

The “IPAT” Equation

References

Ehrlich, P.R. and J.P. Holdren, 1972. Critique: One Dimensional Ecology. *Bulletin of the Atomic Scientists* 28(5): 16, 18-27.

Commoner, Barry. “The Environmental Cost of Economic Growth.” in Population, Resources and the Environment. Washington, DC: Government Printing Office Pp. 339-63, 1972.

Disaggregating the Problem

$$\text{Impact} = \text{Population} \times \frac{\text{Goods \& Services}}{\text{Person}} \times \frac{\text{Impact}}{\text{Goods \& Services}}$$

$$*I = P \times A \times T*$$

The IPAT equation is a mathematical identity that shows that the underlying environmental problems are related to “scale”. Growth in Population and Affluence have exceeded improvements in Technology. Furthermore the terms in the equation are highly coupled!

for infinitesimals

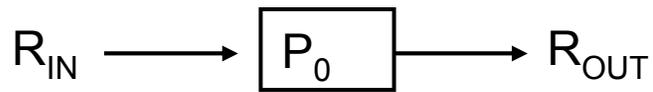
$$\frac{\Delta I}{I} = \frac{\Delta P}{P} + \frac{\Delta A}{A} + \frac{\Delta T}{T}$$

Population Growth

Affluence = GWP per capita

Technology

Population Dynamics



$$\Delta R = [\textit{birth} - \textit{death}] \\ + [\textit{immigration} - \textit{emigration}]$$

$$\frac{dP}{dt} = \Delta R \cdot P$$

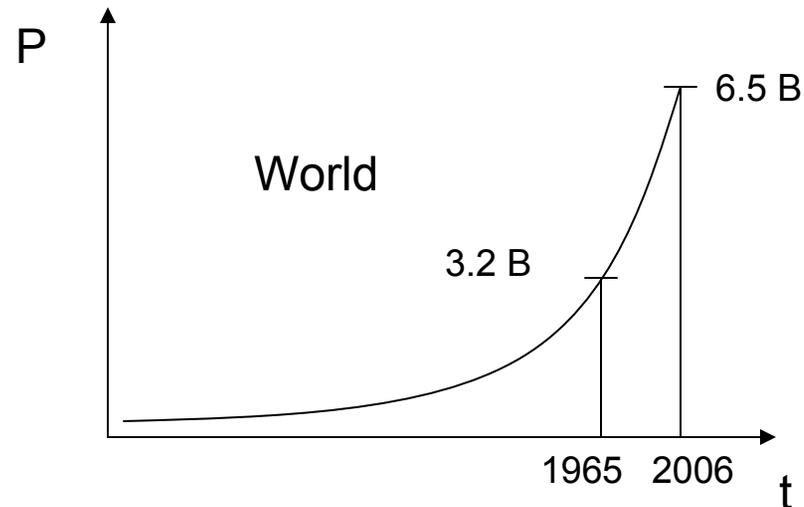
$$\frac{dP}{P} = \Delta R \cdot dt$$

$$P = P_0 e^{\Delta R \cdot t}$$

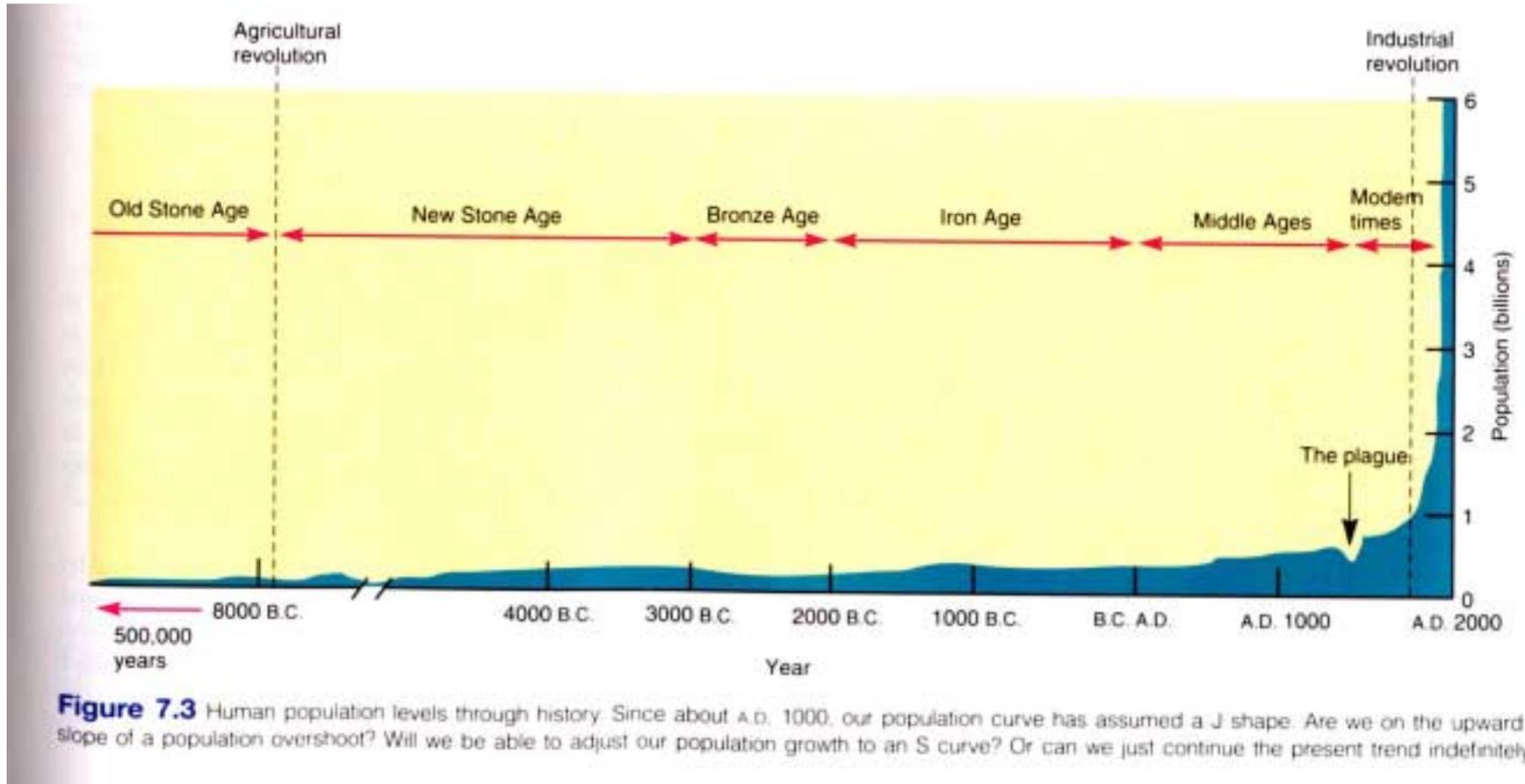
in the discrete form...

$$P = P_0 (1 + i)^n$$

Currently $i \approx 1\%$



We are adding 70-80 M people/yr

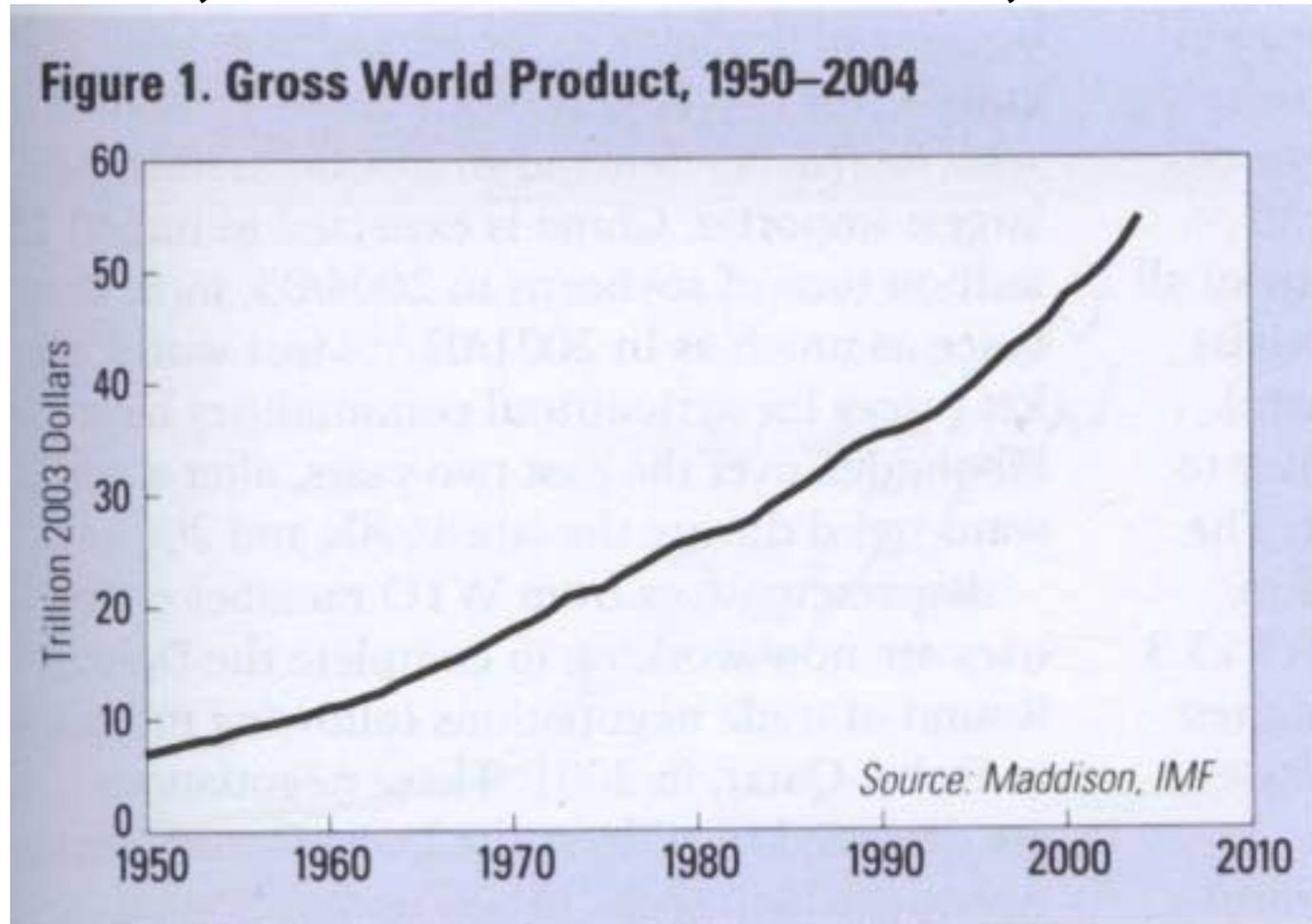


Add one Germany or 2X Canada each year

Affluence and GDP, GWP

- GDP = Gross Domestic Product
- GWP = Gross World Product
- GWP = market value of all goods and services produced for a year

GWP, $i \approx 5\%$ for 2004, 2005



Over the last several decades the growth in GWP has been less, more like 3%

To improve, we want...

$$\frac{\Delta I}{I} = \frac{\Delta P}{P} + \frac{\Delta A}{A} + \frac{\Delta T}{T} < 0$$

“technology”

Based on
global
estimates...

$$1\% + 4\% - 5\% = 0$$

We must improve our environmental performance on goods and services by 5% a year just to stay even.

“IPAT “ examples

1. Automobiles and gasoline
2. pig iron and energy
3. global carbon

1. Gasoline Used in Automobiles

What are the factors that influence the amount of gasoline we burn in automobiles?

$$\text{gasoline} = \text{number of cars} \times \frac{\text{miles driven}}{\text{car}} \times \frac{\text{gasoline}}{\text{mile}}$$

↑ ↑ ↗ ↗

Impact population service provided technology

“I” “P” car “T”

“A”

2. Energy used to make pig iron

$$\text{Energy} = \text{number of factories} \times \frac{\text{pig iron}}{\text{factory}} \times \frac{\text{energy}}{\text{pig iron}}$$

$$\text{Energy} = \text{pig iron produced} \times \frac{\text{energy}}{\text{pig iron}}$$

Again the energy used per ton pig iron produced depends upon the technology used.

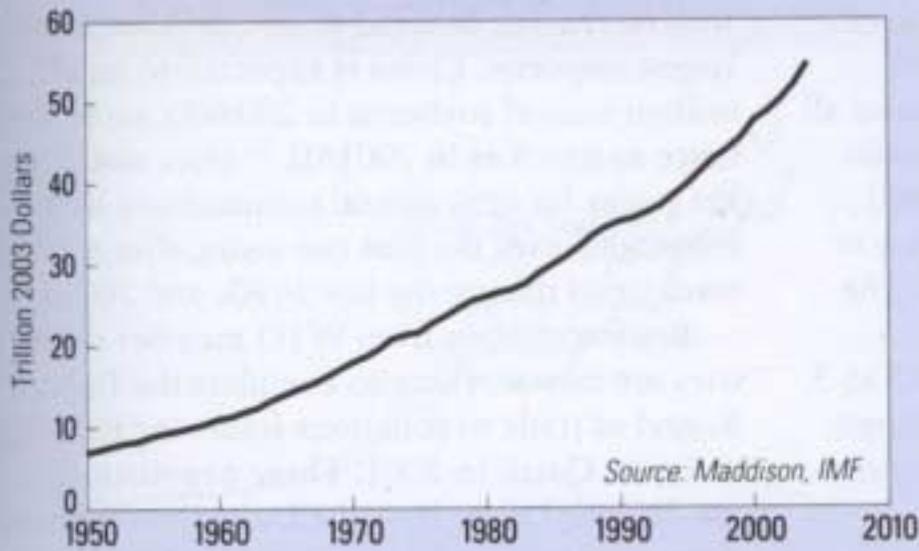
3. Carbon emissions

$$\text{Carbon} = \text{Population} \times \frac{\text{GWP}}{\text{Pop}} \times \frac{\text{Energy}}{\text{GWP}} \times \frac{\text{Carbon}}{\text{Energy}}$$

$$\frac{\Delta \text{Carbon}}{\text{Carbon}} = +1\% \quad +2\% \quad -1.25\% \quad -0.25\% = +1.5\%$$

These are *rough* averages over the last 3 decades,
data taken or calculated from Pacala & Socolow, Science 2004

Figure 1. Gross World Product, 1950–2004



Tons Per Million Dollars of Output

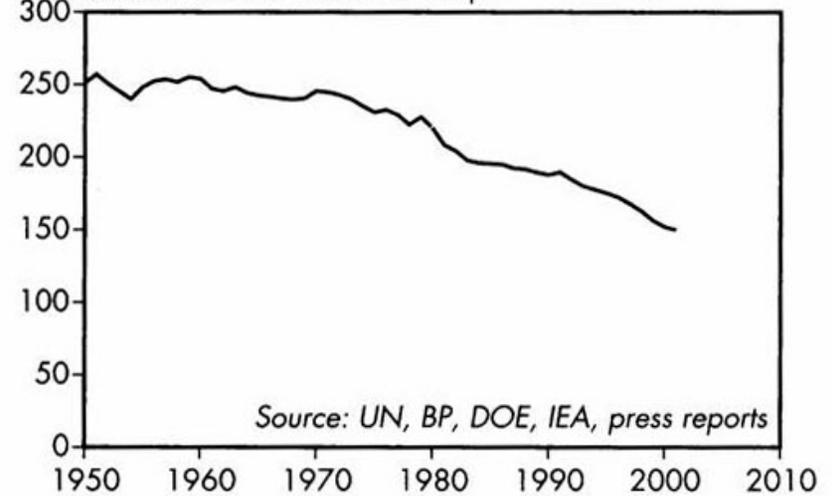
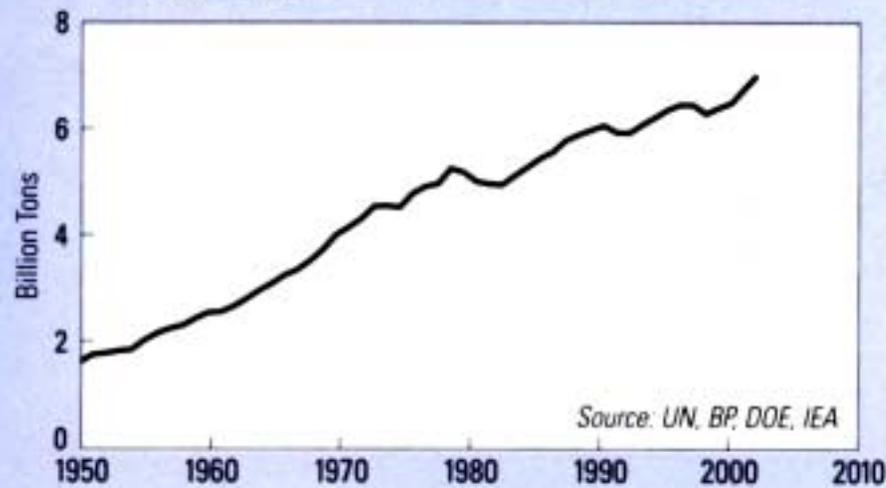


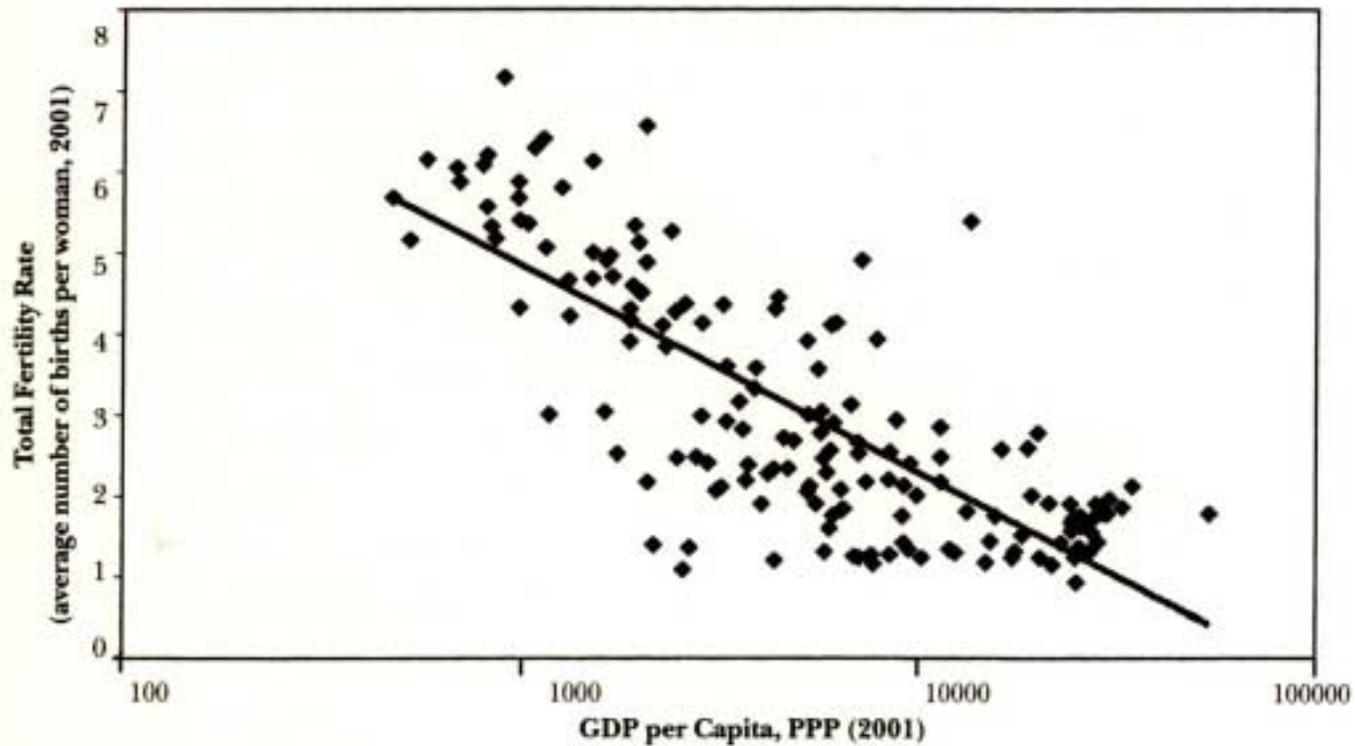
Figure 2: Carbon Intensity of the World Economy, 1950–2001

Figure 3. Carbon Emissions from Fossil Fuel Burning, 1950–2003



Fertility and Affluence

Figure 1: Fertility and Economic Development

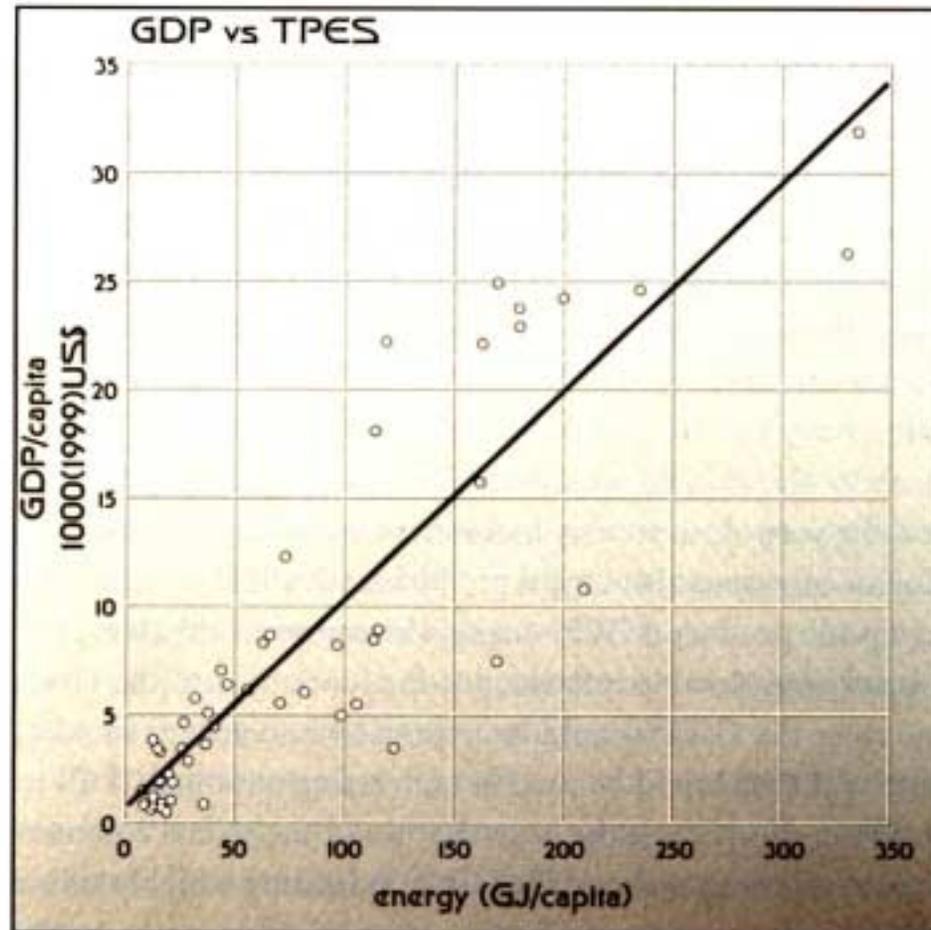


Note: X axis is on a logarithmic scale.

Source: Calculated using data from World Bank (2004).

see www.Harvard.edu

Affluence and Energy are correlated

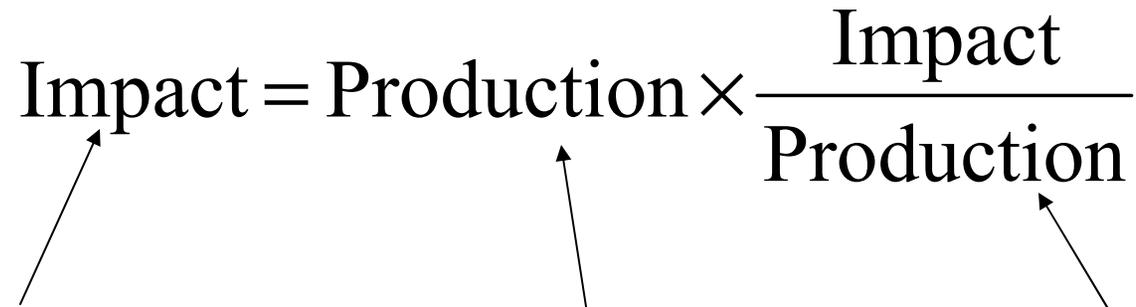


From Smil

Figure 2.1

A high correlation between TPES and GDP, with both values expressed as per capita averages for the year 2000. Values calculated from data in BP (2001) and UNDP (2001).

From a Production point of view

$$\text{Impact} = \text{Production} \times \frac{\text{Impact}}{\text{Production}}$$
The diagram shows the equation $\text{Impact} = \text{Production} \times \frac{\text{Impact}}{\text{Production}}$. Three arrows point from labels below to the terms in the equation: one from 'Energy Used' to 'Impact', one from 'Production (P) or Consumption' to 'Production', and one from '1/efficiency (e)' to the denominator 'Production' in the fraction.

Energy Used

Production (P) or Consumption

1/efficiency (e)

$$I = P \times \frac{1}{e}$$

Differentiating

$$\frac{dI}{dt} = \frac{1}{e} \frac{dP}{dt} - \frac{P}{e^2} \frac{de}{dt} \leq 0$$

Normalizing, and taking yearly increments, you are an environmentally benign producer when...

$$\frac{\Delta e}{e} \geq \frac{\Delta P}{P}$$

The Gold Standard

Note that “e” and “P” are coupled!

- *$e = f(P)$ Increased production leads to increased efficiency through learning effects and economies of scale*
- *$P = f(e)$ Increased efficiency can lead to reduced prices and increased demand. The phenomenon is called the “rebound effect”*