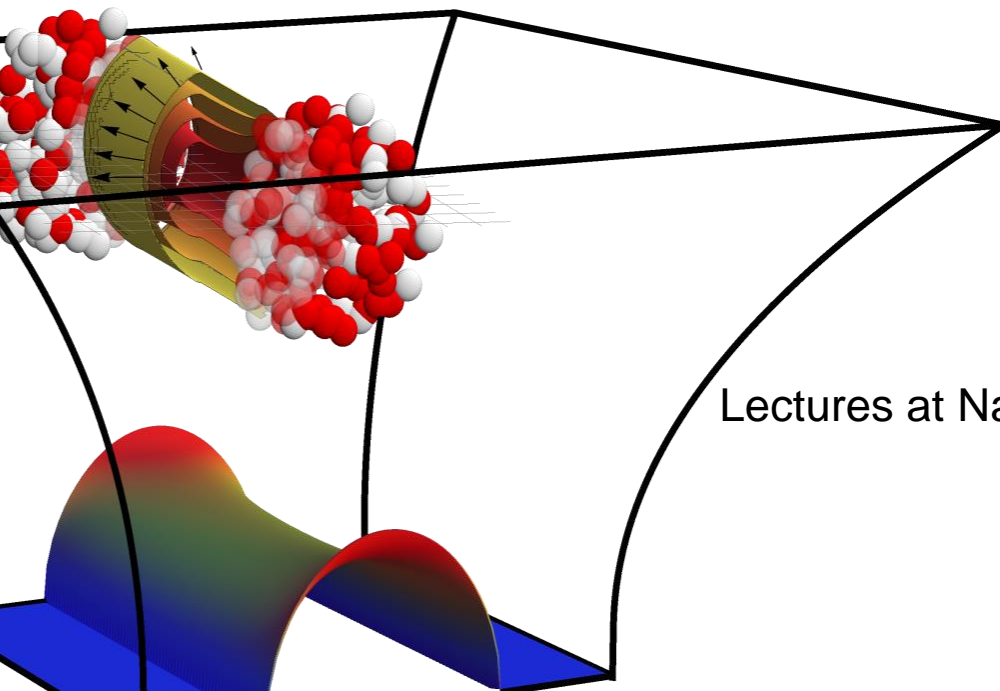


QUARK-GLUON PLASMA

HOT QCD, FLOWING PLASMA, JETS AND A TINY BIT OF STRING THEORY



Wilke van der Schee

Lectures at National Nuclear Physics Summer School,
MIT, 25 July 2016

OUTLINE

First lecture

- Heavy ion collisions, forming quark-gluon plasma
 - “the ridge” and particle spectra
- The standard model of heavy ion collisions
 - Initial dynamics (second)
 - Relativistic hydrodynamics (first)
 - Freeze-out / hadronic rescattering (not covered)

Second lecture

- Jets as probes of the medium
 - Internal jet structure
- The challenge: strong interactions, a bit of string theory

WHY DO WE STUDY QGP?

Quark gluon plasma in the early universe

- Heavy ion collisions, forming quark-gluon plasma
- Also: heavy ion collisions full of surprises 😊

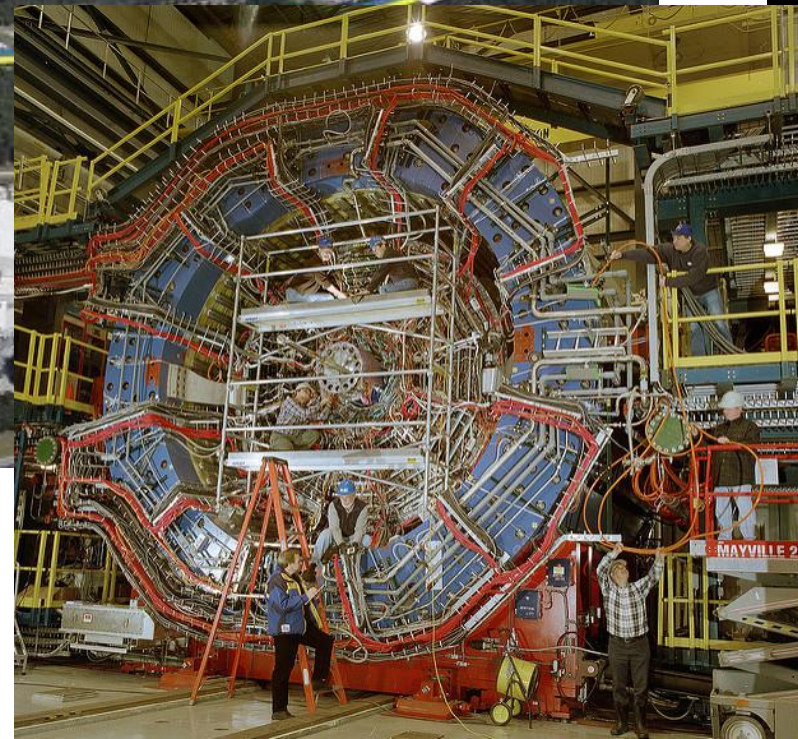
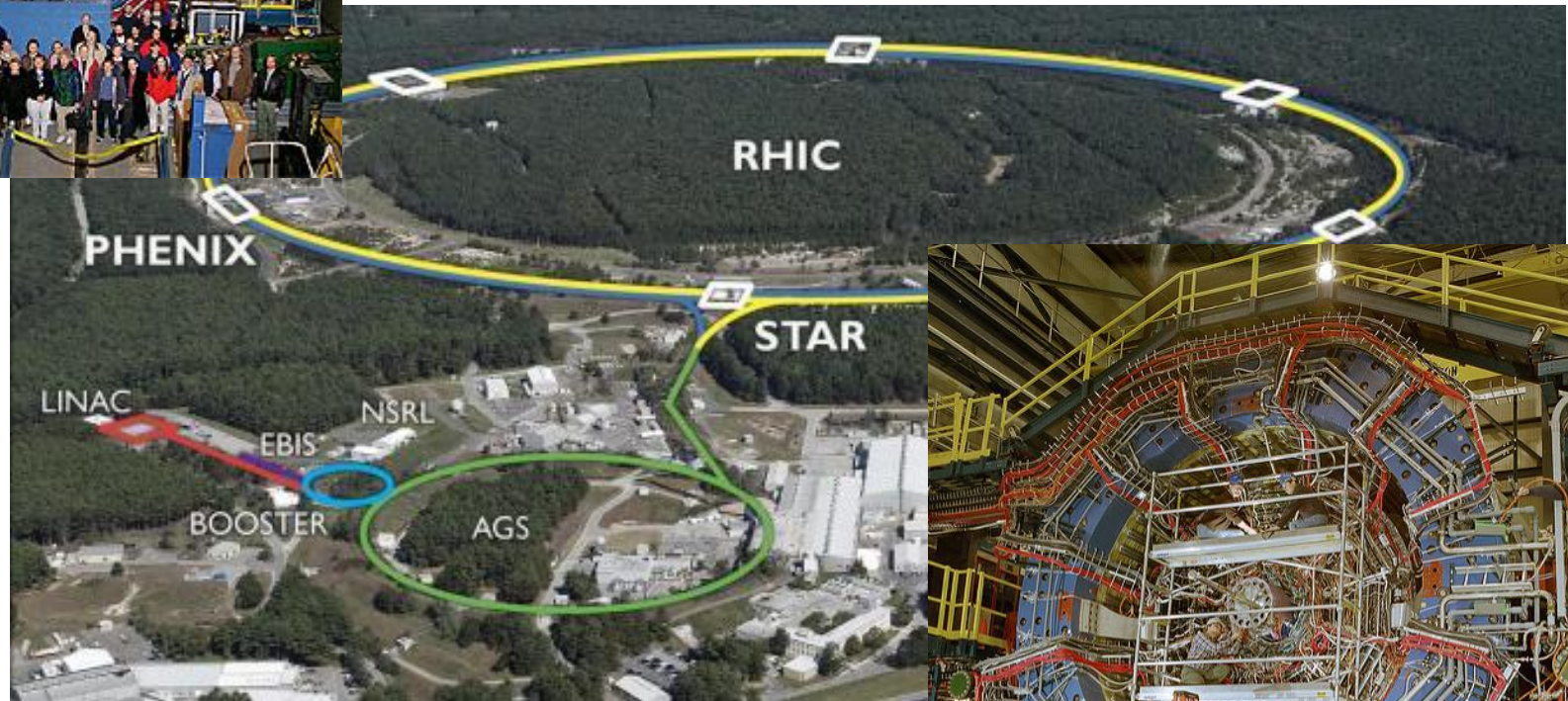
Strong force – Quantum Chromo Dynamics

- No doubt about underlying Lagrangian and perturbative QCD
- But QCD non-perturbative and lattice is limited (Euclidean)
- Recent: perhaps insights in structure proton?

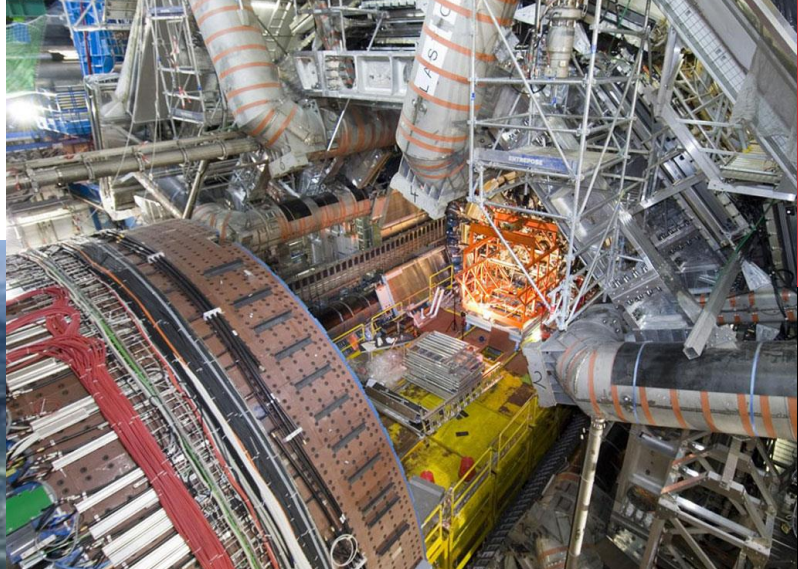
Strongly interacting quantum matter

- QGP may be one of cleanest systems of quantum matter
- Interesting properties: low viscosity, fast thermalization
- Even connections to high temperature superconductors??

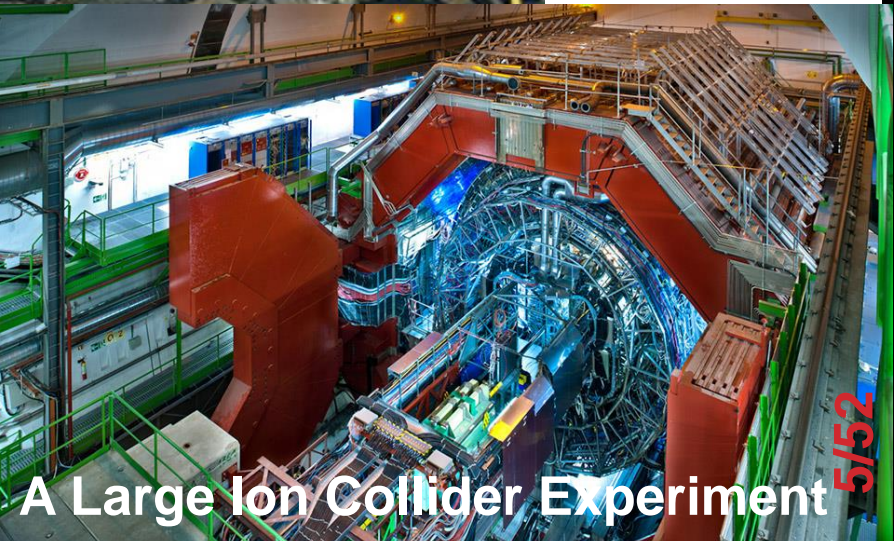
WHERE DO WE STUDY QGP? RHIC



WHERE DO WE STUDY QGP? LHC



(1/12 months)



A Large Ion Collider Experiment

WHERE DO WE STUDY QGP?

Different energies

- RHIC: from 3.5 – 100 GeV per nucleon, i.e. top energy $\sqrt{s_{NN}} = 200$ GeV
- LHC: $\sqrt{s_{NN}}$ 2.76 and 5.02 TeV for Pb-Pb and 5.02 TeV for p-Pb

Exercise: explain these numbers from pp collisions (7, 8 and 13 TeV)

Exercise: what is the transverse and longitudinal size? (Pb radius ~ 6.7 fm)

Different ions

- RHIC: wide variety, d^3 , Cu^{64} , Au^{197} , also He^3 , Uranium²³⁸ (funny shapes)
- LHC: mostly Pb^{208}
- Also interesting: asymmetric collisions, i.e. d-Au or p-Pb

Different observables

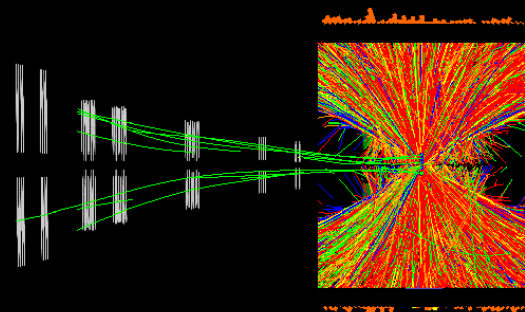
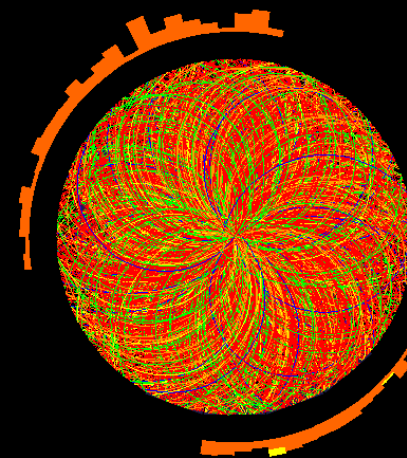
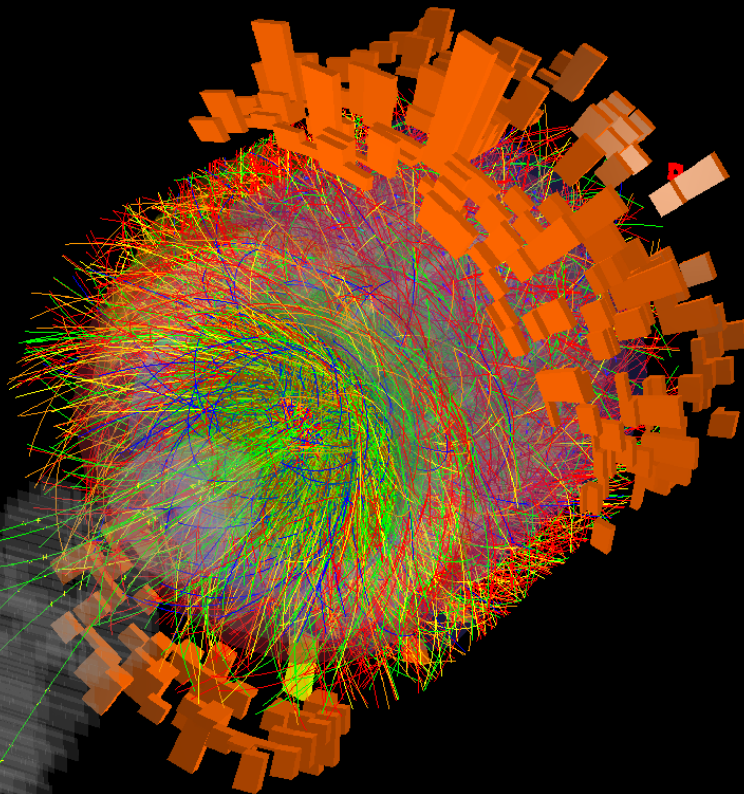
- QGP maybe one of cleanest systems of quantum matter
- Interesting properties: low viscosity, fast thermalization
- Even connections to high temperature superconductors??

HOW DO WE STUDY QGP?

We only see resulting particles



ALICE



QGP IS ALSO COOL! (OR HOT..)

As close to big bang as we can get (about a millisecond)

- Temperatures: 4×10^{12} °K or 7×10^{12} °F (100.000 hotter than interior sun)
- Lifetime: 7×10^{-23} s, size 20×10^{-15} m
- Accelerations: 10^{31} g

QGP may behave much like a black hole horizon

- A fluid-like horizon, in 4+1 dimensions, later more...

One unfortunate fact

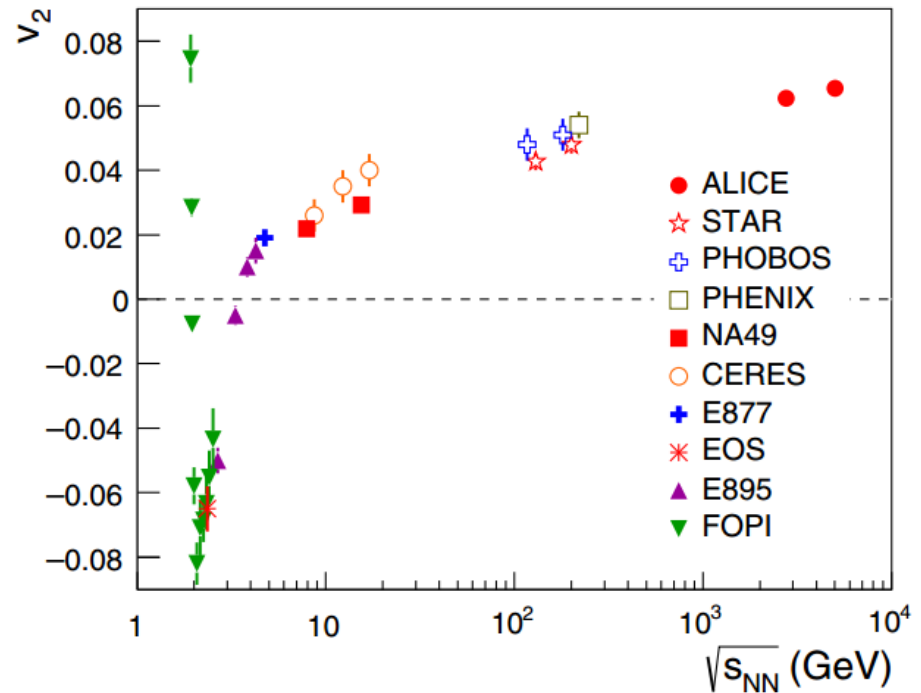
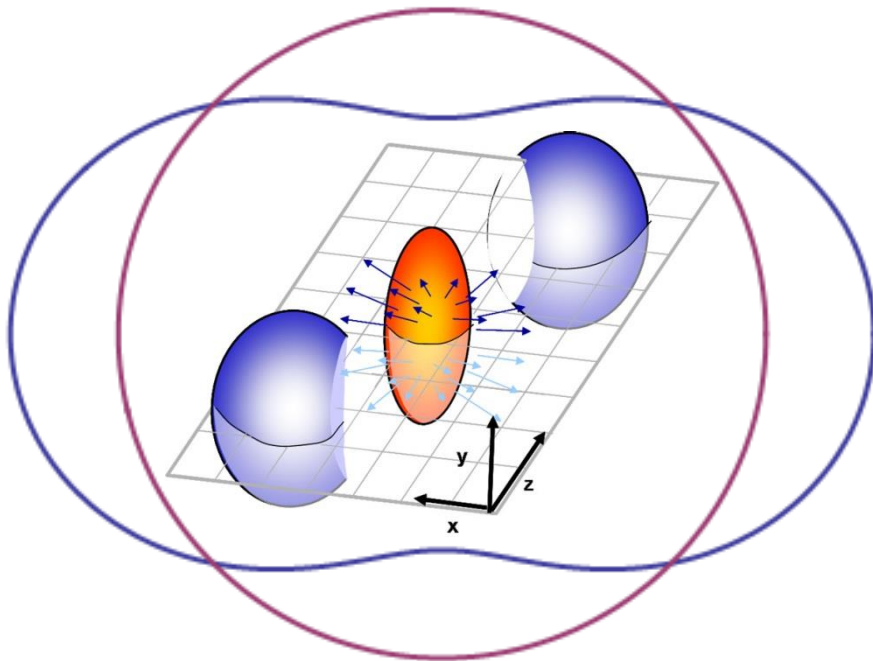
- QGP is hottest man-made plasma
- Unfortunately cosmic rays have higher $\sqrt{s_{NN}}$ and are hence even hotter



ELLIPTIC FLOW: V_2 , QGP IS INTERESTING

How anisotropic is the final state?

- Ideal gas/weak coupling
- Perfect fluid/strong coupling

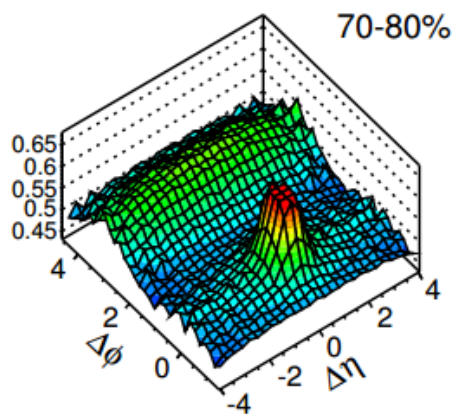
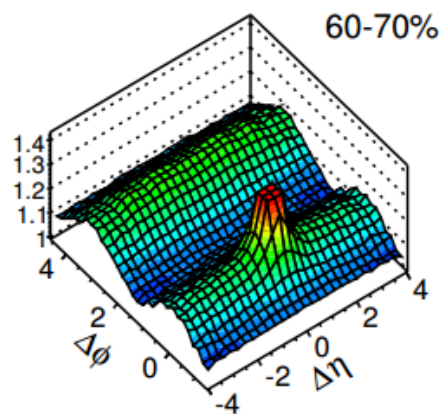
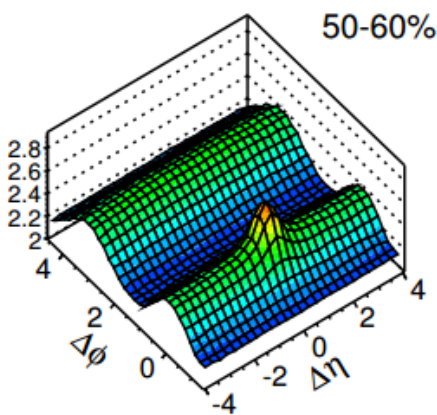
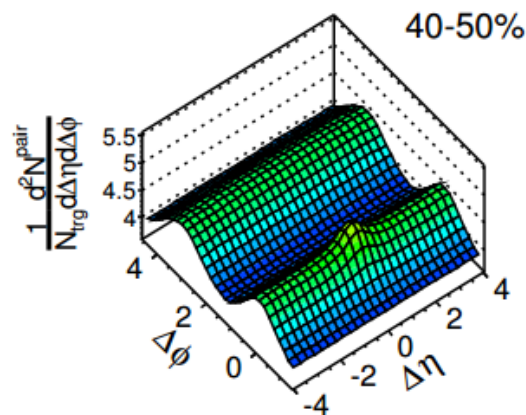
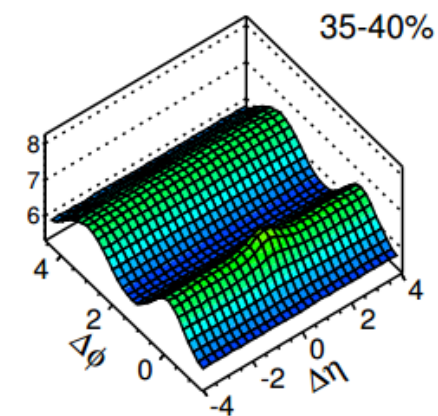
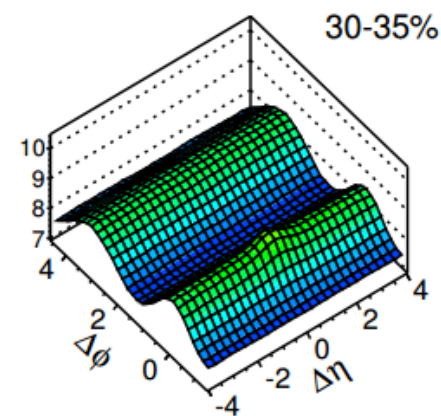
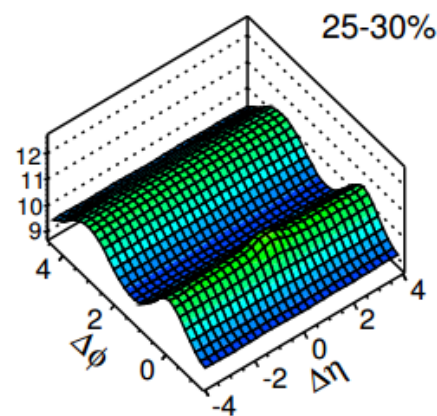
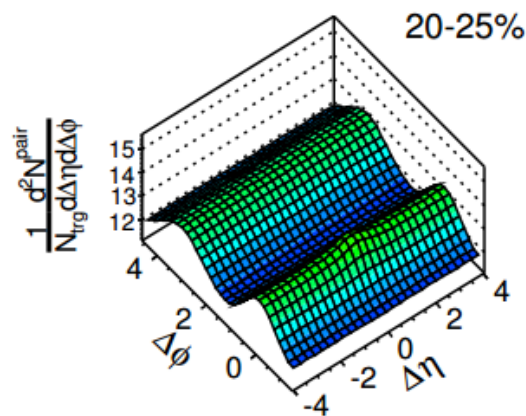
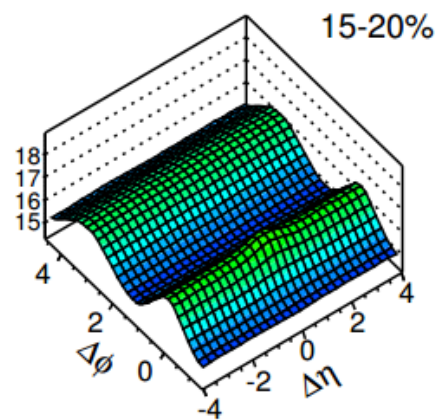
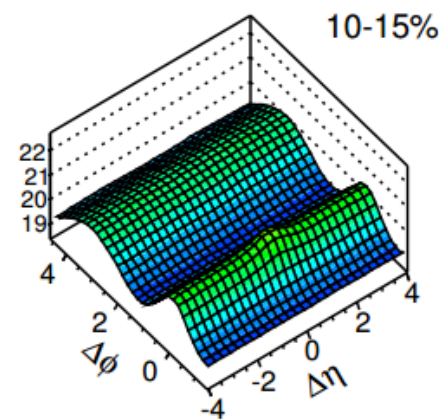
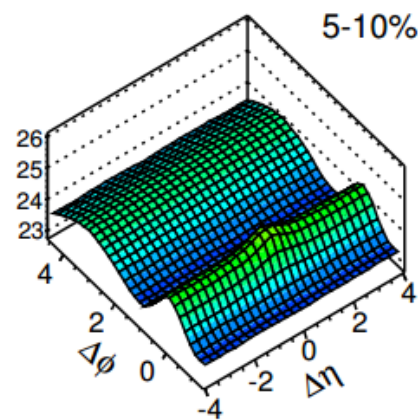
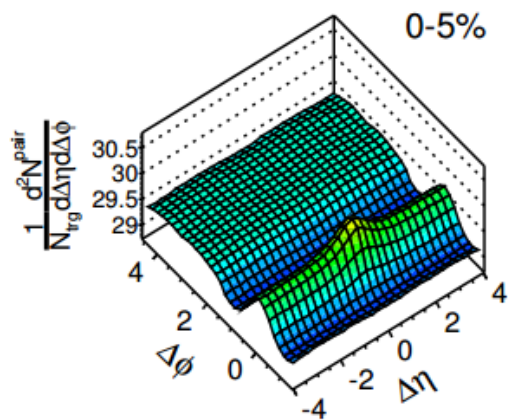


CMS $L_{\text{int}} = 3.9 \mu\text{b}^{-1}$

PbPb $\sqrt{s_{\text{NN}}} = 2.76 \text{ TeV}$

$3.0 < p_{\text{T}}^{\text{trig}} < 3.5 \text{ GeV}/c$

$1.0 < p_{\text{T}}^{\text{assoc}} < 1.5 \text{ GeV}/c$



(PSEUDO)RAPIDITY

Transverse and longitudinal dynamics

- Note distinction between space and momentum rapidity
- Boost invariance: no y -dependence
Bjorken symmetry, simplest model for expanding plasma

$$t = \tau \cosh(y_s)$$

$$z = \tau \sinh(y_s)$$

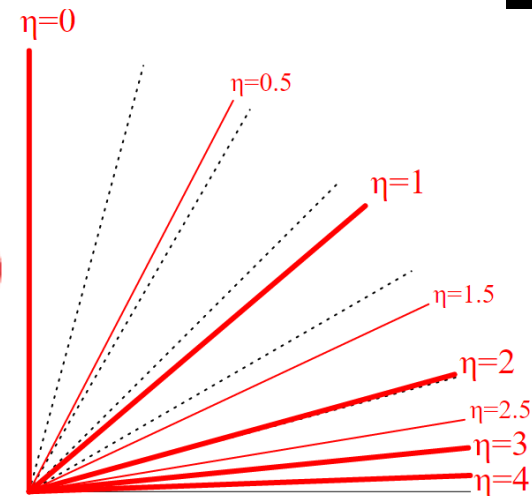
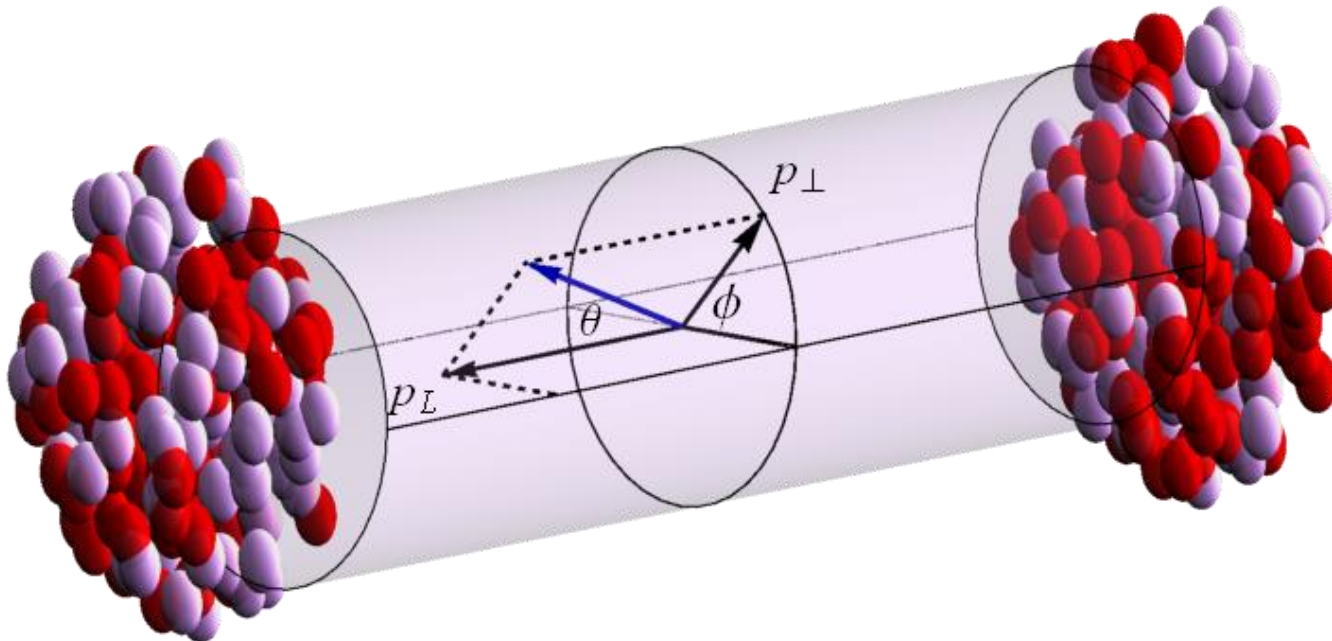
$$E = m \cosh(y_p) = \gamma m$$

$$|\mathbf{p}| \text{ or } p_L = m \sinh(y_p) = \gamma m v$$

$$y_p = \tanh^{-1} \left(\frac{p_L}{E} \right)$$

$$\eta_p = \tanh^{-1} \left(\frac{p_L}{|\mathbf{p}|} \right)$$

$$= -\log(\tan(\theta/2))$$

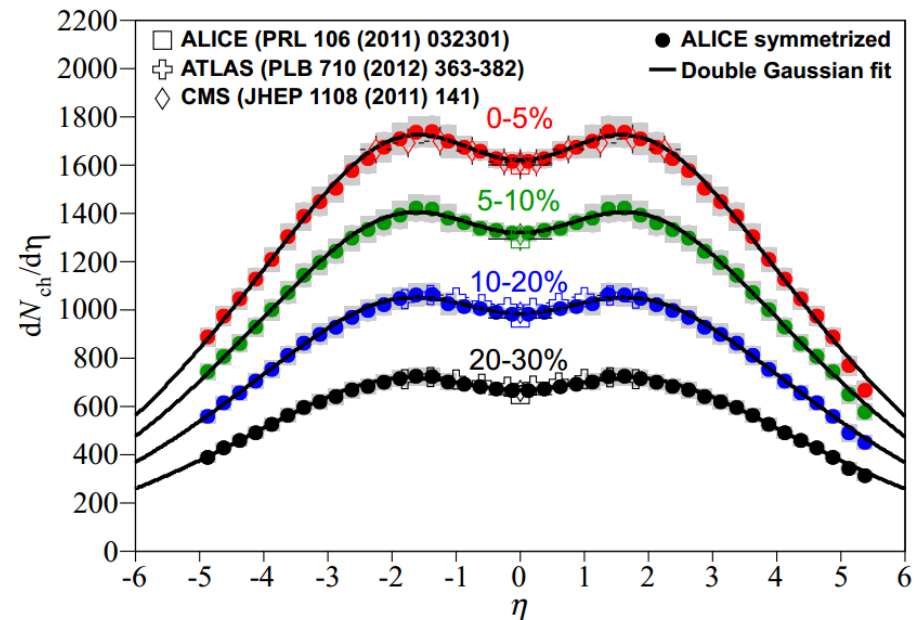
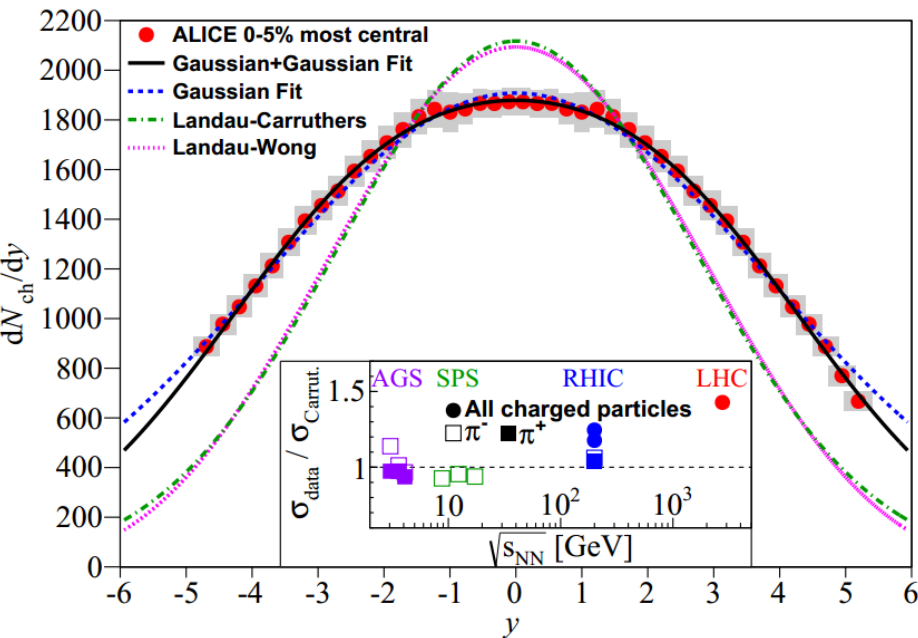


Exercise: ALICE measures up to $\eta=5.1$, 4cm from beam, how big is the detector?

RAPIDITY VERSUS PSEUDO-RAPIDITY

Longitudinal particle spectrum

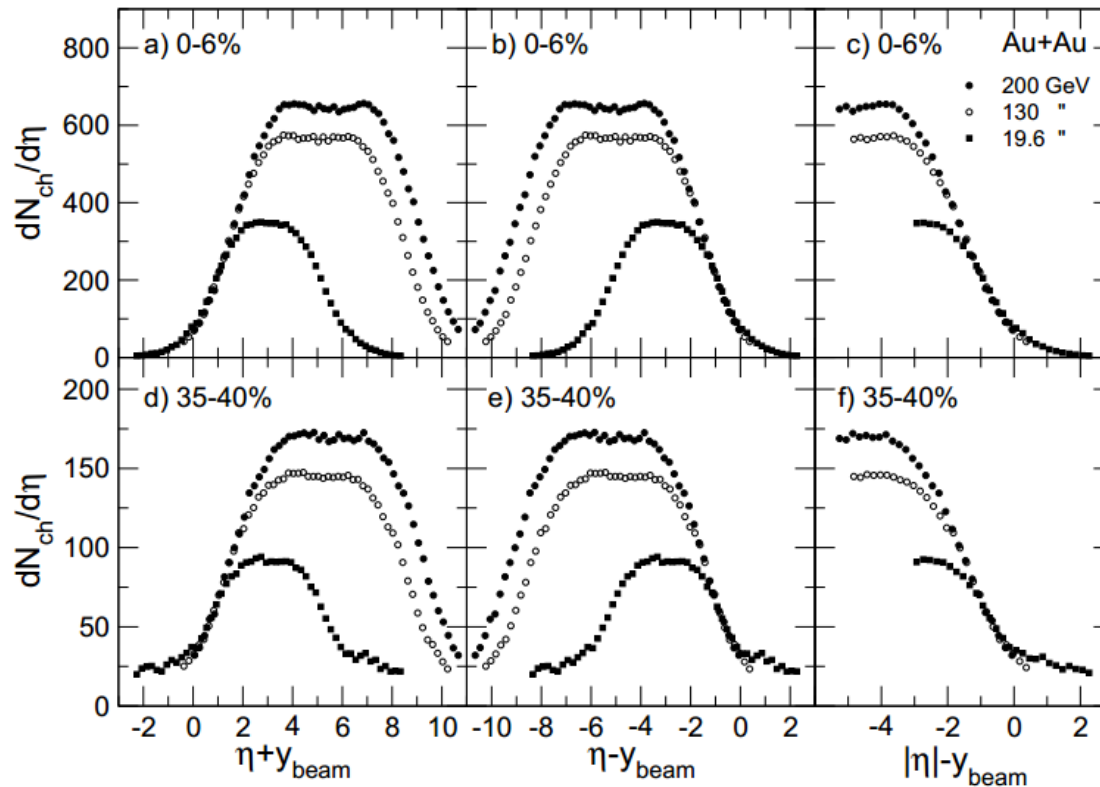
- No real boost invariance: rapidity dependence Gaussian width (~ 2 at RHIC, ~ 3 at LHC), with Jacobian depending on mass
- Theorists prefer y , experimentalists η



RAPIDITY SPECTRUM AT RHIC

Longitudinal particle spectrum at 19.6, 130 and 200 GeV

- Spectrum gets wider at higher energies
- Coincidence: pseudo-rapidity very flat at top RHIC energies
- Interesting: as a function of $\eta+y_{\text{beam}}$ they collapse (limiting fragmentation, related to saturation (?))



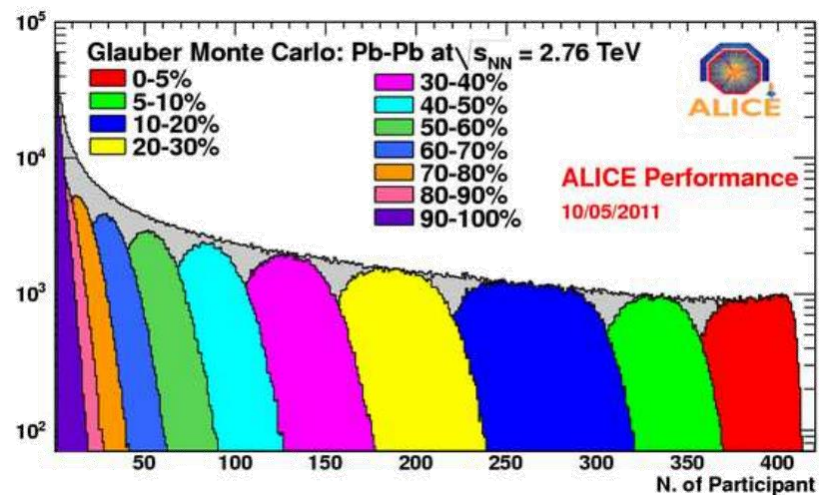
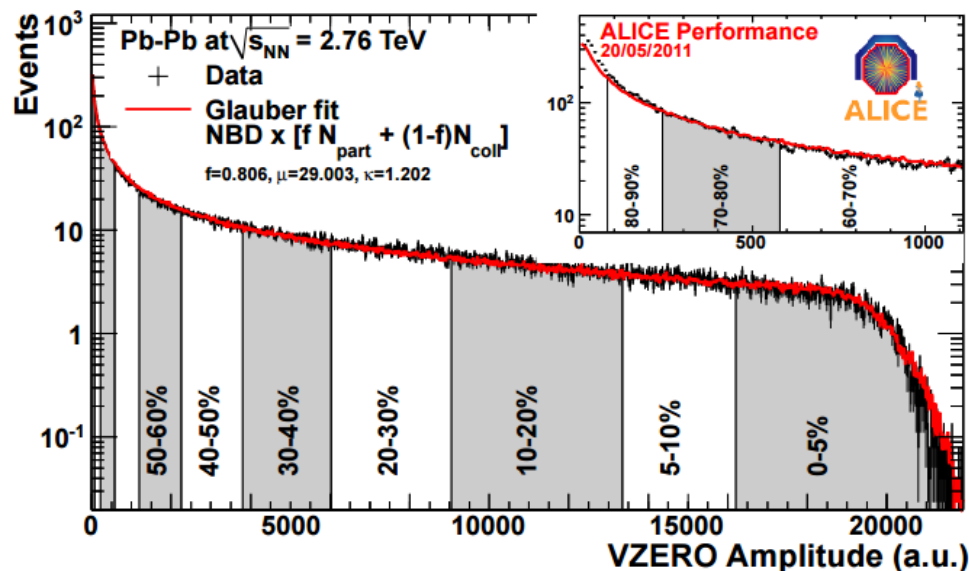
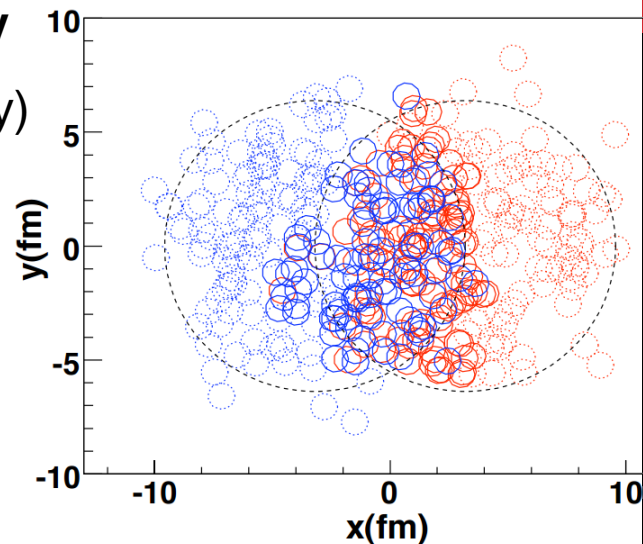
CENTRALITY

Ions collide with an impact parameter b : centrality

- 0% is head on: highest multiplicity (at mid-rapidity)
- >50% peripheral: skimming ions

Related to number of participants/spectators

- Estimate by Monte Carlo Glauber
- Subtleties defining centrality (especially in p-Pb)

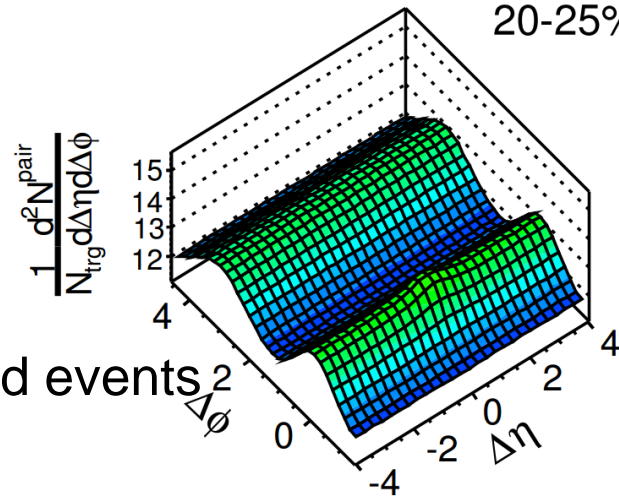


'THE RIDGE'

20-25%

Two particle correlator

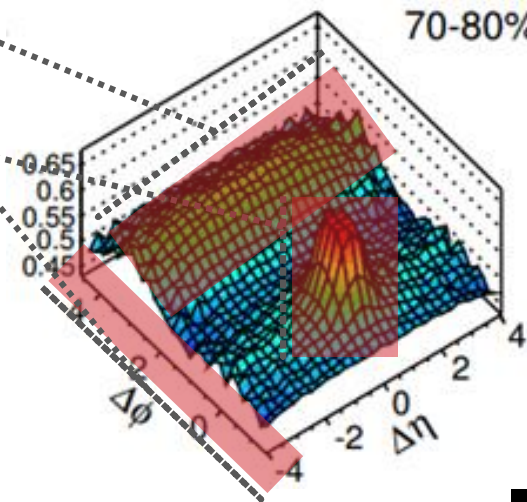
- Trigger particle and response particle
- Compare particles in same event versus mixed events (to avoid detector effects)
- 'jet' contribution, transverse momentum conservation



$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi} = B(0,0) \times \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)},$$

$$S(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{same}}}{d\Delta\eta d\Delta\phi}$$

$$B(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{mix}}}{d\Delta\eta d\Delta\phi}$$



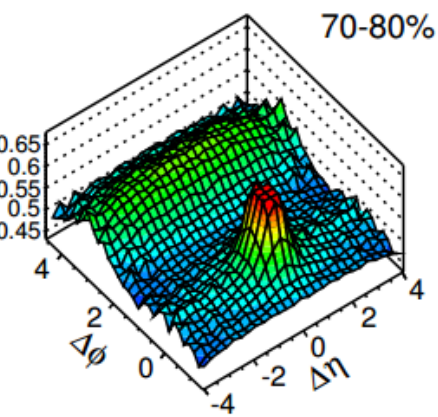
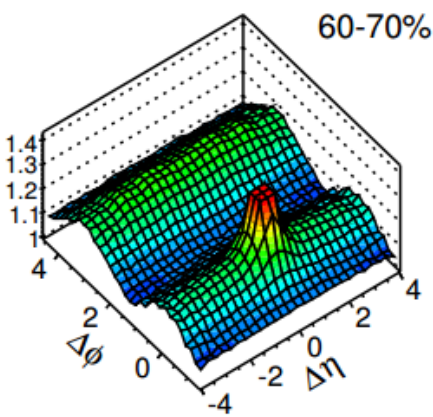
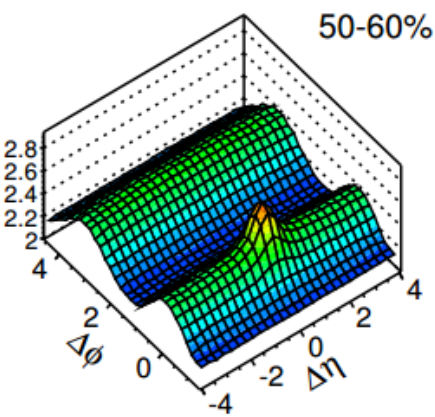
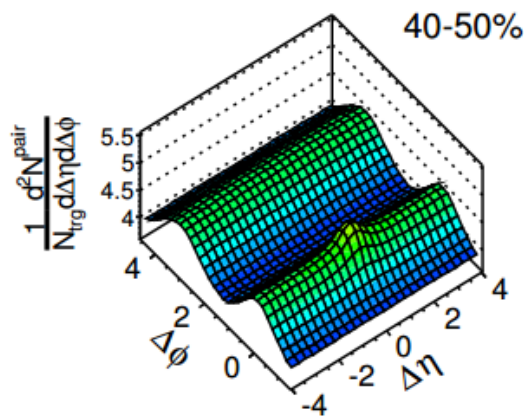
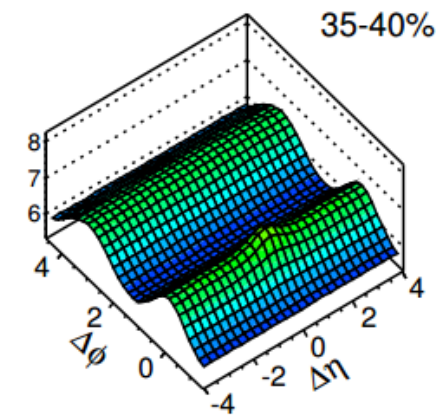
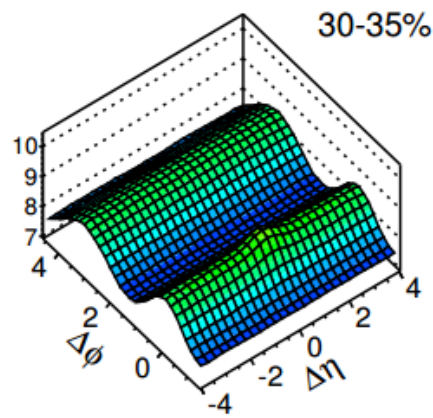
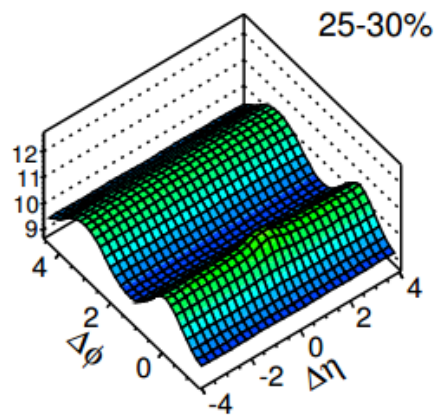
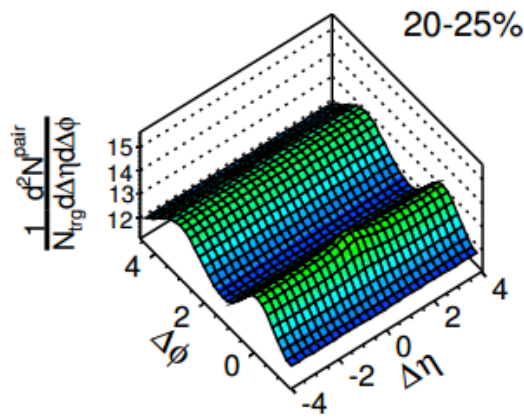
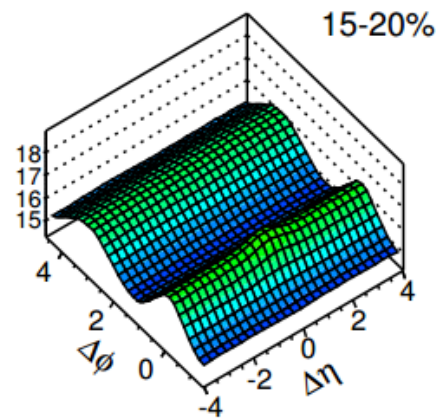
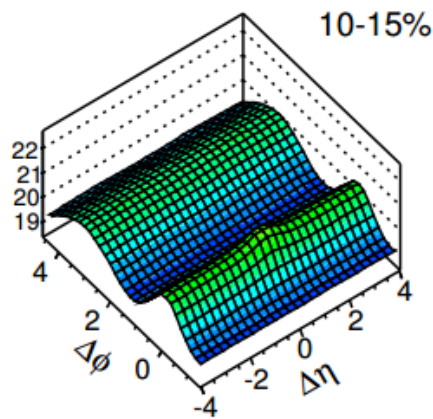
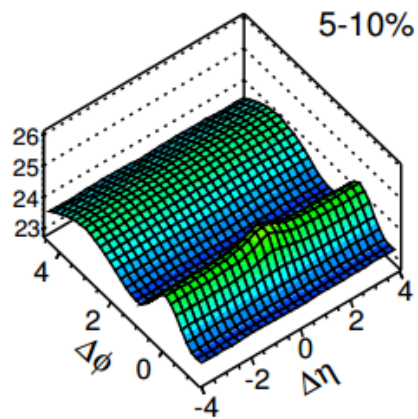
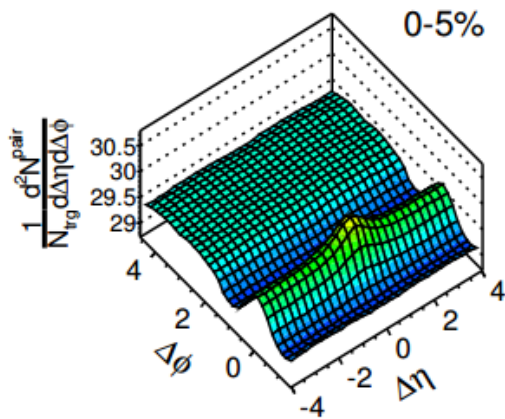
70-80%

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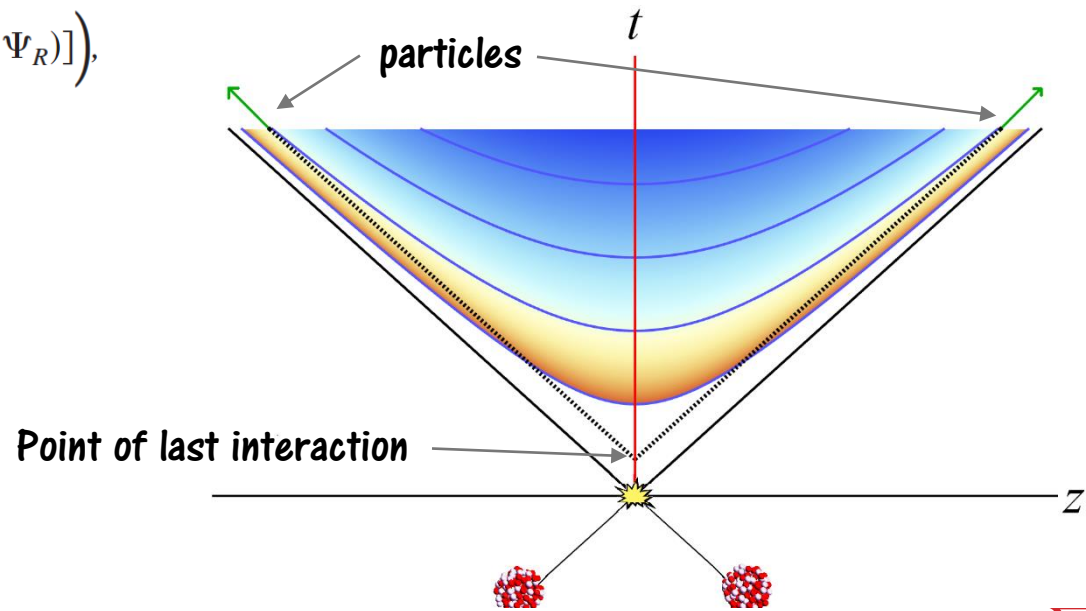
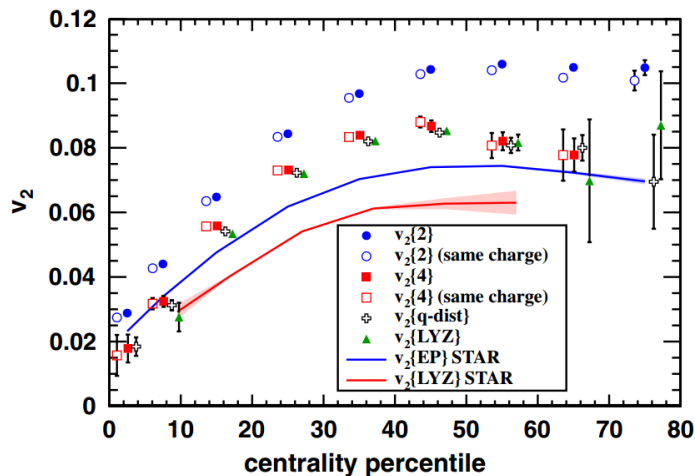
'THE RIDGE'

exclude short range 'jet': $|\Delta\eta| > 2$

More fun: average over $\Delta\eta$ to extract 'flow'

- Quantifies response to initial correlations (causality)
 - Natural explanation is hydrodynamics (more later)
- Also causality in transverse plane
 - Centrality dependence of v_2 is convincing for hydrodynamics

$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_t dp_t dy} \left(1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\phi - \Psi_R)] \right),$$

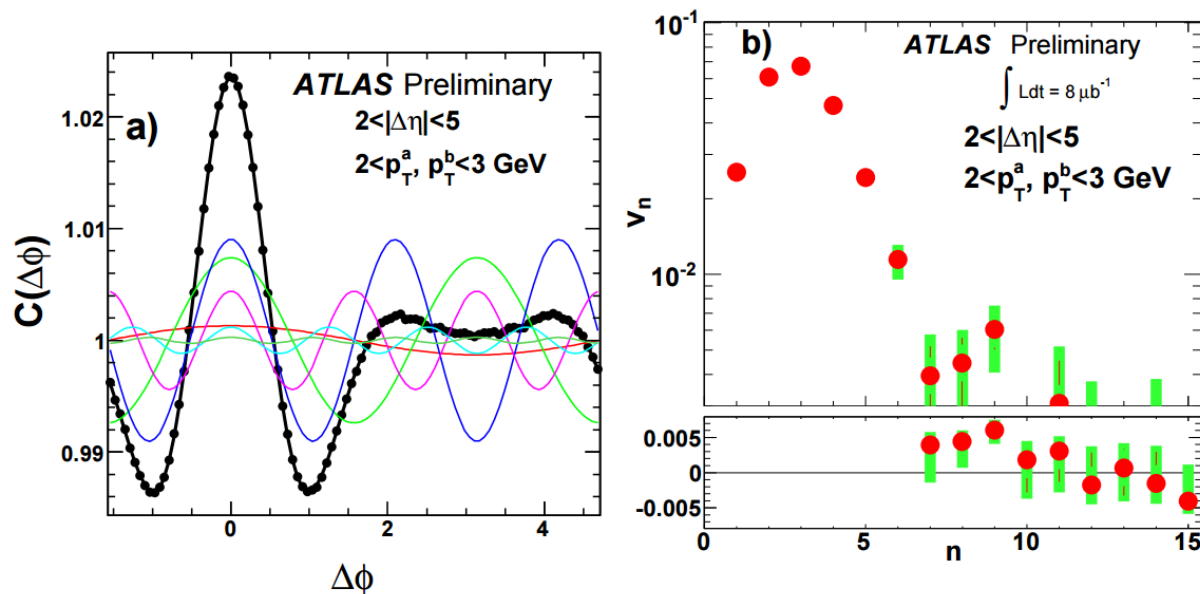


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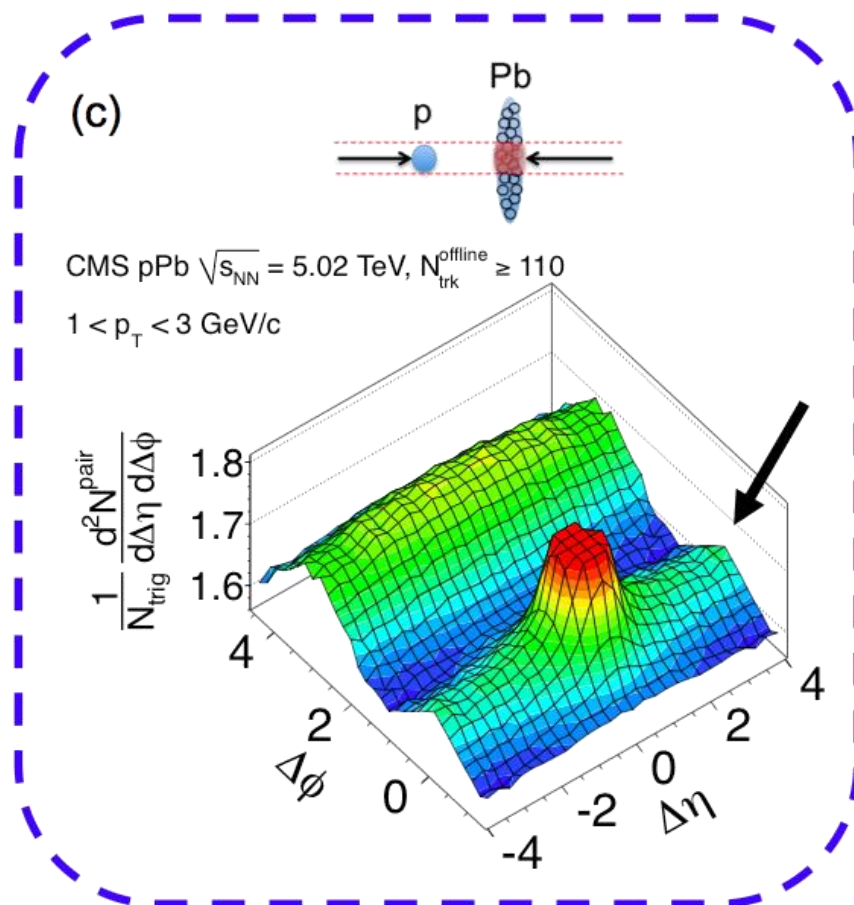
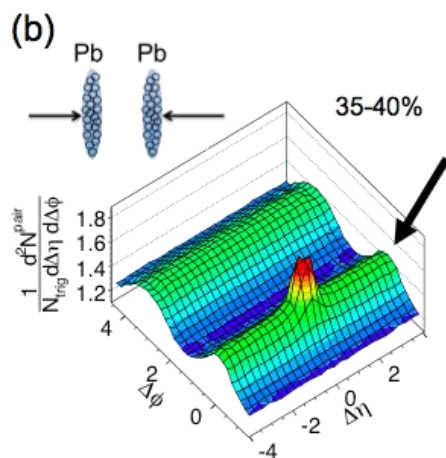
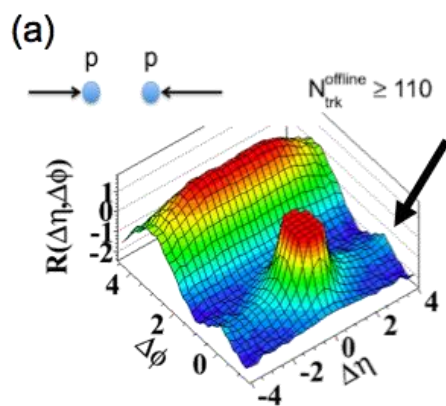


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'THE RIDGE'

Preview of small systems, recent excitement

- Ridge also seen in p-Pb *and* p-p (at high multiplicity? – spoiler)



'THE RIDGE'

More fun: average over 4, 6 or 8 particle correlation to get 'flow'

- Technique to remove short range correlation (i.e. momentum)
- Typical expectation weak coupling: weaker correlations
- Typical expectation hydro/strong coupling: 'constant' correlations

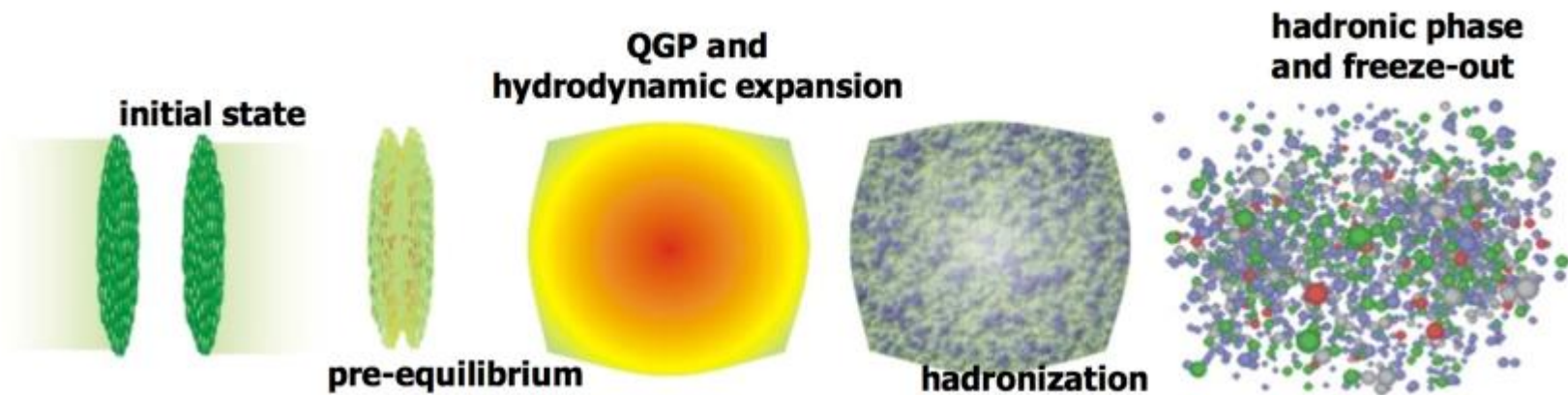
More non-trivial checks:

- Mass-ordering of pions/kaons/protons elliptic flow versus p_t
- Particles produced according to Boltzmann-distribution (more later)

THEORETICAL DESCRIPTION

Standard model of heavy ion collisions

- Will start with hydrodynamics
- Later: initial pre-equilibrium stage



RELATIVISTIC HYDRODYNAMICS

Hydrodynamics is a gradient expansion

- Start with homogeneous thermal state moving at constant v
- Promote temperature and velocity to field, assuming small variations

Evolution

- Equations of motion are conservation equations
- Extra input is equation of state and transport coefficients
- In real life: use 2nd order hydrodynamics (causal)

$$T_{\mu\nu} = e u_\mu u_\nu + p[e] \Delta_{\mu\nu} + \pi_{\mu\nu}, \text{ where,}$$

$$\Delta_{\mu\nu} = g_{\mu\nu} + u_\mu u_\nu \text{ and}$$

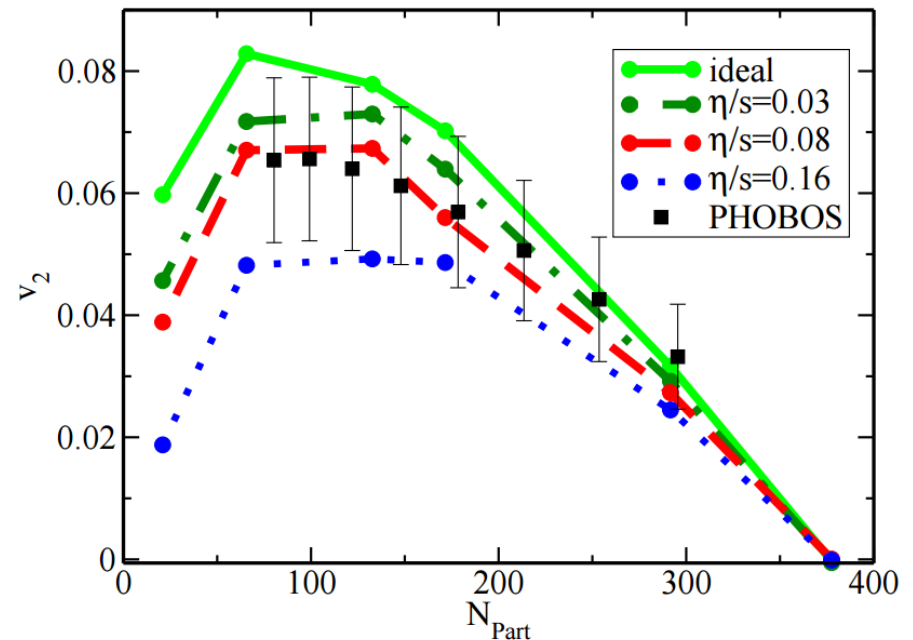
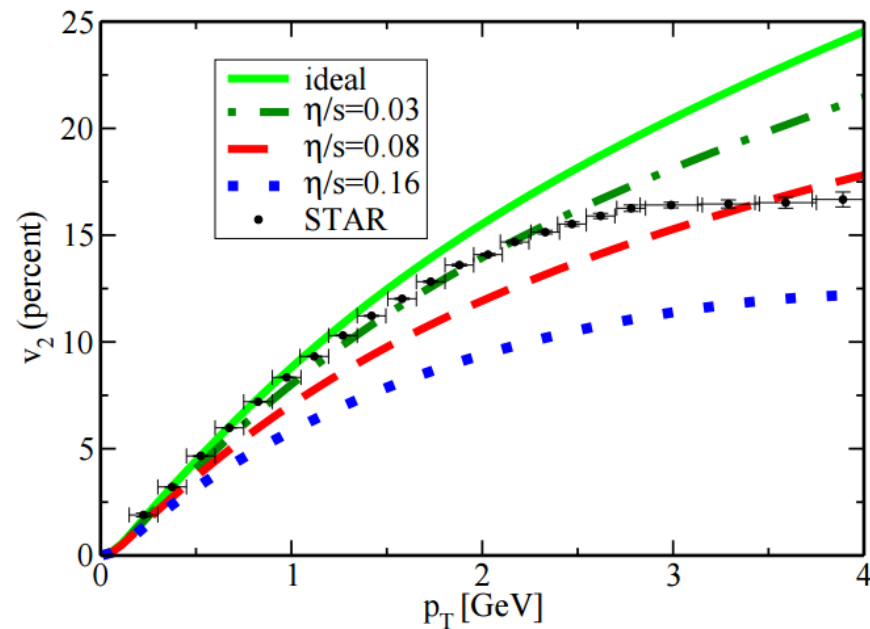
$$\pi_{\mu\nu} = -\eta[e] \sigma_{\mu\nu} - \zeta[e] \Delta_{\mu\nu} (\nabla \cdot u) + \mathcal{O}(\partial^2), \text{ with}$$

$$\sigma_{\mu\nu} = \Delta_{\mu\alpha} \Delta_{\nu\beta} (\nabla^\alpha u^\beta + \nabla^\beta u^\alpha) - \frac{2}{d-1} \Delta_{\mu\nu} \Delta_{\alpha\beta} \nabla^\alpha u^\beta,$$

RELATIVISTIC HYDRODYNAMICS

Hydrodynamic simulations

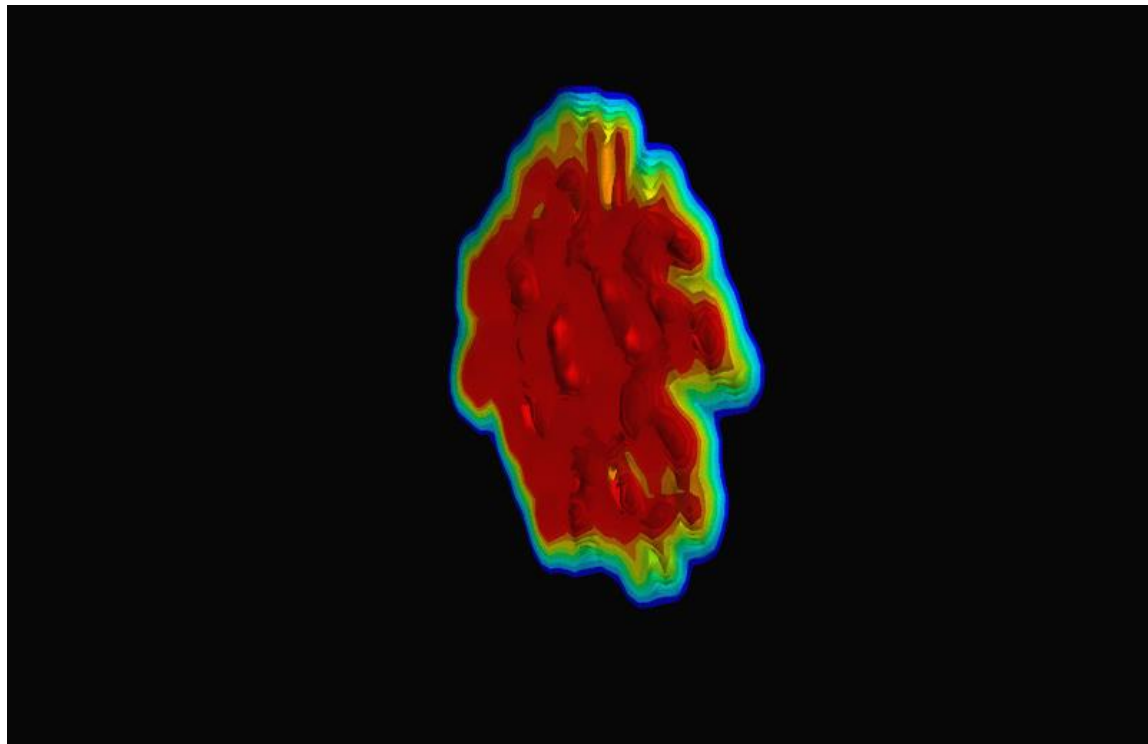
- Need initial conditions: simple Wood-Saxon shape of nucleus
- Has involved a lot of fitting in the past...



HEAVY ION STATE-OF-THE-ART (BJORN SCHENKE)

Start with energy density from Wood-Saxon profile

- Fluctuations may follow from glasma/saturation
- Profile in rapidity largely put in by hand (BI+cut-off)



PARTICLE MULTIPLICITY \approx ENTROPY

Around temperature of 170 MeV QGP cross-over into hadron gas

- After few scatterings, and many resonance decays: free-streaming to detector (freeze-out)
- In local rest-frame particle distribution precisely known (Boltzmann): Cooper-Frye prescription (on constant temperature hypersurface)
- Direct link between entropy and multiplicity:

$$N_{\text{ch}} \approx S / 7.5$$
- Also: entropy approx constant during hydrodynamic evolution
- Subtlety: when anisotropic also momentum distribution anisotropic

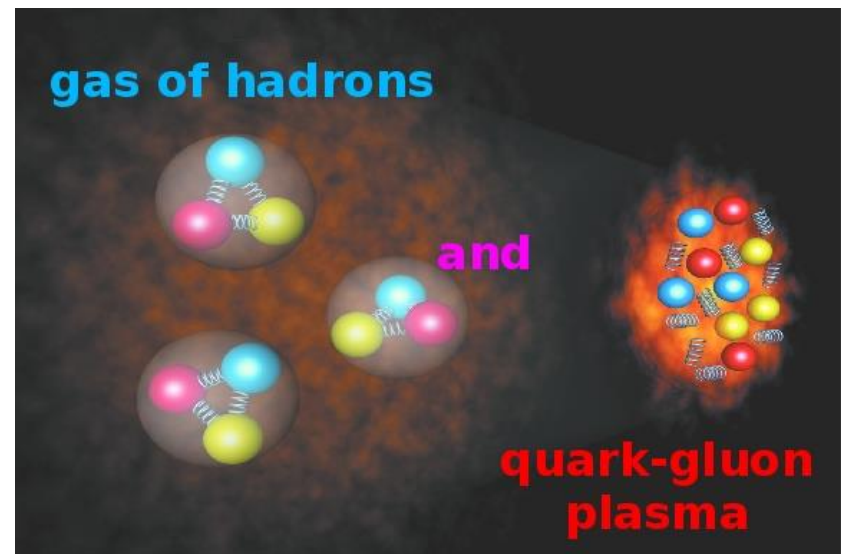
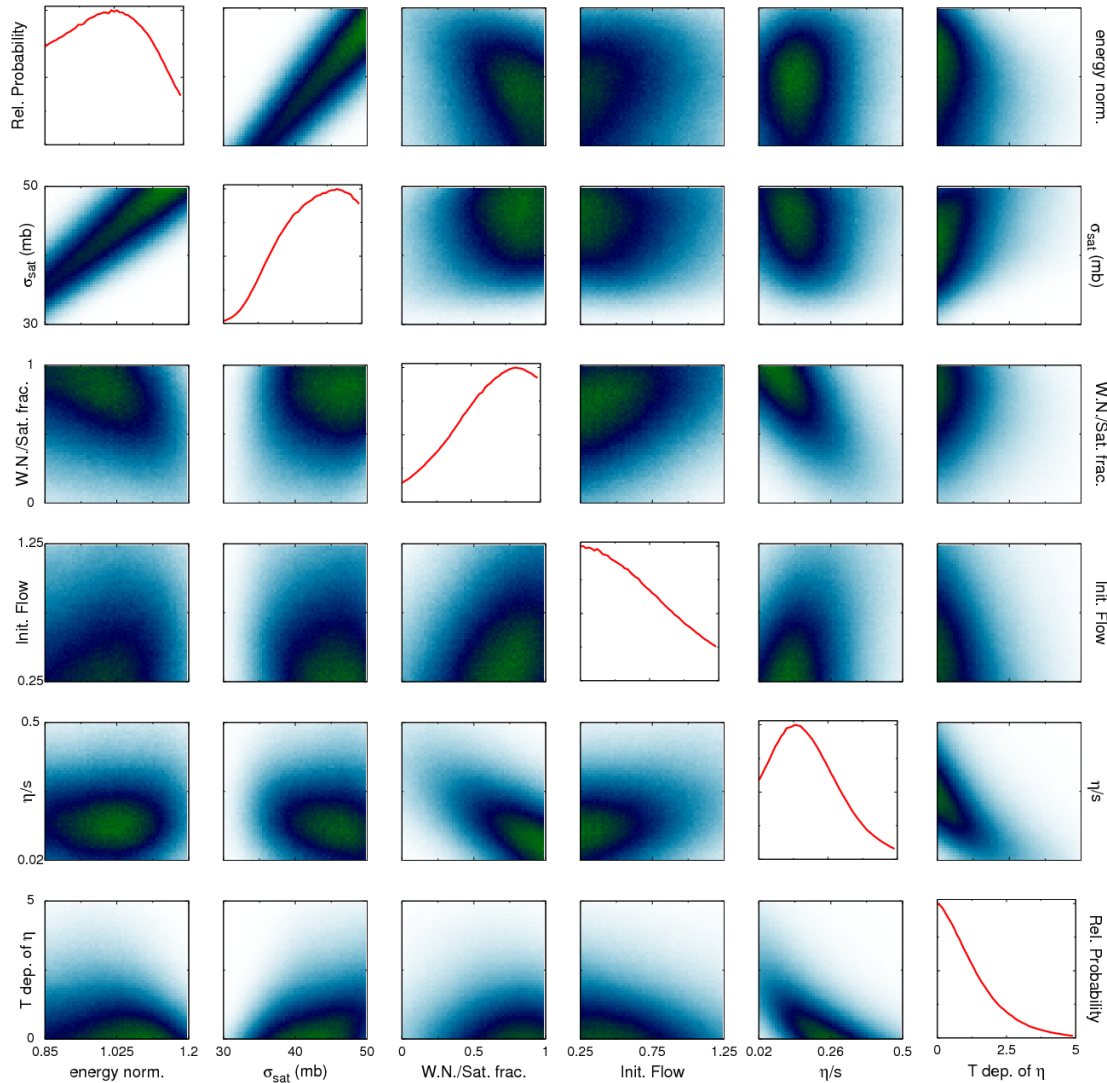


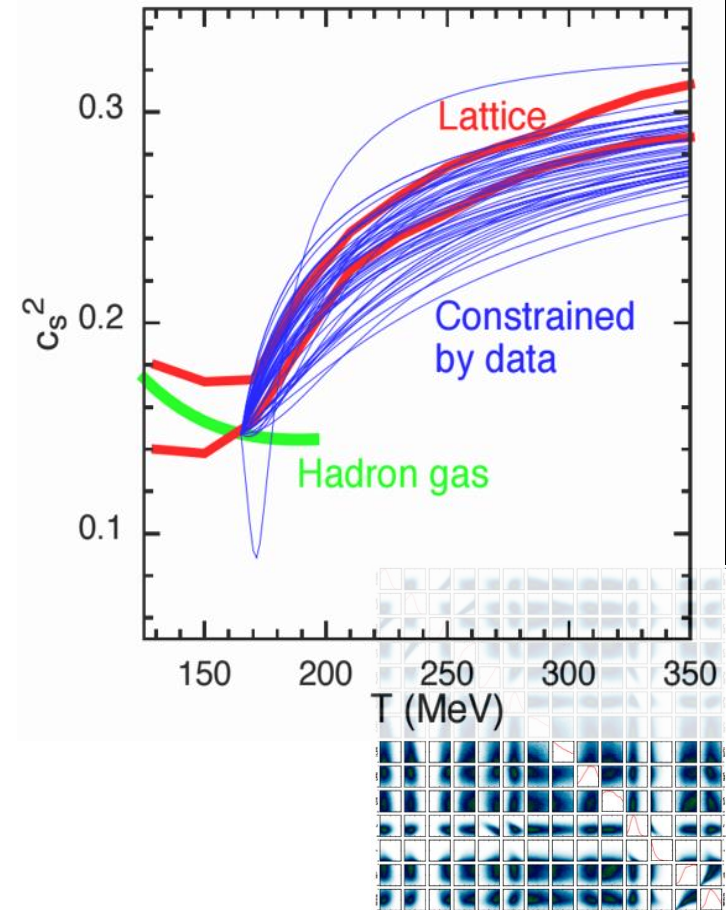
Figure NA61

EMULATOR + PRINCIPLE COMPONENT ANALYSIS (PCA)



Likelihood of i.e. η/s , EOS

- Requires many models * events



SUMMARY FIRST LECTURE

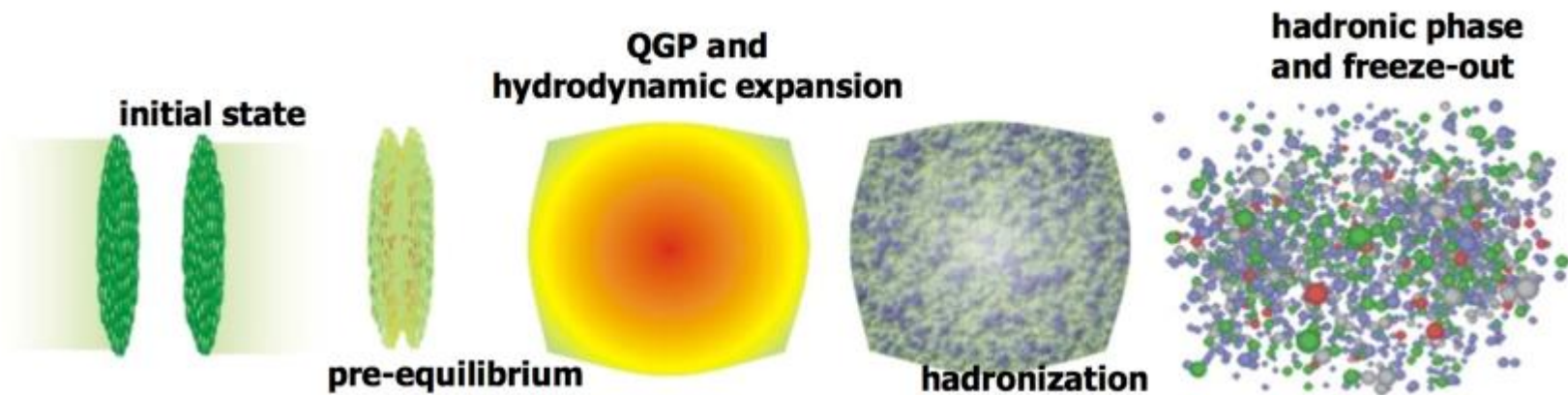
Heavy ion collisions are fun, interesting study of QGP

- Perhaps most striking: ridge
 - Suggests hydrodynamic flow
 - Non-trivial as function of rapidity and centrality
 - Can be used to estimate viscosity etc
- Still several puzzles
 - How to get initial conditions for hydrodynamics (Wednesday)
 - How to constrain physics more, such as viscosity versus temperature
 - Effect QGP on jets (Wednesday)
- Recent puzzles: is there QGP in proton-proton collisions?

THEORETICAL DESCRIPTION

Standard model of heavy ion collisions

- Now: initial pre-equilibrium stage



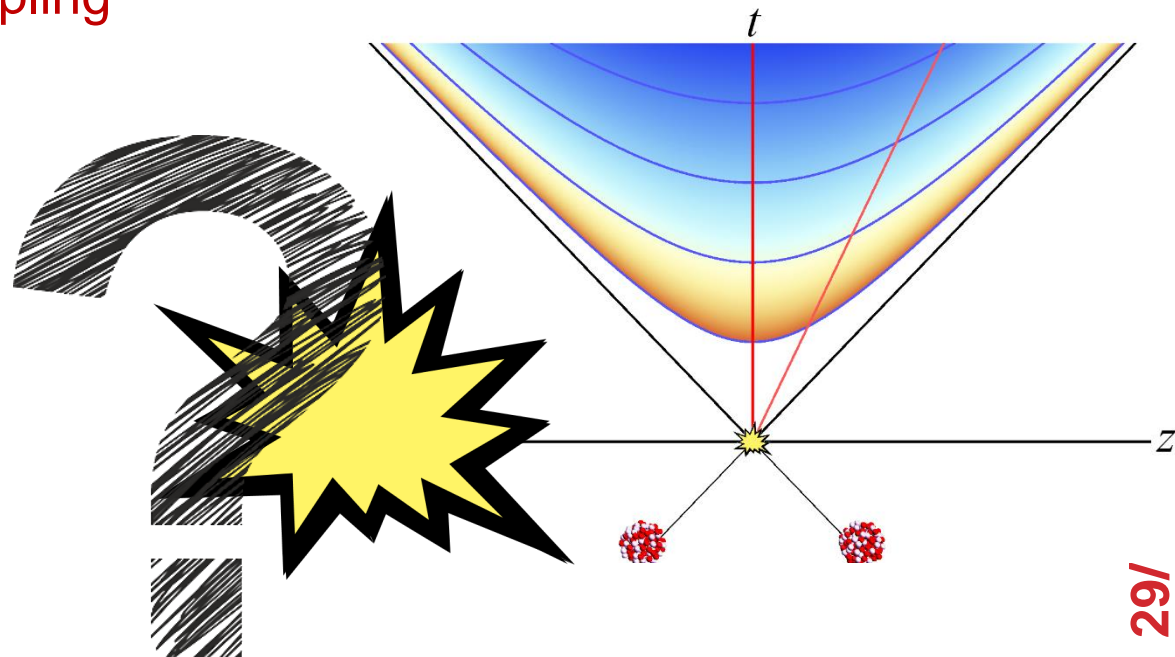
INITIAL STAGE

Hydrodynamics needs initial conditions

- Energy density, velocity, as function of space at initial time
- (Gradient tensors for 2nd order hydro)

QCD is well understood theory??

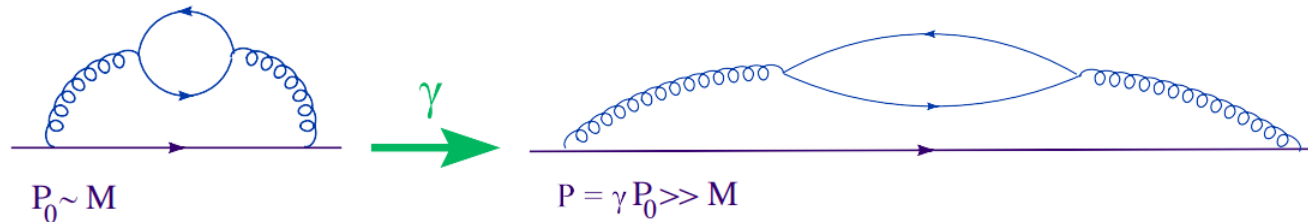
- Perhaps at weak coupling



INITIAL STAGE – PERTURBATIVE QCD

Many more gluons when probed at high energy

- Intuition: at short time scale vacuum fluctuations separated from loops
- Now we can treat (loop) gluons as partons, for purpose of scattering



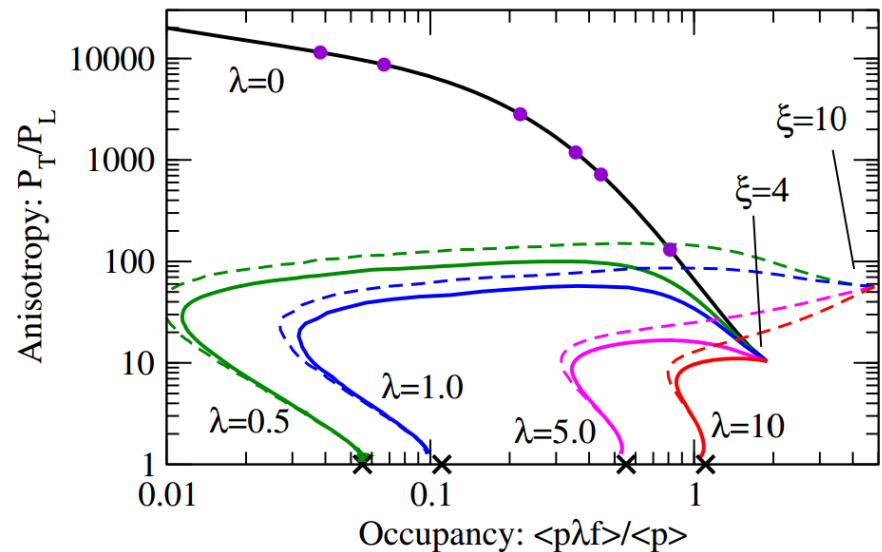
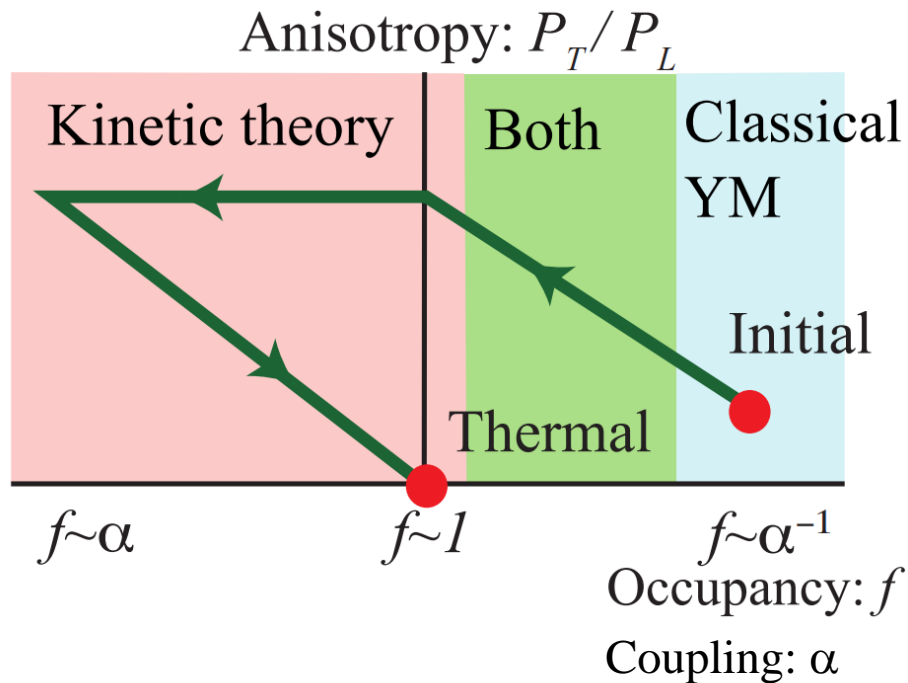
Initial dynamics is governed by classical evolution of Yang-Mills charge

- Much like coherent photons together are described by Maxwell eqn
- System dilutes and at weak coupling becomes kinetic theory

INITIAL STAGE – PERTURBATIVE QCD

Typical process of thermalization:

- Far-from-equilibrium universal scaling (Berges et al)
- Kinetic theory towards thermal equilibrium (time of order 1 fm/c)





INITIAL STAGE – STRING THEORY

A theory of (more than?) everything?



Theory and Particle



Juan Maldacena
Theoretical Astrophysics Professor
Institute for Advanced Studies

STRING THEORY

A theory of (more than?) everything?



String Theory and Particle
Physics
TRT: 02:07:03

An excerpt from
The Search for ToE
interview with:

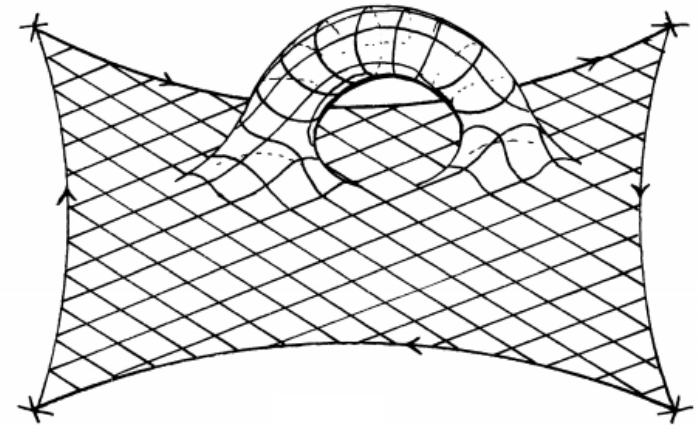
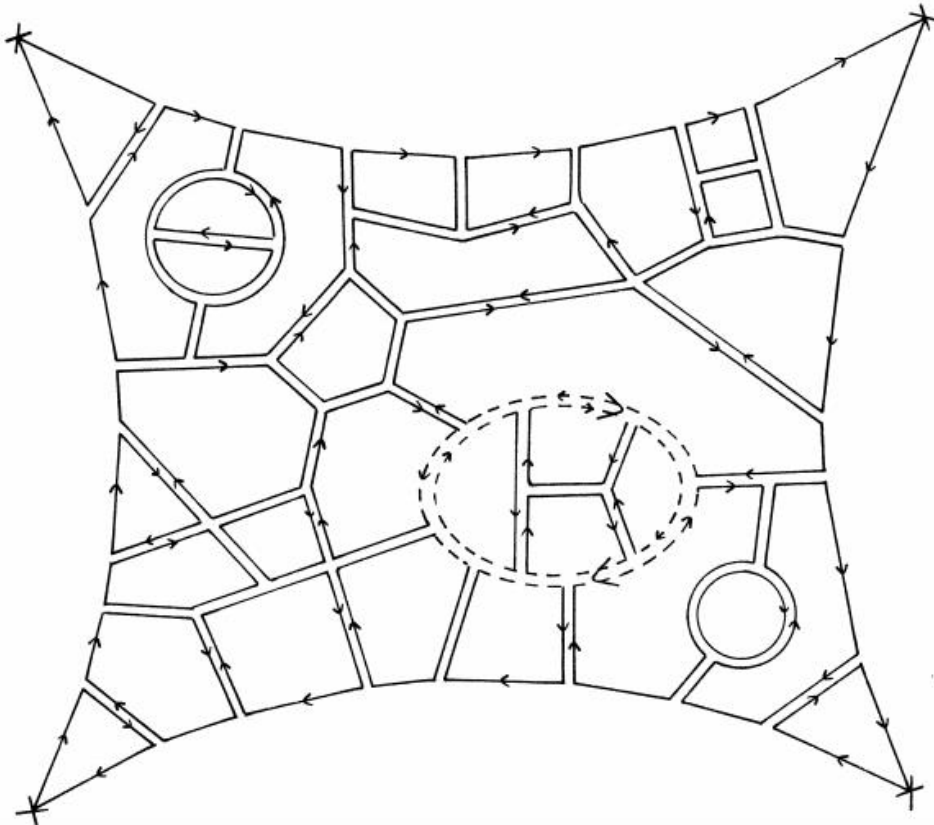
Juan Maldacena
Theoretical Astrophysics Professor
Institute for Advanced Studies

ToE *The Search for the Theory of Everything*

A large, stylized number '3' is centered within a thin white circle. The number is a light gray color. The text 'ToE' is positioned to the left of the circle, and 'The Search for the Theory of Everything' is written in a smaller font below the circle.

LARGE N GAUGE THEORIES

At strong coupling we can get GR



Planar limit:

$$\lambda = g^2 N \text{ fixed}$$

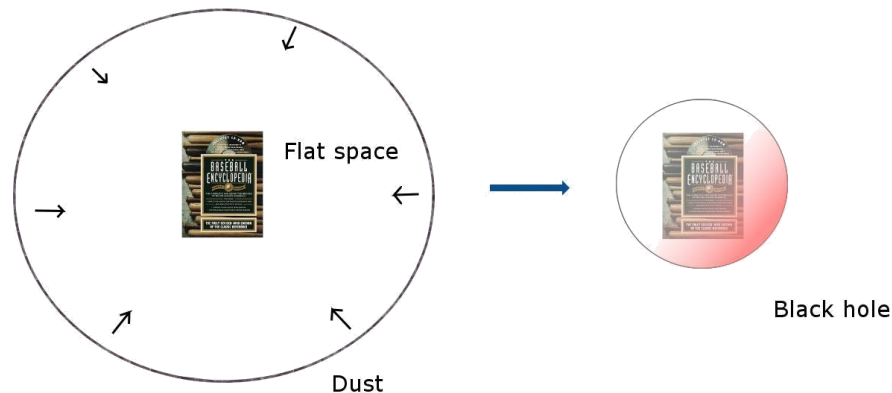
$$N \rightarrow \infty$$

THE WORLD AS A HOLOGRAM

A very curious fact: black hole entropy proportional to area!

$$S_{BH} = A/4$$

Thought experiment: collapse entropy to black hole



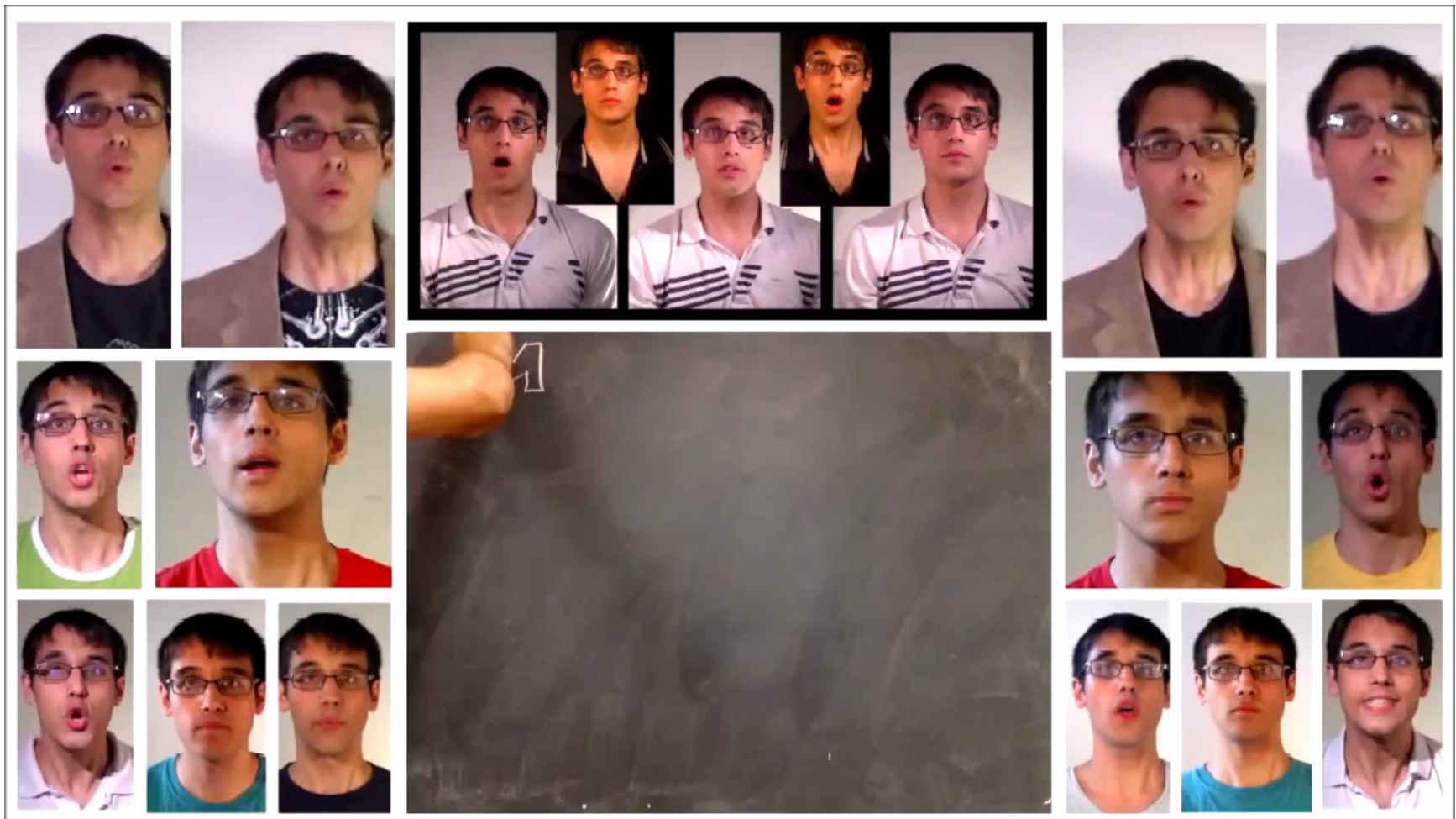
Intuition: gravity provides UV cut-off in space due to BH formation

Jacob Bekenstein, Black holes and entropy (1973)

Stephen Hawking, Particle creation by black holes (1975)

Gerard 't Hooft, Black hole quantization and a connection to string theory (1990)

ADS/CFT



QUICK GUIDE TO HOLOGRAPHY

Exact equivalence between string theory and quantum field theory

$$\mathcal{Z}_{bulk} [\phi(\vec{x}, z)|_{z=0} = \phi_0(\vec{x})] = \langle e^{\int d^4x \phi_0(\vec{x}) \mathcal{O}(\vec{x})} \rangle_{\text{Field Theory}}$$

$$\langle \mathcal{O} \rangle = -i \frac{\delta \mathcal{Z}_{bulk}[\phi(0)]}{\delta \phi(0)} \stackrel{N \rightarrow \infty}{=} \frac{\delta S[\phi(0)]}{\delta \phi(0)}$$

Holography synonyms:
AdS/CFT, gauge/gravity duality,
gauge/string duality

Dictionary:

- Original: type IIB string theory $AdS_5 \times S_5 \sim \mathcal{N} = 4 \text{SU}(N_c) \text{ SYM}$ on \mathbb{R}^4
- Near-boundary metric of AdS \sim stress tensor
- Black hole \sim thermal state
- Fundamental string \sim Quark-antiquark pair

Most famous result: $\eta/s = \frac{1}{4\pi}$ (from black hole horizon)

Also: insights information paradox, fast thermalization, ... (14000+)

ARE WE PERHAPS NOT CHEATING WITH $\mathcal{N}=4$ SYM?

SU(N): $3 \approx \infty$?

- Good for thermal

Quarks?

- Replaced by (dominant) gluons

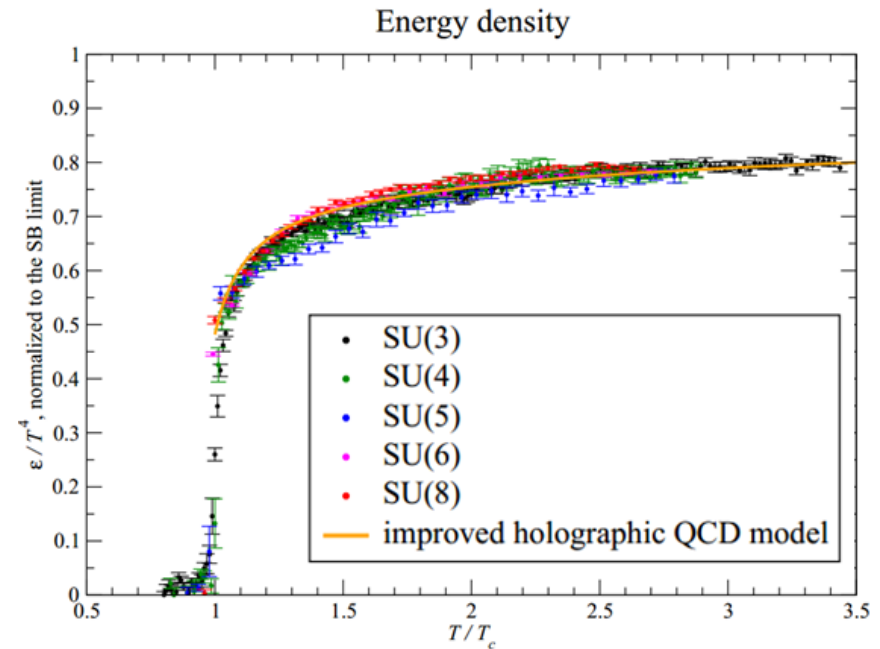
Infinite coupling strength?

- But coupling runs only logarithmically...

Theories not the same:

$$\mathcal{E} = \frac{3N_c^2 \pi^2}{8} T^4 \approx 33.3 T^4 (\mathcal{N} = 4) \quad \mathcal{E} \approx 11 T^4 (\text{QCD})$$

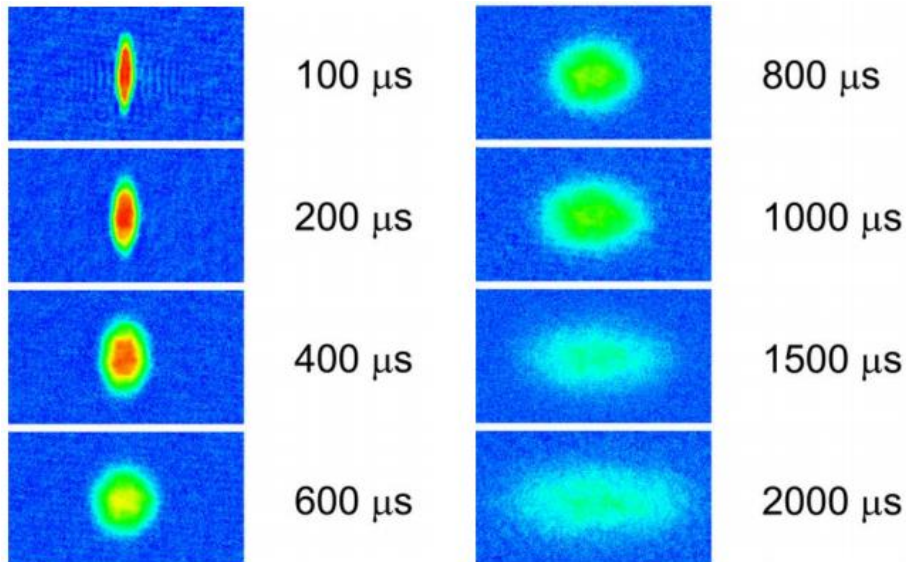
So maybe not too bad; and with room for improvement ☺



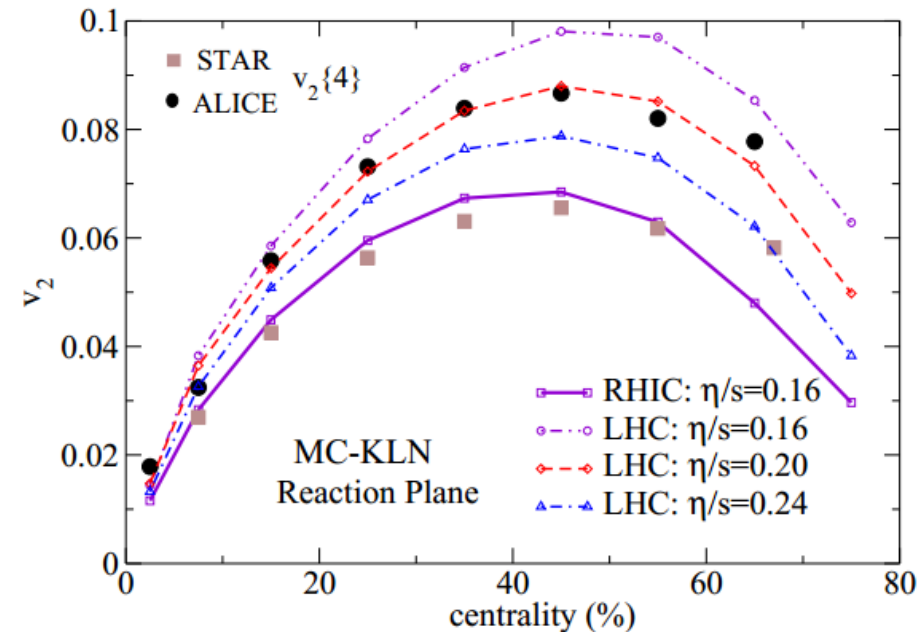
THE MOST PERFECT LIQUID?

Famous viscosity: $\frac{\eta}{s} = \frac{1}{4\pi} \approx 0.08$

Fermions at unitarity

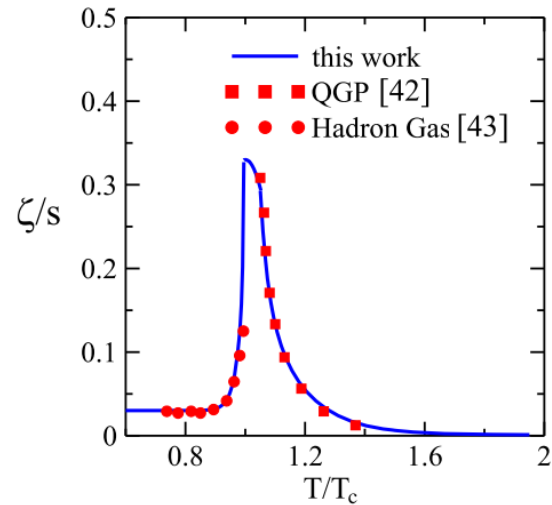
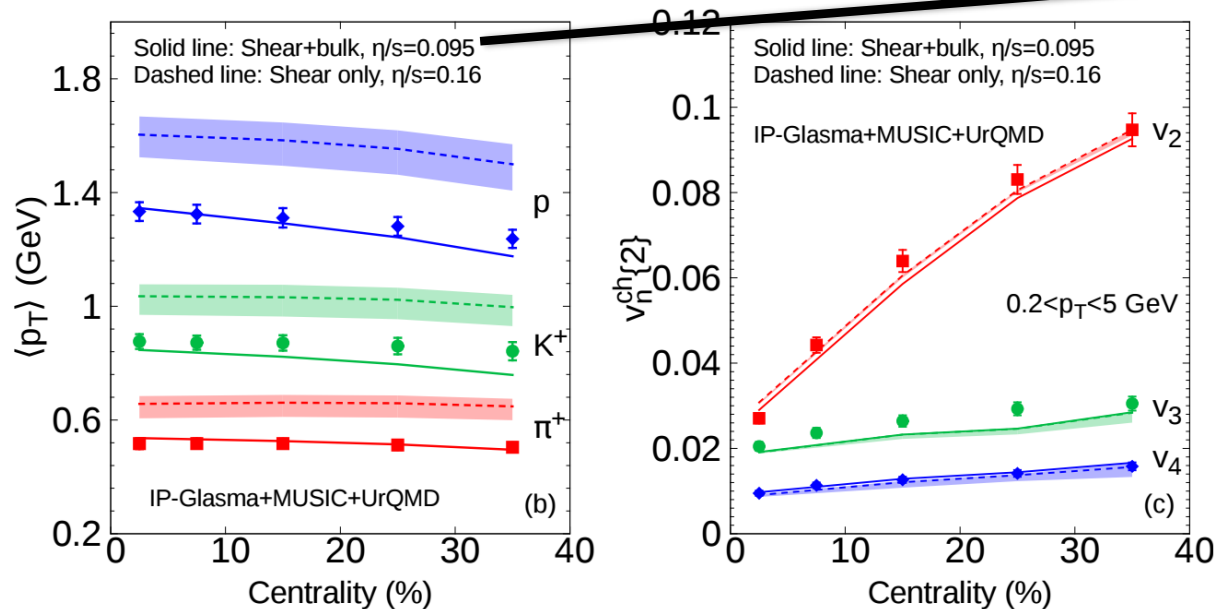


Quark-gluon plasma



ADS/CFT VISCOSITY REVISITED?

New experimental estimate for shear viscosity QGP: $\eta/s=0.095$



Many caveats applying N=4 SYM to QCD:

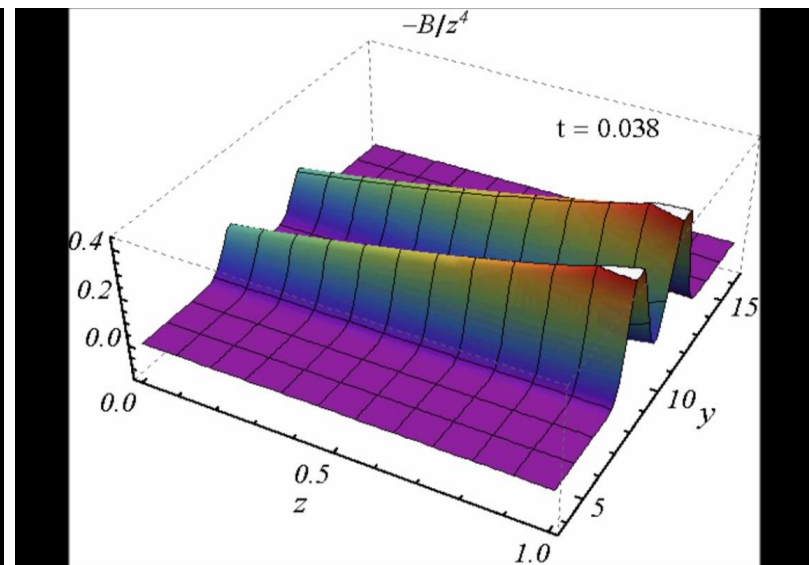
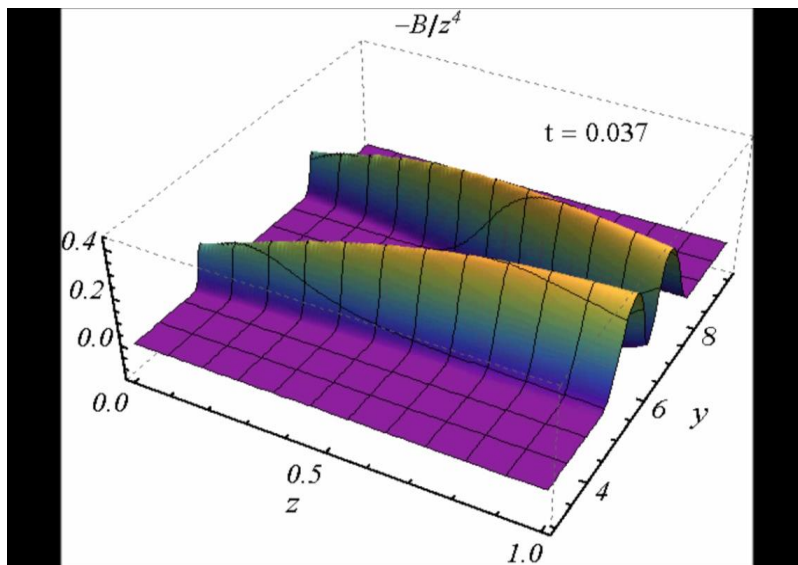
- Infinite coupling limit (QCD = intermediate coupling?)
- SYM vs YM, no confinement, what to collide?, jet production?

Idea: get strong coupling benchmark/intuition + improve model

STRONG COUPLING – INITIAL STAGE

Colliding lump of energy = gravitational shock waves!

- In one extra dimension, solve Einstein equations numerically
- Extract field theory stress-energy tensor
- Get resulting hydrodynamic fluid, both time and profile ☺



A DYNAMICAL CROSS-OVER

Low energy:

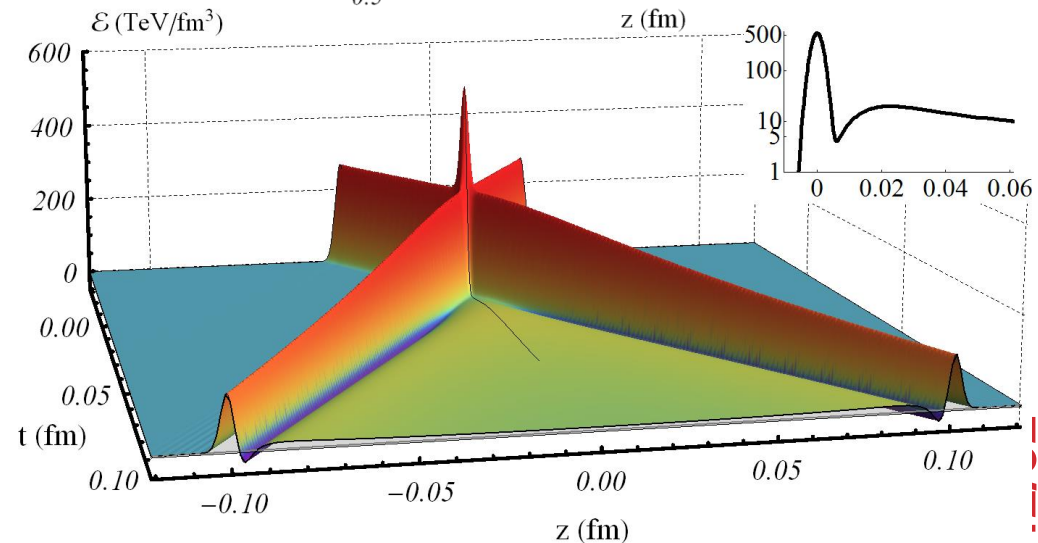
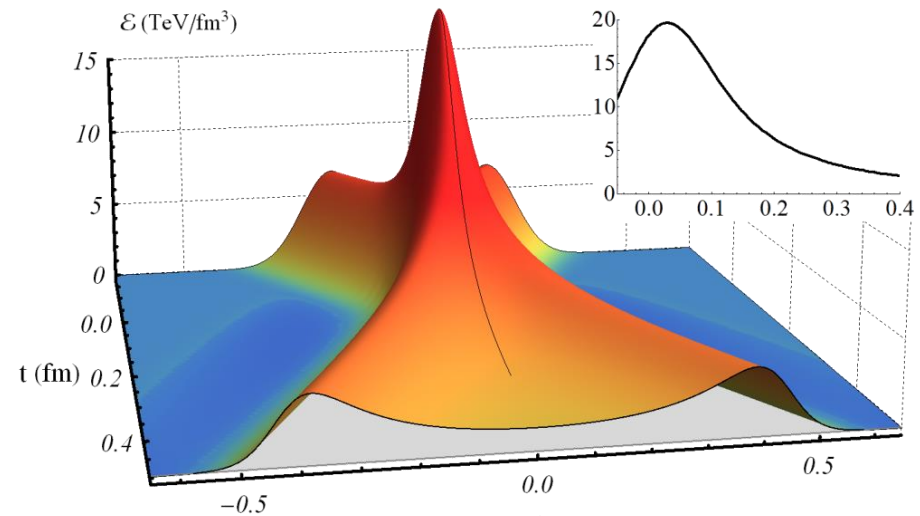
- Stopping, piling up of energy
- Expansion by hydro
- Compressed Landau model

RHIC energy

- Landau model

High energy:

- no stopping
- plasma forms more slowly
- negative energy





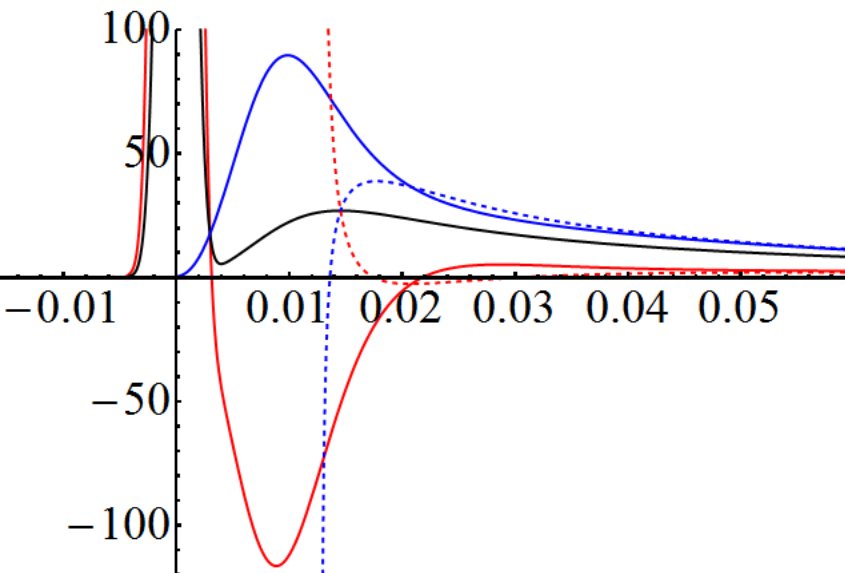
THERMALISATION/PRESSURES

Pressures, energy starts at zero, grows (unique to holography?)

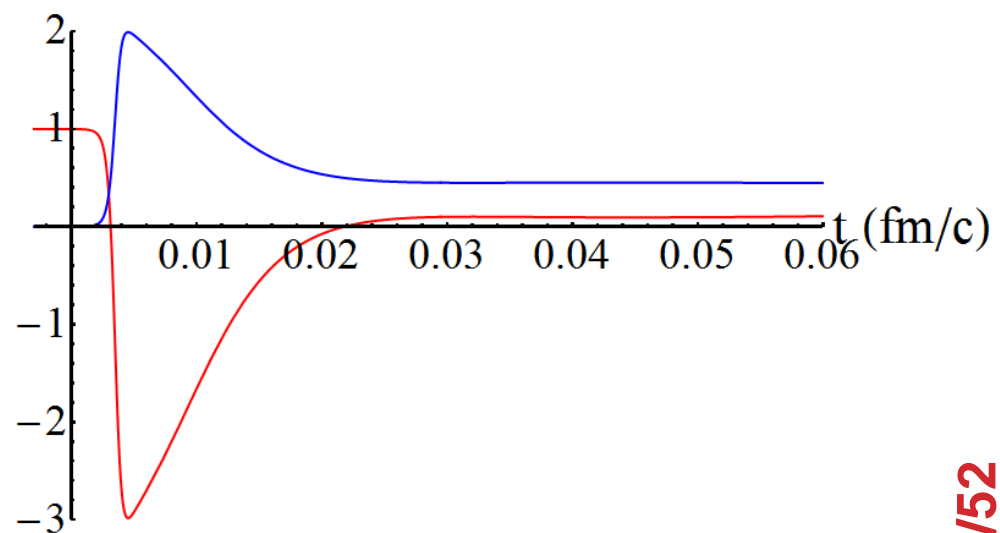
Thermalises very fast (hydro applies in perhaps 0.02 fm/c)

- Thermalisation = relaxation non-hydro modes
- Gradients + viscous corrections are big

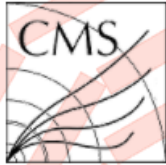
$e/3$ (black), P_L (red), P_T (blue) at $z = 0$ fm



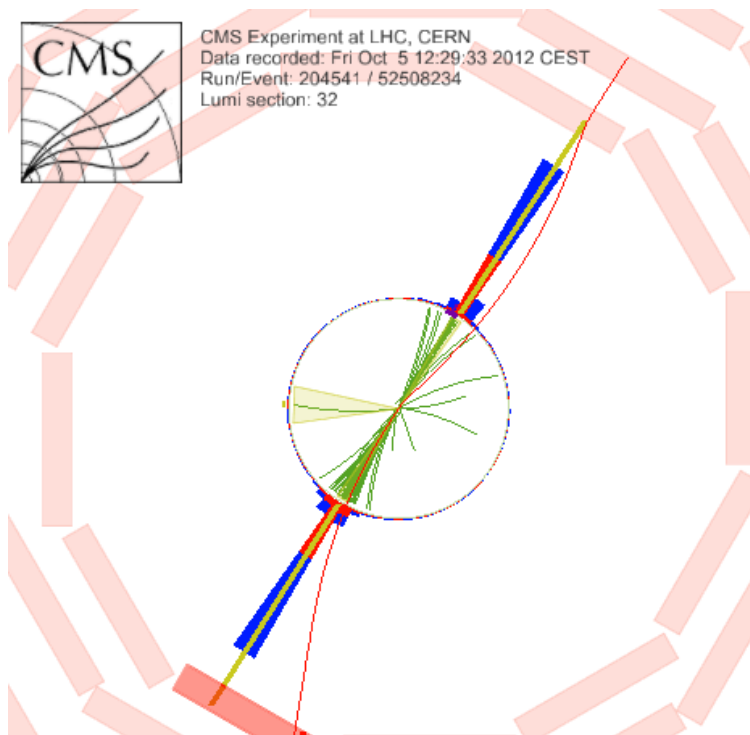
P_L/e (red) and P_T/e (blue), $z = 0$ fm



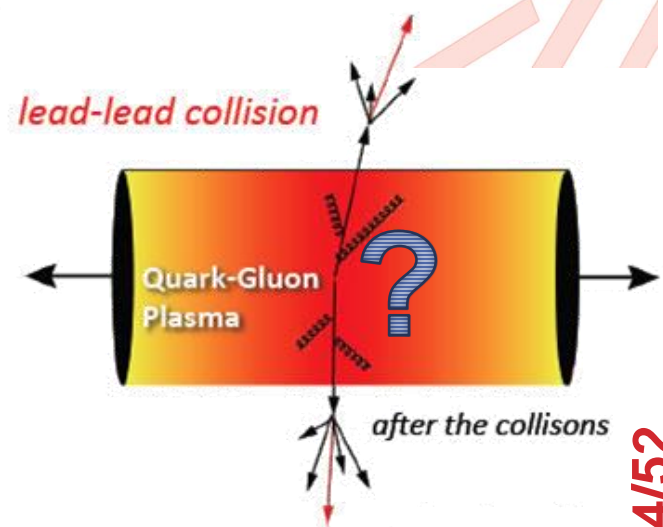
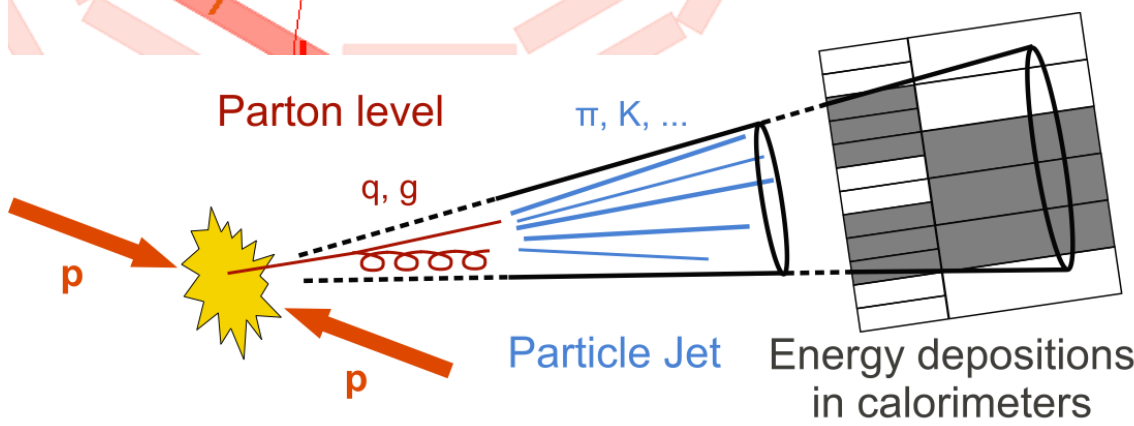
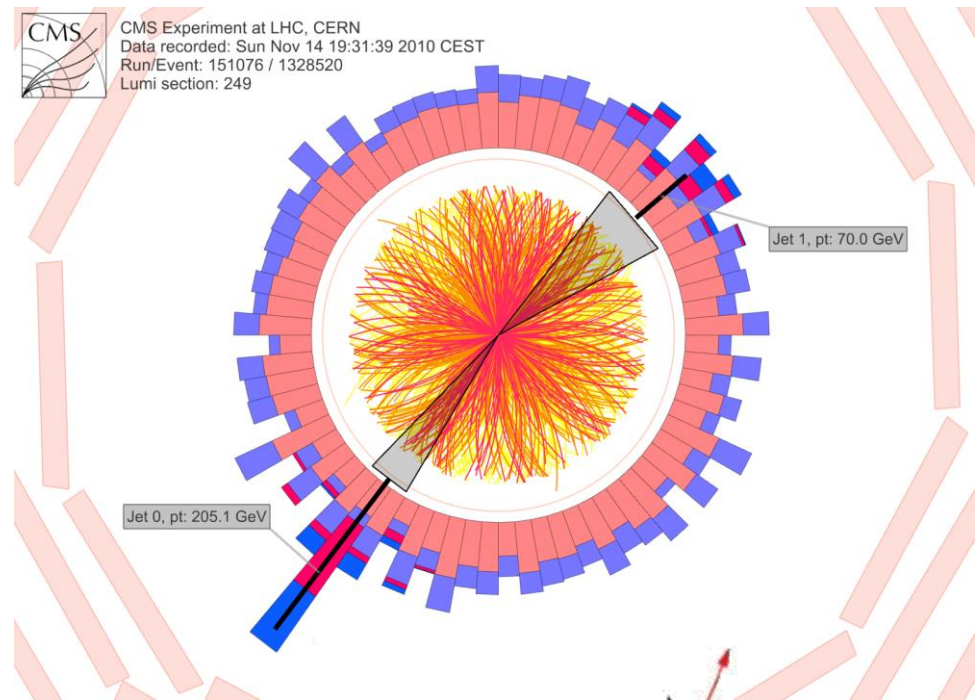
JETS IN QGP



CMS Experiment at LHC, CERN
 Data recorded: Fri Oct 5 12:29:33 2012 CEST
 Run/Event: 204541 / 52508234
 Lumi section: 32



CMS Experiment at LHC, CERN
 Data recorded: Sun Nov 14 19:31:39 2010 CEST
 Run/Event: 151076 / 1328520
 Lumi section: 249

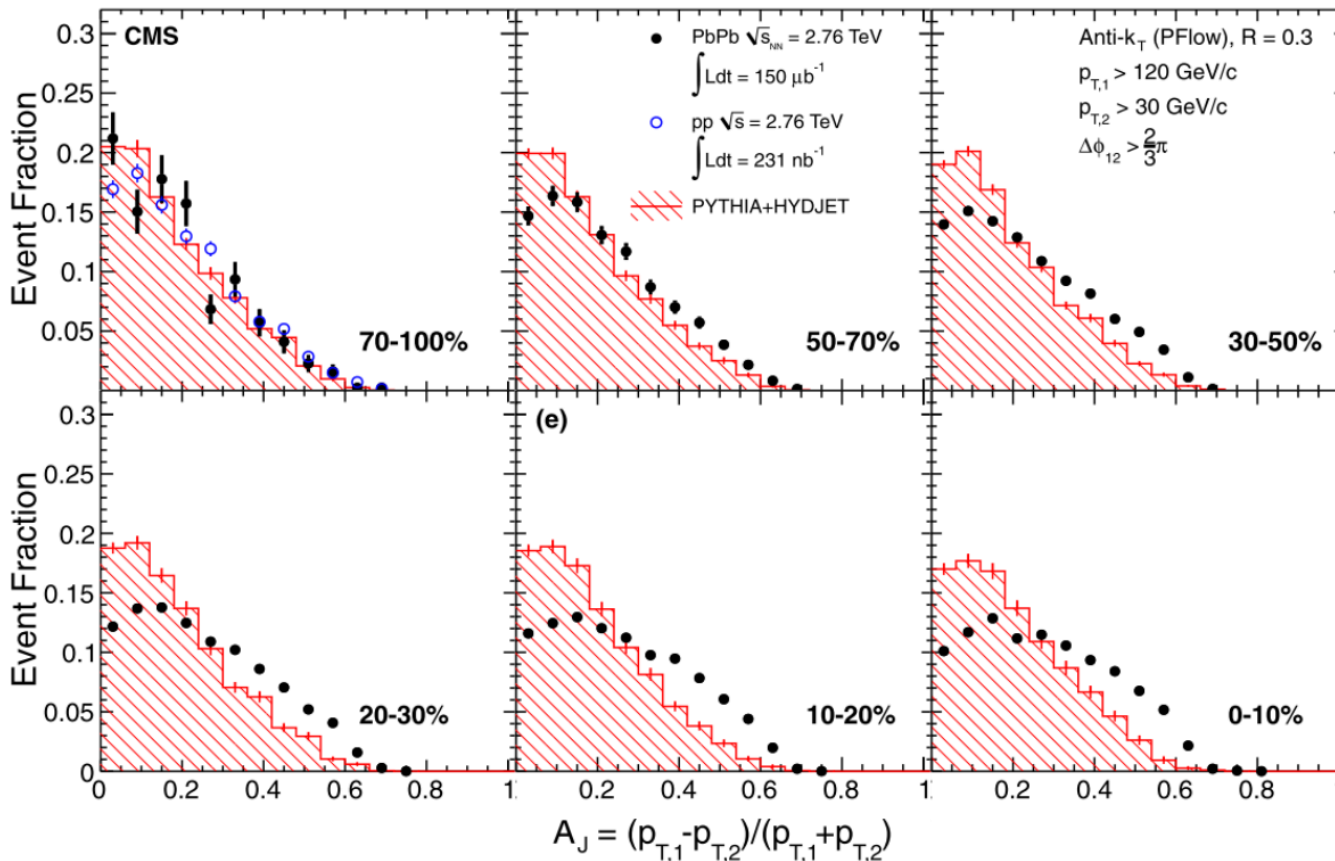


JETS – DIJET ASYMMETRY

QGP affects fast moving quarks/gluons

- One jet loses more energy due to QGP
→ Stronger asymmetry in jet energies
- Subtlety: compare with HYDJET/PYTHIA simulations

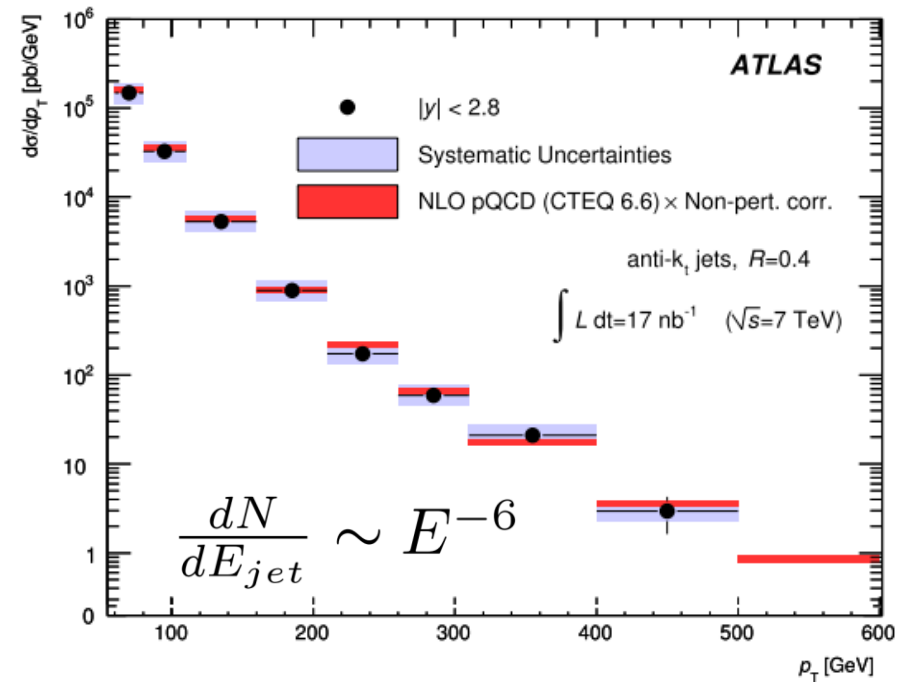
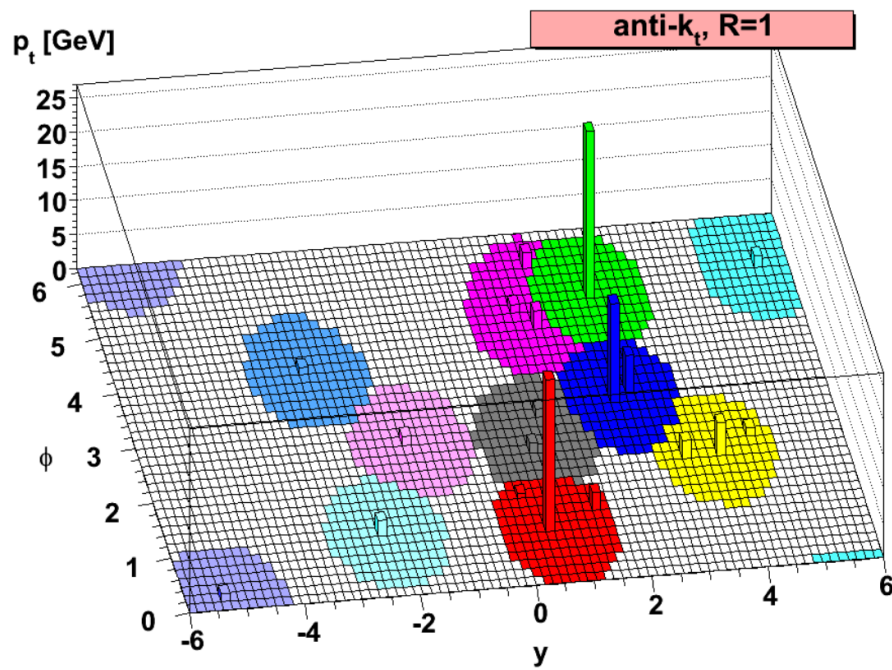
$$A_J = \frac{p_{T,1} - p_{T,2}}{p_{T,1} + p_{T,2}}$$



HOW TO DEFINE A JET?

Relatively recent consensus: anti- k_T

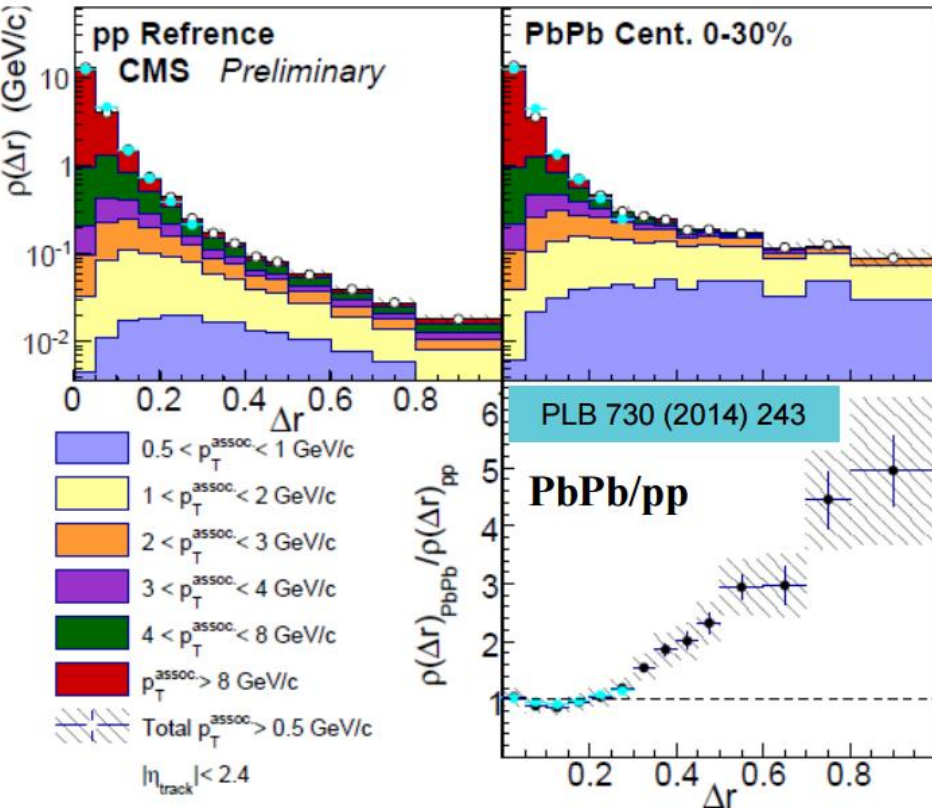
- Cluster around hard cores: $d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2}$, $d_{iB} = \frac{1}{p_{ti}^2}$



Leading

A_J Inclusive
pp 5.3 pb⁻¹ (2.76 TeV)

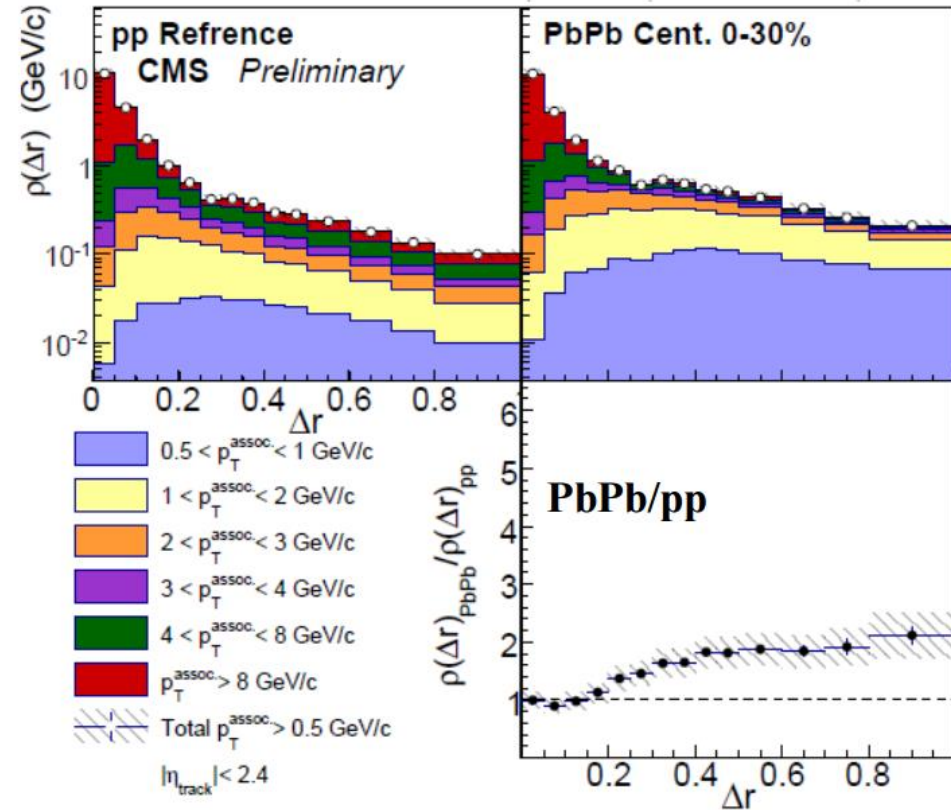
Leading Jet Shape
PbPb 166 μb⁻¹ (2.76 TeV)



Subleading

A_J Inclusive
pp 5.3 pb⁻¹ (2.76 TeV)

SubLeading Jet Shape
PbPb 166 μb⁻¹ (2.76 TeV)



● New measurement of jet shapes up to large radial distances

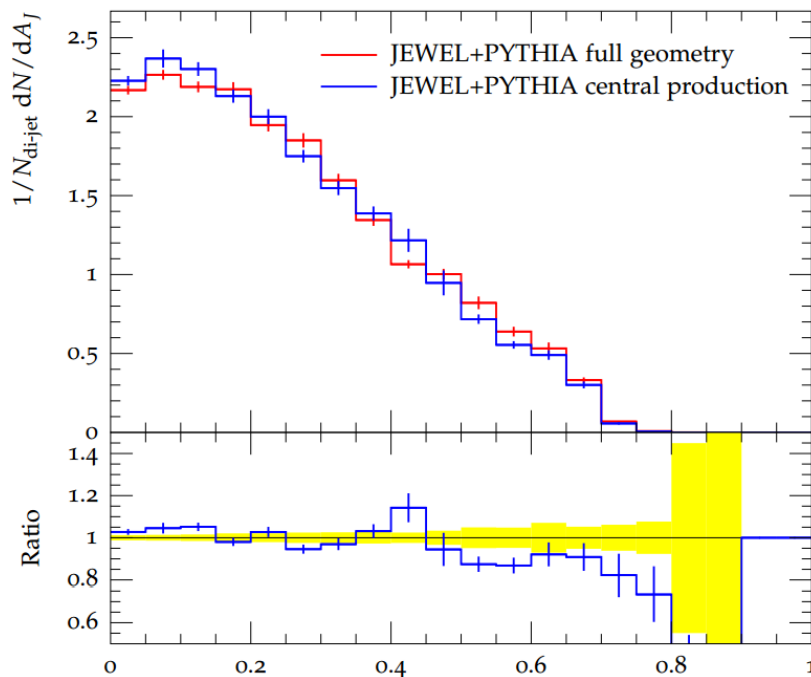
$$\rho(r) = \frac{1}{\delta r} \frac{1}{N_{\text{jets}}} \sum_{\text{jets}} \frac{\sum_{\text{tracks} \in (r_a, r_b)} p_T^{\text{track}}}{p_T^{\text{jet}}}$$

RECENT DEVELOPMENT: JET SHAPES

Look at distribution of particles/energy within a jet

- Using perturbative QCD, i.e. JEWEL + PYTHIA
- Compare path length dependence versus jet shape dependence

Di-jet asymmetry distribution



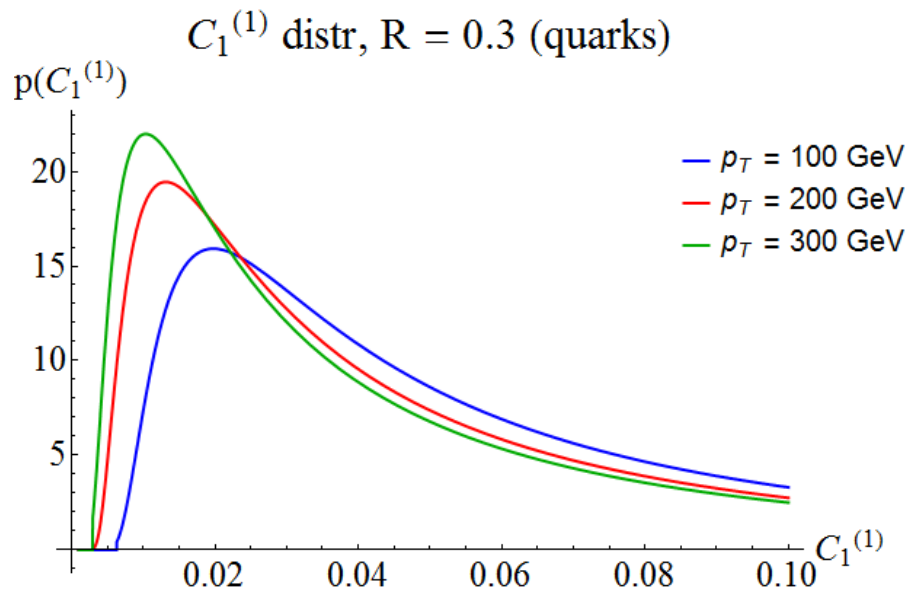
- Central production, i.e. artificially turned off path-length dependence
- `Normal' binary collisions distribution over transverse plane
- Very little difference! I.e. most of energy loss asymmetry is caused by different jet shape, not by path length difference

JET SHAPES AT STRONG COUPLING

Jets in thermal plasma correspond to strings in black hole in AdS

Would like to mimic distribution of real QCD jets

- Motivation: how is distribution affected by QGP?
- Take from pQCD (compares well with PYTHIA)



$$C_1^{(\alpha)} \equiv \sum_{i,j} z_i z_j \left(\frac{|\theta_{ij}|}{R} \right)^\alpha$$

z_i : fraction of jet energy

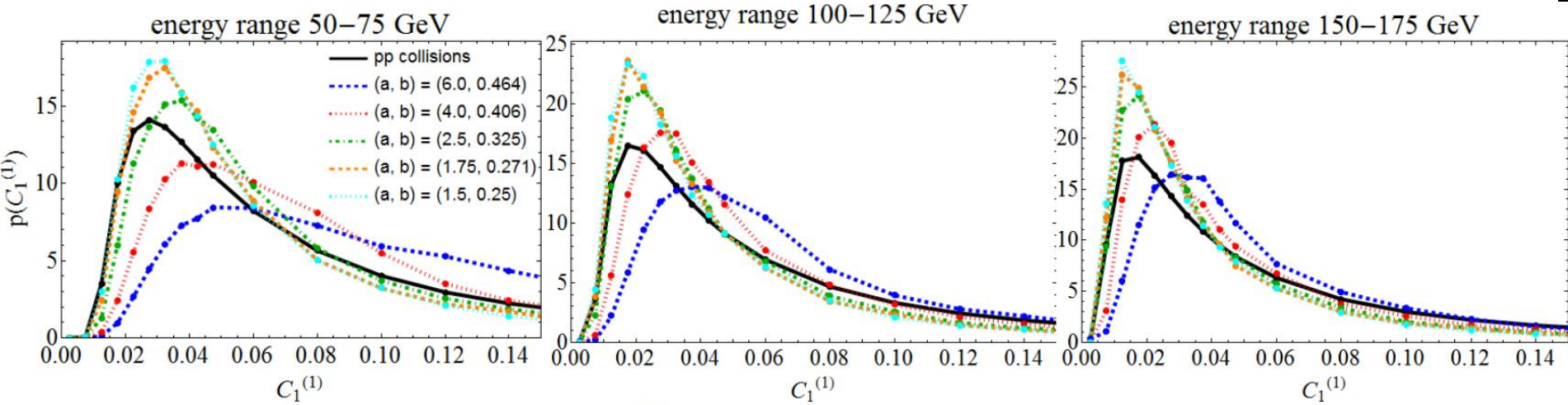
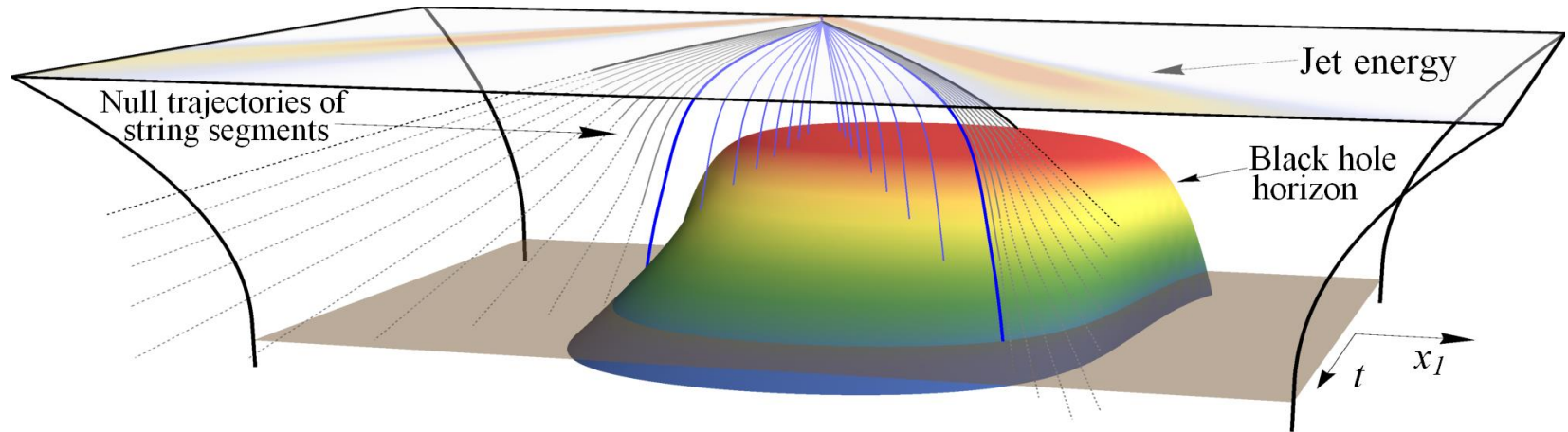
θ_{ij} : angle between particle i and j

R : jet radius parameter

Link opening angle $C_1^{(1)}$ to AdS angle: $C_1^{(1)} = a \sigma_0$

FIRST EFFECT: JETS WIDEN

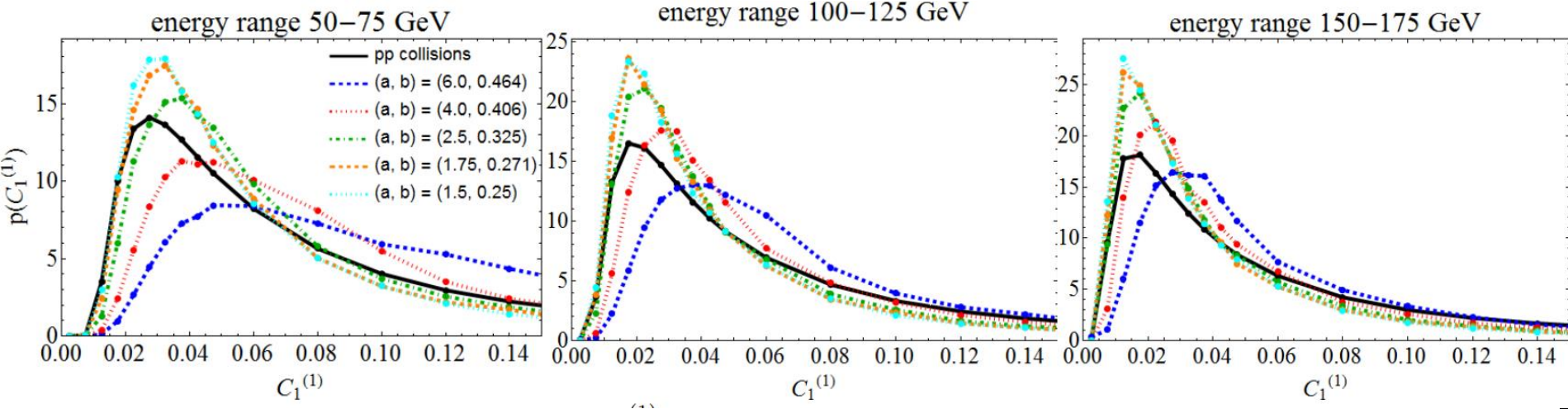
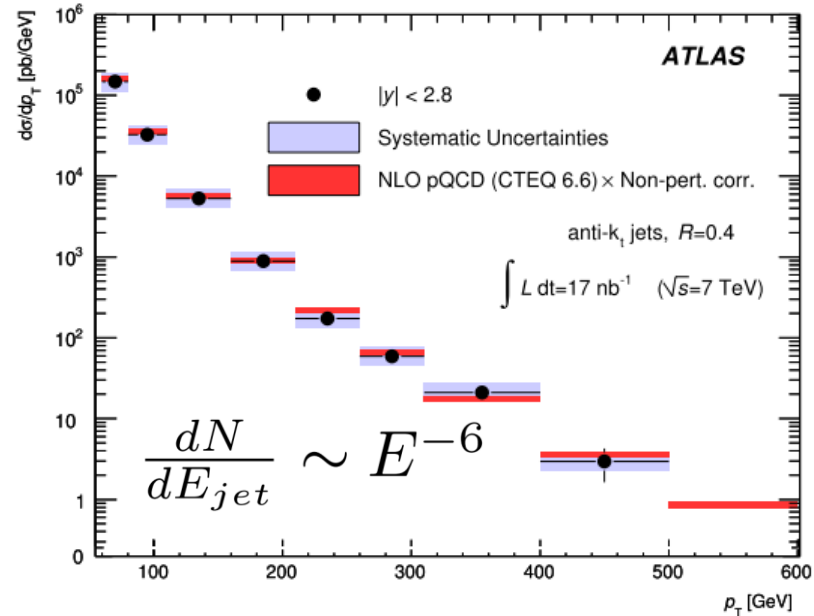
Change of probability distributions of jet opening angle



Has not been measured ☺ (could/should be possible)

SECOND EFFECT: NARROWER JETS

- Energy distribution falls steeply ($\sim E^{-6}$)
- Wide jets lose (much) more energy
- \rightarrow selection bias on narrow jets



DISCUSSION

Heavy ion physics is a lot of fun, full of surprises

- Plenty of pieces of the puzzle of QCD collisions, i.e. centrality dependence, p_t dependence, geometry (p-Pb, d-Au, He3), even pp collisions (!), jet energy loss, jet shape evolution, event-by-event distributions
- Robust 'standard model of heavy ion collisions', but many gaps, i.e. initial stage, transport coefficients (as function of T), hadronic freeze-out, medium effects to jets

Physics allows us to improve our understanding

- Quantitative tests of QCD framework, such as color glass
- Close to comparison with lattice QCD, such as viscosity or EOS
- May be one of cleanest ways to test AdS/CFT, at least at qualitative level
- Can have implications for other non-perturbative physics, i.e. unitary fermi gasses, high temperature superconductors, neutron stars ...
- Insights into quantum gravity (??)