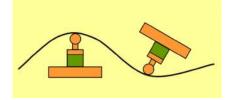


Sheet Metal Forming 2.810 D. Cooper

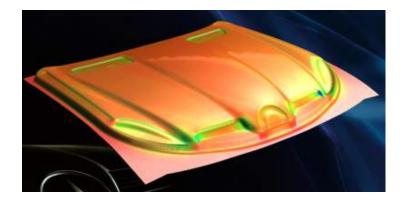
"Sheet Metal Forming" Ch. 16 Kalpakjian
"Design for Sheetmetal Working",
Ch. 9 Boothroyd, Dewhurst and Knight





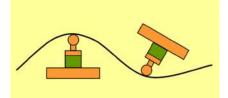
Examples-sheet metal formed



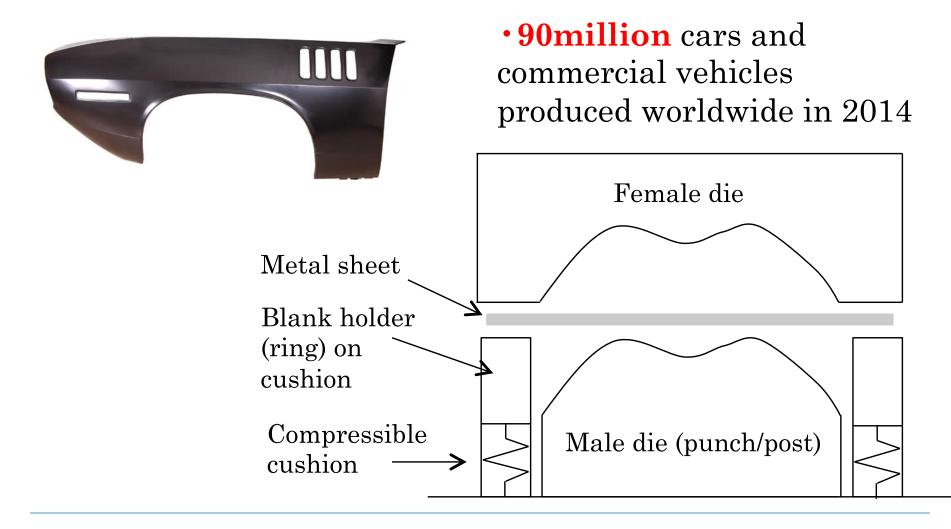




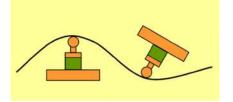




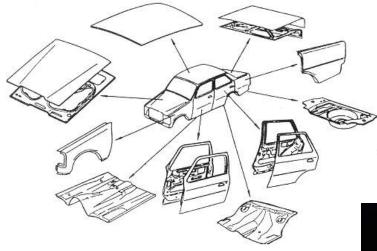
Sheet metal stamping/drawing – car industry





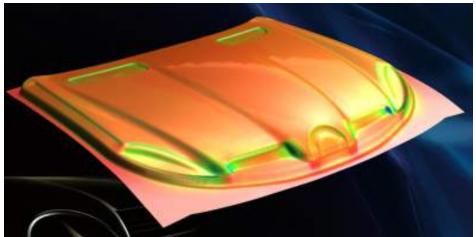


Stamping Auto body panels

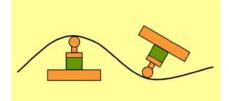


- \cdot 3 to 5 dies each
- Prototype dies ~ \$50,000
- Production dies ~ 0.75-1

- Forming dies
- Trimming station
- Flanging station







Objectives

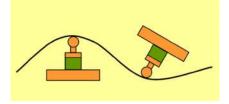
By the end of today you should be able to...

...**describe** different forming processes, when they might be used, and **compare** their production rates, costs and environmental impacts

...**calculate** forming forces, **predict** part defects (tearing, wrinkling, dimensional inaccuracy), and **propose** solutions

...**explain** current developments: opportunities and challenges

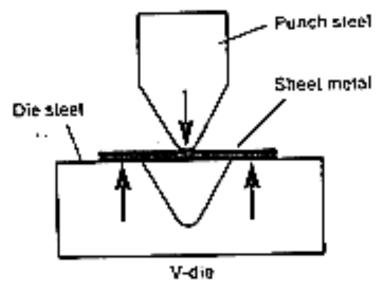




LMP Shop

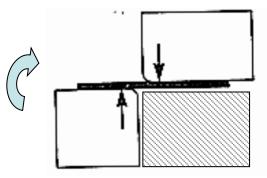
Brake press





Finger brake





Technology – a brief review

Forming Speed

<u>Material drawn into shape</u>

•Conventional drawing/stamping – expensive tooling, no net thinning, quick **20-1000pts/hr**

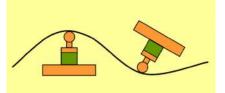
•Hydro-forming – cheap tooling, no net thinning, slow, high formability **7-13cycles/hr**

<u>Material stretched into shape</u>

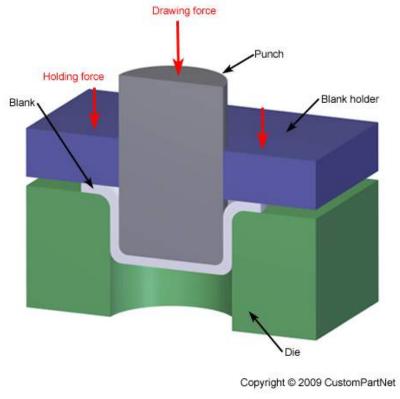
•Stretch forming – very cheap tooling, net thinning, slow, low formability **3-8pts/hr**

•Super-plastic forming – cheap tooling, net thinning, expensive sheet metal, slow, very high formability **0.3-4pts/hr**

Massachusetts Institute of Technology



Drawing – expensive tooling, no net thinning, quick



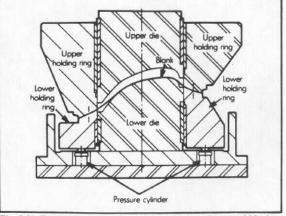
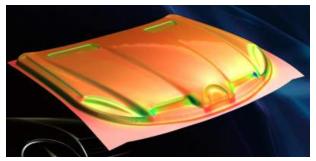


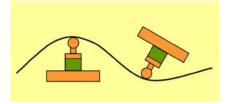
Fig. 7-23 Tooling for stretch-draw forming fenders from steel blanks. (Oldsmobile Div., General Motors Corp.)



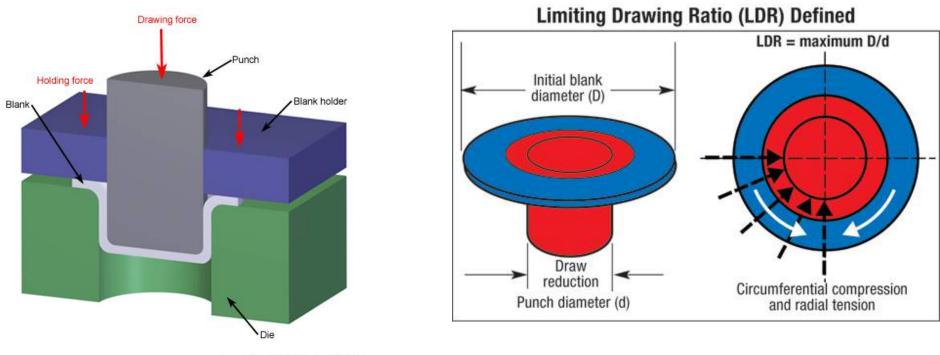
Deep-drawing

Shallow-drawing (stamping)





Deep-drawing

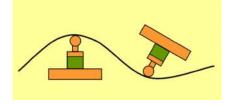


Copyright © 2009 CustomPartNet

Blank holder helps prevent wrinkling and reduces springback

Blank holder not necessary if blank diameter / blank thickness is less than 25-40. Smaller values for deeper forming.

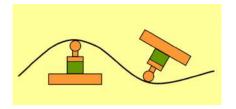




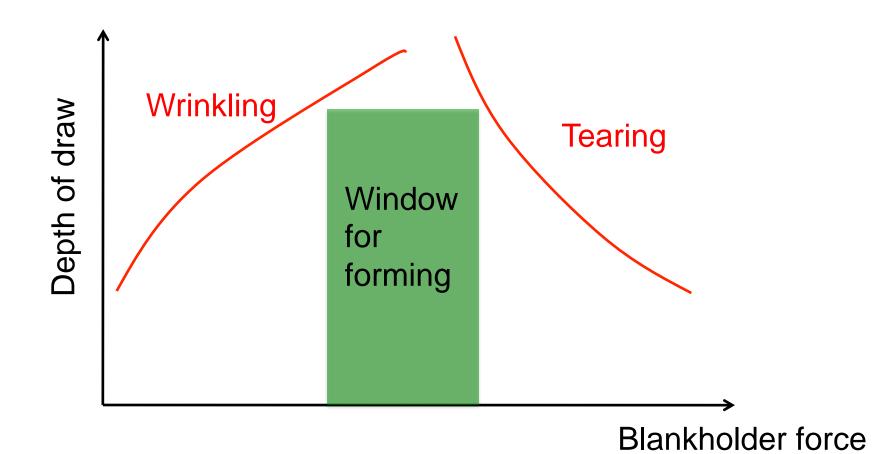


http://www.thomasnet.com/articles/custom-manufacturing-fabricating/wrinkling-during-deep-drawing





Blank holder force: forming window





Deep Drawing of drinks cans



Hosford and Duncan (can making): http:// www.chymist.com/ Aluminum %20can.pdf

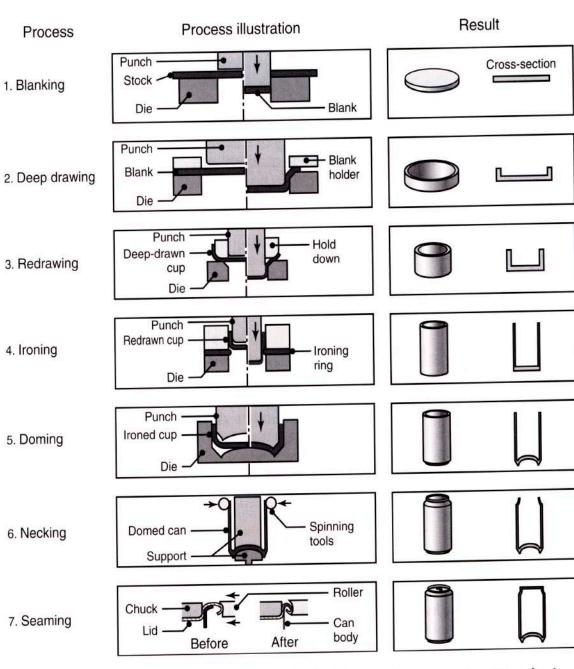
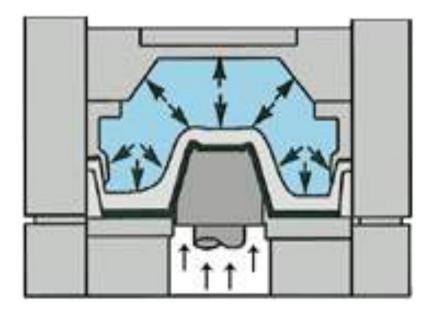


FIGURE 16.31 beverage can.

5.31 The metal-forming processes involved in manufacturing a two-piece aluminum.

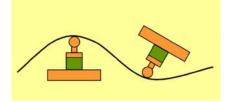
Hydro-forming – cheap tooling, no net thinning, slow(ish), high formability





Low volume batches

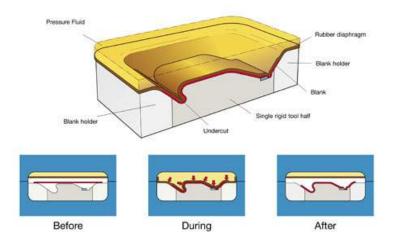




Hydro-forming – cheap tooling, no net thinning, slow(ish), high formability

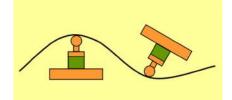


Flexform – Principle



Low volume batches



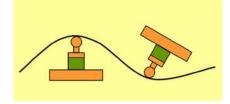


Hydro-forming – cheap tooling, no net thinning, slow, high formability

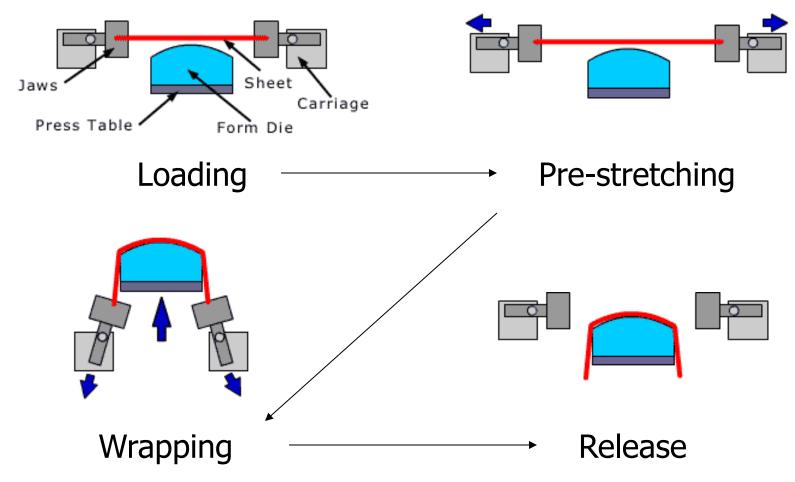


Small flexforming tool made by additive manufacturing





Stretch forming – very cheap tooling, net thinning, slow, low formability, sheet metal up to 15mx9m



* source: http://www.cyrilbath.com/sheet_process.html

Low volume batches

Stretch forming: Example parts

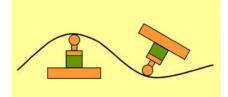




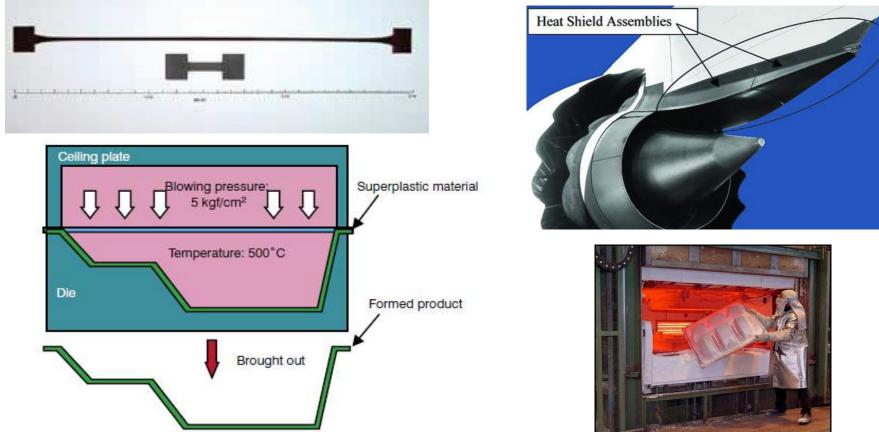


Higher aspect ratio, deeper parts



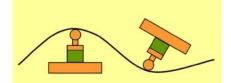


Super-plastic forming – cheap tooling, net thinning, slow, expensive sheet metal, very high formability



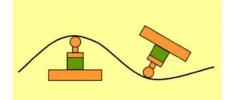
Low volume batches, 0.5-0.75 melting temp



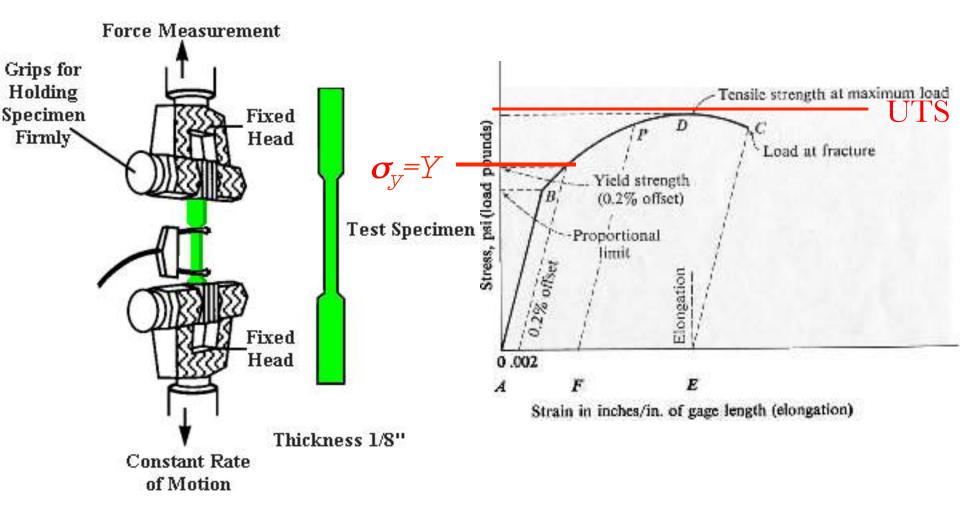


Forming forces and part geometry

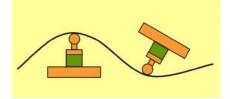


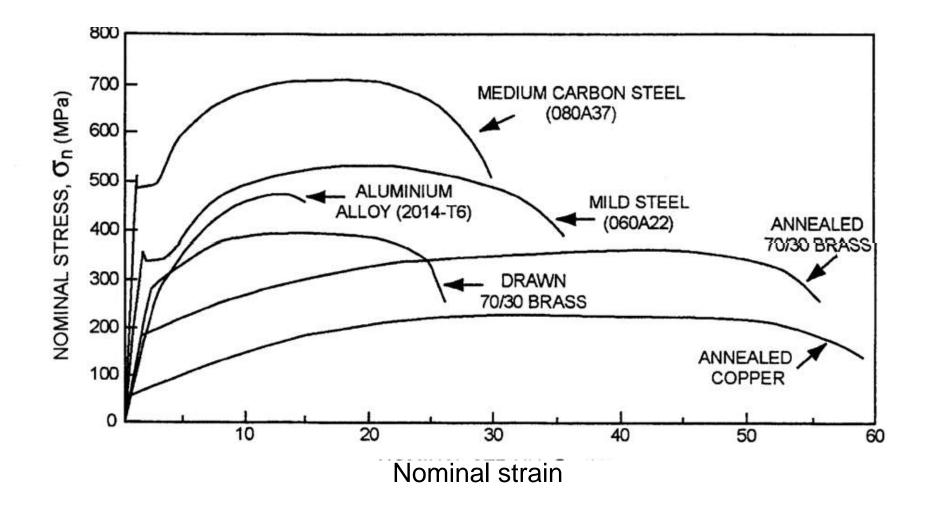


Tensile test – the Stress-strain diagram

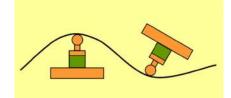




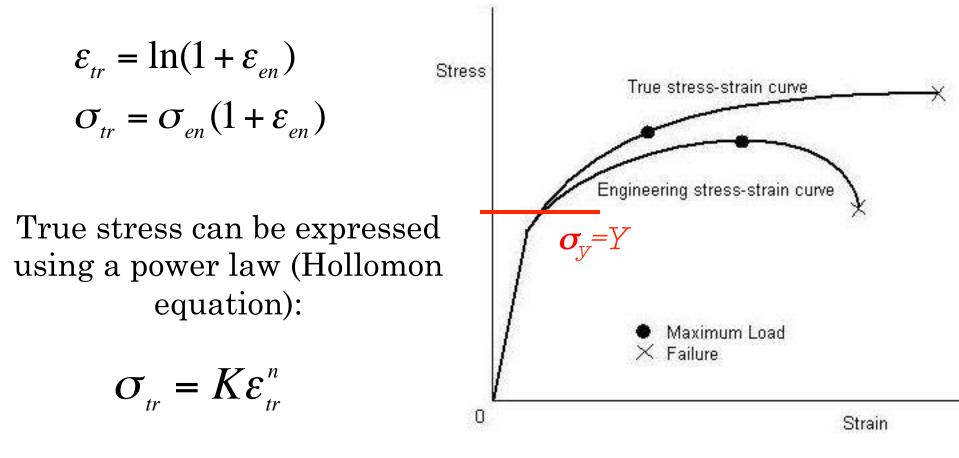




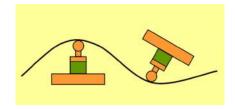


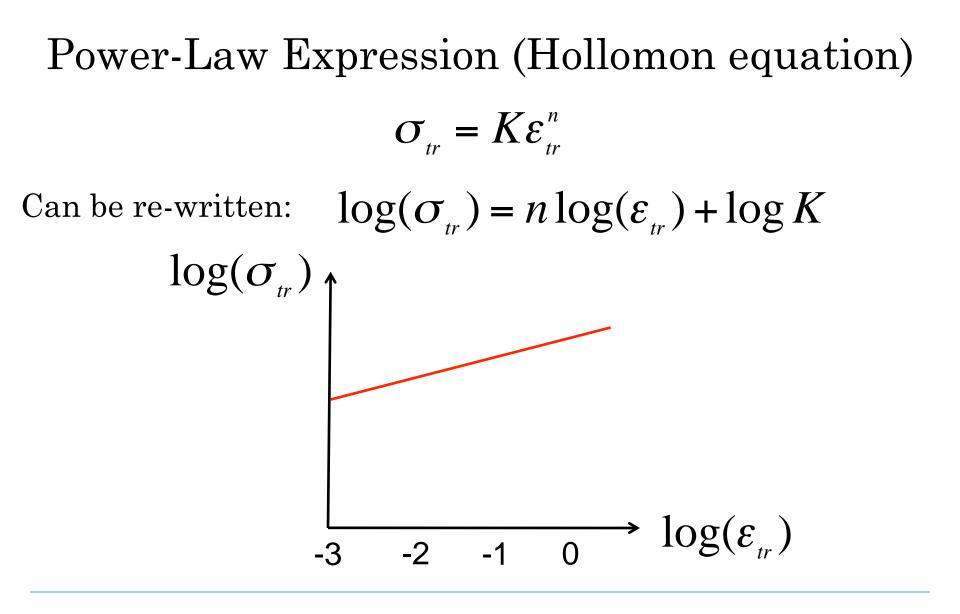


True stress & strain

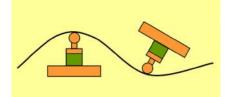












Power-Law Expression (Hollomon equation) $\sigma_{tr} = K \varepsilon_{tr}^{n}$ $\log(\sigma_{tr}) = n \log(\varepsilon_{tr}) + \log K$ Can be re-written: $\log(\sigma_{tr})$ $\rightarrow \log(\mathcal{E}_{tr})$ -2 \mathbf{O} -3 -1



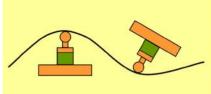
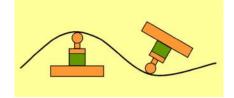


TABLE 2.3

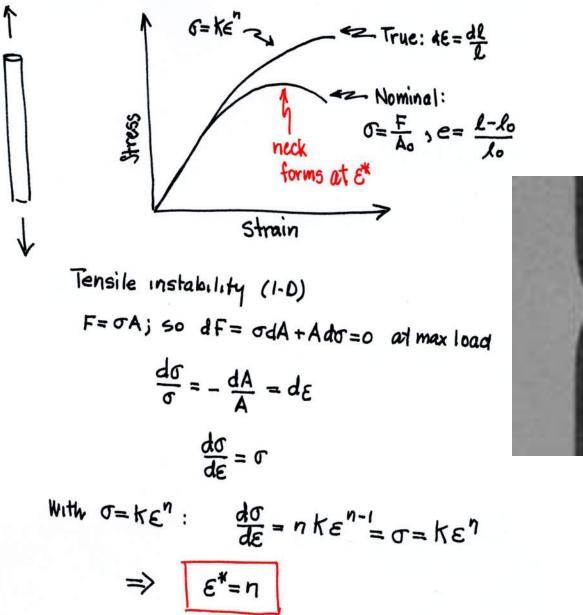
Typical	Values	for k	(and	n for	Selected	
Metals						

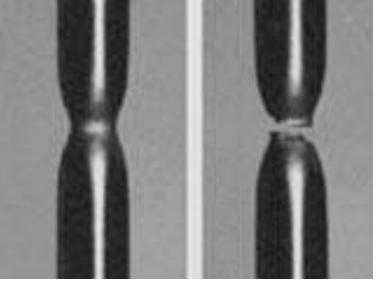
Material	K (MPa)	n
Aluminum		
1100-O	180	0.20
2024-T4	690	0.16
5052-O	202	0.13
6061-O	205	0.20
6061-T6	410	0.05
7075-O	400	0.17
Brass		
70-30, annealed	900	0.49
85-15, cold rolled	580	0.34
Cobalt-based alloy, heat treated	2070	0.50
Copper, annealed	315	0.54
Steel		
Low-C, annealed	530	0.26
1020, annealed	745	0.20
4135, annealed	1015	0.17
4135, cold rolled	1100	0.14
4340, annealed	640	0.15
304 stainless, annealed	1275	0.45
410 stainless, annealed	960	0.10
Titanium		
Ti-6Al-4V, annealed, 20°C	1400	0.015
Ti-6Al-4V, annealed, 200°C	1040	0.026
Ti-6Al-4V, annealed, 600°C	650	0.064
Ti-6Al-4V, annealed, 800°C	350	0.146

Massachusetts Institute of Technology

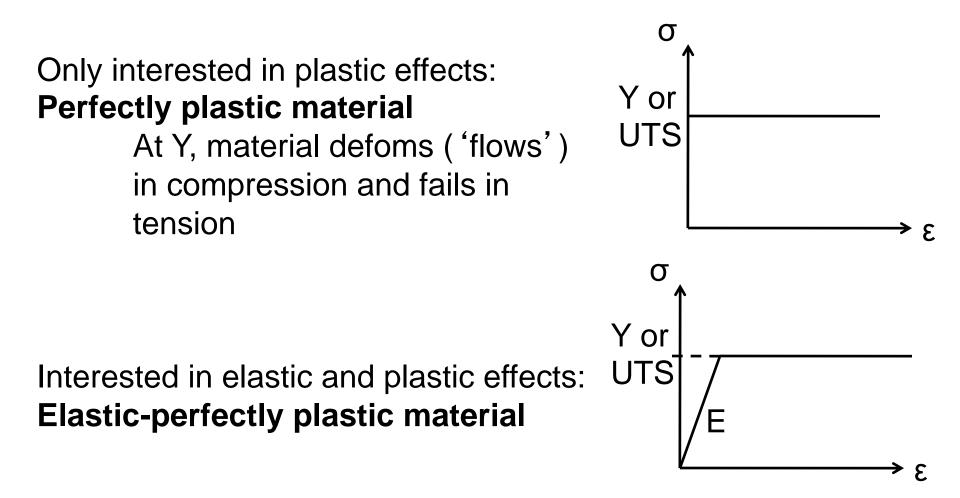


Tensile instability - necking

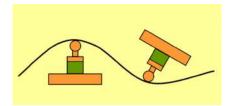


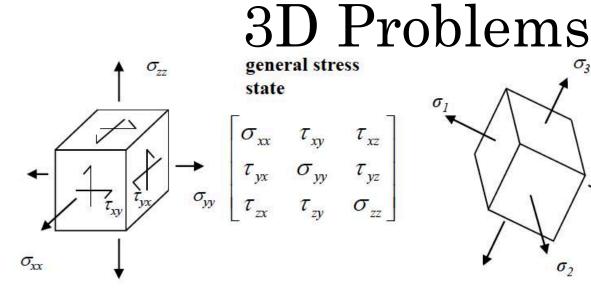


Useful assumptions



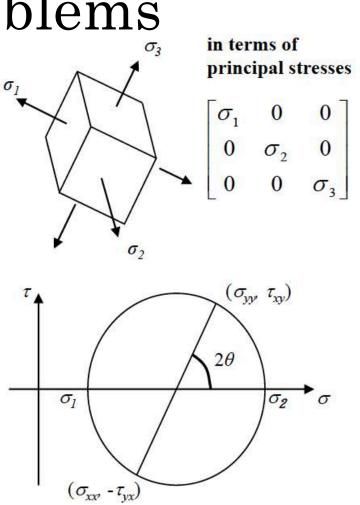






For any general stress state we can find a set of *principal axes*. The stress tensor for these axes contains no off-diagonal (shear) terms – only three principal stresses along the three axes.

Mohr's circle allows rotation of axes in two dimensions about one principal axis



In 1-D, $\sigma = K\varepsilon^{n}$ assuming perfectly plastic, yielding at: $\sigma = Y$ In 3-D, $\sigma_{eff} = K\varepsilon^{n}_{eff}$ assuming perfectly plastic, yielding at: $\sigma_{eff} = Y$

3D Yield Criteria

Tresca: Yielding occurs at a maximum shear stress

Von Mises: Yielding at maximum distortion strain energy

Effective stress (in principal directions):

Massachusetts

Institute of

Technology

$$\sigma_{eff} = \left[\sigma_i - \sigma_j\right]_{\substack{\text{max,}\\ i \neq j}}$$

Yield criterion:

$$\sigma_{eff} = Y$$
$$\tau_{max} = k = \frac{Y}{2}$$

Effective strain:

$$\mathcal{E}_{eff} = \left(\mathcal{E}_i\right)_{\max}$$

Effective stress (in principal directions):

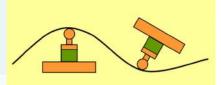
$$\sigma_{eff} = \sqrt{\frac{1}{2} \times \begin{bmatrix} \theta \sigma_2 - \sigma_3 \end{pmatrix}^2 + (\sigma_3 - \sigma_1)^2 \\ \theta (\sigma_1 - \sigma_2)^2 \end{bmatrix}}$$

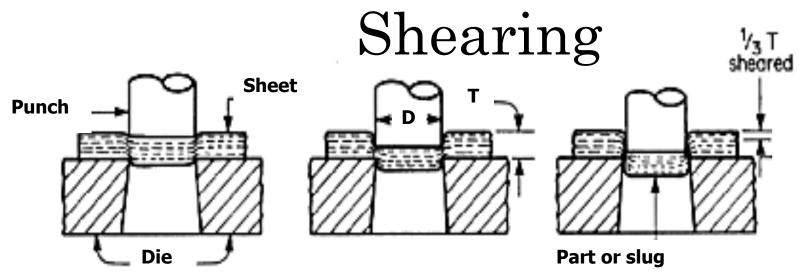
Yield criterion:

$$\sigma_{eff} = Y$$
$$Y = \sqrt{3}k$$

Effective strain:

$$\varepsilon_{eff} = \sqrt{\begin{pmatrix} \hat{\boldsymbol{\rho}} \\ \boldsymbol{\rho} \\ \boldsymbol{\rho} \end{pmatrix}} \begin{pmatrix} \rho \\ \boldsymbol{\rho} \\ \boldsymbol{\rho} \\ \boldsymbol{\rho} \end{pmatrix} \begin{pmatrix} \varepsilon_1^2 + \varepsilon_2^2 + \varepsilon_3^2 \end{pmatrix}$$





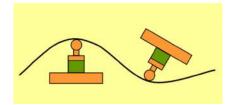
F = 0.7 T L (UTS)

T = Sheet Thickness L = Total length Sheared UTS = Ultimate Tensile Strength of material



Shear press - LMP Shop





Side Note: For a general state of stress use "effective stress"

2-6 EFFECTIVE STRESS

With either yield criterion, it is useful to define an effective stress denoted as $\bar{\sigma}$ which is a function of the applied stresses. If the *magnitude* of $\bar{\sigma}$ reaches a critical value, then the applied stress state will cause yielding; in essence, it has reached an effective level. For the von Mises criterion,

$$\bar{\sigma} = \frac{1}{\sqrt{2}} [(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2]^{1/2}$$
(2-16)

while for the Tresca criterion,

$$\bar{\sigma} = \sigma_1 - \sigma_3$$
 where $\sigma_1 > \sigma_2 > \sigma_3$ (2-17)

Yielding occurs when
$$\sigma_{\text{effective}} = Y$$

Material taken from *Metal Forming*, by Hosford and Caddell

Origin of effective strain

2-7 EFFECTIVE STRAIN

Effective strain is *defined* such that the incremental work per unit volume is

$$dw = \bar{\sigma} d\bar{\epsilon} = \sigma_1 d\epsilon_1 + \sigma_2 d\epsilon_2 + \sigma_3 d\epsilon_3 \qquad (2-18)$$

For the von Mises criterion, the effective strain is given by

$$d\bar{\epsilon} = \frac{\sqrt{2}}{3} [(d\epsilon_1 - d\epsilon_2)^2 + (d\epsilon_2 - d\epsilon_3)^2 + (d\epsilon_3 - d\epsilon_1)^2]^{1/2} \quad (2-19)$$

which may be expressed in a simpler form as

$$d\bar{\epsilon} = \left[\frac{2}{3}(d\epsilon_1^2 + d\epsilon_2^2 + d\epsilon_3^2)\right]^{1/2}$$
(2-20)

If the straining is proportional (with a constant ratio of $d\epsilon_1$: $d\epsilon_2$: $d\epsilon_3$), the total effective strain may be expressed in terms of the total strains as

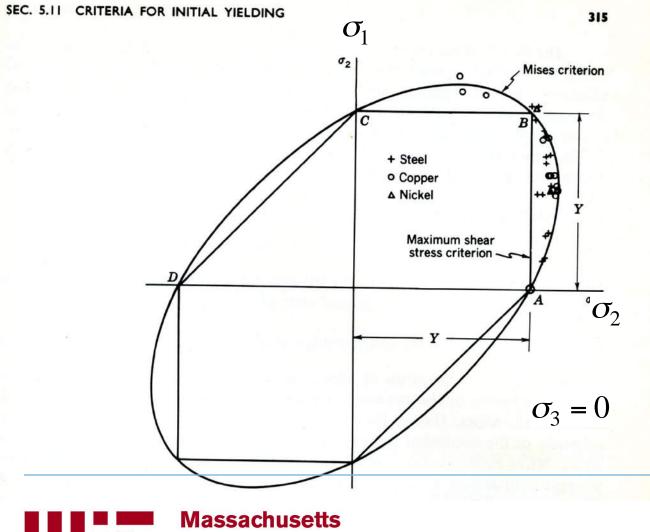
$$\bar{\epsilon} = \left[\frac{2}{3}(\epsilon_1^2 + \epsilon_2^2 + \epsilon_3^2)\right]^{1/2} \tag{2-21}$$

If the strain path is not constant, $\bar{\epsilon}$ must be found from a path integral of $d\bar{\epsilon}$. In

$$\overline{\sigma} = K\overline{\varepsilon}^n$$

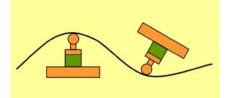
Material taken from *Metal Forming*, by Hosford and Caddell

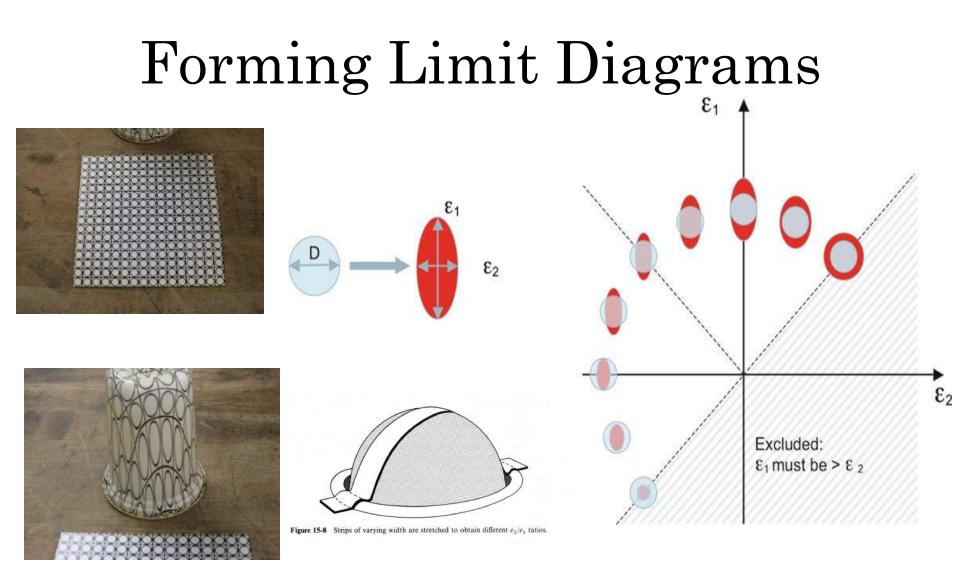
3D Yield Effective stress



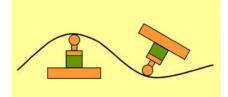
Tresca predicts 'flow' for lower stresses than von Mises

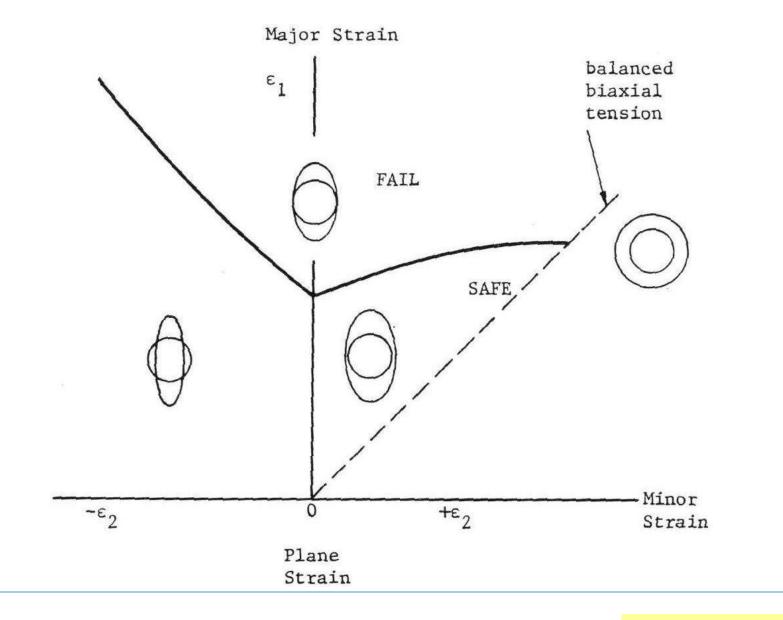
Massachusetts Institute of Technology



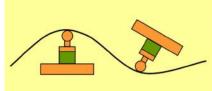


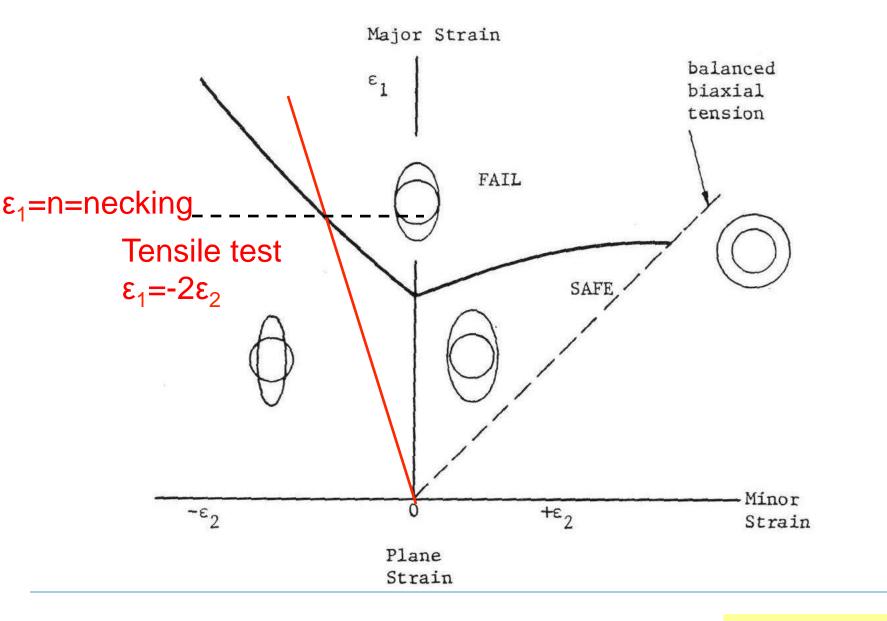




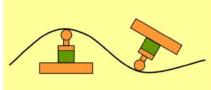


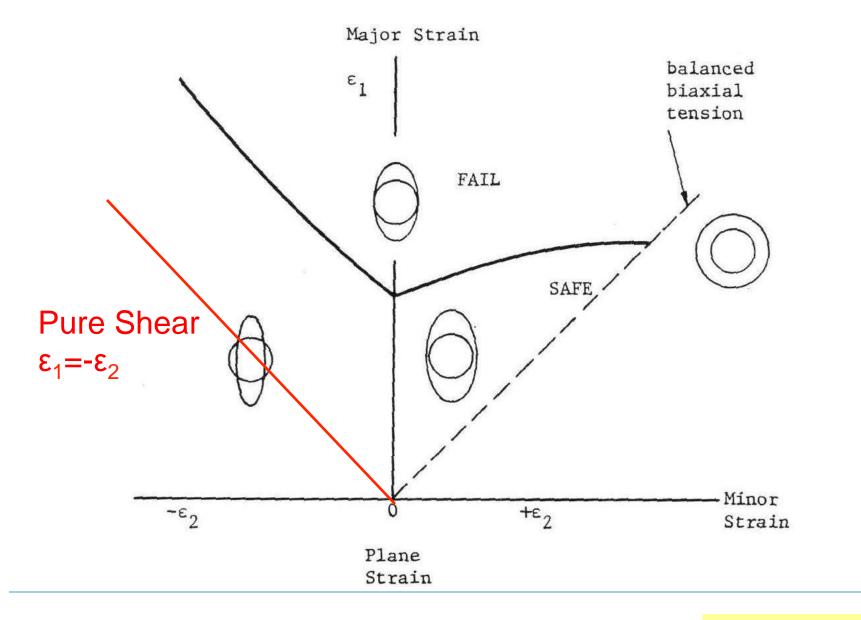




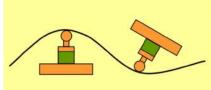












Stretch forming: Forming force



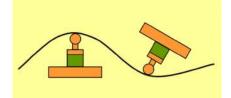




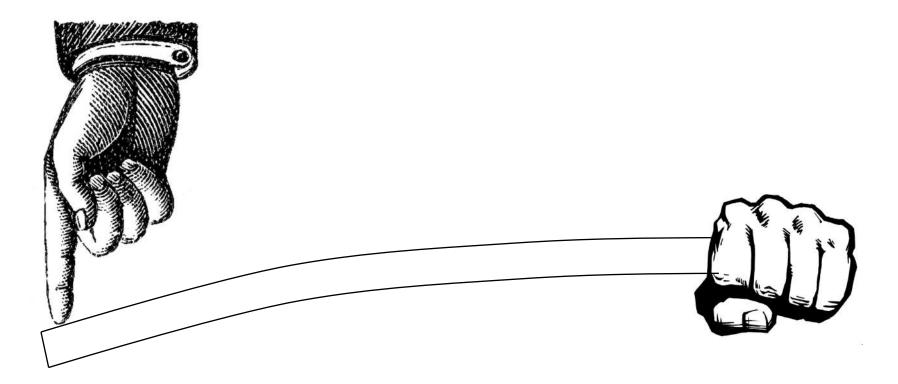
$F = (Y_{S} + UTS)/2 * A$

F = stretch forming force (lbs) Y_s = material yield strength (psi) UTS = ultimate tensile strength of the material (psi) A = Cross-sectional area of the workpiece (in2)

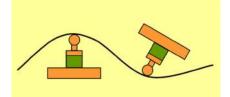


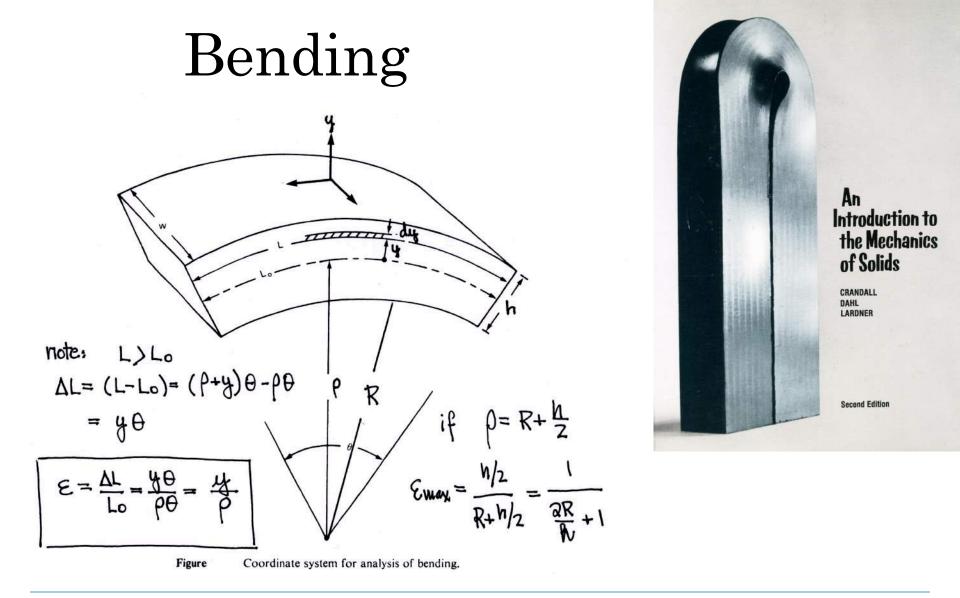


Forces needed to bend sheet metal

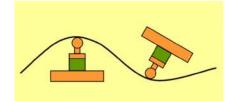




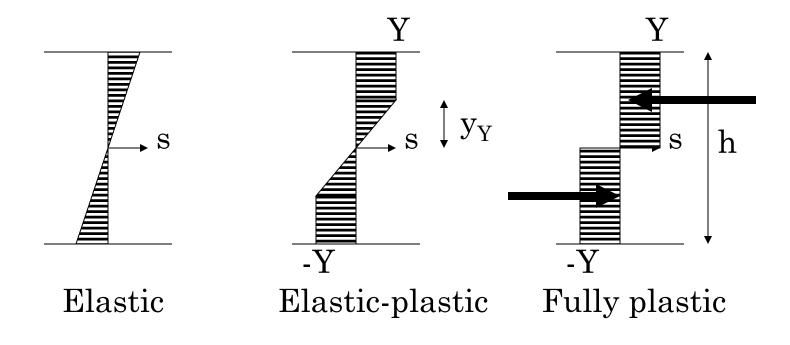






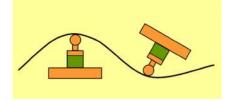


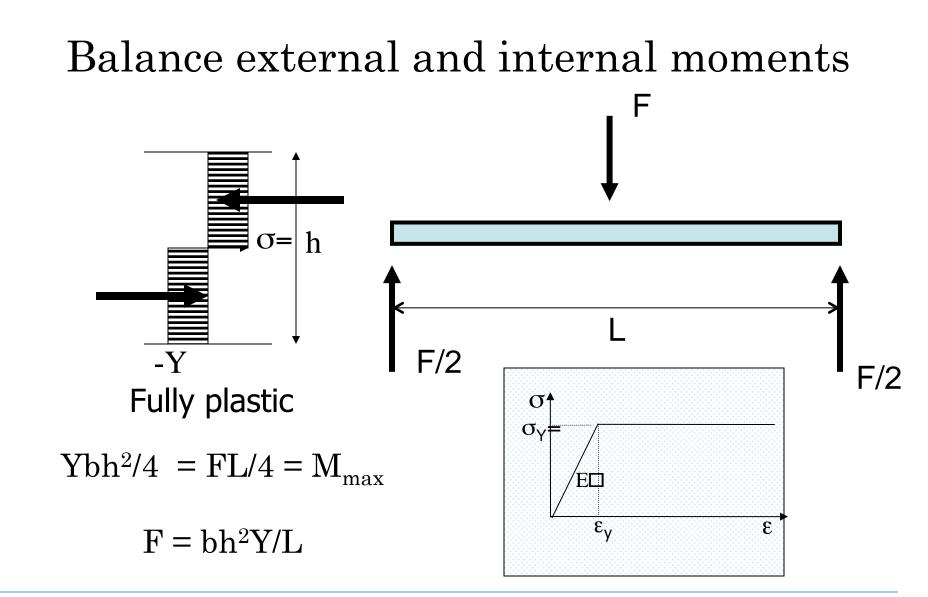
Stress distribution through the thickness of the part



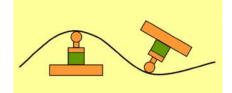
Fully Plastic Moment, M = Y (b h/2) h/2 = Ybh²/4

Massachusetts Institute of Technology

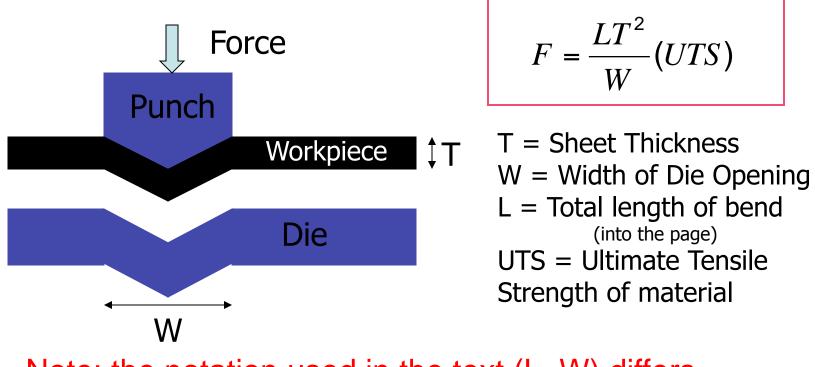






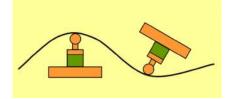


Bending Force Requirement



Note: the notation used in the text (L, W) differs from that used in the previous development (b, L).

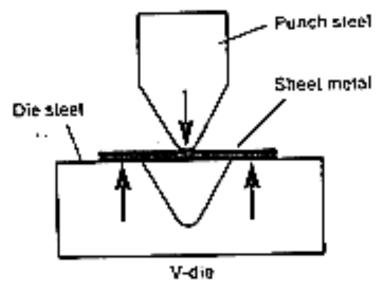




LMP Shop

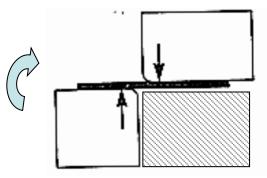
Brake press



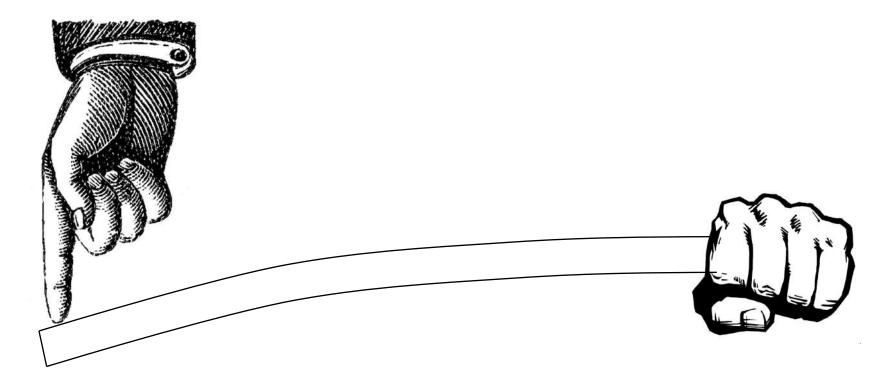


Finger brake

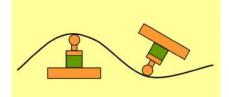


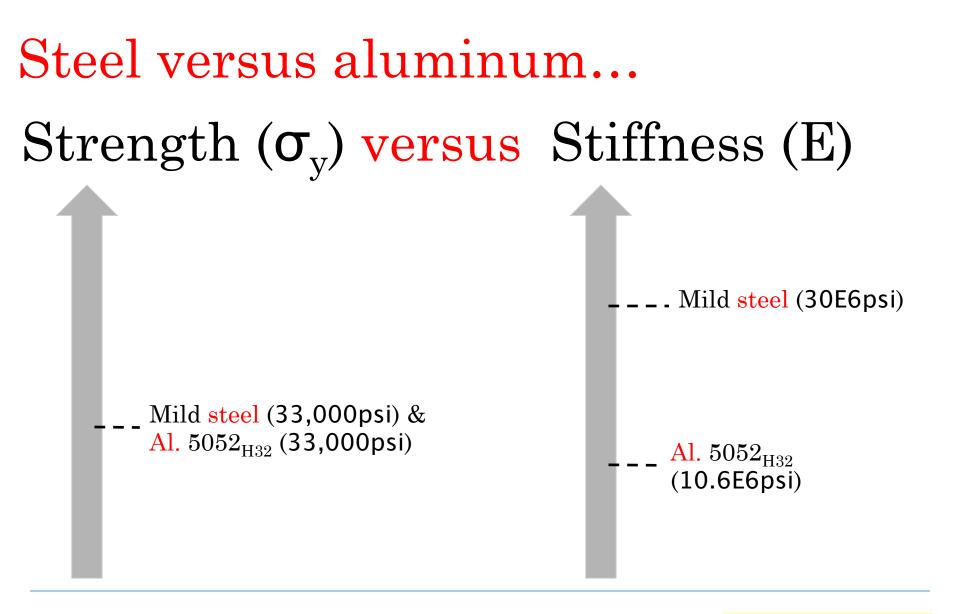


What shape have we created?

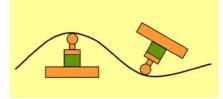


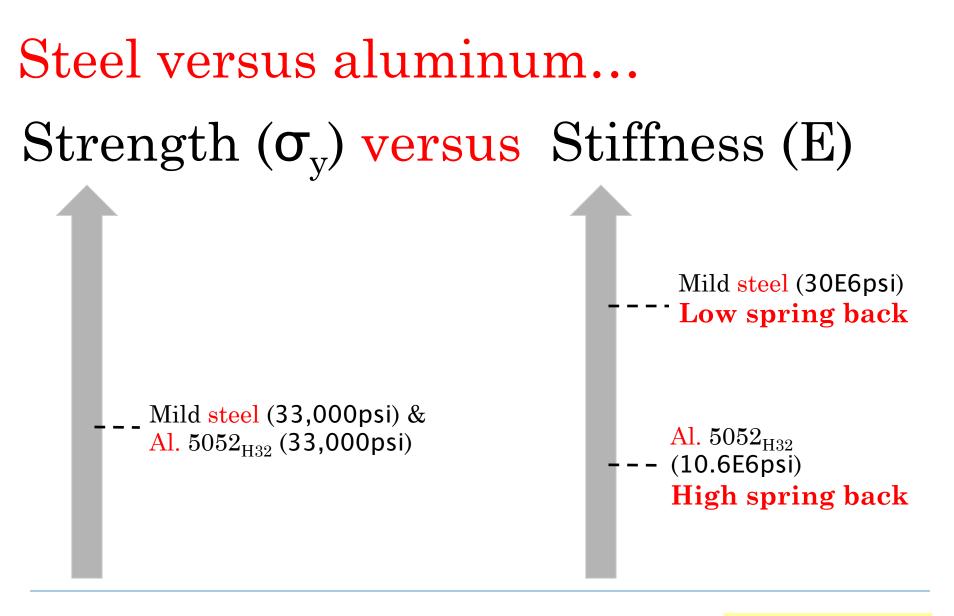




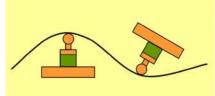


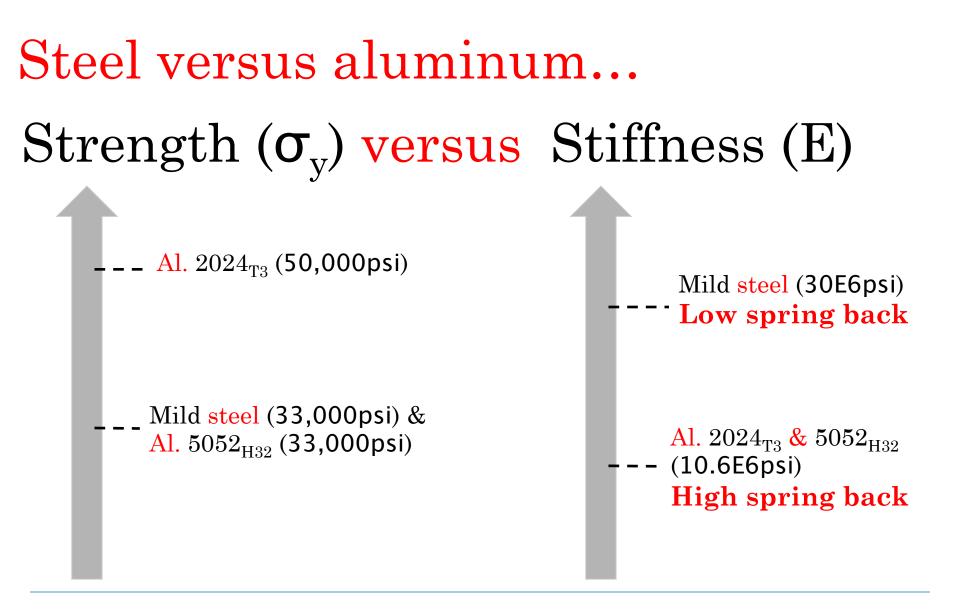




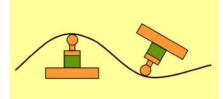


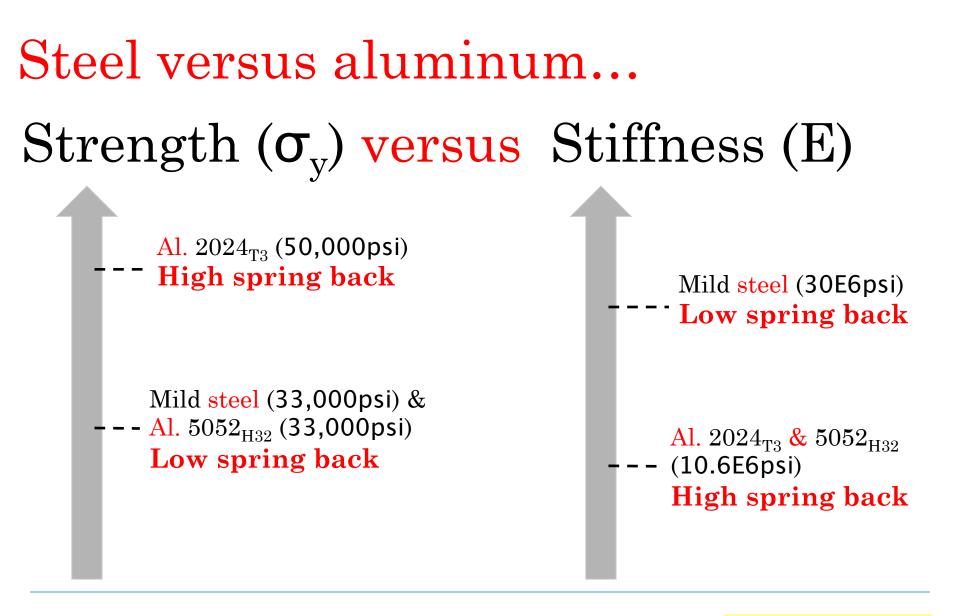




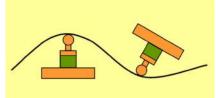


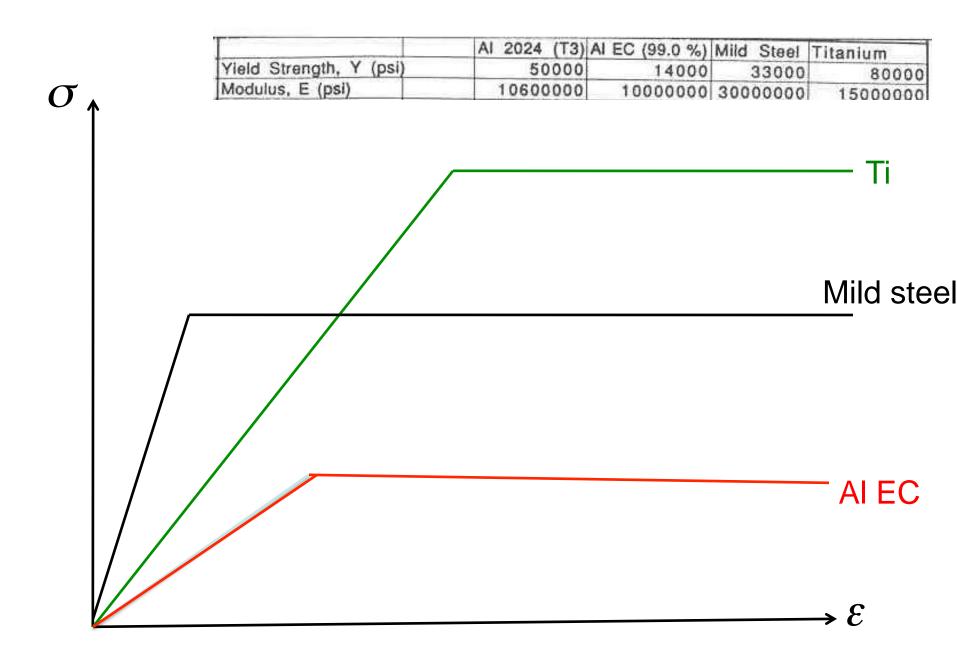


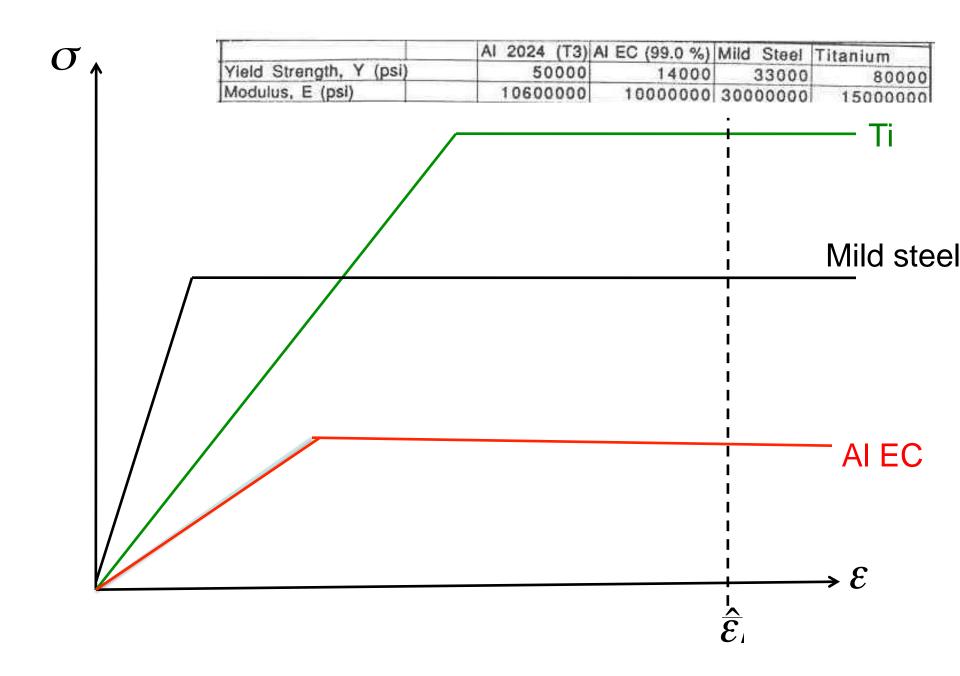


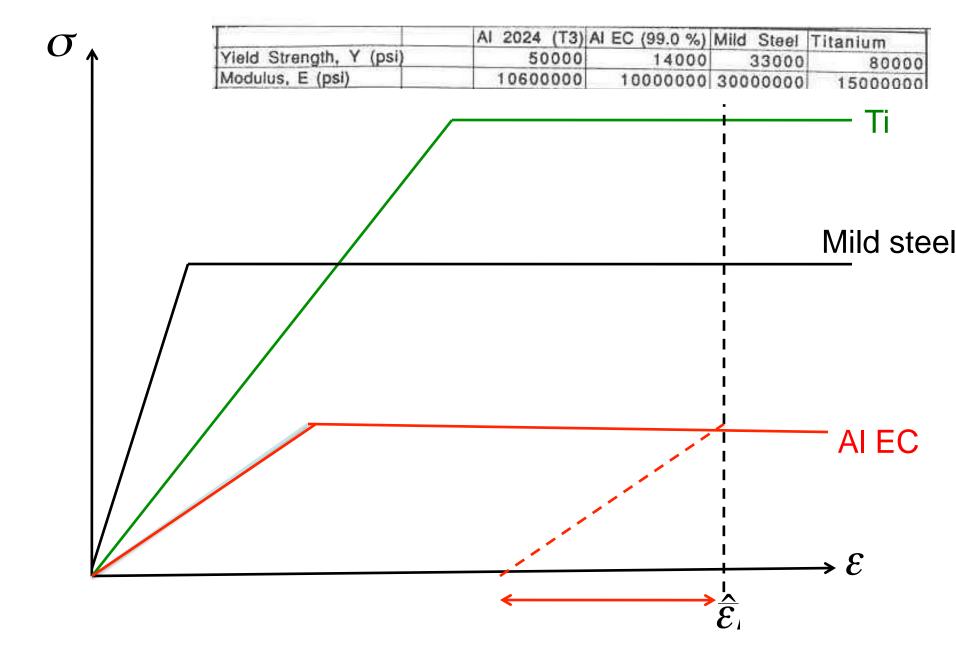


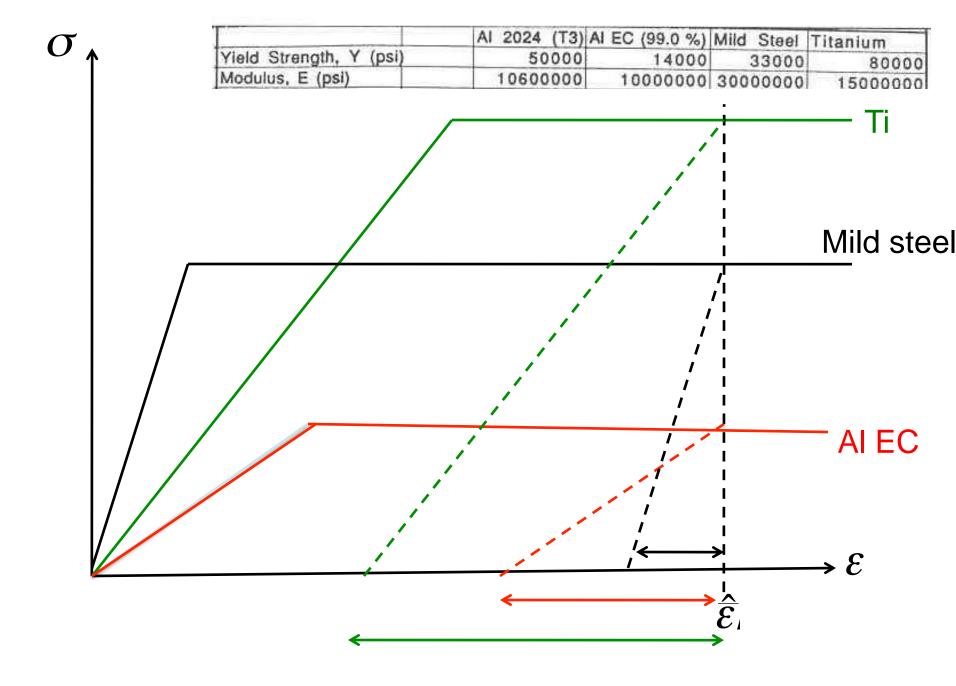




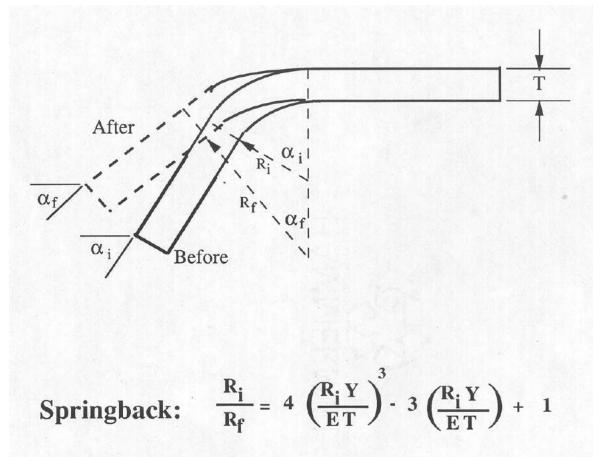




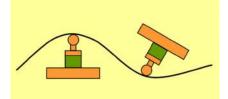




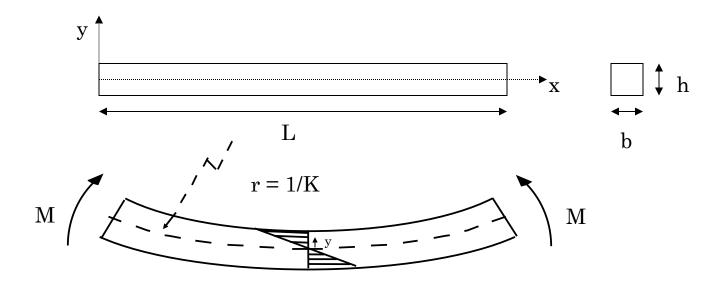
Springback note R in the figure below is mislabeled, should go to the centerline of the sheet



Massachusetts Institute of Technology



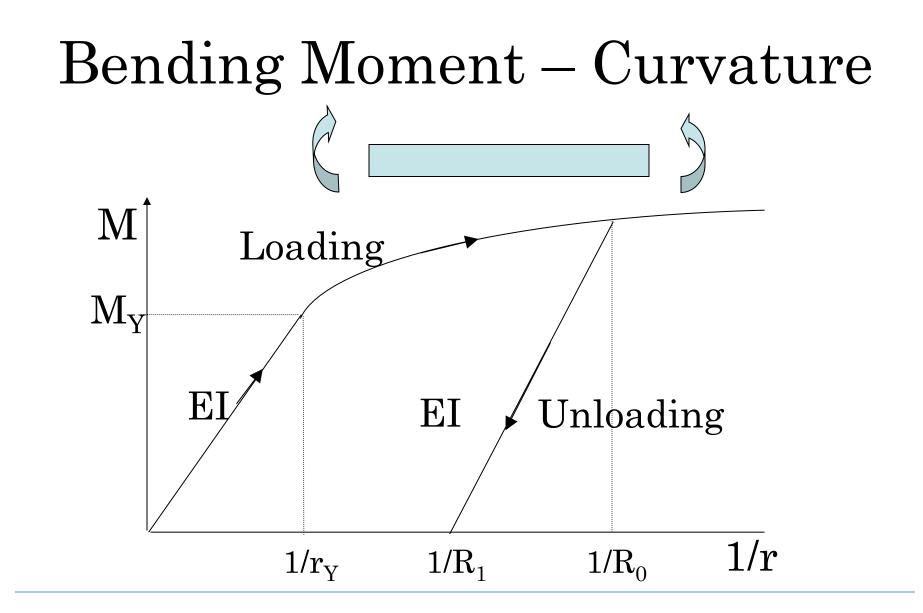
Elastic Springback Analysis



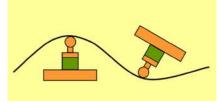
1. Assume plane sections remain plane: $e_y = -y/r$

(1)

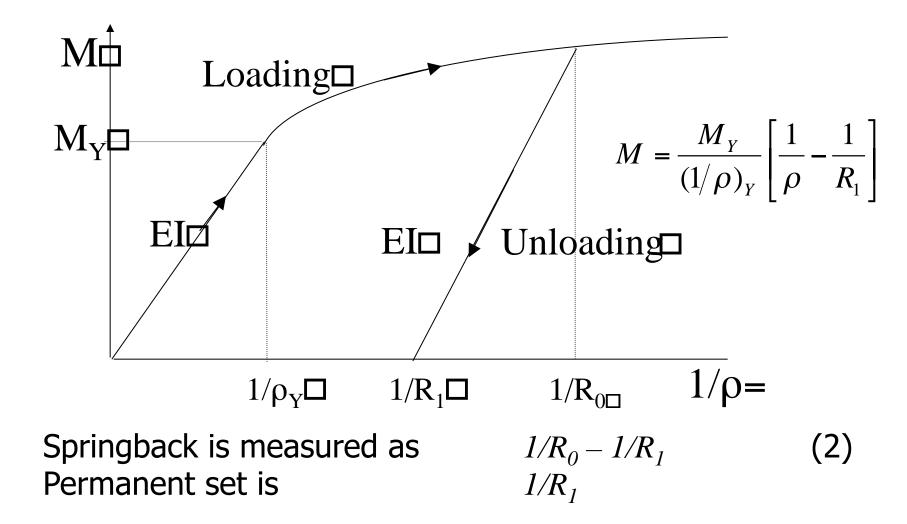
2. Assume elastic-plastic behavior for material s_{Y} $\sigma = E e e < e_{\psi}$ $\sigma = \sigma_{Y}$ $e \ge e$



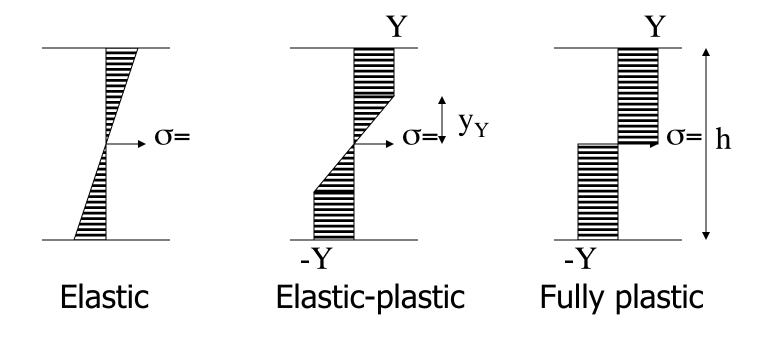




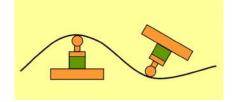
3. We want to construct the following Bending Moment "M" vs. curvature " $1/\rho$ " curve



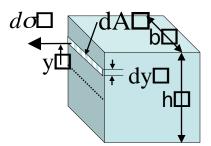
4. Stress distribution through the thickness of the beam







5.
$$M = \int_A \sigma y \, dA$$



Elastic region

$$M = \int \sigma y dA = -E \int \frac{y^2}{\rho} dA = -\frac{EI}{\rho}$$
(3)
At the onset of plastic behavior
 $\sigma = -y/\rho E = -h/2\rho E = -Y$ (4)

This occurs at

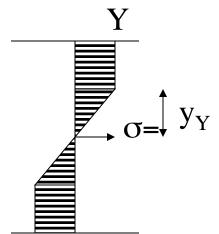
$$l/\rho = 2Y/hE = l/\rho_Y \tag{5}$$

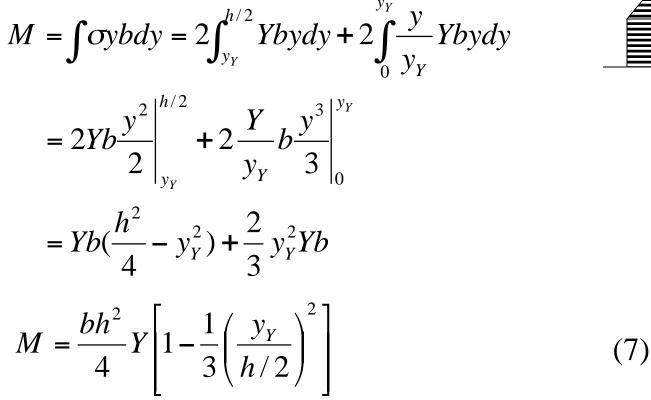
Substitution into eqn (3) gives us the moment at on-set of yield, $M_{\rm Y}$

$$M_Y = -EI/\rho_Y = EI \, 2Y / hE = 2IY/h \tag{6}$$

After this point, the M vs 1/r curve starts to "bend over." Note from M=0 to M=M_Y the curve is linear.

In the elastic – plastic region





Note at $y_Y = h/2$, you get on-set at yield, $M = M_Y$ And at $y_Y = 0$, you get fully plastic moment, $M = 3/2 M_Y$ To write this in terms of M vs $1/\rho$ rather than M vs y_Y , note that the yield curvature $(1/\rho)_Y$ can be written as (see eqn (1))

$$\frac{1}{\rho_Y} = \frac{\varepsilon_Y}{h/2} \tag{8}$$

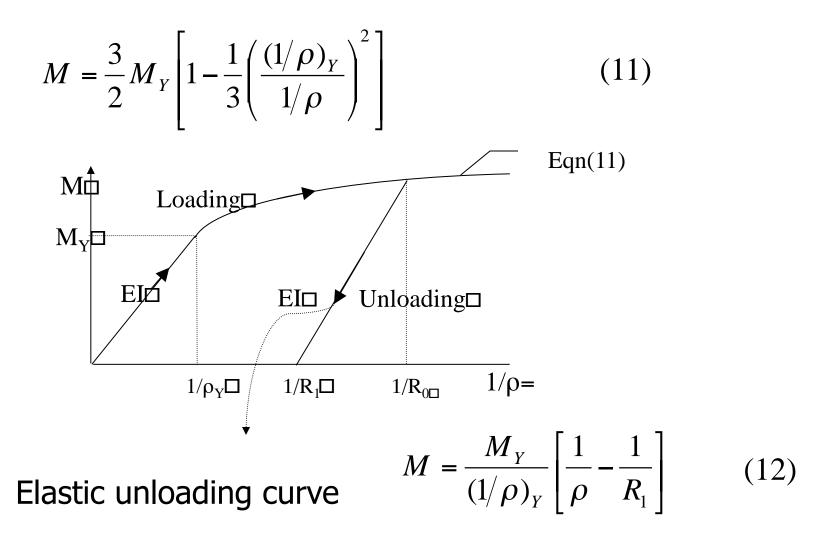
Where $\epsilon_{\rm Y}$ is the strain at yield. Also since the strain at $y_{\rm Y}$ is - $\epsilon_{\rm Y}$, we can write

$$\frac{1}{\rho} = \frac{\varepsilon_Y}{y_Y} \tag{9}$$

Combining (8) and (9) gives

$$\frac{y_Y}{h/2} = \frac{(1/\Box)_Y}{1/\Box}$$
(10)

Substitution into (7) gives the result we seek:



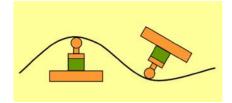
Now, eqn's (11) and (12) intersect at $1/\rho = 1/R_0$ Hence,

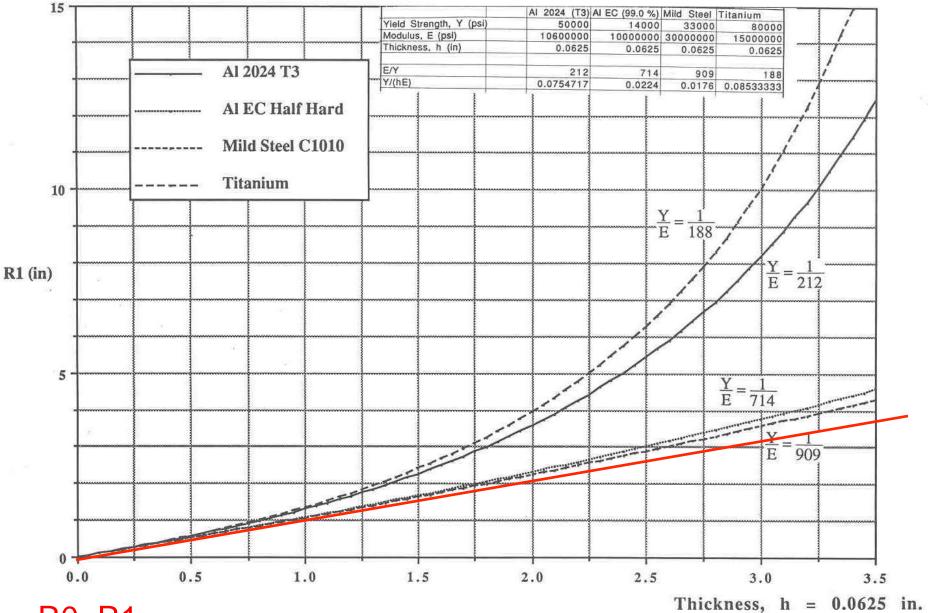
$$\frac{M_Y}{(1/\rho)_Y} \left[\frac{1}{R_0} - \frac{1}{R_1} \right] = \frac{3}{2} M_Y \left[1 - \frac{1}{3} \left(\frac{(1/\rho)_Y}{1/R_0} \right)^2 \right]$$

Rewriting and using $(1/\rho)_Y = 2Y / hE$ (from a few slides back), we get

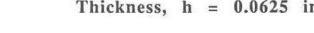
$$\left[\frac{1}{R_0} - \frac{1}{R_1}\right] = 3\frac{Y}{hE} - 4R_0^2 \left(\frac{Y}{hE}\right)^3$$
(13)

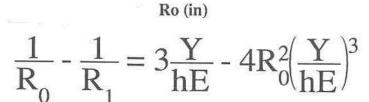








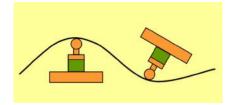


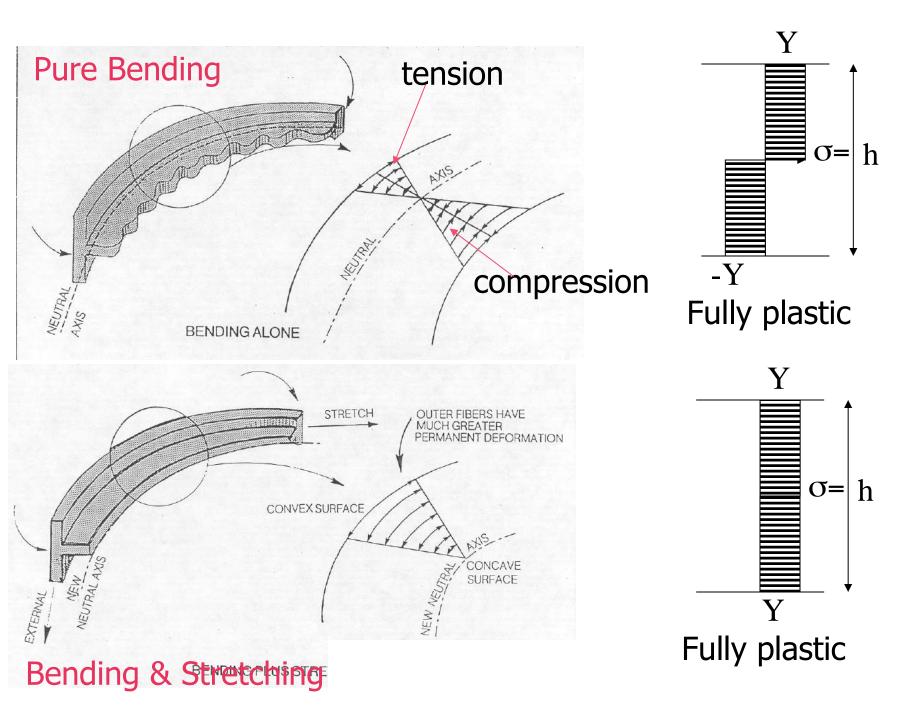


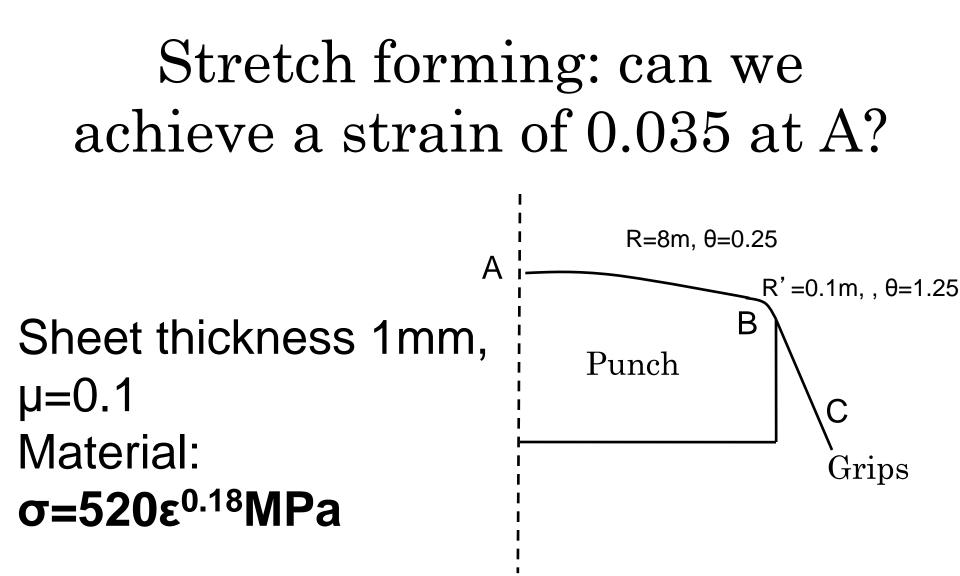
Methods to reduce springback

- Smaller Y/E
- Larger thickness
- Over-bending
- Stretch forming
- "coining" or bottoming the punch

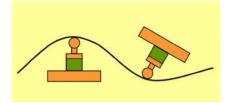




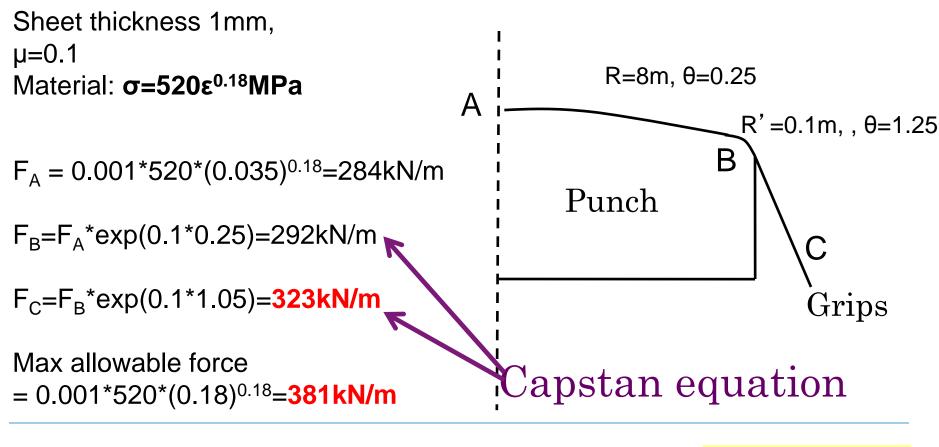




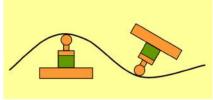




Can we achieve a strain of 0.035 at A?



Massachusetts Institute of Technology

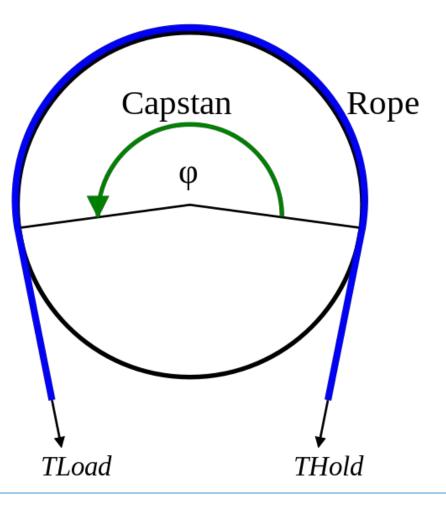


Friction and the capstan equation

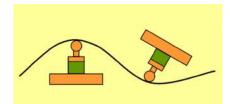
Typical stamping lubricants:

Oil-based lubricants
Aqueous lubricants
Soaps and greases
Solid films

$$T_{load} = T_{hold} \times \exp(\mu\theta)$$

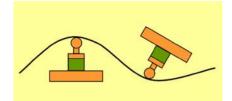






Research opportunities and challenges: reducing cost and environmental impacts



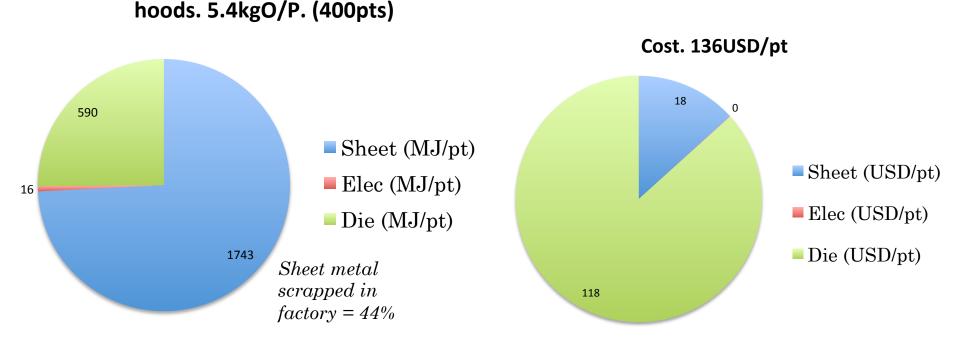


Energy & cost: Stamping alum car hoods

- Final part = 5.4kgs
- Total number of parts made = 400

Energy. 2.3GJ/pt. Stamping alum. car

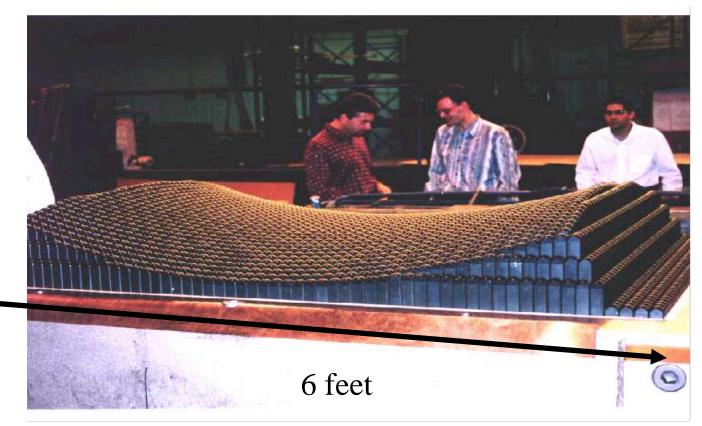
• Die material: cast and machined zinc alloy



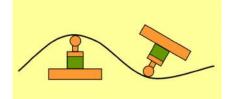
Source: Unpublished work: Cooper, Rossie, Gutowski (2015)

Excludes equipment depreciation and labor during forming

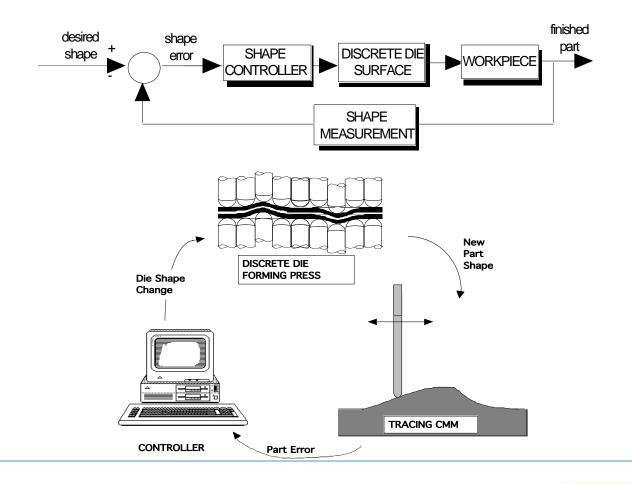
60 Ton Discrete Die Press (LMP - Hardt)



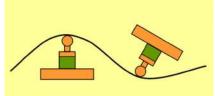




The Shape Control Concept



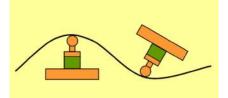




Stretch Forming with Reconfigurable Tool @ Northrop Grumman







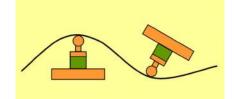
Flexible Forming at Ford



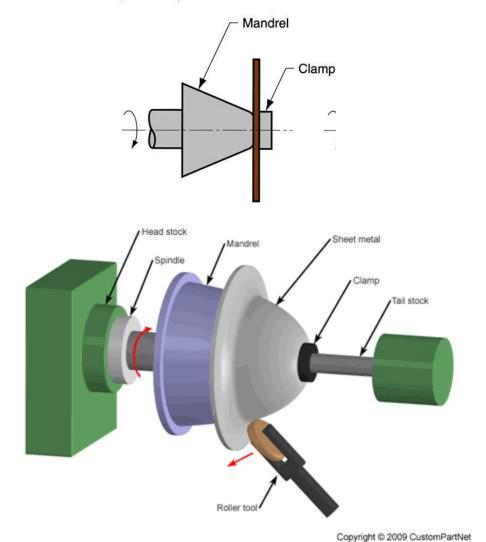


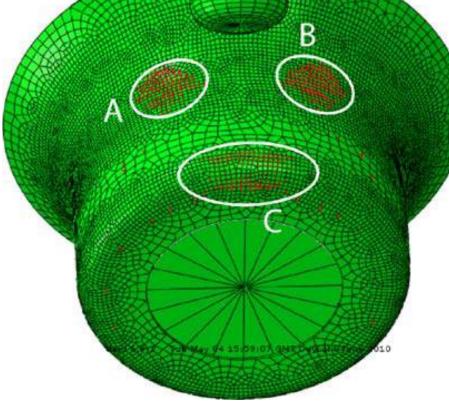






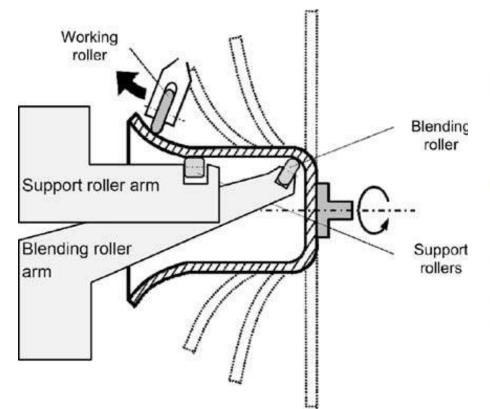
Conventional Spinning





http://www.custompartnet.com/wu/sheet-metal-forming

Flexible Spinning





(b) Machine in operation





Elliptical cup



Rectangular cup



Kidney bean

Music, O., & Allwood, J. M. (2011). Flexible asymmetric spinning. *CIRP Annals -Manufacturing Technology*, *60*(1), 319–322. doi:10.1016/j.cirp. 2011.03.136

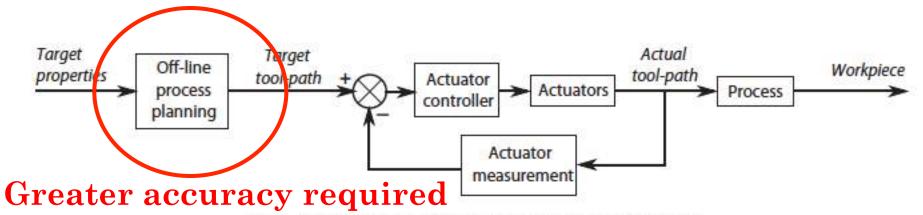


Fig. 1. A system diagram for open-loop control of metal forming.

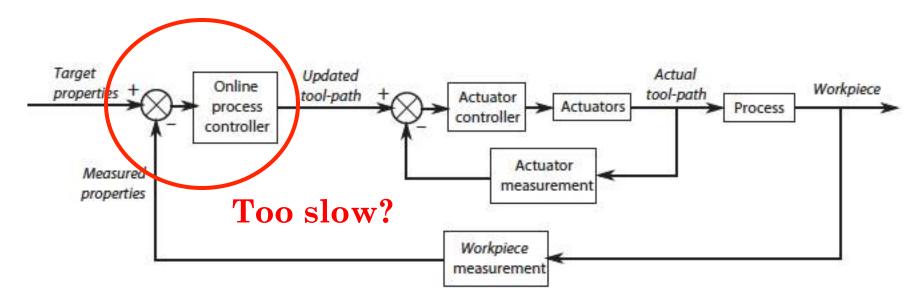
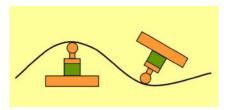


Fig. 2. A system diagram for closed-loop control of metal forming.



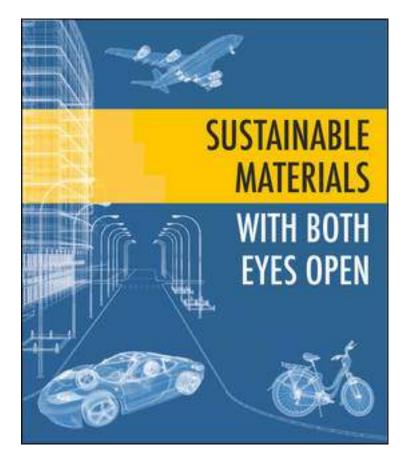
Polyblank, J. a., Allwood, J. M., & Duncan, S. R. (2014). Closed-loop control of product properties in metal forming: A review and prospectus. *Journal of Materials Processing Technology*, *214*(11), 2333– 2348. doi:10.1016/j.jmatprotec.2014.04.014



Thank you

Sheet metal forming in a low carbon future? See the wonderful... <u>http://</u> <u>www.withbotheyesopen.com</u>

Allwood, J., Cullen, J., Carruth, M., Cooper, D., McBrien, M., Milford, R., ... Patel, A. (2012). *Sustainable Materials with Both Eyes Open*. Cambridge: UIT.







Extra slides – just for fun



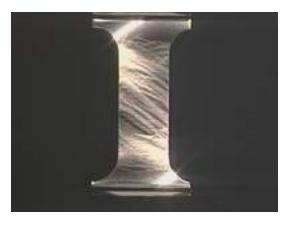


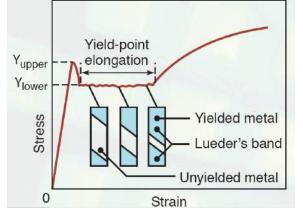
Surface finish defects

• Orange peel effect

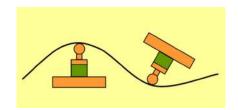


• Lüders bands

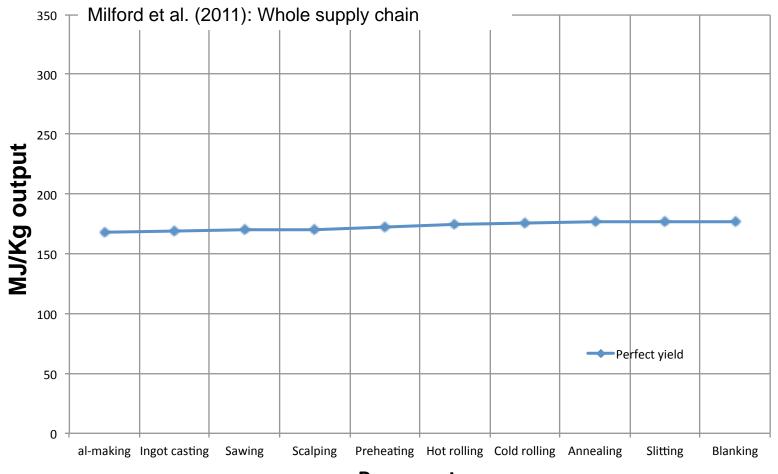






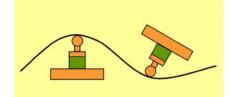


Material embodied energy: Aluminum primary production

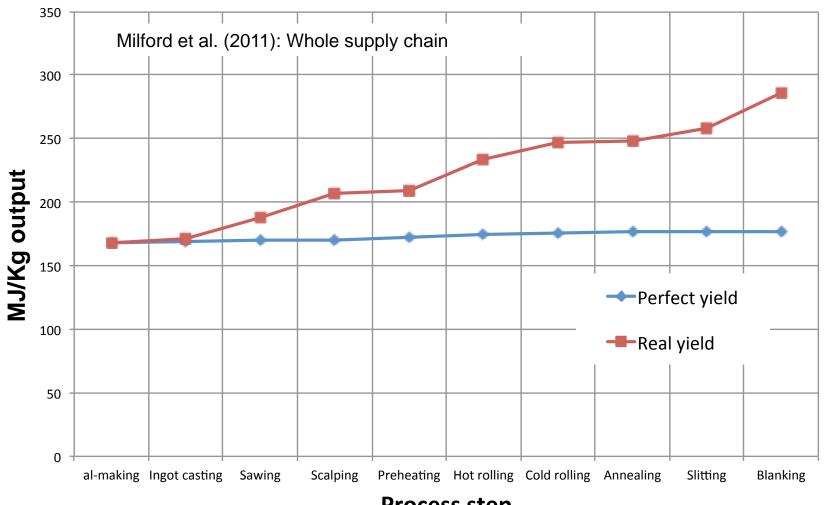


Process step



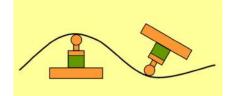


Material embodied energy: Aluminum primary production

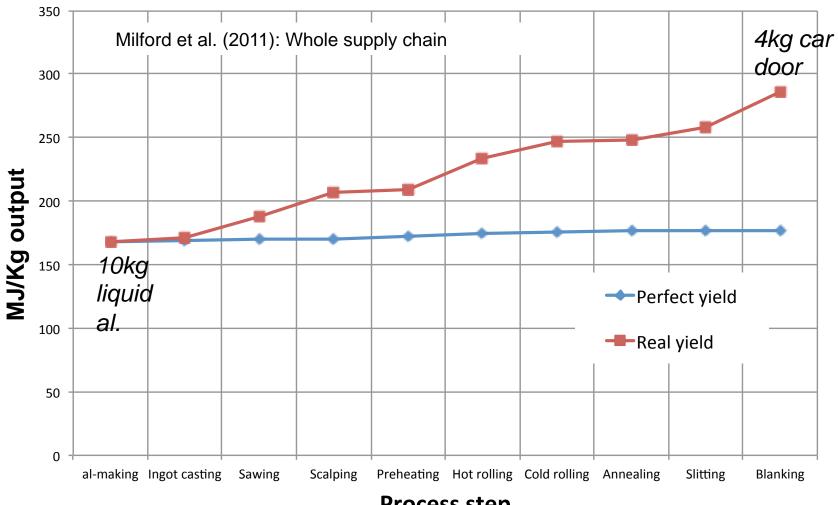


Process step





Material embodied energy: Aluminum primary production



Process step



