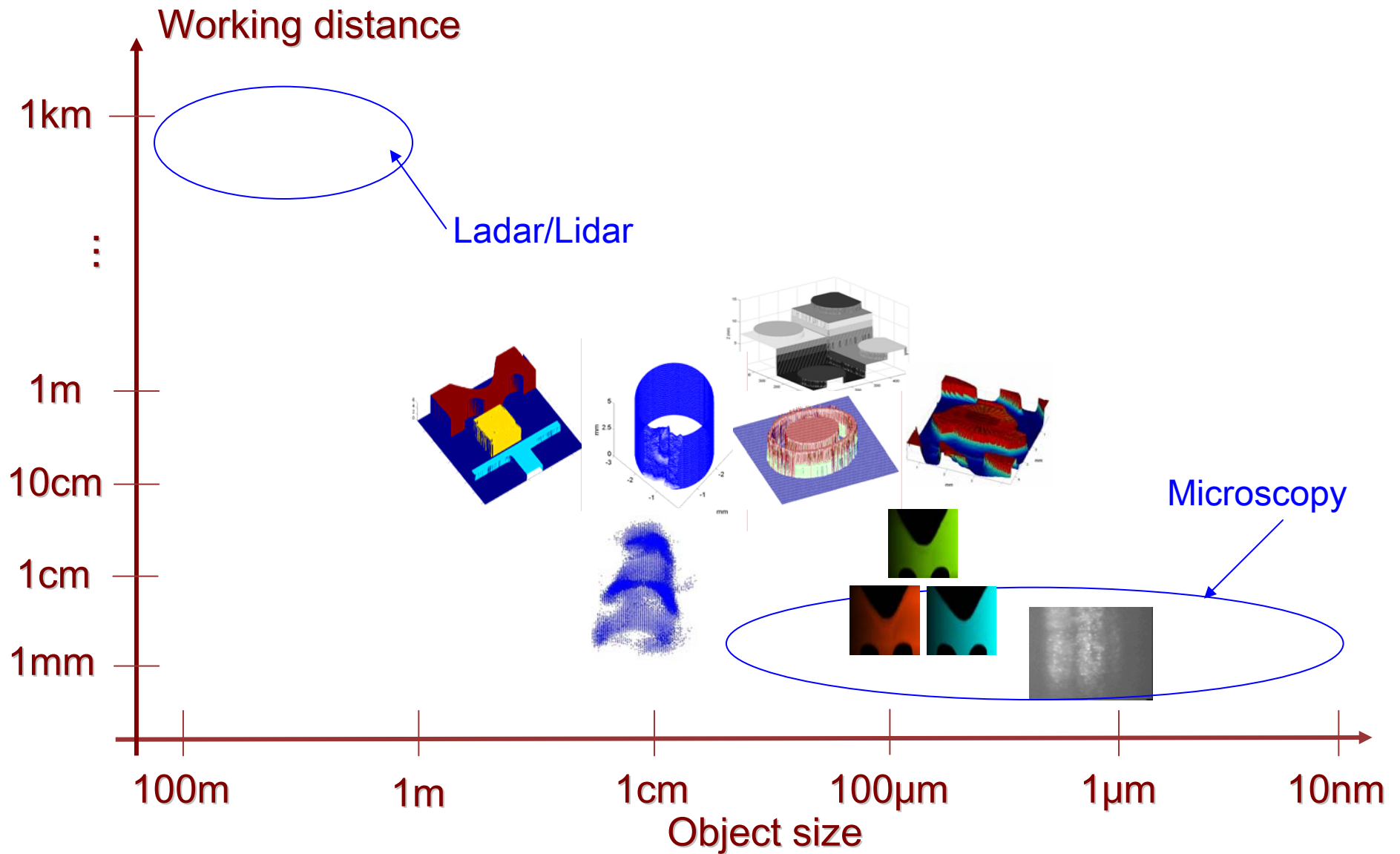
Blinking spot of 3D pupil



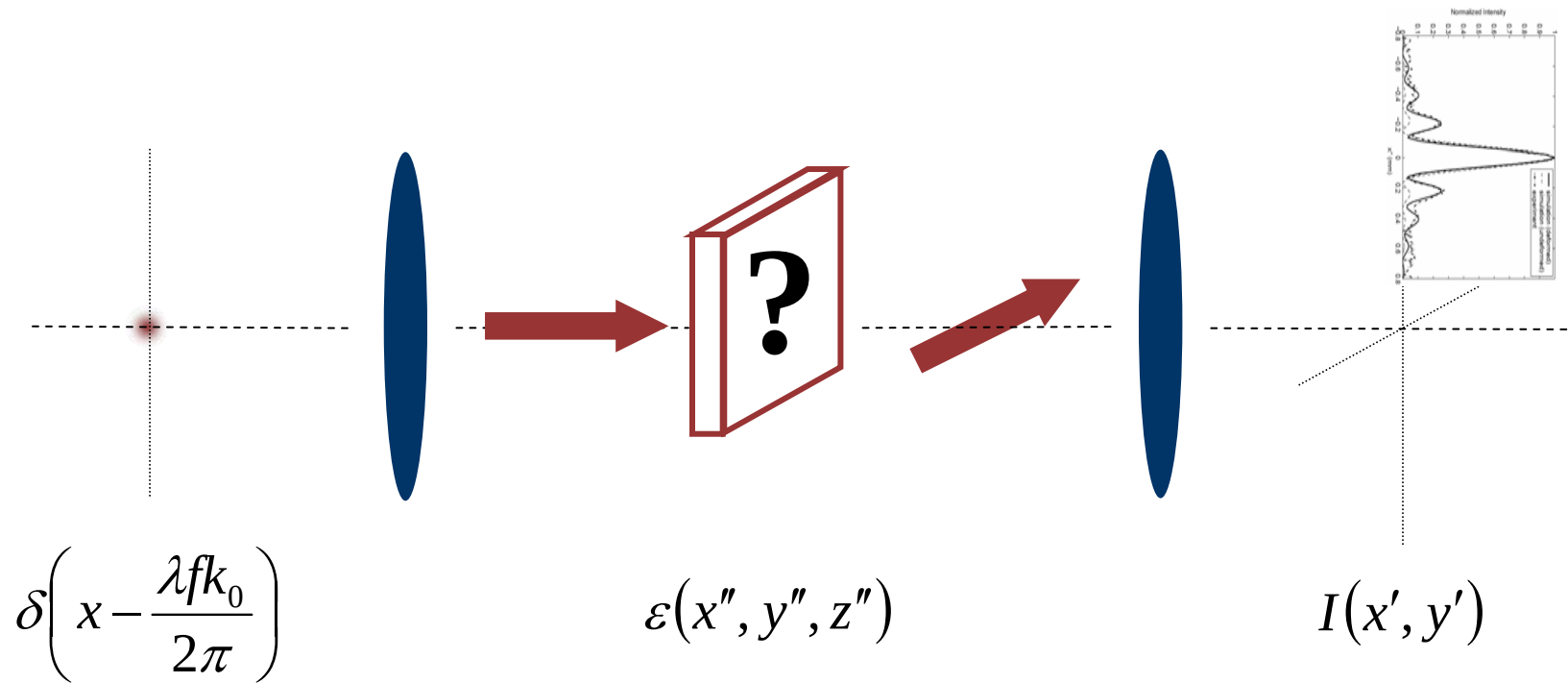
Applications: 3D holographic optical imaging



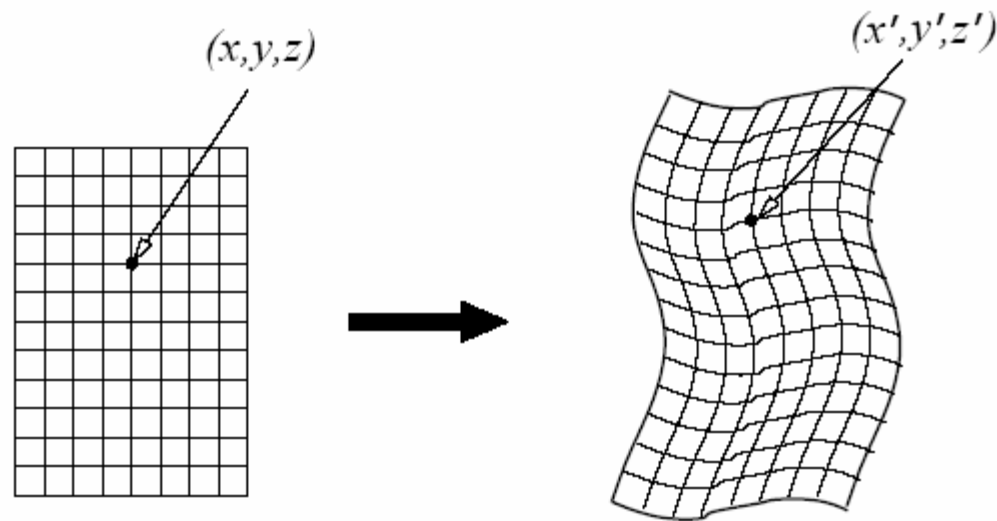
3D optics for imaging: summary



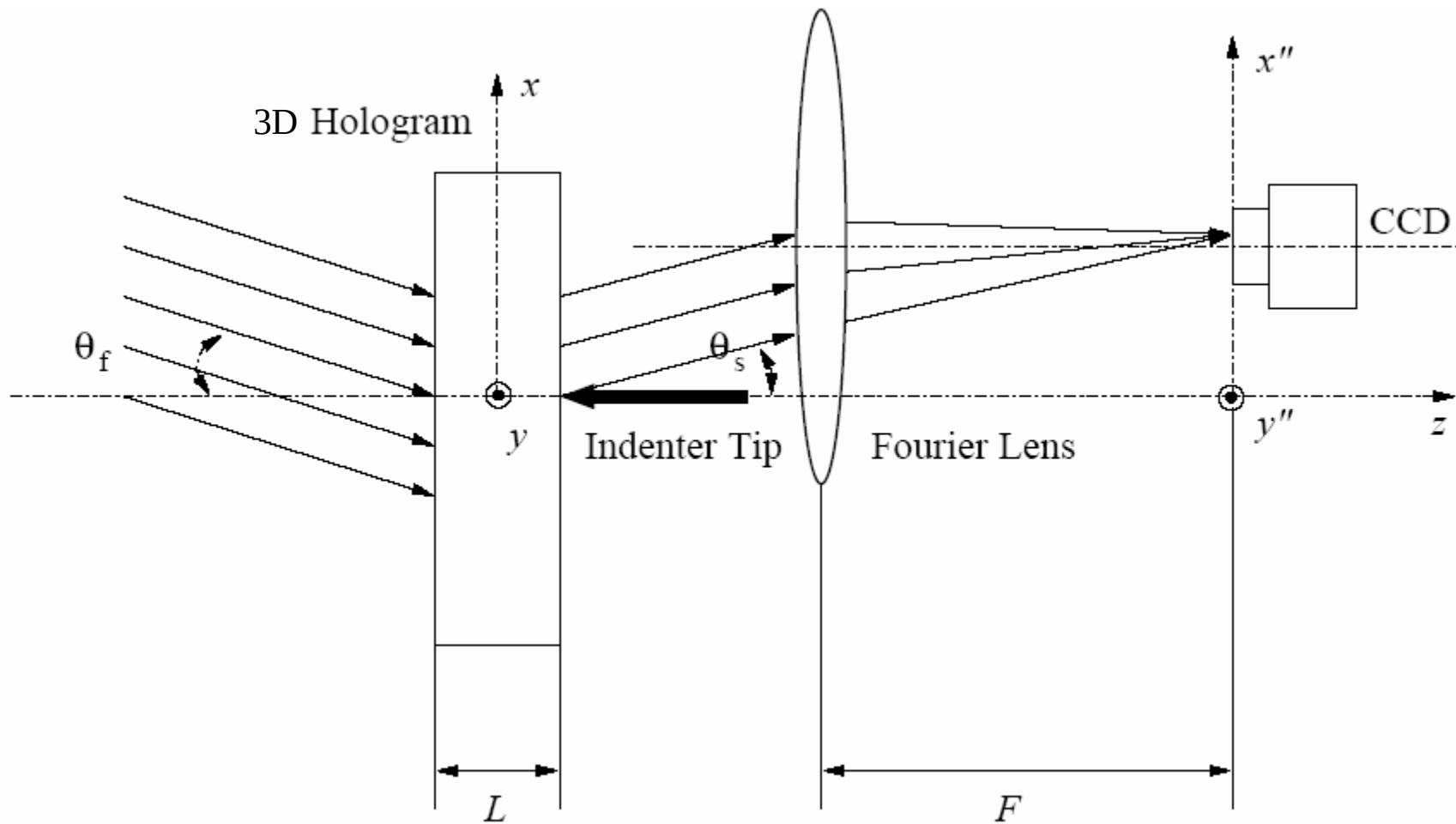
Probing unknown 3D holograms



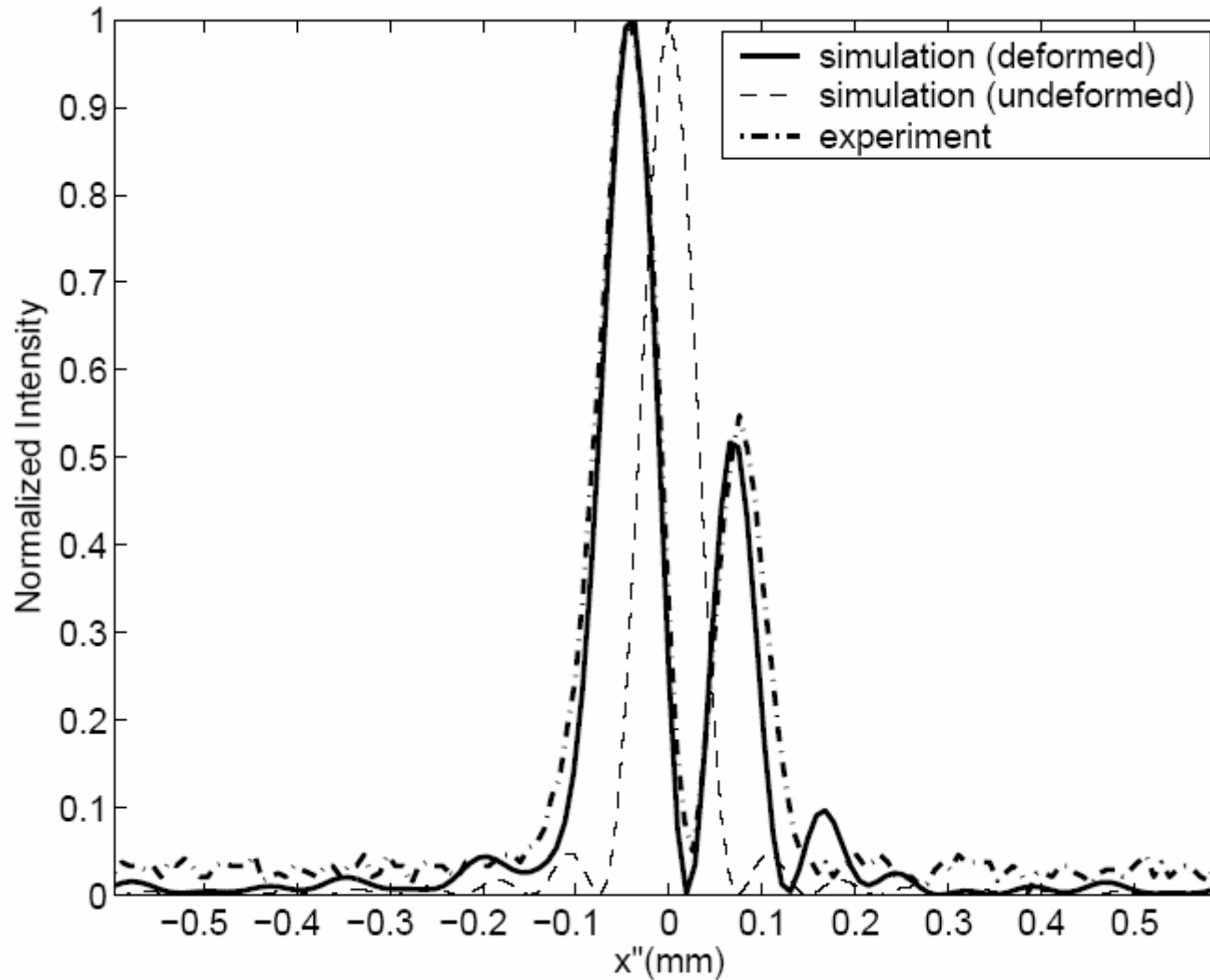
Diffraction from deformed 3D holograms



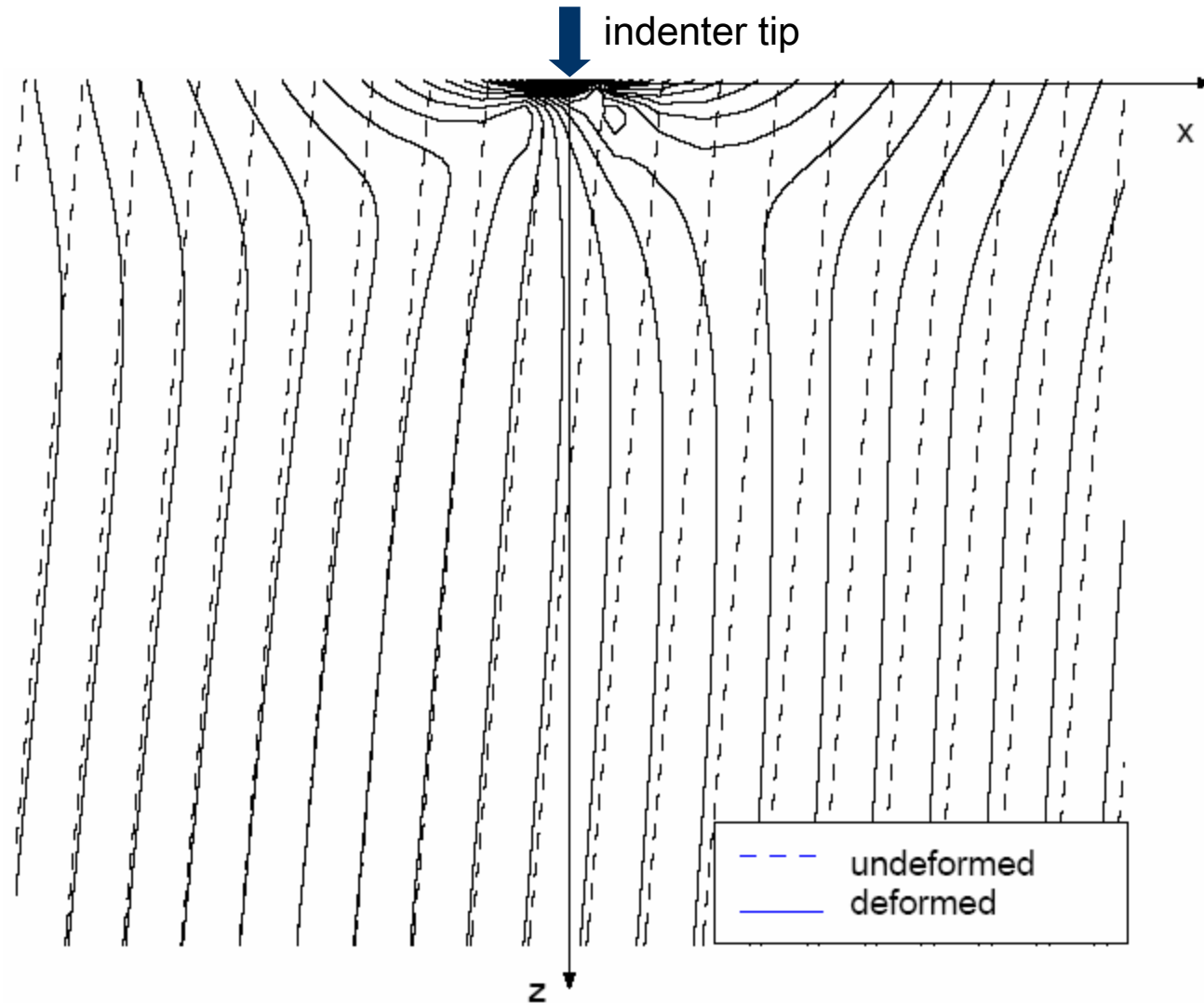
Experimental arrangement: transmission geometry



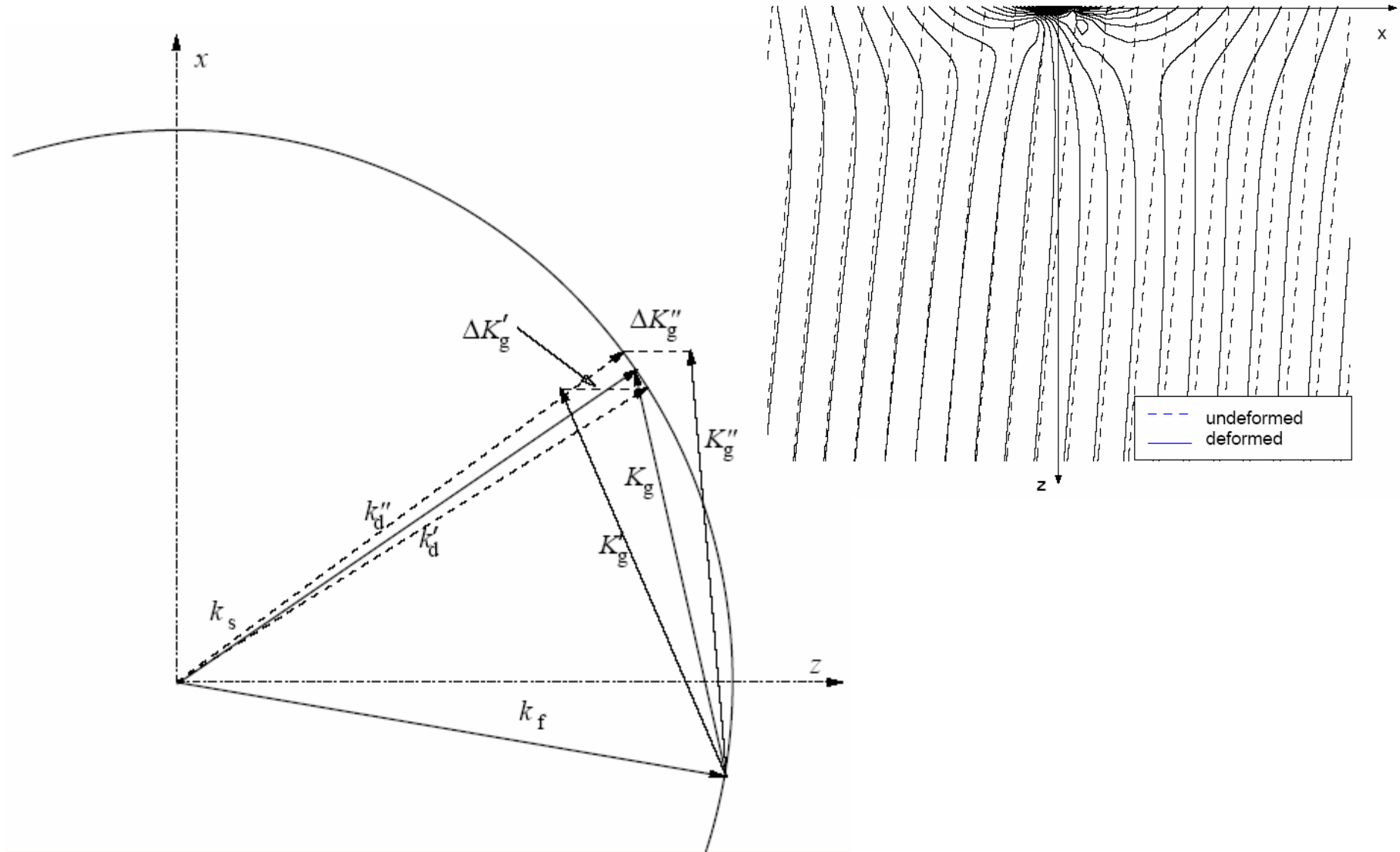
Experiment: diffraction from indented 3D hologram



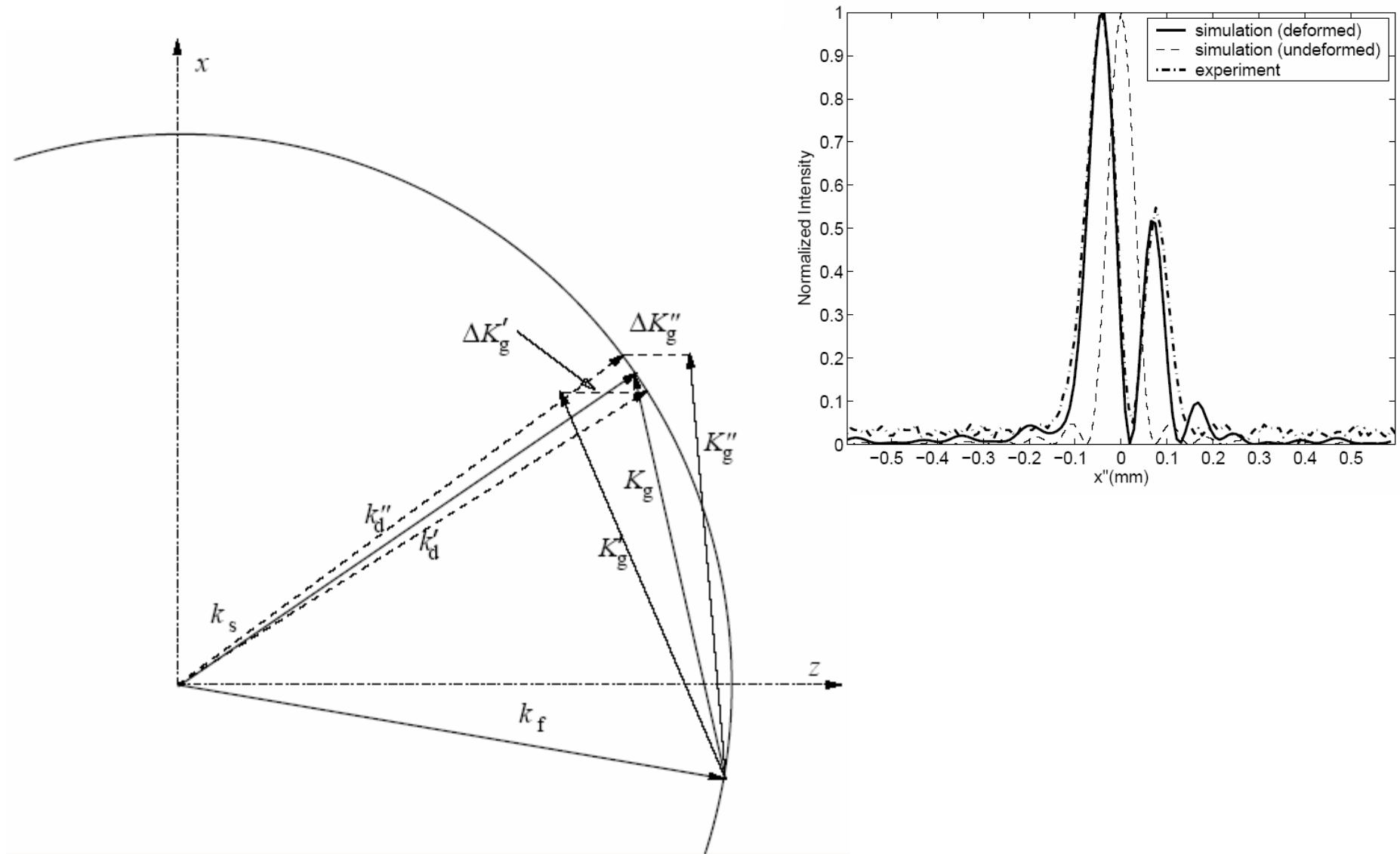
Fringe deformation due to indenter (transmission)



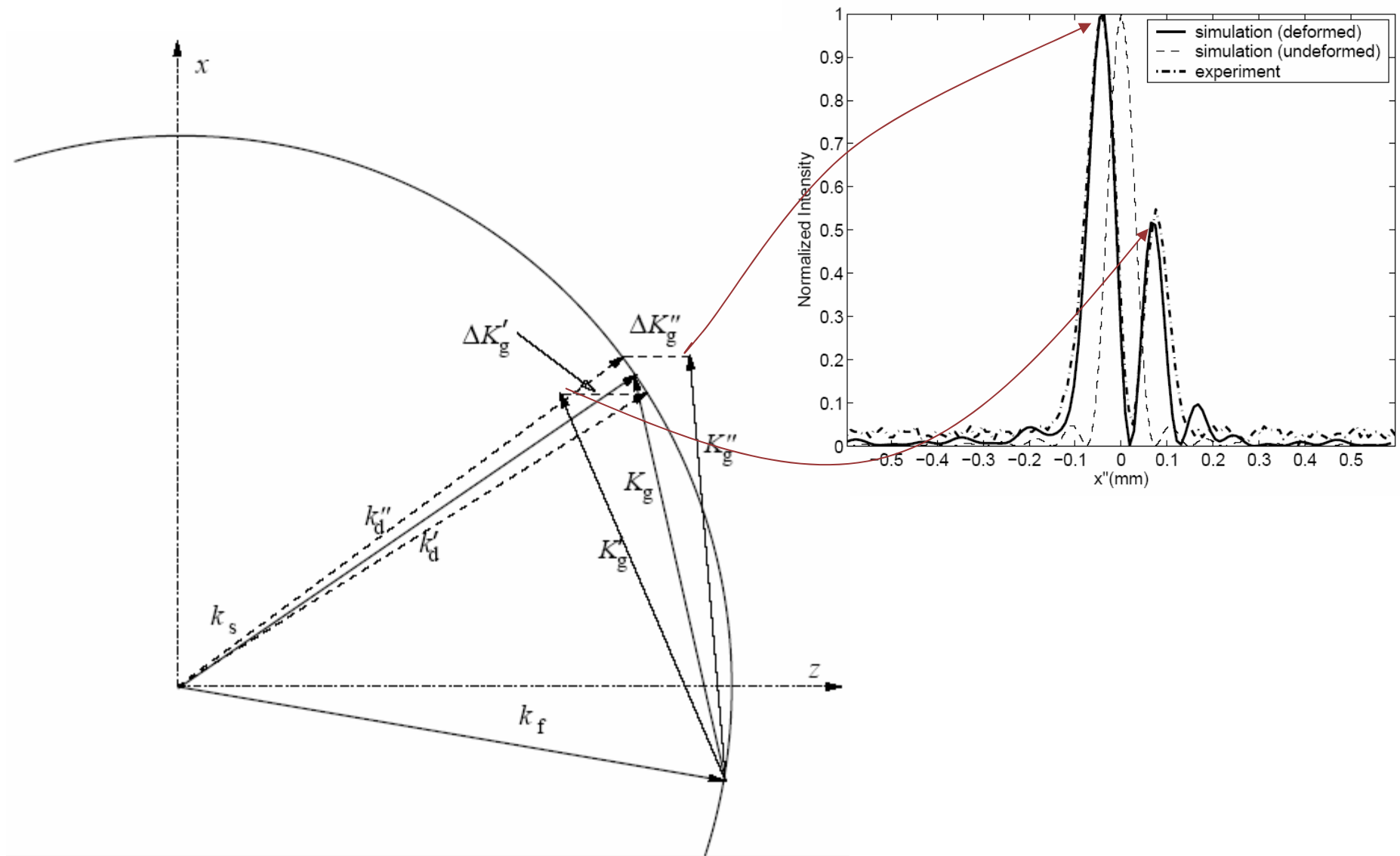
Deformed transmission 3D hologram in k -space



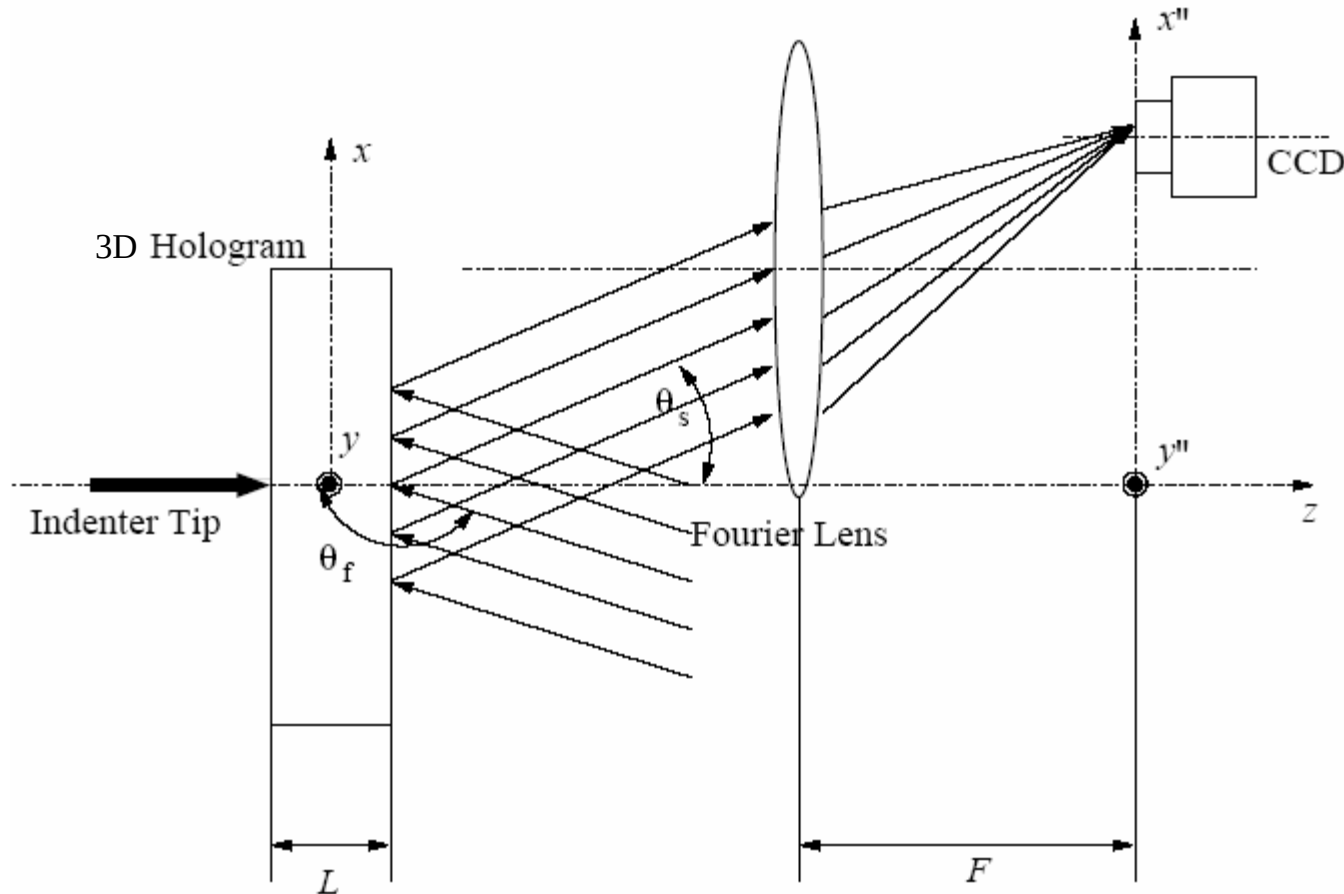
Deformed transmission 3D hologram in k -space



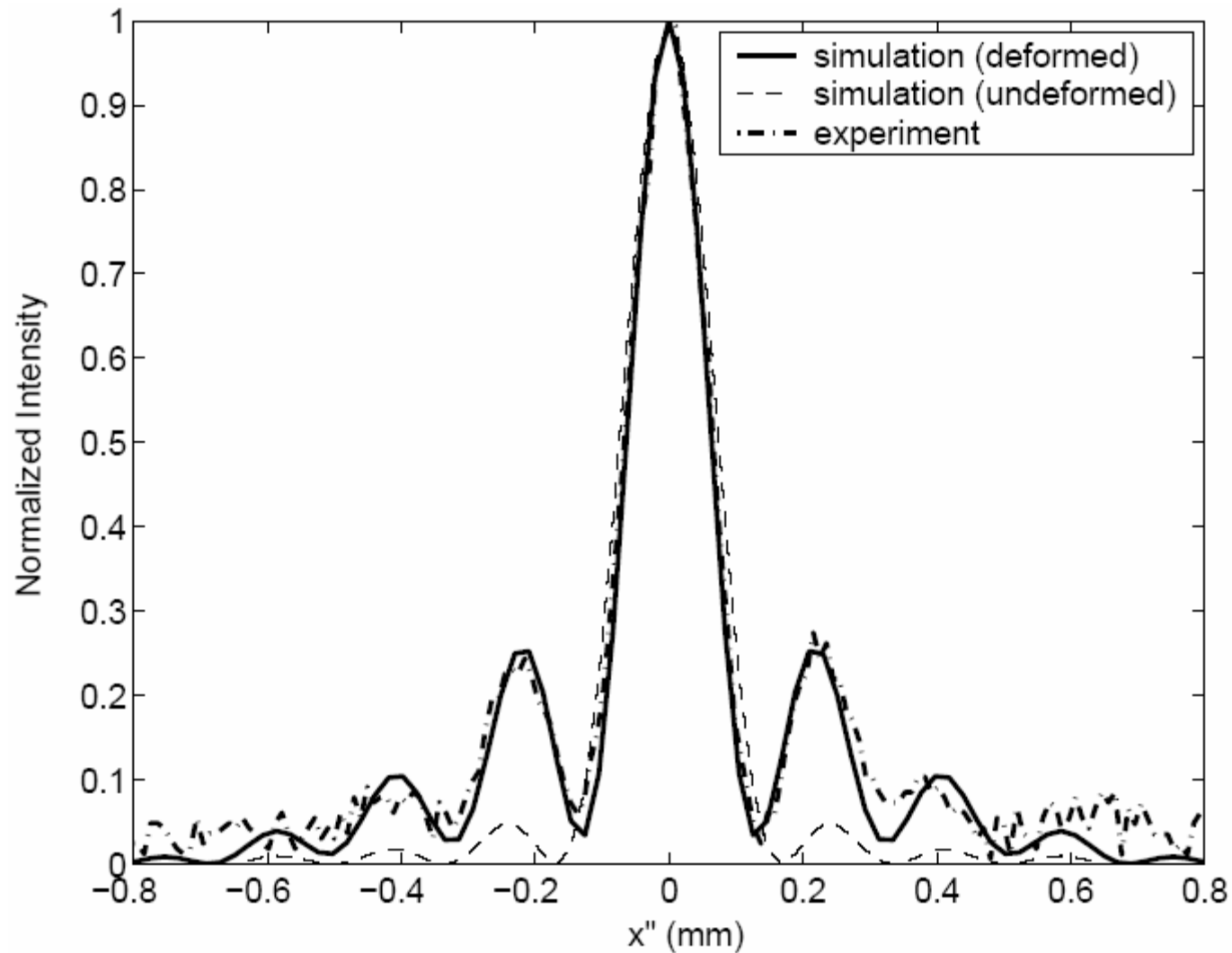
Deformed transmission 3D hologram in k -space



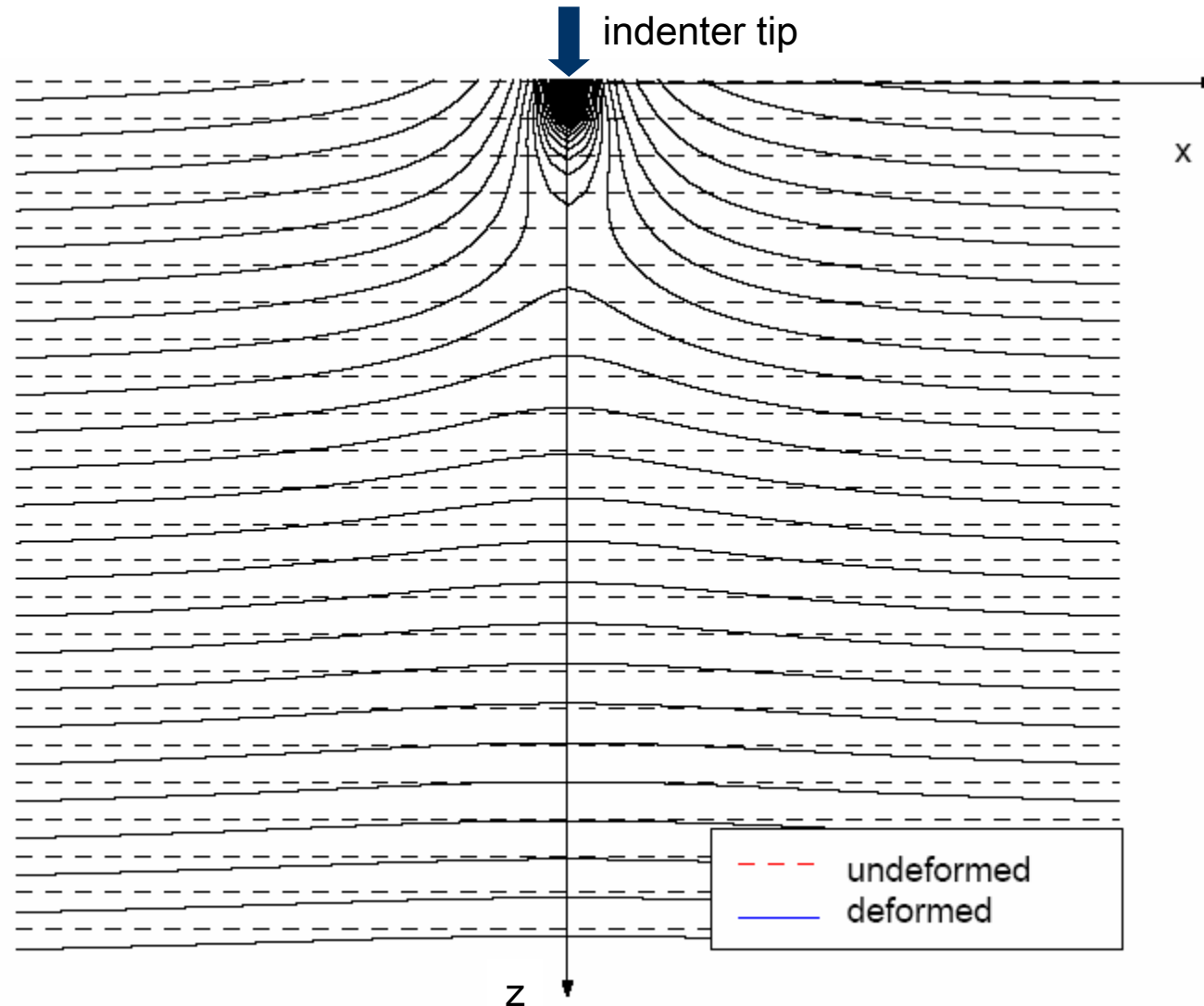
Experimental arrangement: reflection geometry



Experiment: diffraction from indented 3D hologram



Fringe deformation due to indenter (reflection)



Deformed reflection 3D hologram in k -space

