2.710

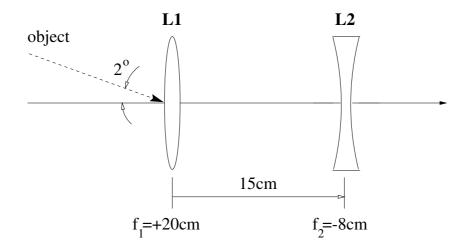
Quiz 1

**2.710 Optics** QUIZ 1

Fall '05

Wednesday, Oct. 12, 2005

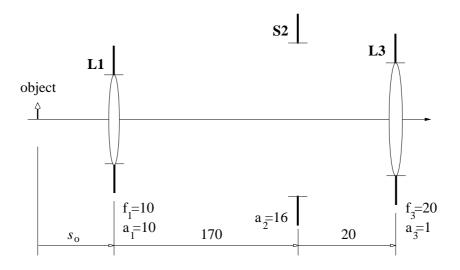
1. (40%) The optical instrument shown below is a "telephoto lens." It consists of a combination of two thin lenses L1, L2 of focal lengths  $f_1$  and  $f_2$ , respectively. The schematic is not drawn to scale.



- **1.a)** Locate the principal planes of this telephoto lens and determine the effective focal length.
- **1.b)** Find the image size of a very distant object subtending angle of 2° with respect to the telephoto axis.
- 1.c) Determine the distance from L2 to the image plane.
- **1.d)** If we were to replace the given telephoto by a single positive lens with equal magnifying power, how far would the positive lens have to be located from the image plane? Based on this result, can you justify the purpose of using a telephoto lens (*i.e.*, a combination of a positive and a negative lens as shown above) instead of a single positive lens?

PLEASE TURN OVER!

2. (60%) The optical instrument shown below, consisting of lenses L1, L3 and stop S2, is intended for direct viewing by human observers, with the observer's eye located to the right of L3. The symbols  $\{f_1, a_1\}$ ,  $\{f_3, a_3\}$  denote the focal lengths and radii of L1, L3, respectively, and  $a_2$  is the radius of S2. All distance units are in millimeters, and the schematic is not drawn to scale.

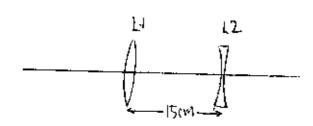


- **2.a)** Determine the object distance  $s_0$  so that a human observer's unaccommodated eye may focus the image on the observer's retina.
- **2.b)** What is the best way to use this instrument? Based on your answer, define the instrument's magnifying power (MP) appropriately, and calculate the MP according to your definition.
- **2.c)** Locate the aperture stop, the entrance and exit pupils, and the field stop. What is the maximum lateral size of an object that can be imaged by this instrument?
- **2.d)** Identify a significant problem that this instrument is subject to, due to the location of the stops. Where must the human observer's eye be placed to mitigate this problem? What is a better way to design this instrument so this problem is eliminated?

GOOD LUCK!

Quiz # 1 Solution

1. Da



The system matrix for the telephote lows.

$$T = \begin{bmatrix} 1 & \frac{1}{8} \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 15 & 1 \end{bmatrix} \begin{bmatrix} 1 & -\frac{1}{20} \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 2.875 & -0.0188 \\ 15 & 0.25 \end{bmatrix}$$

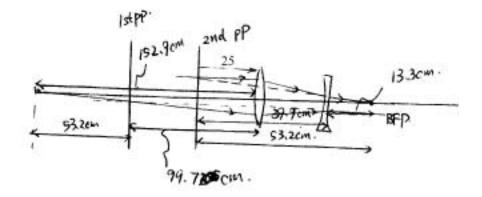
EFL = 1 = 53.2 cm

Propagate a parallel incident ray.

⇒ BFL= 0.25 = 13.3cm.

Propogate a row through FFP.

Sketch the PPs and Form points as shown below



1(b). The internediate image through L1 is at.

and (c)

This forms a virtual object to £2. with

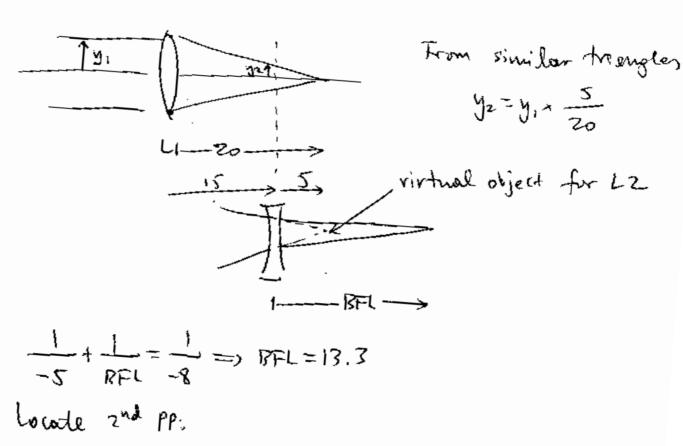
$$50 \quad \frac{1}{5} + \frac{1}{5!} = \frac{1}{f_2}$$

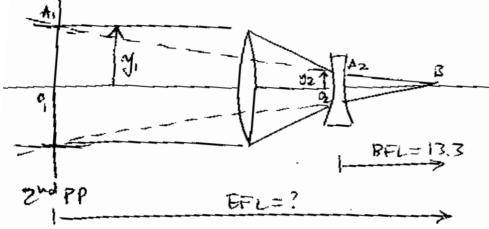
$$\frac{1}{5!} = -\frac{1}{8} + \frac{1}{5}$$

$$= \frac{3}{40}$$

with beight of  $0.7 \cdot \frac{13.3}{5} = 1.86$  cm below the optical axis

Another may to selve the telephoto (without using metrices):

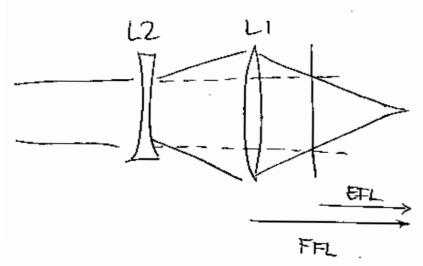




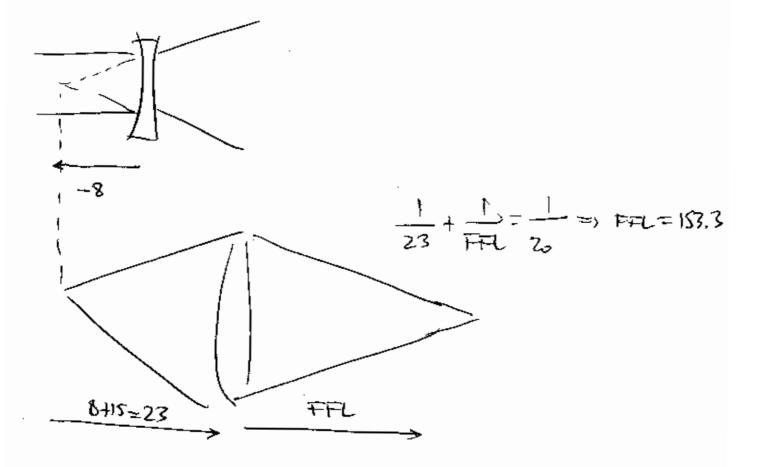
From similar triangles OAB and OZAZB and ne have

$$\frac{y_1}{EFL} = \frac{y_2}{BFL} \Rightarrow EFL = BFL \times \frac{y_1}{y_2} = 13.7 \times 4 = 53.3$$

Locate 1st PP: easiest may is to locate 2nd pp of flipped system, i.e.

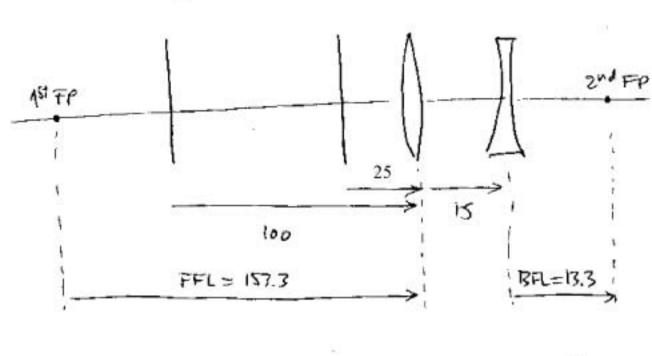


To find the FFL:



EFL is still 53.3 so 1st PP is 100 units to the left of LI

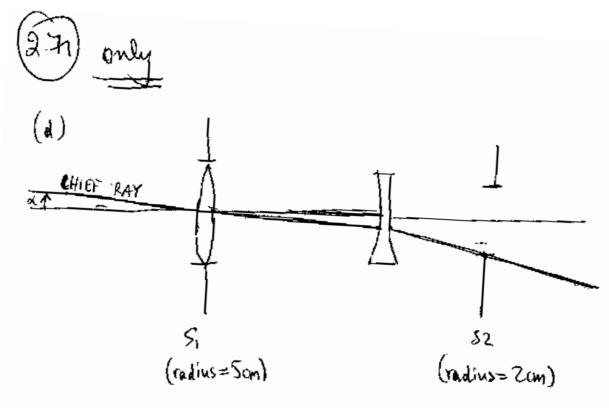
Finally,



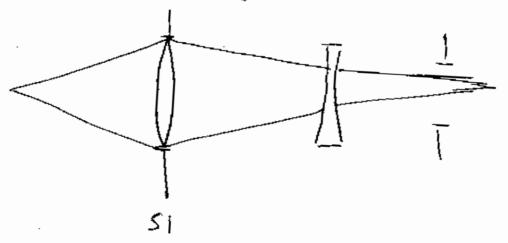
With this in mind me can also easily answer part (b):

So 
$$y_1 = \left(2^{\circ} \times \frac{77}{180}\right) \times 53.3 = 1.86 \text{ cm}.$$

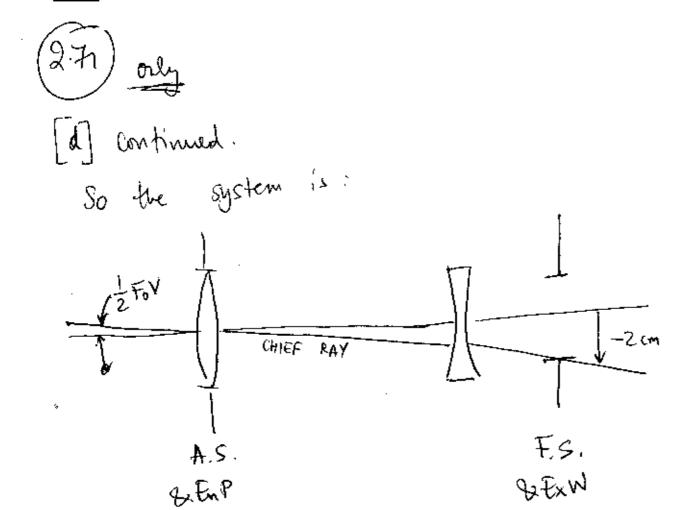
ed in radious



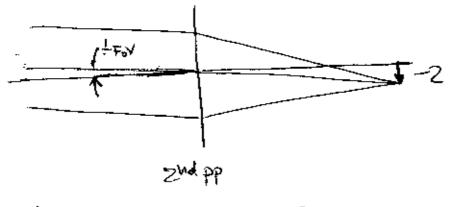
S2 is the Field Stop, because it limits the size of the image (and the angular acceptance of objects located at infinity)



SI limits the acceptance angle for on-axis remote objects (including objects at 20) so SI is the Aperture Stop



(e). To find the FoV, we can use the same method as in question (c), except now ne are given the Chief Rouje focal point at -2cm:

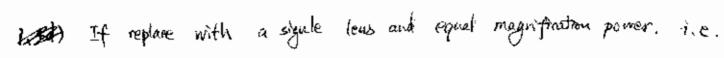


only slightly larger (c)!

( than the object (c)!

( pren in part (c)!  $\left|\frac{1}{2}(F_0V)\right| = \frac{2}{E+L} = \frac{2}{53.3} = 0.0375 \text{ vol} = 2.15^{\circ}$ 

> see (270)(d) next page





(2.70) image at the same heigh

The  $f' = \frac{1.86 \text{ cm}}{\frac{2}{180}} = 53.2 \text{ cm}$ .  $\Leftarrow$  same as EFL.

The low most be placed 53.20m before the image.

So obviously, using the telephoto structure reduced the length of a lens w/ long tou foral distance.

2. 2.a) To let the human's unaccommodated eye to foous the image on retina. L3 should form a virtual image at infinity.

So L1 forms the intermediate image at 32 plane.

As. 
$$\frac{1}{s_0} + \frac{1}{170} = \frac{1}{10}$$

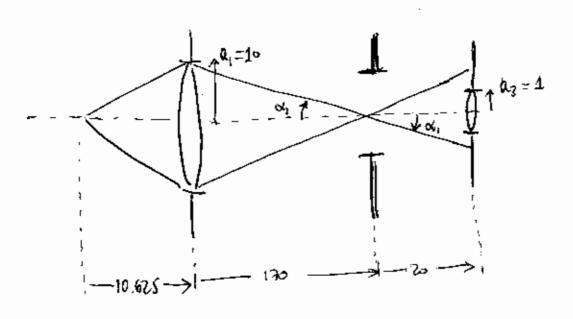
S.= 10.625 mm.

2.6) Plane a small object at So, the intrument arts as a to microscope. The MP is the ratio that unage formed with intrument an human's votina to the image size formed on the ration with rational with naked eye.

 $MP = M_L \cdot M_d = \frac{170}{10.625} \cdot \frac{254}{20} = 203 \times$ 

2.c) According to part (a), S2 is at an intermediate image plane, so it is not the aperture stop. [We will prove later that 52 is the field stop]. Potential aperture stops are then the rims of either L1 or 13. The A.S. Should be the smallest of the two.

Consider the following schemetic:



 $0 = \frac{10}{170}$  is the angle admitted by the rim of L1 but L3 only admits an angle  $\frac{1}{20} < \frac{10}{170}$ So 132 as the rim of L3 is the A.S. If we image the rim of 13 through 11, we can find the docation and sine or the image as fellows:

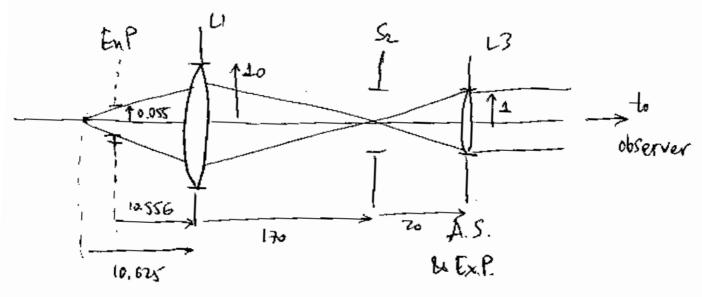
(first flip the system so 13 is to the deft of 11)

$$\frac{1}{120+20} = 180$$

Nim Of L3

$$\frac{1}{180} + \frac{1}{S_0} = \frac{1}{10} = 1 S_0 = 10.556 \text{ mm}. \quad a_0 = a_3 \times \left(-\frac{10.556}{180}\right) = 0.055$$

In the actual system,



The rim of 13 is A.S. and also Ex.P. rince there is no optics to its right.

To find the field stop, we need to image S2 through L1. We find that the image S2' is located exactly at the object plane, at the size of S2' is

$$16 \times \frac{10.625}{170} = 1$$
mm.

Now consider a chief ray that goes through the edge of S2' and the center of the EnP. This ray subtends an angle of  $\arctan[1mm/(10.625-10.556)mm]=86$  degrees!! On the other hand, let us consider a chief ray that goes through the edge of L1 and the center of the EnP. Instead, this ray subtends an angle of  $\arctan(10/10.556)=46.5$  degrees, which is smaller than the previous one. We see that the stop limiting the field of view is not S2 (or S2') but L1. Therefore, L1 is the Field Stop. The maximum lateral size of an object that can be viewed is  $2 \times (10.625-10.556)mm \times \tan(45.6^0)=0.13mm$ .

(d) In traditional microscopes, the aperture stop (A.S.) is located at the objective's rim; therefore, the subsequent optics create an image of the A.S. (that is, the Exit Pupil) that is located to the right of the eyepiece. The observer's eye can be comfortably located such that the eye's pupil coincides with the Exit Pupil and the image can be observed without vignetting. In this case, the eyepiece is the A.S. and it is collocated with the Exit Pupil. To avoid vignetting, the eye pupil would have to be adjacent to the eyepiece, which is of course infeasible because (a) the eye pupil is located behind the cornea, and (b) even if the small distance between the cornea and pupil could be neglected, it would be really uncomfortable for the viewer to place his or her eye in contact with the eyepiece. One remedy to this problem is to stop down the objective, i.e. reduce its radius so that it becomes the A.S. instead of the eyepiece; that is not a good solution because, as we will see when we do wave optics, this solution reduces the overall numerical aperture of the system and, hence the resolution of the microscope. A better remedy is to replace the eyepiece with one that has larger radius (assuming we can afford one.) Then again the objective becomes the A.S. as desired.

The schematic below justifies why L1 is the F.S. and also why this system is subject to vignetting.

