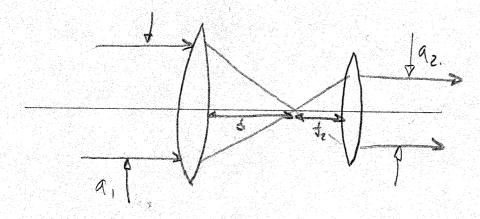


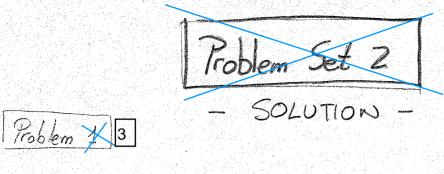
By inspection:

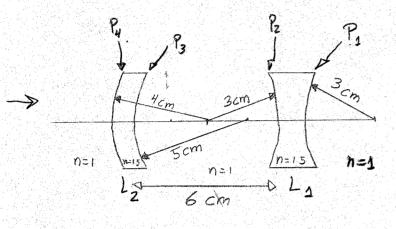
Li will bring a collimated beaut to focus @ fi. Similart, if we place 12, for from this focus, hight will emerge collimated.



Separation = 
$$d = f_1 + f_2$$

Width of outgoing Ray =  $\frac{5z}{5}$ ,  $a_1$ 





System Matrix

$$P_1 = \frac{1-1.5}{3} = -\frac{1}{6}$$

$$P_2 = \frac{1.5-1}{-3} = -\frac{1}{6}$$

$$P_3 = \frac{1-1.5}{5} = -\frac{1}{6}$$

$$P_4 = \frac{1}{5} = \frac{1}{4} = \frac{1}{8}$$

$$\begin{pmatrix} X_{OUT} \\ X_{OUT} \end{pmatrix} = \begin{pmatrix} Mahrix for \\ L_1 \end{pmatrix} \begin{pmatrix} Propagation \\ of 6cm \end{pmatrix} \begin{pmatrix} Mahrix for \\ L_2 \end{pmatrix} \begin{pmatrix} X_{in} \\ X_{in} \end{pmatrix}$$

Hehix for a fluck leas = 
$$\left(\frac{1-\frac{P'D}{n}}{n} - \left[\frac{P+P'-\frac{PP'D}{n}}{n}\right]\right)$$
 See Annex 1 for the derivation of this formula.

$$\begin{pmatrix}
Matrix for \\
L_1
\end{pmatrix} = \begin{pmatrix}
1 - \frac{P_1 \cdot 1 \text{ on}}{15} & - \left[P_2 + P_3 - \frac{P_2 \cdot P_3 \cdot 1 \text{ on}}{1.5}\right] \\
\frac{3 \text{ cm}}{1.5} & 1 - \frac{P_2 \cdot 1 \text{ cm}}{1.5}
\end{pmatrix} = \begin{pmatrix}
1.11 & 0.352
\end{pmatrix}$$

$$\begin{pmatrix}
Propagation \\
0 + 6 \text{ cm}
\end{pmatrix} = \begin{pmatrix}
1 & 0 \\
6 & 1
\end{pmatrix}$$

$$\begin{pmatrix}
Mahix for \\
Lz
\end{pmatrix} = \begin{pmatrix}
3 - \frac{13 \text{ 1cm}}{1.5} & -\left[\frac{1}{1.5} + \frac{1}{1.5} - \frac{1}{1.5} + \frac{1}{1.5} - \frac{1}{1.5} -$$

$$\begin{pmatrix} d_{\text{OUT}} \\ \chi_{\text{OUT}} \end{pmatrix} = \begin{pmatrix} 1.11 & 0.352 \\ 0.666 & 1.11 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 6 & 1 \end{pmatrix} \begin{pmatrix} 1.067 & -0.03 \\ 0.67 & 0.917 \end{pmatrix} \begin{pmatrix} \chi_{\text{IN}} \\ \chi_{\text{IN}} \end{pmatrix}$$

$$= \begin{pmatrix} 3.67 & 0.215 \\ 8.56 & 0.77 \end{pmatrix} \begin{pmatrix} \chi_{\text{IN}} \\ \chi_{\text{IN}} \end{pmatrix}$$

$$Power = -M_{12} = -0.215.$$

Plane wave incident from the left:

$$\begin{pmatrix}
X_{017} \\
X_{017}
\end{pmatrix} = \begin{pmatrix}
1 & 0 \\
D & 1
\end{pmatrix} \begin{pmatrix}
M \\
M \\
X_{1N}
\end{pmatrix}$$

$$= \begin{pmatrix}
1 & 0 \\
D & 1
\end{pmatrix} \begin{pmatrix}
3.67 & 0.215 \\
8.56 & 0.77
\end{pmatrix} \begin{pmatrix}
0 \\
X_{1N}
\end{pmatrix}$$

$$= \begin{pmatrix}
1 & 0 \\
D & 1
\end{pmatrix} \begin{pmatrix}
6.215 X_{1N} \\
0.77 X_{1N}
\end{pmatrix} = \begin{pmatrix}
0.215 X_{1N} \\
(6.215 \cdot D + 0.77) X_{1N}
\end{pmatrix}$$

focal length =  $f = \frac{1}{0.215} = -4.65$  cm (This is the Effective Focal Length (EFL) This distance is referenced to the principal control of the

This distance is referenced to the principal planes of the system)

Focus Condition: Xout = 0

$$X_{or} = (0.215D + 0.79) = 0$$

$$D = -3.58 \text{ cm}$$

$$D = -3.58 cm$$

This distance is referenced to the last surface of the optical system, as depicted in the diagram

(3)

c) Object @ infinity

The image will be virtual.

DA thin 6i-convex lens of index 1.5 is known to have I focal length of 50 cm in air When immersed in a transparent liquid medium, the focal length is measured to be 250 cm. What is the refractive lindex in of the liquid Soln.

power 
$$P = (n_g - n_s) \left(\frac{1}{R_i} - \frac{1}{R_l}\right)$$

+> find the foral length of

$$\left(\frac{1}{n_s}\right)\left(\frac{1}{0}\right)\left(\frac{1}{y}\right) = \left(\frac{1}{n_s}\right)\left(\frac{1}{y}\right) = \left(\frac{1}{n_s}\right)\left(\frac{1}{y}\right) = \left(\frac{1}{n_s}\right)\left(\frac{1}{y}\right) = \left(\frac{1}{n_s}\right)\left(\frac{1}{y}\right)$$

$$\left(1-\frac{Pd}{n_s}\right)y=0$$
 (for all y)  $\Rightarrow d=\frac{n_s}{P}$ 

olir: 
$$\frac{1}{(1.5-1)(\frac{1}{R}-\frac{1}{R_1})}=50$$

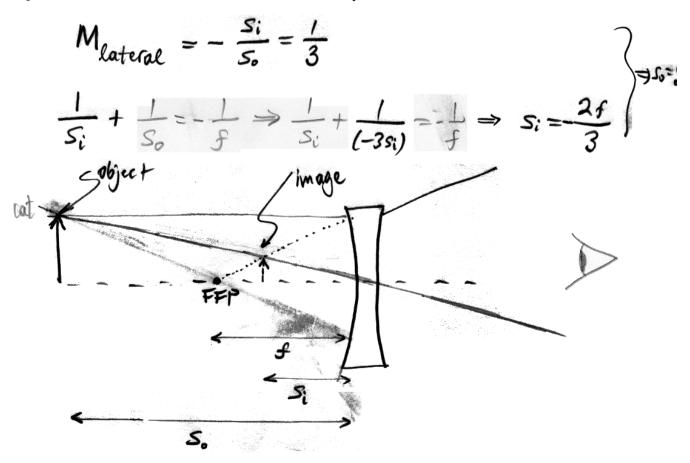
liquid: 
$$\frac{n}{(1.5-n)(\frac{1}{6}-\frac{1}{6})} = 250$$

divide 
$$\frac{n}{15-n} = \frac{250}{50} \Rightarrow n = 1.36$$

2) You'd like to look through a lens at your pet kitten and see it standing right-side up but shrunk to 1/3 its normal cheight. If the absolute value of the focal is f, determine what kind of lens is needed lie. positive or negative) as well as the object & image distances in terms of f.

Soln,

image de-magnified & crect -> need negative lens (see Hecht Table 5.3 p. 165)



- 1. (45%) We intend to use a spherical ball lens of radius R and refractive index n as magnifier in an imaging system, as shown in Figure A. The refractive index satisfies the relationship 1 < n < 4/3, and the medium surrounding the ball lens is air (refractive index = 1).
  - 1.a) Calculate the effective focal length (EFL) of the ball lens. Use the thick lens model with appropriate parameters.
  - 1.b) Locate the back focal length (BFL), the front focal length (FFL) and the principal planes of the ball lens.
  - 1.c) An object located at distance d to the left of the back surface of the ball lens, as shown in Figure A, where

$$d = R\frac{4-3n}{4(n-1)}.$$

Show that the object is one half (EFL) behind the principal plane, and use this fact to find the location of the image plane.

- 1.d) Is the image real or virtual? Is it erect or inverted? What is the magnification?
- 1.e) Locate the aperture stop and calculate the numerical aperture (NA) of the optical system of Figure A.
- 1.f) Sketch how a human observer using the optical system of Figure A as input to her eye would form the final image of the object on her retina.

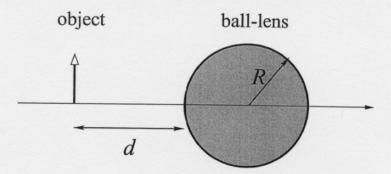
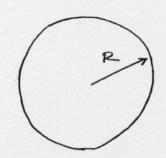


Figure A

## Problem 1.

(1.a)



positive spherical propagation negative spherical surface, by 2R surface

Matrix method:

$$\left( \begin{array}{ccc} 1 & -\frac{1-n}{-R} \\ 0 & 1 \end{array} \right) \left( \begin{array}{ccc} \frac{2R}{n} & 1 \end{array} \right) \left( \begin{array}{ccc} 1 & -\frac{n-1}{R} \\ 0 & 1 \end{array} \right)$$

$$= \left(\begin{array}{ccc} 1 + \frac{1-n}{R} \cdot \frac{2R}{n} & \frac{1-n}{R} \\ \frac{2R}{n} & 1 \end{array}\right) \left(\begin{array}{ccc} 1 & -\frac{n-1}{R} \\ 0 & 1 \end{array}\right)$$

$$= \left(\frac{2n-1}{2k} - \frac{1-n}{R}\right) \left(\frac{1-n-1}{R}\right) = \left(\frac{2n-1}{R} - \frac{2n-1}{R} + \frac{n-1}{R} + \frac{1-n}{R}\right)$$

$$= \left(\frac{2n-1}{R} - \frac{2n-1}{R} + \frac{n-1}{R} + \frac{1-n}{R}\right)$$

$$= \left(\frac{2n-1}{R} - \frac{2n-1}{R} + \frac{n-1}{R} + \frac{1-n}{R}\right)$$

$$= \begin{pmatrix} \frac{2}{n} - 1 & \frac{2(n-1)}{nR} \\ \frac{2R}{n} & \frac{2}{n} - 1 \end{pmatrix}$$

$$\Rightarrow$$
 EFL =  $\frac{nR}{2(n-1)} \equiv f$ 

(mote f>0 always)

(1.6)

$$\begin{vmatrix}
1 & 0 \\
6 & 1
\end{vmatrix} \begin{pmatrix}
\frac{2}{n} - \frac{2(n-1)}{nR} \\
\frac{2R}{n} & \frac{2}{n-1}
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} =$$

$$= \begin{pmatrix}
\frac{2}{n} - 1 & -\frac{2(n-1)}{nR} \\
\frac{2}{n-1}b + \frac{2R}{n} & -\frac{2(n-1)b}{nR} + \binom{2}{n-1}
\end{pmatrix} \begin{pmatrix}
y
\end{pmatrix} = \begin{pmatrix}
-\frac{2(n-1)y}{nR} \\
-\frac{2(n-1)y}{nR}
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
-\frac{2(n-1)y}{nR} \\
-\frac{2(n-1)y}{nR}
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
-\frac{2(n-1)y}{nR} \\
-\frac{2(n-1)}{nR}
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
-\frac{2(n-1)y}{nR} \\
-\frac{2(n-1)}{nR}
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
-\frac{2(n-1)y}{nR} \\
-\frac{2(n-1)}{nR}
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
-\frac{2(n-1)y}{nR} \\
-\frac{2(n-1)}{nR}
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
-\frac{2(n-1)y}{nR} \\
-\frac{2(n-1)}{nR}
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
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y
\end{pmatrix} \begin{pmatrix}
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0 \\
y
\end{pmatrix} \begin{pmatrix}
0 \\
y
\end{pmatrix} = \begin{pmatrix}
0 \\
y
\end{pmatrix} \begin{pmatrix}$$

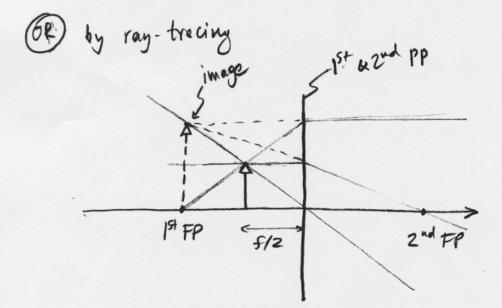
FFL=
$$\frac{R(2-n)}{2(n-1)}$$

EFL= $\frac{nR}{2(n-1)}$ 

EFL= $\frac{nR}{2(n-1)}$ 

$$S = R \frac{4-3n}{4(n-1)} + R = R \frac{4-3n+4n-4}{4(n-1)} = \frac{Rn}{4(n-1)} = \frac{f}{2}$$

$$\frac{1}{5} + \frac{1}{5'} = \frac{1}{f} = \frac{2}{f} + \frac{1}{5'} = \frac{1}{f} \Rightarrow \frac{1}{5'} = -\frac{1}{f} \Rightarrow 3' = -f$$



(1.d) rirtual (need to extend rougs backwards to intersect them)

erect magnified (laterally),  $m_{x} = \frac{s'}{s} = +2$ .