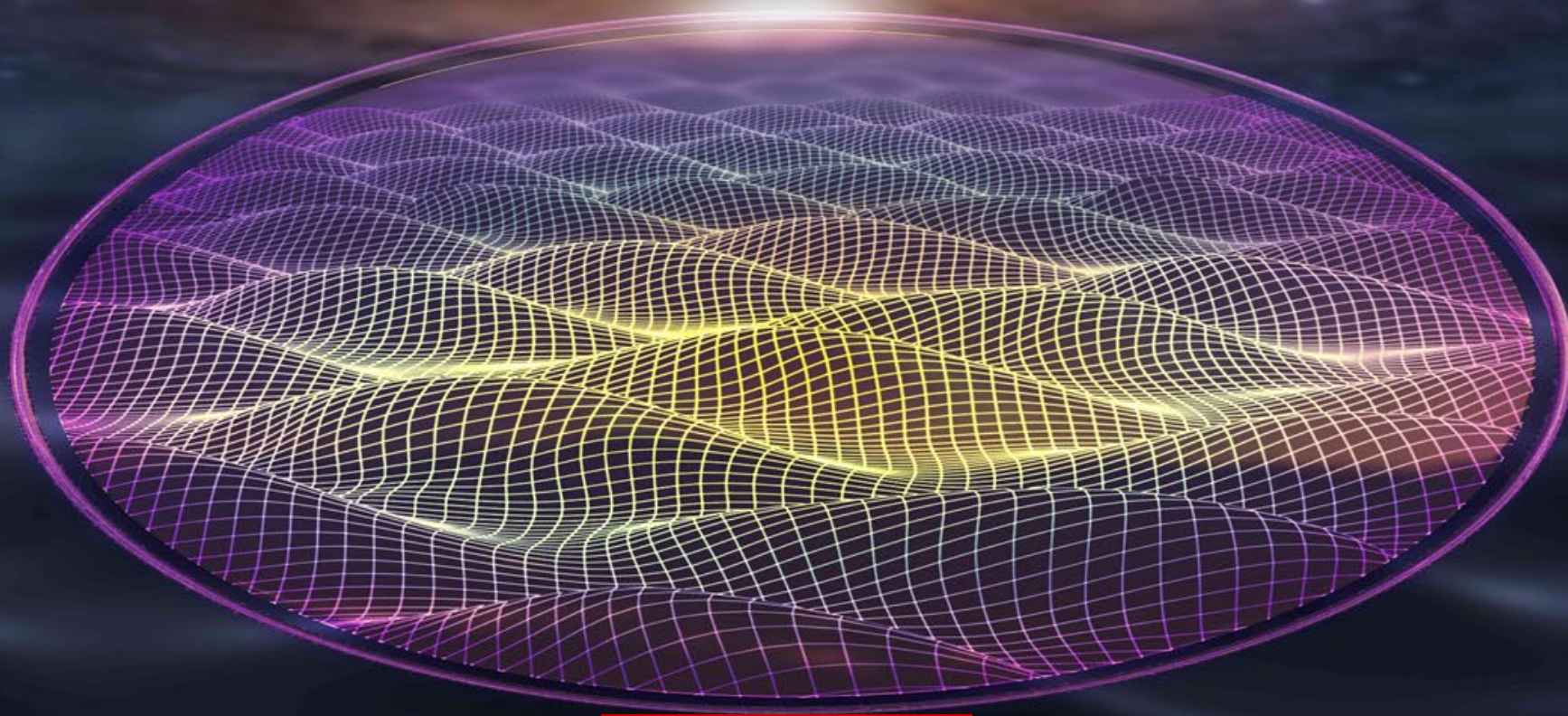


Quantum sensing and dark matter searches

Alex Sushkov



BOSTON
UNIVERSITY



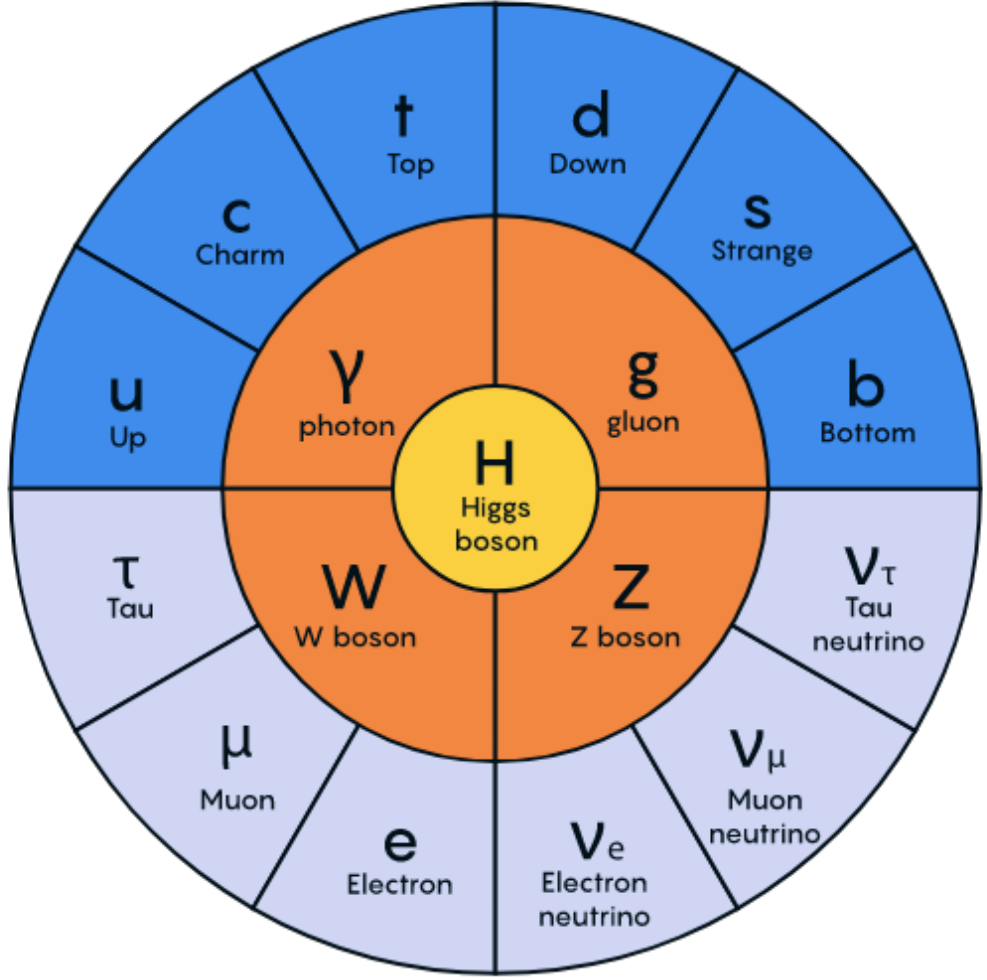
Main points

- Introduction: quantum sensing, dark matter
- Lecture 1: quantum approaches to searching for the electromagnetic interaction of axion-like dark matter
- Lecture 2: quantum approaches to searching for the interaction of axion-like dark matter with nuclear spins



The standard model

The Standard Model



FERMIONS (MATTER) BOSONS (FORCE CARRIERS)

● QUARKS ● LEPTONS ● GAUGE BOSONS ● HIGGS BOSON



**DARK
MATTER**

**STRONG-CP
PROBLEM**

**COSMIC
INFLATION**

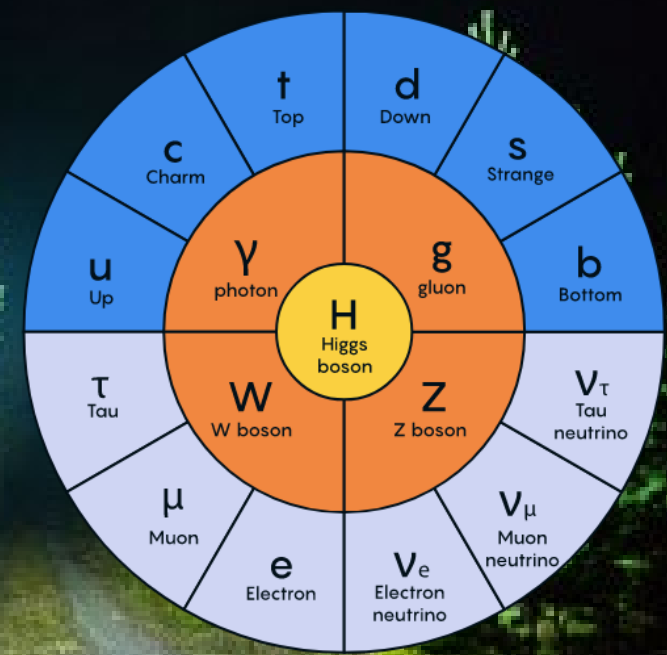
**HIERARCHY
PROBLEM**

**BLACK HOLE
INFORMATION
PROBLEM**

**QUANTUM
GRAVITY**

**NEUTRINO
MASS**

**DARK
ENERGY**





The tools

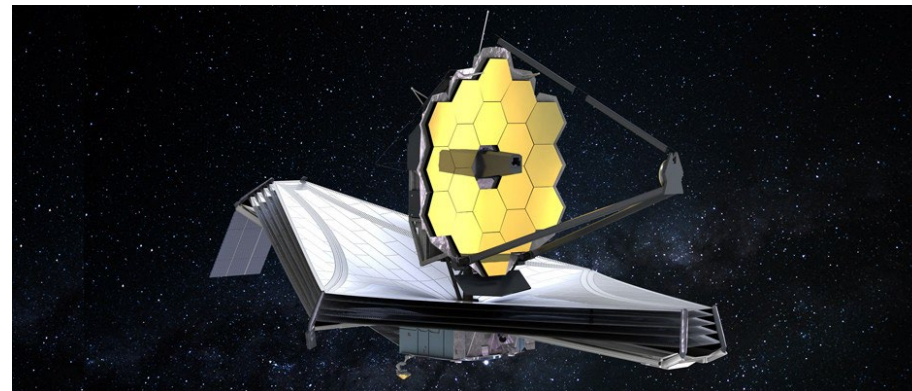
particle accelerators



terrestrial telescopes



space telescopes



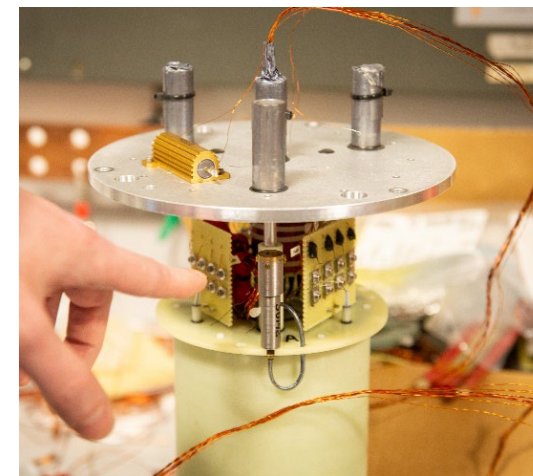
rare event detectors (eg, WIMPs)



gravitational wave observatories



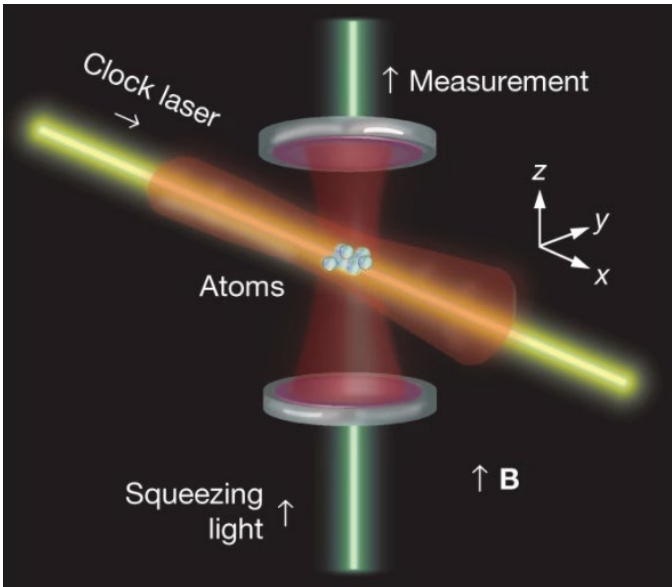
precision lab-scale experiments





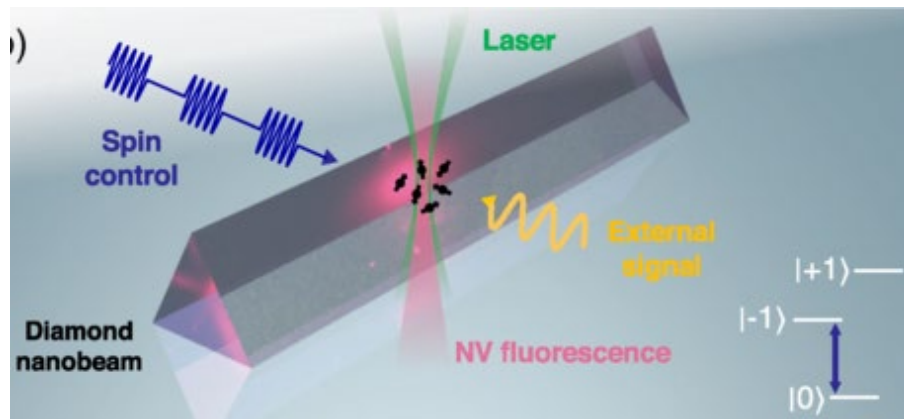
Precision measurements, quantum metrology and sensing

entanglement-enhanced atomic sensors



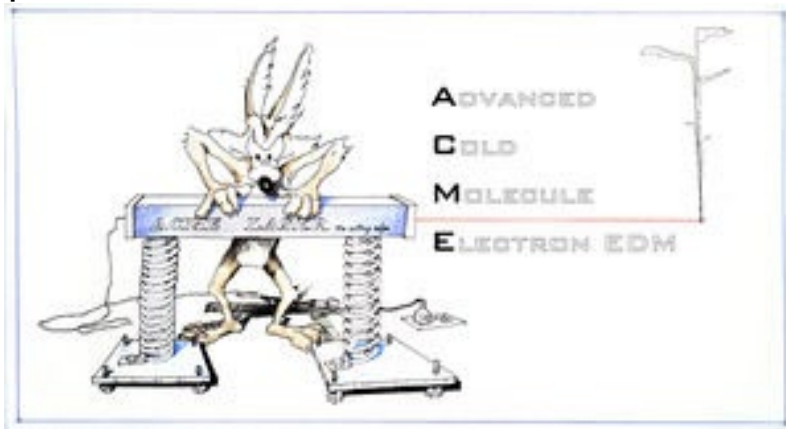
[Nature **588**, 414 (2020)]
[arXiv:2106.03754 (2021)]

NV centers in diamond



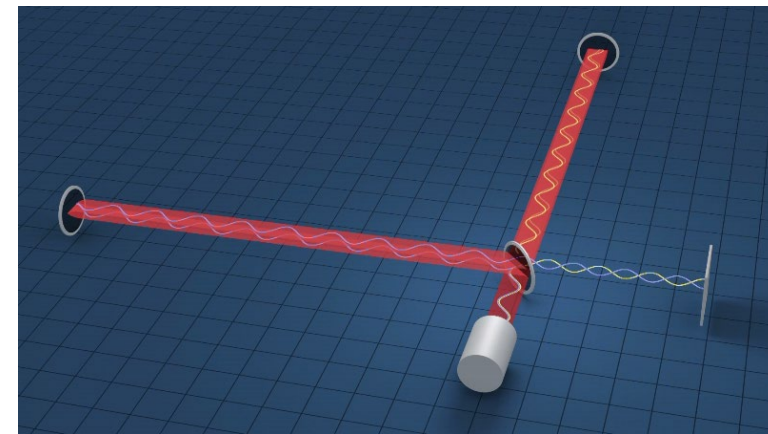
[PRX **10**, 031003 (2020)]

precisions measurements with molecules



[Science **343**, 269 (2013)]
[Nature **562**, 355 (2018)]

interferometry



[Phys. Rev. Lett. **123**, 231107 (2019)]

[Phys. Rev. Lett. **124**, 171102 (2020)]

quantum sensing review:

[Rev. Mod. Phys. **89**, 035002 (2017)]

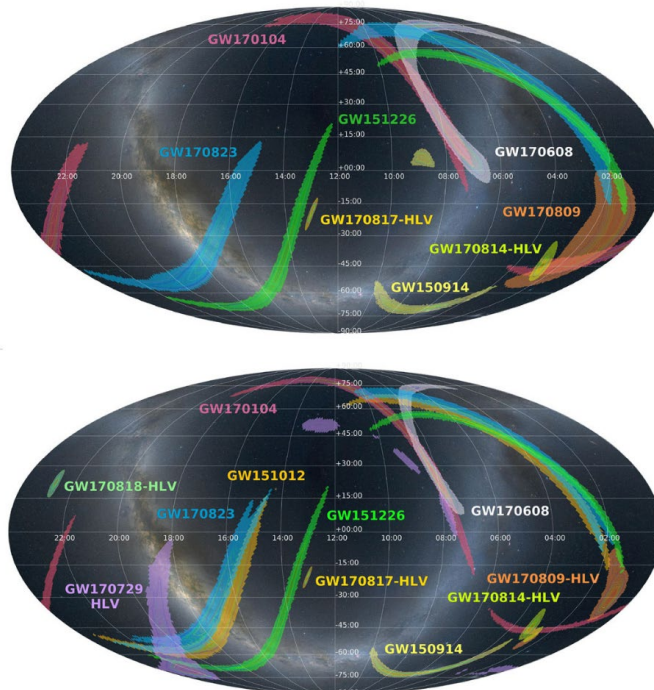


LIGO: an inspiration for quantum metrology

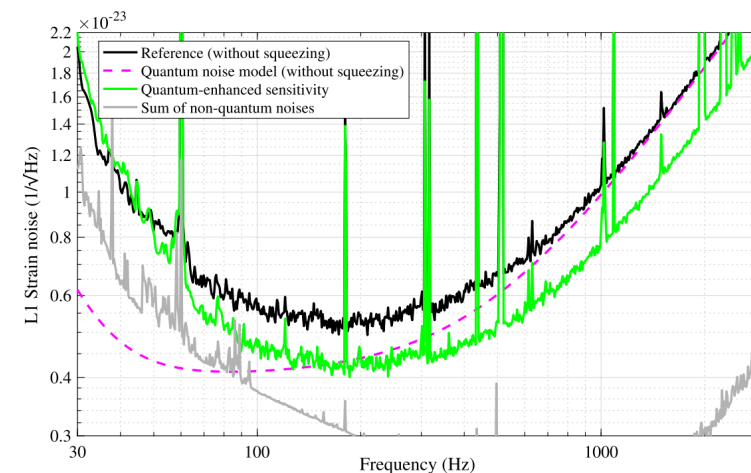
first gravitational wave detection
(GW150914, 2015)



GW events detected in O1 and O2



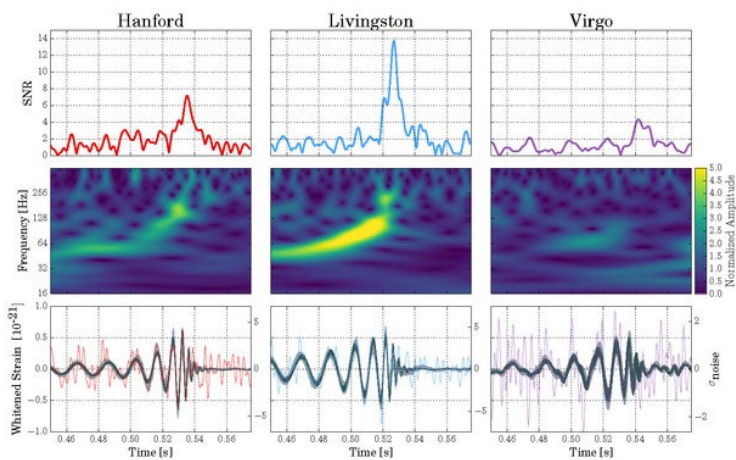
added a squeezed vacuum
source for O3 run (2019-2020)



extended detection range by $\approx 15\%$



increased detection rate by $\approx 45\%$



[Phys. Rev. Lett. **123**, 231107 (2019)]

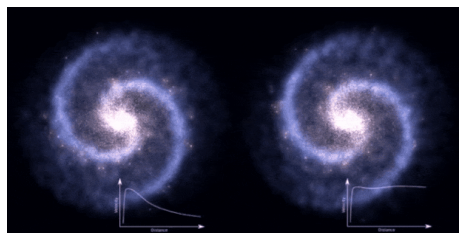
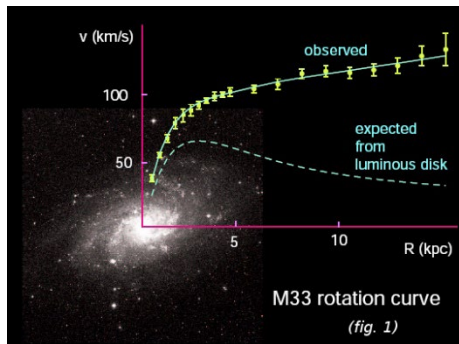
[Phys. Rev. Lett. **124**, 171102 (2020)]

[Liv. Rev. Rel. **23**, 1 (2020)]



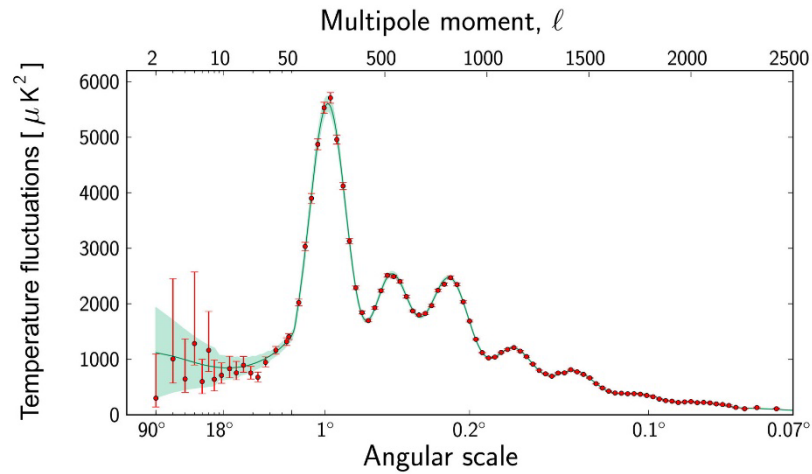
The dark matter problem

galaxy rotation curves

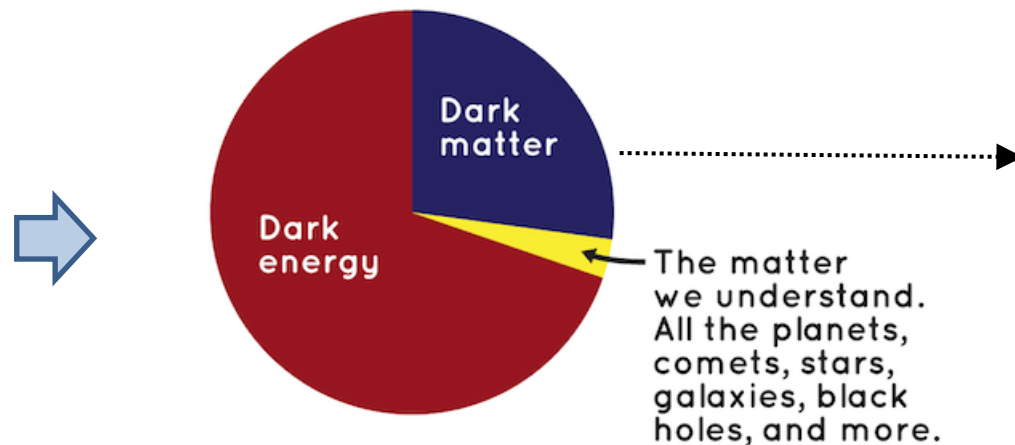
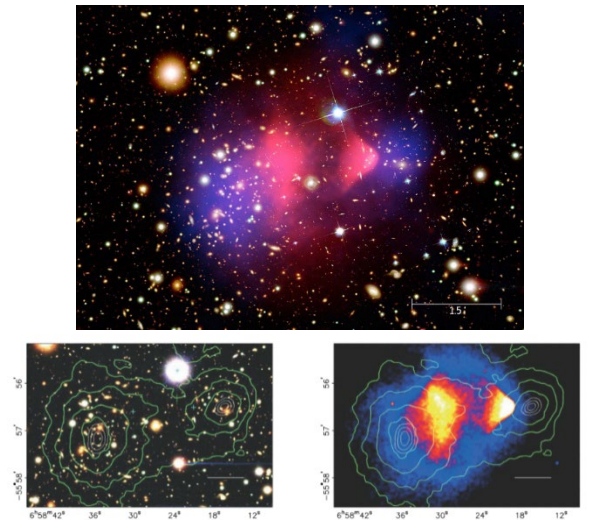


+ many others

CMB angular power spectrum



galaxy clusters: Bullet cluster



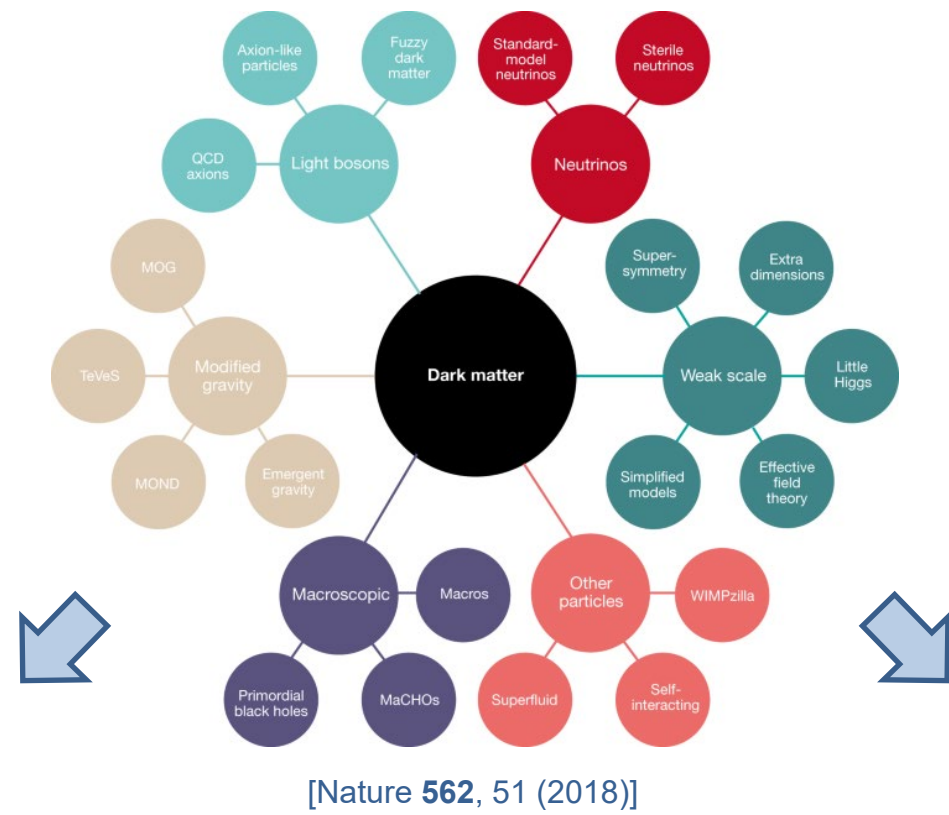
local dark matter energy density: $\rho_{DM} \approx 0.4 \text{ GeV}/\text{cm}^3$



[Nature 562, 51 (2018)]

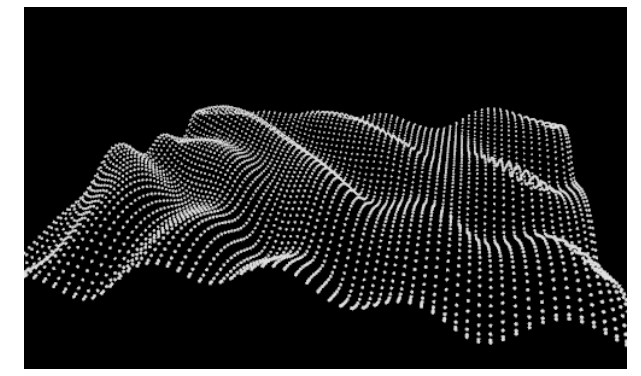


What is dark matter?



particle-like dark matter (eg: WIMPs):
mass ~ 100 GeV

[Phys. Rev. D 96, 035009 (2017)]



wave-like dark matter (eg: axions)
mass << eV

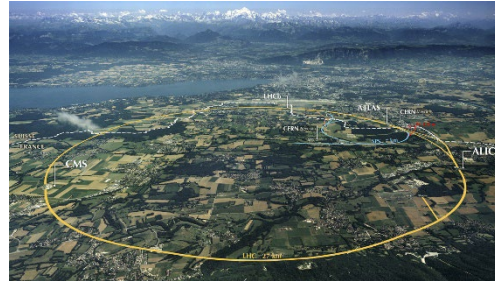
[Phys. Rev. Lett. 118, 061302 (2017)]

Searching for WIMP-like dark matter

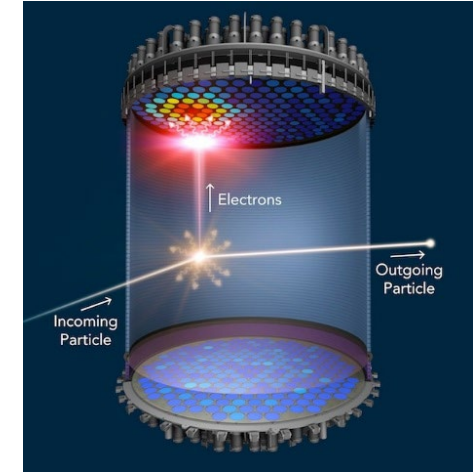
indirect detection



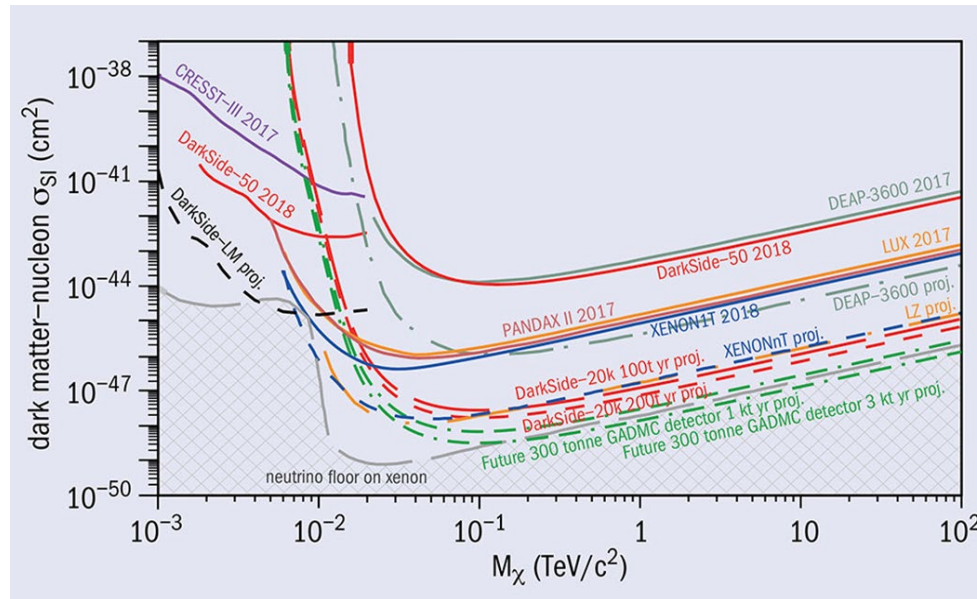
accelerator searches



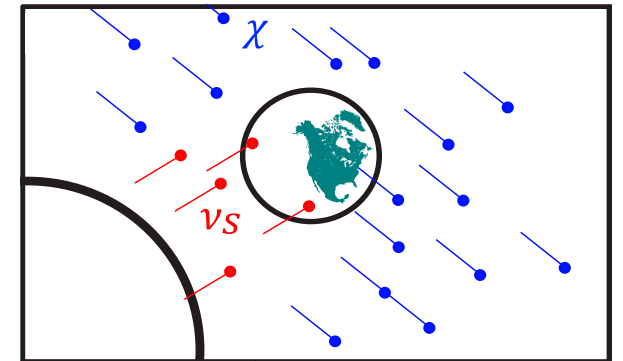
direct detection



a number of extremely sensitive experimental searches



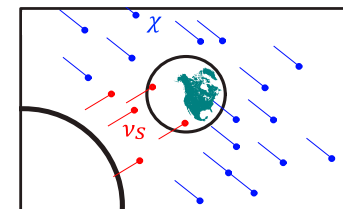
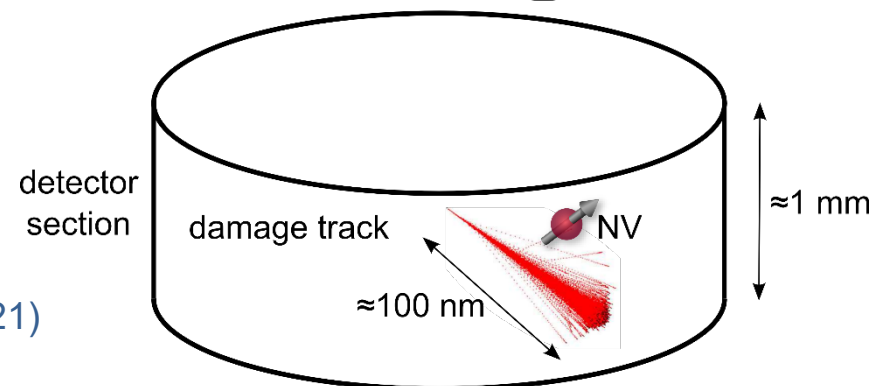
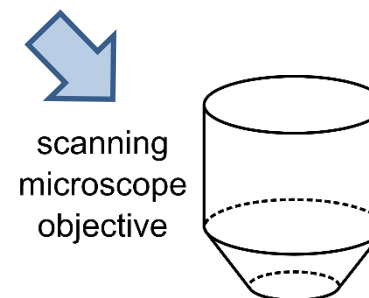
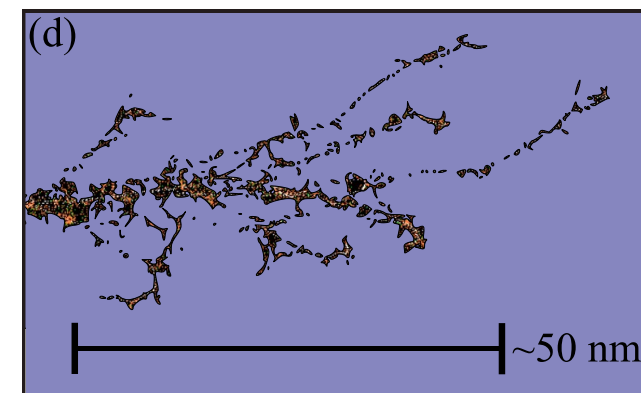
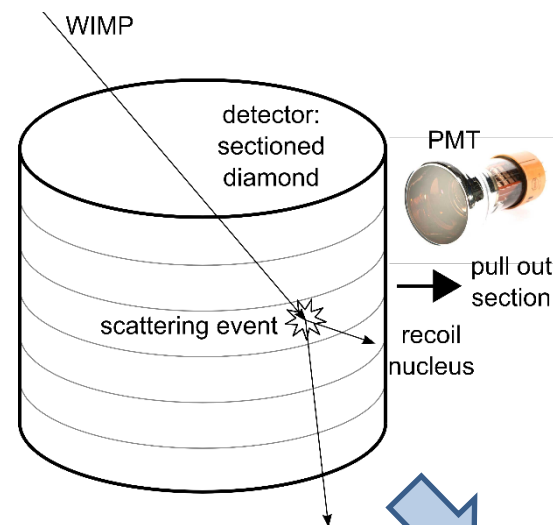
to go beyond the neutrino floor we can use directional information





Idea: direction-sensitive WIMP detector based on quantum defects in diamond

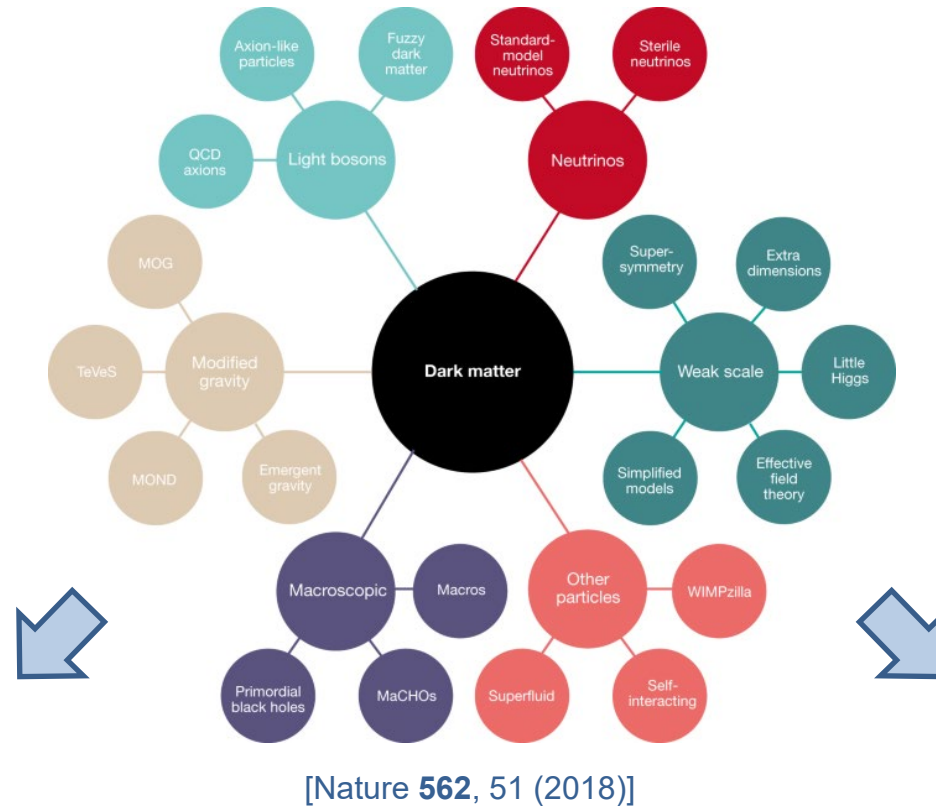
1. detector volume is made up of diamond sections, surrounded by PMTs and/or charge readout sensors
2. a WIMP scattering event is detected and localized via charge collection and scintillation
3. the recoil nucleus produces a track of vacancies ≈ 100 nm long
4. the detector section where the scattering event occurred is pulled out and examined
5. measurements of crystal strain using NV centers allow reconstruction of vacancy distribution, and hence the WIMP momentum direction



a directional detector for
WIMP dark matter

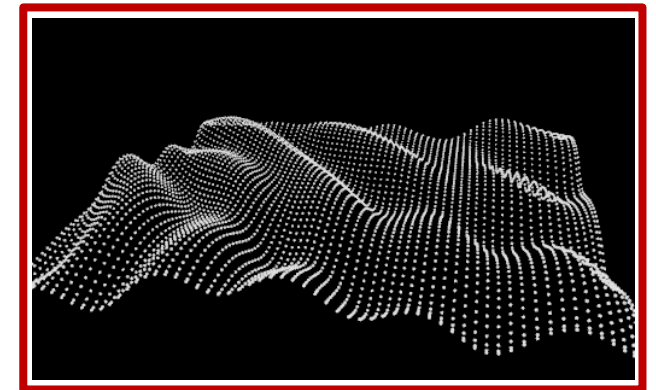
details: S. Rajendran *et al.* arXiv:1705.09760; *Phys. Rev. D* (2017)
M. Marshall *et al.* arXiv: 2009.01028; *Quantum Sci. Technol.* (2021)
M. Marshall *et al.* arXiv:2103.08388; *Phys. Rev. Appl.* (Subm.)
M. Marshall *et al.* arXiv:2107.xxxxx (in preparation)

What is dark matter?



particle-like dark matter (eg: WIMPs):
mass ~ 100 GeV

[Phys. Rev. D **96**, 035009 (2017)]

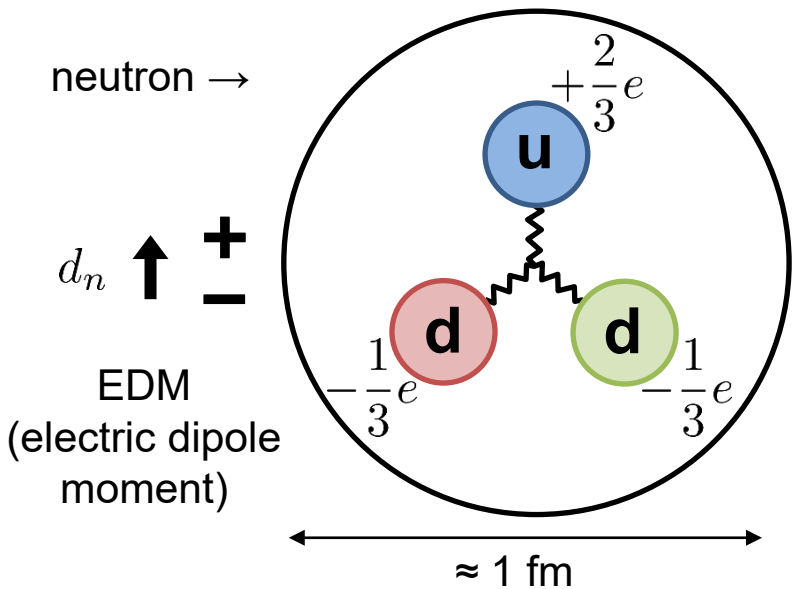


wave-like dark matter (eg: axions)
mass $\ll eV$

[Phys. Rev. Lett. **118**, 061302 (2017)]



The strong-CP problem



(very!) naïve estimate:

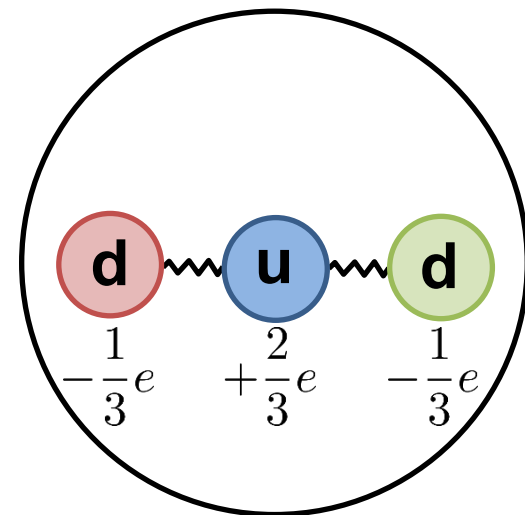
$$d_n \approx e \cdot \text{fm} = 10^{-13} e \cdot \text{cm}$$

experimental limit:

$$d_n < 1.8 \times 10^{-26} e \cdot \text{cm}$$

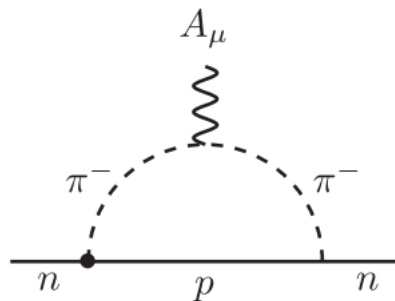
[Phys. Rev. Lett. **124**, 081803 (2020)]

better model for a neutron \rightarrow



CP-violating θ -term in QCD Lagrangian \rightarrow

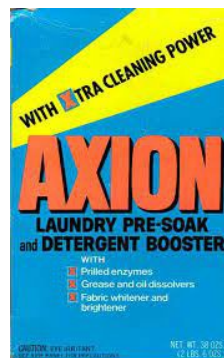
$$\mathcal{L}_\theta = \theta (\alpha_s / 8\pi) G_{\mu\nu}^{(a)} \tilde{G}^{(a)\mu\nu}$$



\Rightarrow neutron EDM: $d_n = \theta \times (2.4 \times 10^{-16}) e \cdot \text{cm}$

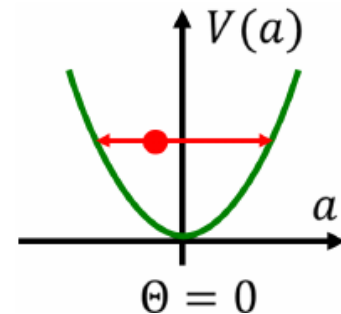
$\Rightarrow \theta < 10^{-10}$

why is θ so small?



$$\theta \rightarrow \frac{a}{f_a}$$

$$\langle \theta \rangle = \langle a \rangle = 0$$



axion solves the strong-CP problem

[Phys. Rev. Lett. **38**, 1440 (1977)] [Phys. Rev. Lett. **40**, 223 (1978)]

[Phys. Rev. D **16**, 1791 (1977)] [Phys. Rev. Lett. **40**, 279 (1978)]

[Rev. Mod. Phys. **82**, 557 (2010)]

Axions and axion-like particles, axion-like dark matter

1. Pseudoscalar light particle: spin = 0, wide range of possible masses [Phys. Rev. D **98**, 035017 (2018)]
2. Proposed to solve the **strong CP problem** of Quantum Chromodynamics
3. Axion-like particles (ALPs) arise naturally in string theories, symmetries broken at GUT (10^{16} GeV) or Planck (10^{19} GeV) scales
4. Well-motivated and thoroughly-studied **dark matter** candidate: $a(t) = a_0 \cos \omega_a t$

ALP mass range
 $m_a c^2 < \text{meV}$



dark matter energy density:
 $\rho_{\text{DM}} \approx 0.4 \frac{\text{GeV}}{\text{cm}^3} \approx (0.05 \text{ eV})^4$



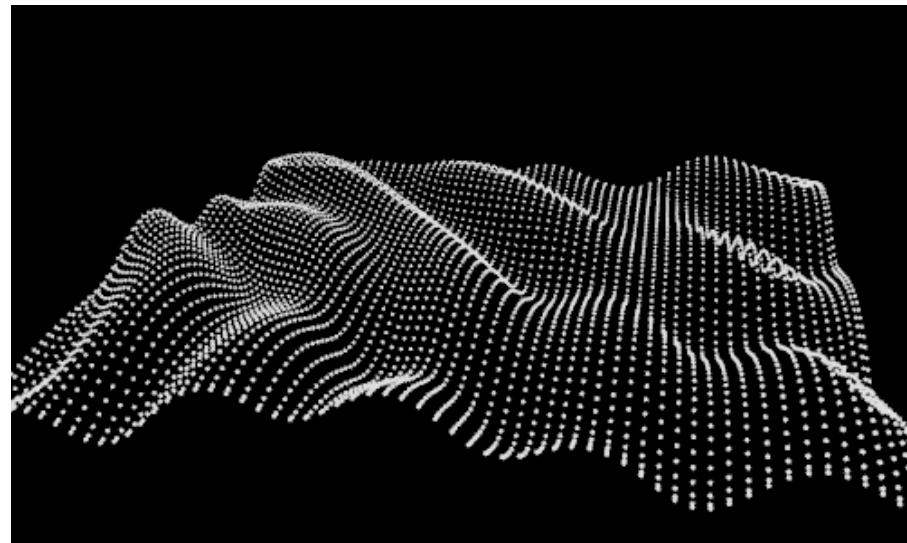
large number of particles
 per de Broglie wavelength



ALP dark matter acts as a classical field

axion-like field: $a(t) = a_0 \cos \omega_a t$

$\omega_a = m_a c^2 / \hbar \rightarrow$ ALP Compton frequency
 $\rho_{\text{DM}} \propto a_0^2 \rightarrow$ dark matter density



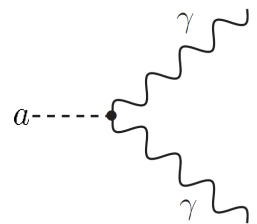
Axions and axion-like particles: basics and motivation

1. Pseudoscalar light particle: spin = 0, wide range of possible masses [Phys. Rev. D **98**, 035017 (2018)]
2. Proposed to solve the **strong CP problem** of Quantum Chromodynamics [Phys. Rev. Lett. **38**, 1440 (1977)]
3. Axion-like particles (ALPs) arise naturally in string theories, symmetries broken at GUT (10^{16} GeV) or Planck (10^{19} GeV) scales
4. Well-motivated and thoroughly-studied **dark matter** candidate: $a(t) = a_0 \cos \omega_a t$
5. Only 3 possible (non-gravitational) interactions with standard model particles:

interaction with photons:

ALP field amplitude $\rightarrow \frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$

symmetry breaking scale $\rightarrow \mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$



\rightarrow ALP \leftrightarrow photon conversion in a magnetic field
 \rightarrow precision electromagnetic sensors

ADMX, HAYSTAC, DMradio, SHAFT, ABRA, ALPS, CAST, IAXO, CAPP, ORGAN, BREAD, SLIC, LC circuit, MADMAX, KLASH, BRASS, many others

interaction with gluons (strong-CP) defines QCD axion:

$$\frac{a}{f_a} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

$$\mathcal{H}_{\text{EDM}} = g_d a \mathbf{E}^* \cdot \mathbf{I} / I$$

\rightarrow nuclear spin \mathbf{I} interacts with an oscillating electric dipole moment (EDM) $d_n = g_d a$ in presence of effective electric field \mathbf{E}^* .

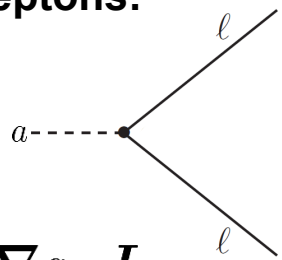
CASPER-electric

interaction with leptons:

$$\frac{\partial_\mu a}{f_a} \bar{\psi}_\ell \gamma^\mu \gamma_5 \psi_\ell$$

$$\mathcal{H}_{aNN} = g_{aNN} \nabla a \cdot \mathbf{I}$$

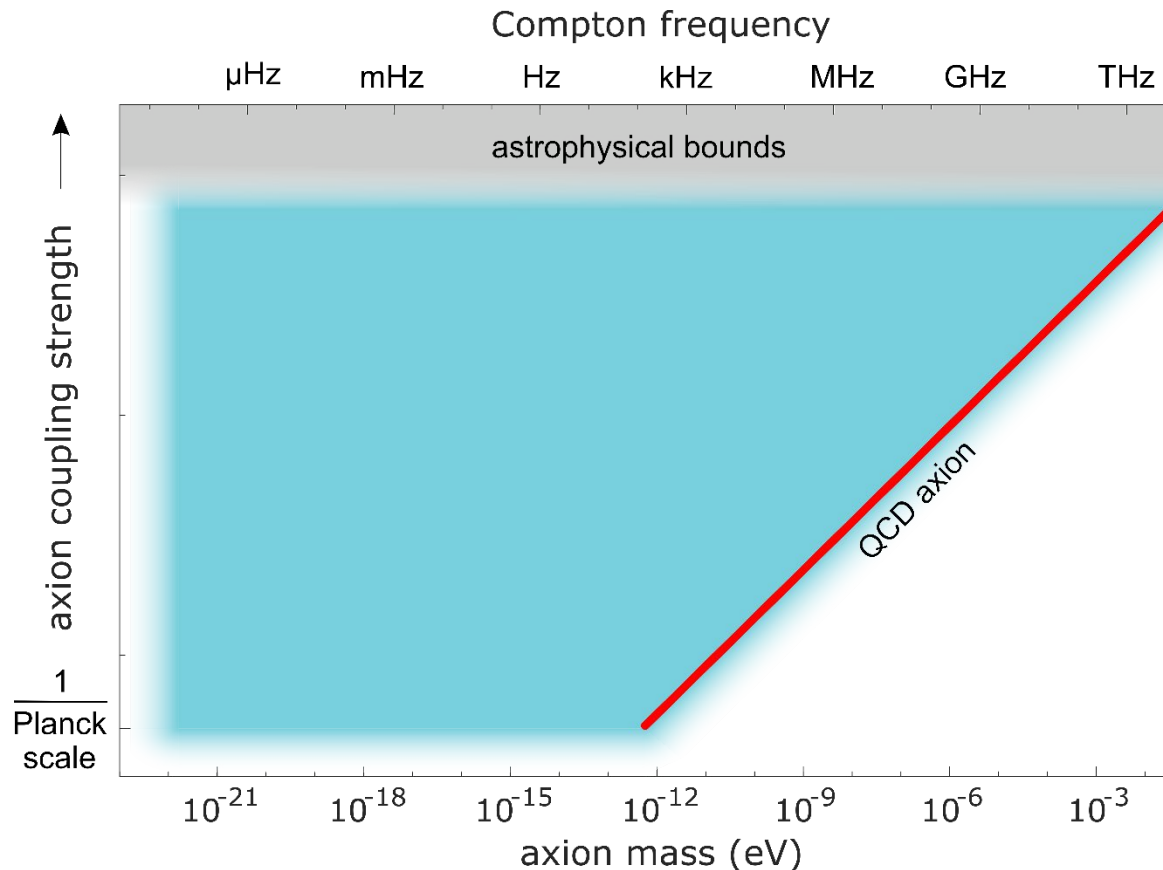
\rightarrow nuclear spin \mathbf{I} interacts with an effective magnetic field ∇a .
 co-magnetometers
 force mediator \rightarrow ARIADNE
 electron spin \rightarrow QUAX



CASPER-gradient

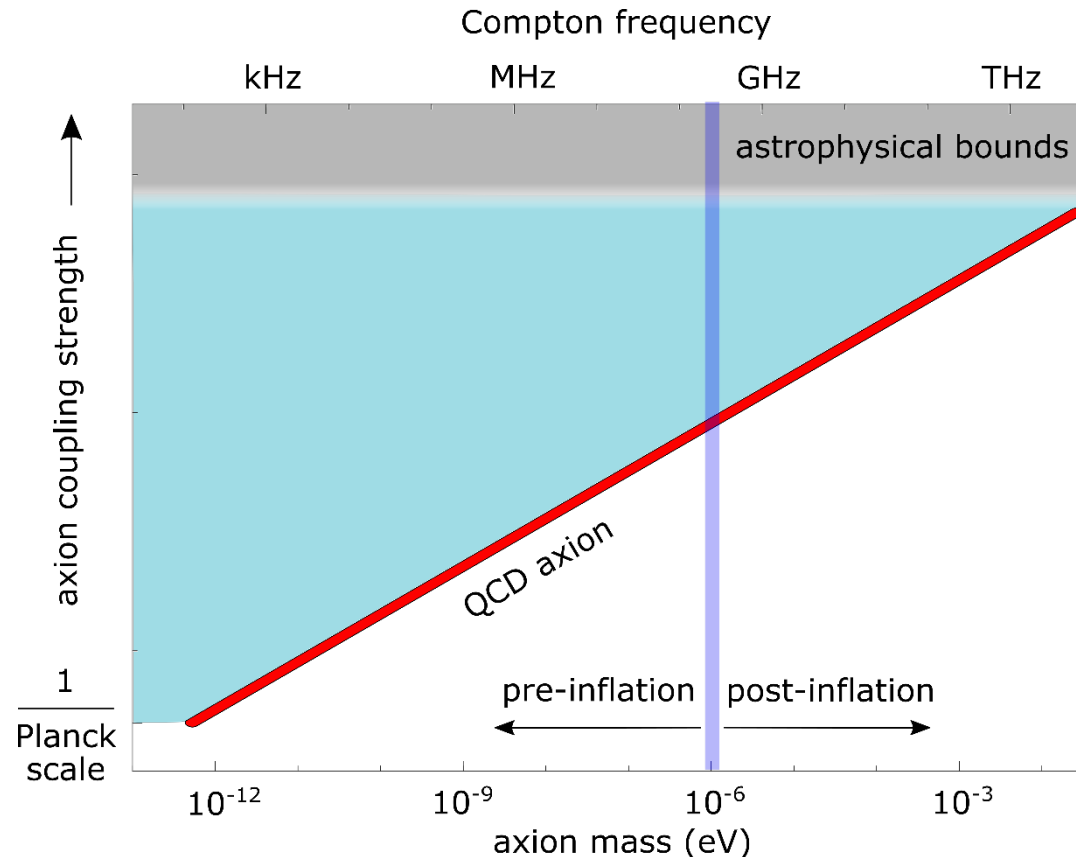
Axions and axion-like particles: basics and motivation

1. Pseudoscalar light particle: spin = 0, wide range of possible masses [Phys. Rev. D **98**, 035017 (2018)]
2. Proposed to solve the **strong CP problem** of Quantum Chromodynamics [Phys. Rev. Lett. **38**, 1440 (1977)]
3. Axion-like particles (ALPs) arise naturally in string theories, symmetries broken at GUT (10^{16} GeV) or Planck (10^{19} GeV) scales
4. Well-motivated and thoroughly-studied **dark matter** candidate: $a(t) = a_0 \cos \omega_a t$
5. Only 3 possible (non-gravitational) interactions with standard model particles



Axions and axion-like particles: basics and motivation

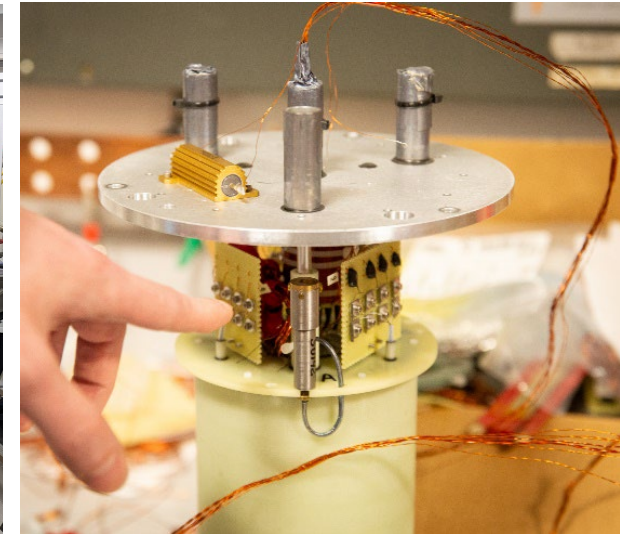
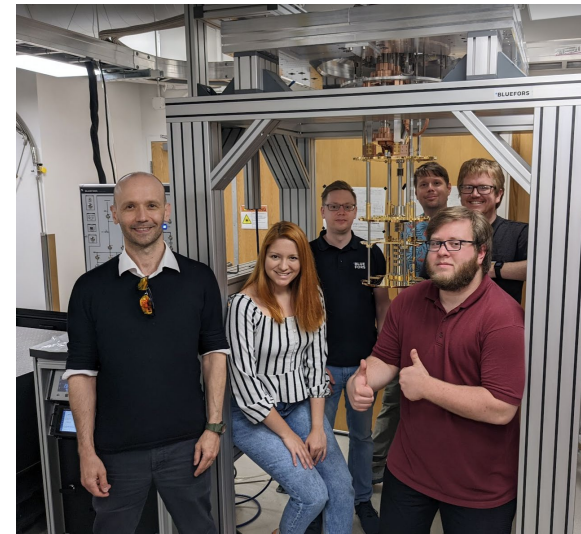
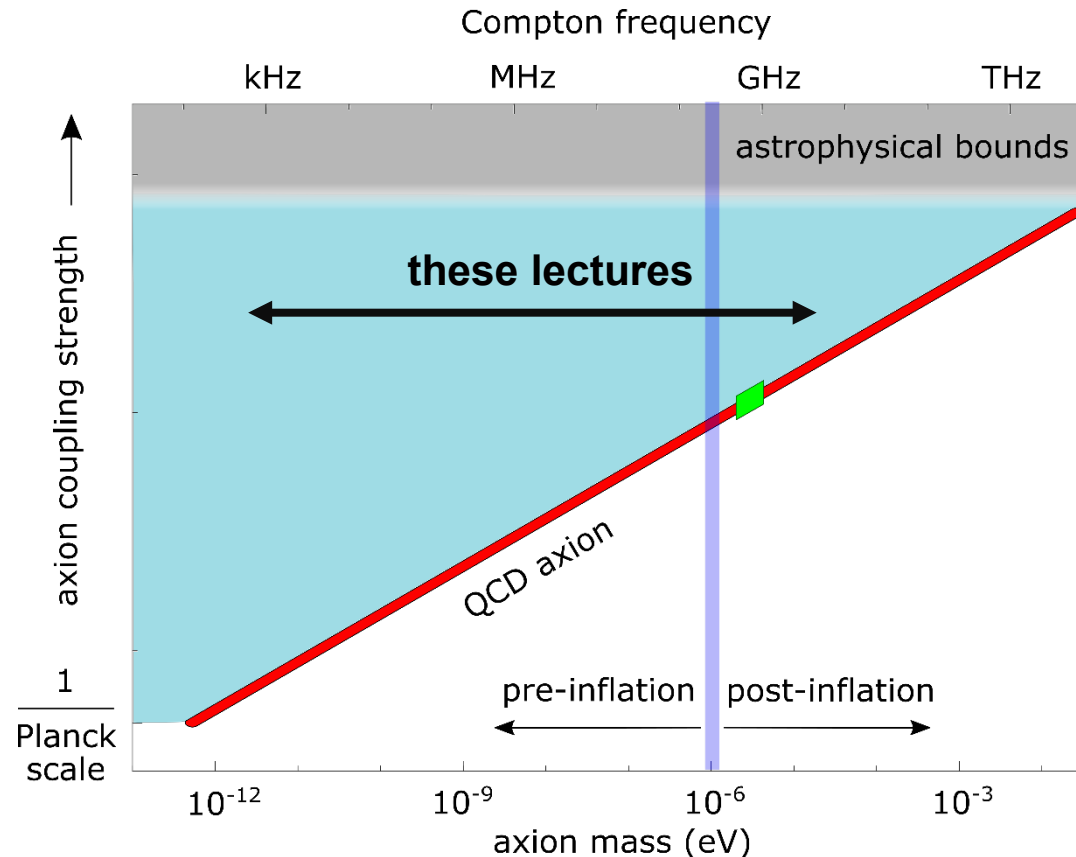
1. Pseudoscalar light particle: spin = 0, wide range of possible masses [Phys. Rev. D **98**, 035017 (2018)]
2. Proposed to solve the **strong CP problem** of Quantum Chromodynamics [Phys. Rev. Lett. **38**, 1440 (1977)]
3. Axion-like particles (ALPs) arise naturally in string theories, symmetries broken at GUT (10^{16} GeV) or Planck (10^{19} GeV) scales
4. Well-motivated and thoroughly-studied **dark matter** candidate: $a(t) = a_0 \cos \omega_a t$
5. Only 3 possible (non-gravitational) interactions with standard model particles
6. Detection of axion dark matter → insight into energy scale of **inflation**



detection of axion dark matter
↓
insight into energy scale of inflation

Axions and axion-like particles: basics and motivation

1. Pseudoscalar light particle: spin = 0, wide range of possible masses [Phys. Rev. D **98**, 035017 (2018)]
2. Proposed to solve the **strong CP problem** of Quantum Chromodynamics [Phys. Rev. Lett. **38**, 1440 (1977)]
3. Axion-like particles (ALPs) arise naturally in string theories, symmetries broken at GUT (10^{16} GeV) or Planck (10^{19} GeV) scales
4. Well-motivated and thoroughly-studied **dark matter** candidate: $a(t) = a_0 \cos \omega_a t$
5. Only 3 possible (non-gravitational) interactions with standard model particles
6. Detection of axion dark matter → insight into energy scale of **inflation**



laboratory-scale experimental searches can explore the axion parameter space

[Science **357**, 990 (2017)]

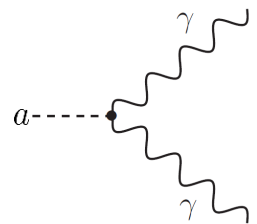
Axions and axion-like particles: basics and motivation

1. Pseudoscalar light particle: spin = 0, wide range of possible masses [Phys. Rev. D **98**, 035017 (2018)]
2. Proposed to solve the **strong CP problem** of Quantum Chromodynamics [Phys. Rev. Lett. **38**, 1440 (1977)]
3. Axion-like particles (ALPs) arise naturally in string theories, symmetries broken at GUT (10^{16} GeV) or Planck (10^{19} GeV) scales
4. Well-motivated and thoroughly-studied **dark matter** candidate: $a(t) = a_0 \cos \omega_a t$
5. Only 3 possible (non-gravitational) interactions with standard model particles:

interaction with photons:

ALP field amplitude $\rightarrow \frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$

symmetry breaking scale $\rightarrow \mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$



\rightarrow ALP \leftrightarrow photon conversion in a magnetic field
 \rightarrow precision electromagnetic sensors

ADMX, HAYSTAC, DMradio, SHAFT, ABRA,
 ALPS, CAST, IAXO, CAPP, ORGAN, BREAD,
 SLIC, LC circuit, MADMAX, KLASH, BRASS,
 many others

interaction with gluons (strong-CP) defines QCD axion:

$$\frac{a}{f_a} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

$$\mathcal{H}_{\text{EDM}} = g_d a \mathbf{E}^* \cdot \mathbf{I} / I$$

\rightarrow nuclear spin \mathbf{I} interacts with an oscillating electric dipole moment (EDM) $d_n = g_d a$ in presence of effective electric field \mathbf{E}^* .

CASPEr-electric

interaction with leptons:

$$\frac{\partial_\mu a}{f_a} \bar{\psi}_\ell \gamma^\mu \gamma_5 \psi_\ell$$

$$\mathcal{H}_{aNN} = g_{aNN} \nabla a \cdot \mathbf{I}$$

\rightarrow nuclear spin \mathbf{I} interacts with an effective magnetic field ∇a .
 co-magnetometers
 force mediator \rightarrow ARIADNE
 electron spin \rightarrow QUAX

CASPEr-gradient



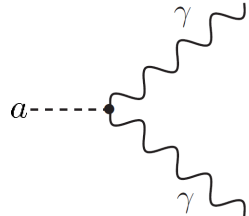
Searches for electromagnetic interaction of axion-like dark matter

$$a(t) = a_0 \cos \omega_a t$$

interaction with photons:

ALP field amplitude

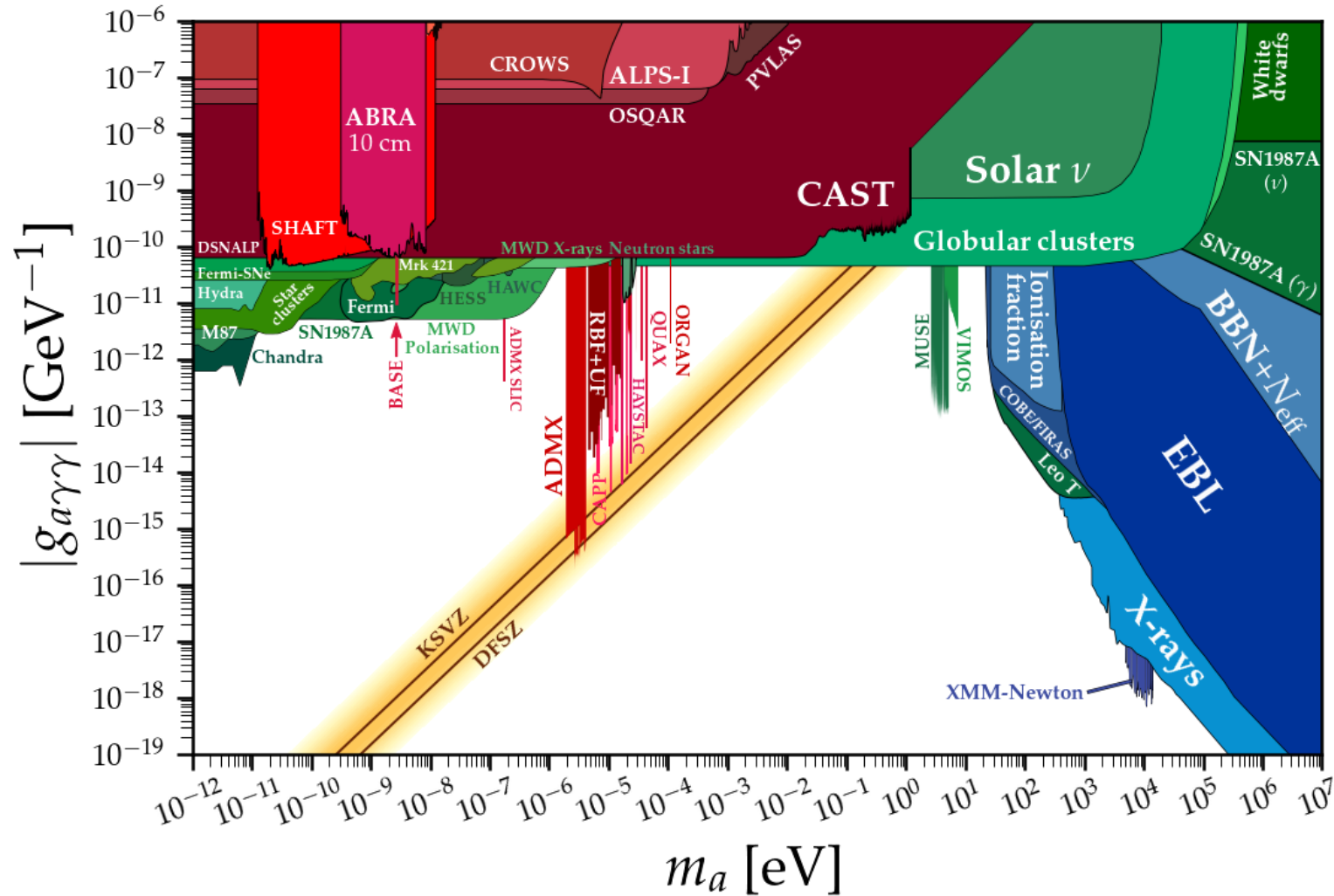
$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



symmetry breaking scale

$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP ↔ photon conversion in a magnetic field
- precision electromagnetic sensors



Lumped-element searches for axion-like dark matter

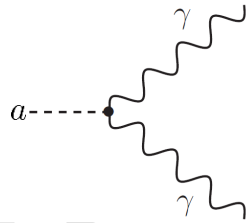
$$a(t) = a_0 \cos \omega_a t$$

goal: search for electromagnetic coupling of axion-like dark matter in in mass (frequency) range where experiment size \ll wavelength

interaction with photons:

ALP field amplitude

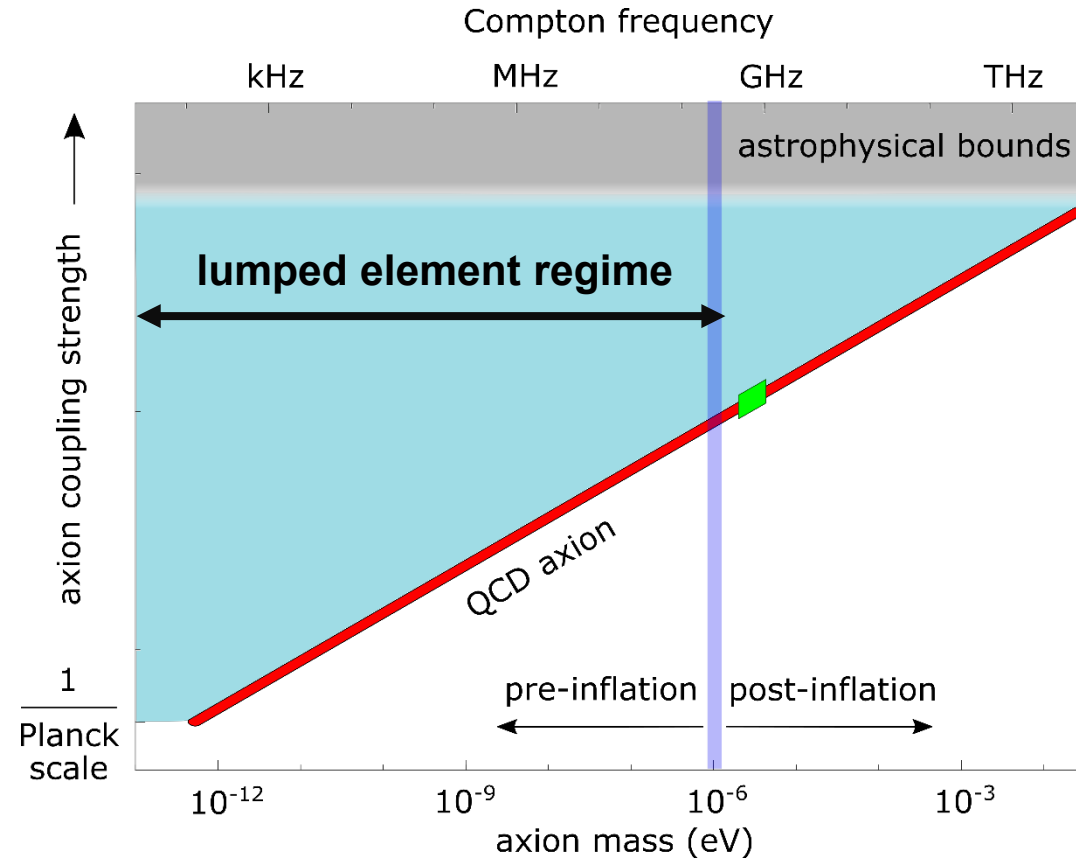
$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



symmetry breaking scale

$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP \leftrightarrow photon conversion in a magnetic field
- precision electromagnetic sensors



Lumped-element searches for axion-like dark matter

$$a(t) = a_0 \cos \omega_a t$$

goal: search for electromagnetic coupling of axion-like dark matter in in mass (frequency) range where experiment size \ll wavelength

approach \rightarrow additional term in Ampere's law



$$\nabla \times \mathbf{H} = \mathbf{J}_f$$

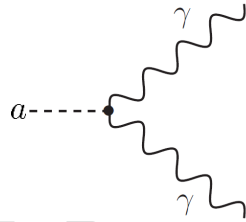
interaction with photons:

ALP field amplitude

symmetry breaking scale

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$



\rightarrow ALP \leftrightarrow photon conversion in a magnetic field
 \rightarrow precision electromagnetic sensors

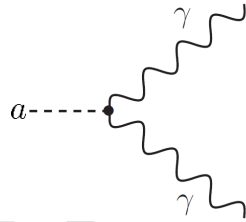
Lumped-element searches for axion-like dark matter

goal: search for electromagnetic coupling of axion-like dark matter in mass (frequency) range where experiment size \ll wavelength

interaction with photons:

ALP field amplitude

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



symmetry breaking scale

$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP \leftrightarrow photon conversion in a magnetic field
- precision electromagnetic sensors

approach → additional term in Ampere's law



$$\nabla \times \mathbf{H} = \mathbf{J}_f + \frac{g_{a\gamma\gamma}}{\mu_0 c} \frac{\partial a}{\partial t} \mathbf{B}$$

\mathbf{J}^*

azimuthal static magnetic field \mathbf{B}_0



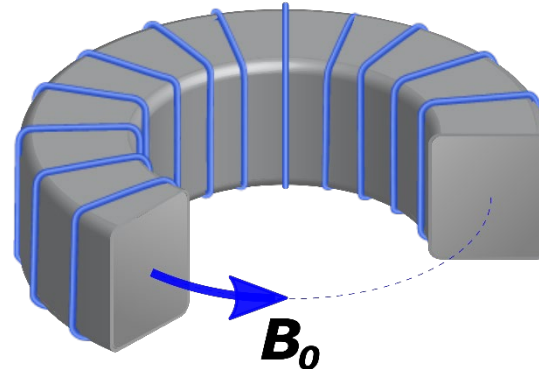
axion field

$$a(t) = a_0 \cos \omega_a t$$



azimuthal effective current

$$\mathbf{J}^* = \frac{g_{a\gamma\gamma}}{\mu_0 c} \frac{\partial a}{\partial t} \mathbf{B}_0$$



[Phys. Rev. Lett. **112**, 131301 (2014)]

[Phys. Rev. D **92**, 075012 (2015)]

[Phys. Rev. Lett. **117**, 141801 (2016)]

[arXiv: 1811.03231 (2018)]

[Phys. Rev. Lett. **122**, 121802 (2019)]

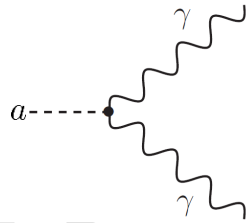
Lumped-element searches for axion-like dark matter

goal: search for electromagnetic coupling of axion-like dark matter in mass (frequency) range where experiment size \ll wavelength

interaction with photons:

ALP field amplitude

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



symmetry breaking scale

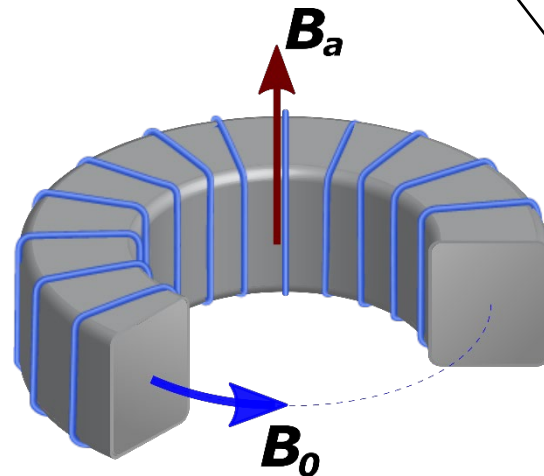
$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP \leftrightarrow photon conversion in a magnetic field
- precision electromagnetic sensors

approach → additional term in Ampere's law



$$\nabla \times \mathbf{H} = \mathbf{J}_f + \mathbf{J}^*$$



azimuthal static magnetic field B_0



axion field

$$a(t) = a_0 \cos \omega_a t$$



azimuthal effective current

$$\mathbf{J}^* = \frac{g_{a\gamma\gamma}}{\mu_0 c} \frac{\partial a}{\partial t} \mathbf{B}_0$$



axial oscillating magnetic field B_a

[Phys. Rev. Lett. **112**, 131301 (2014)]

[Phys. Rev. D **92**, 075012 (2015)]

[Phys. Rev. Lett. **117**, 141801 (2016)]

[arXiv: 1811.03231 (2018)]

[Phys. Rev. Lett. **122**, 121802 (2019)]

[Nature Physics **17**, 79 (2021)]

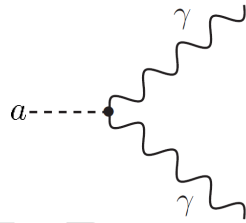
Lumped-element searches for axion-like dark matter

goal: search for electromagnetic coupling of axion-like dark matter in mass (frequency) range where experiment size \ll wavelength

interaction with photons:

ALP field amplitude

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



symmetry breaking scale

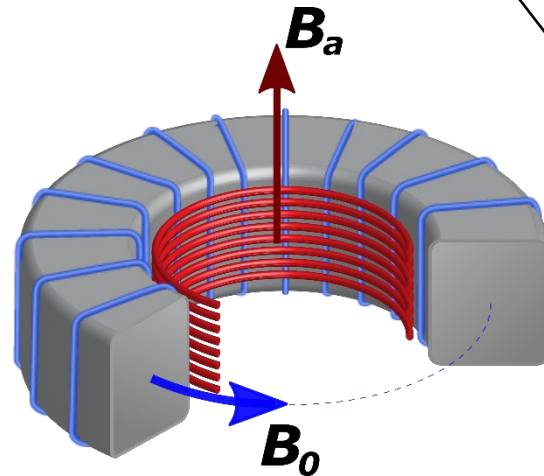
$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP \leftrightarrow photon conversion in a magnetic field
- precision electromagnetic sensors

approach → additional term in Ampere's law



$$\nabla \times \mathbf{H} = \mathbf{J}_f + \mathbf{J}^*$$



azimuthal static magnetic field B_0



axion field

$$a(t) = a_0 \cos \omega_a t$$



azimuthal effective current

$$\mathbf{J}^* = \frac{g_{a\gamma\gamma}}{\mu_0 c} \frac{\partial a}{\partial t} \mathbf{B}_0$$



axial oscillating magnetic field B_a



signal detected by SQUID $\propto B_0$

[Phys. Rev. Lett. **112**, 131301 (2014)]

[Phys. Rev. D **92**, 075012 (2015)]

[Phys. Rev. Lett. **117**, 141801 (2016)]

[arXiv: 1811.03231 (2018)]

[Phys. Rev. Lett. **122**, 121802 (2019)]

[Nature Physics **17**, 79 (2021)]

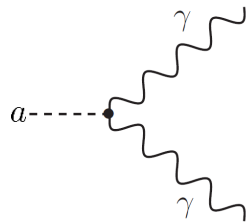
Lumped-element searches for axion-like dark matter

goal: search for electromagnetic coupling of axion-like dark matter in mass (frequency) range where experiment size \ll wavelength

interaction with photons:

ALP field amplitude

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



symmetry breaking scale

$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP \leftrightarrow photon conversion in a magnetic field
- precision electromagnetic sensors

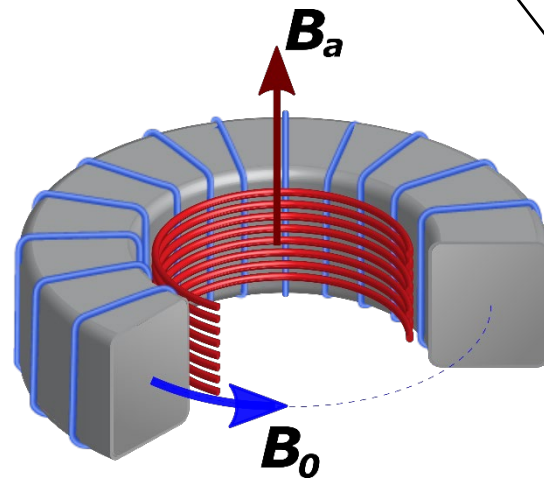
key experimental parameters:

- magnetic field $B \rightarrow$ larger is better
- volume $V \rightarrow$ larger is better
- temperature \rightarrow colder is better
- sensor noise and back-action

approach \rightarrow additional term in Ampere's law



$$\nabla \times \mathbf{H} = \mathbf{J}_f + \mathbf{J}^*$$



azimuthal static magnetic field B_0



axion field

$$a(t) = a_0 \cos \omega_a t$$



azimuthal effective current

$$\mathbf{J}^* = \frac{g_{a\gamma\gamma}}{\mu_0 c} \frac{\partial a}{\partial t} \mathbf{B}_0$$



axial oscillating magnetic field B_a



signal detected by SQUID $\propto B_0$

[Phys. Rev. Lett. **112**, 131301 (2014)]

[Phys. Rev. D **92**, 075012 (2015)]

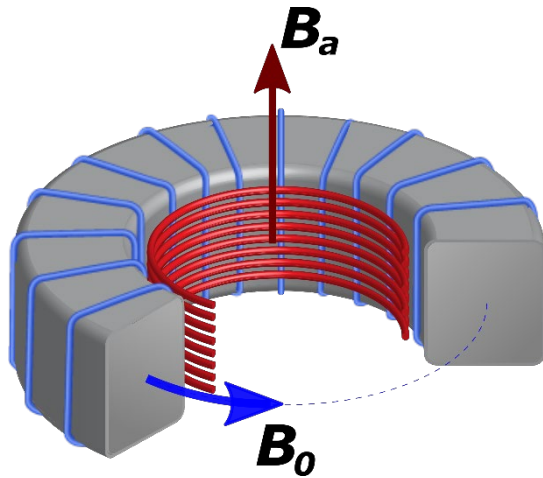
[Phys. Rev. Lett. **117**, 141801 (2016)]

[arXiv: 1811.03231 (2018)]

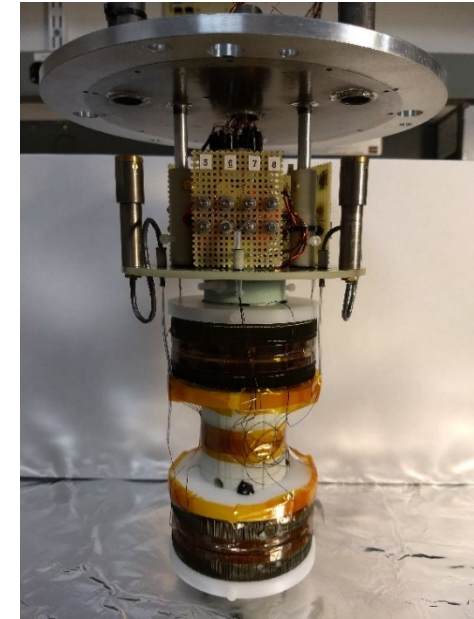
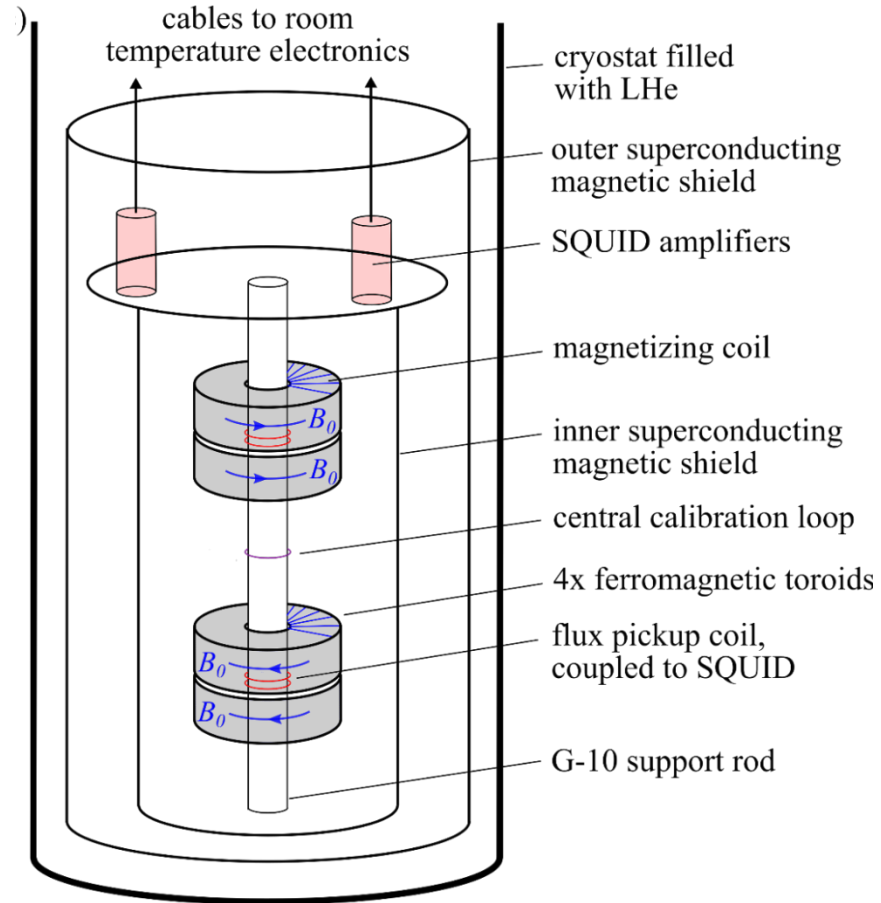
[Phys. Rev. Lett. **122**, 121802 (2019)]

[Nature Physics **17**, 79 (2021)]

Experimental setup, broadband searches: SHAFT, ABRACADABRA

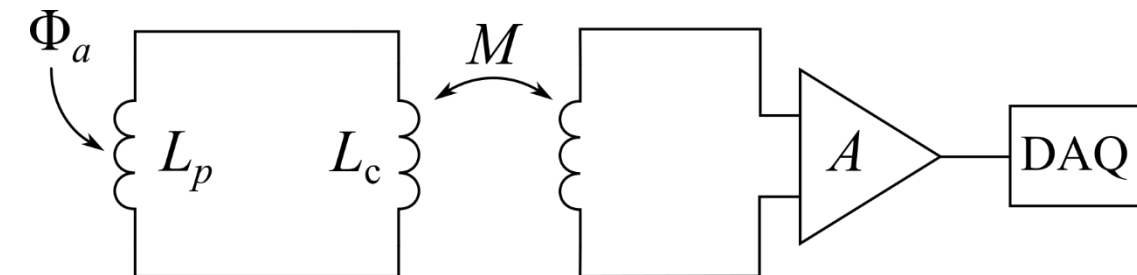


$\Phi_a \rightarrow$ magnetic flux due to axion-like dark matter

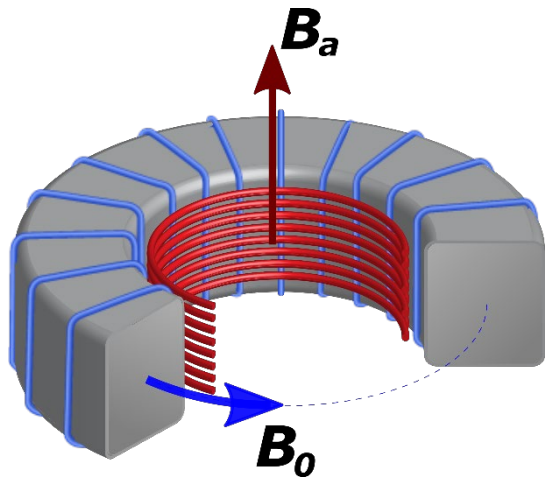


sensitivity limited by amplifier imprecision noise

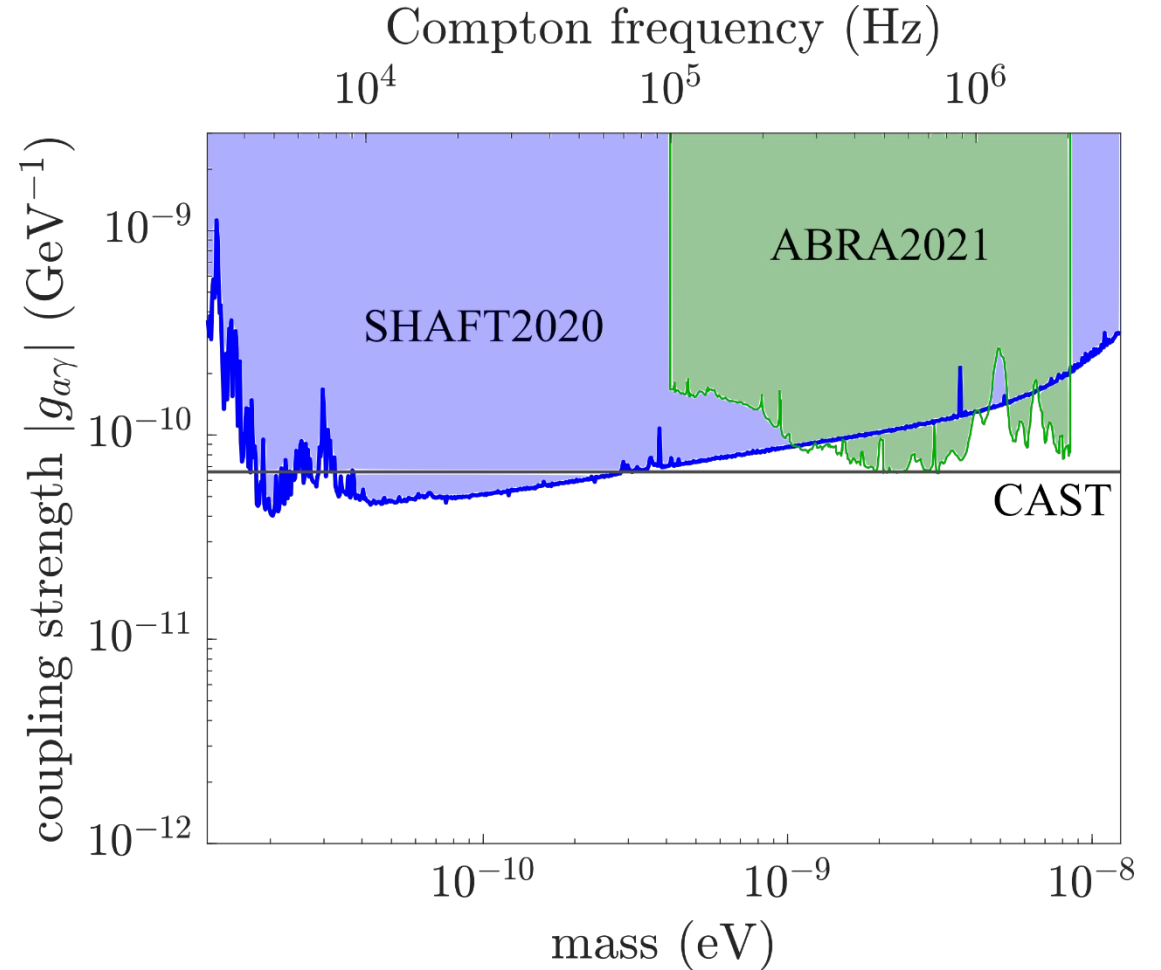
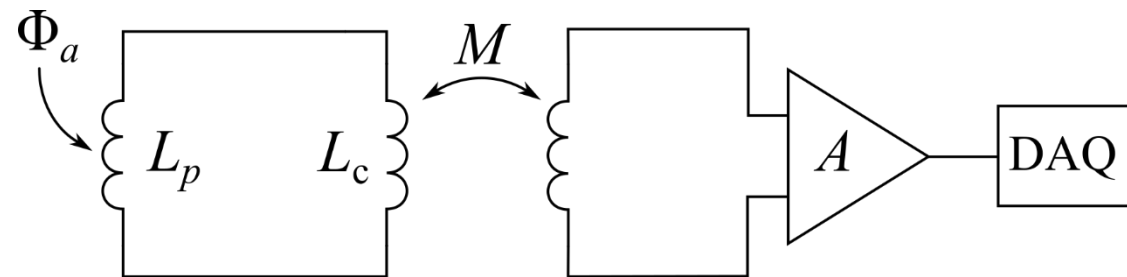
[A. Gramolin et al., *Nature Physics* **17**, 79 (2021)]
[C. Salemi et al., *Phys. Rev. Lett.* **127**, 081801 (2021)]



Experimental setup, broadband searches: SHAFT, ABRA



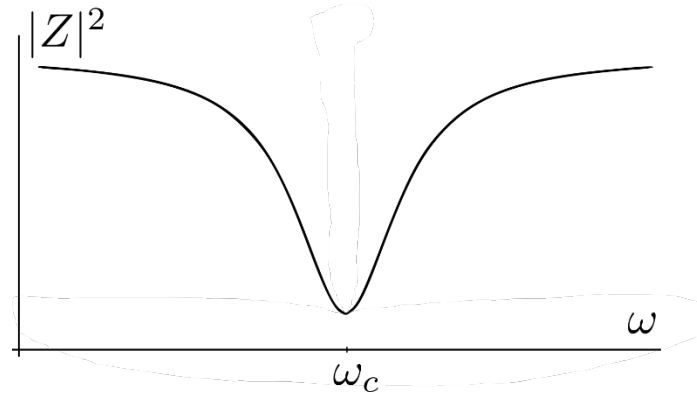
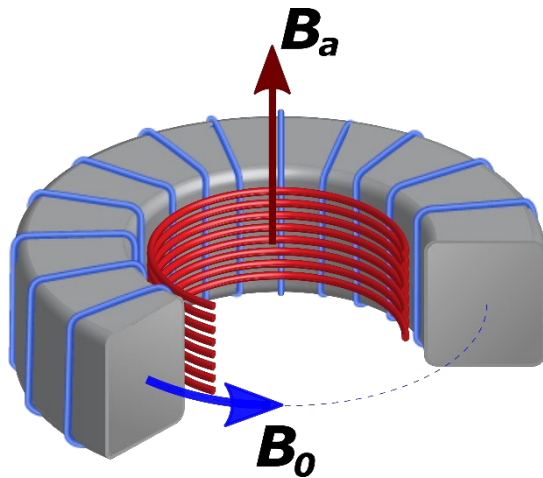
$\Phi_a \rightarrow$ magnetic flux due to axion-like dark matter



sensitivity limited by
amplifier imprecision noise

Experimental setup, resonant searches: DM radio

$$a(t) = a_0 \cos \omega_a t$$



search for unknown axion mass
(Compton frequency) is performed by
scanning the resonance frequency

➔ this is what makes these searches hard

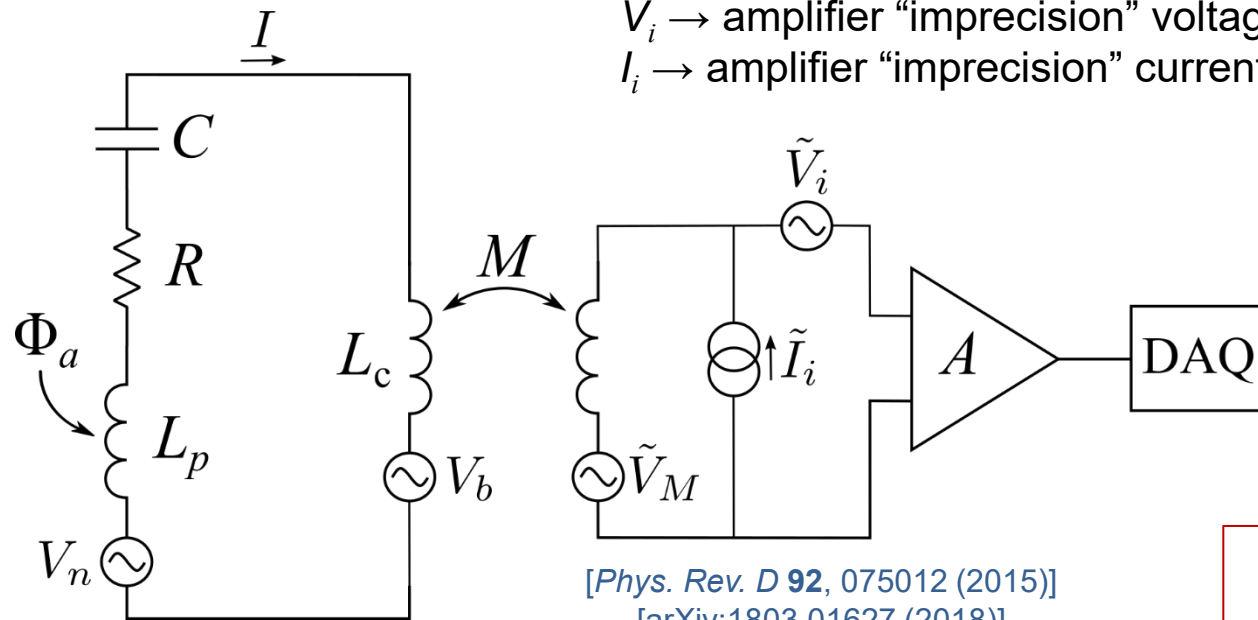
standard quantum limit
(SQL)

$$N(\omega) = \frac{1}{e^{\hbar\omega/k_B T} - 1} + \frac{1}{2}$$

in the lumped element regime $\hbar\omega \lesssim k_B T$

➔ sensitivity is limited by thermal noise

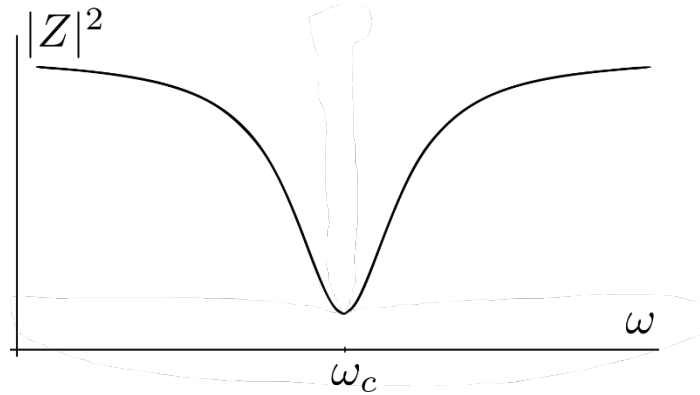
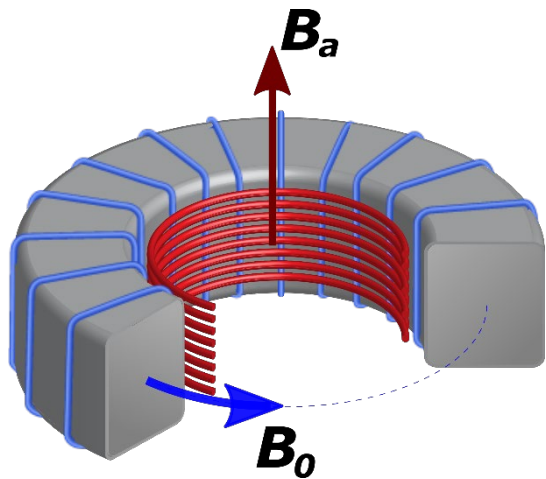
$V_n \rightarrow$ thermal + quantum noise
 $V_b \rightarrow$ back-action noise
 $V_i \rightarrow$ amplifier “imprecision” voltage noise
 $I_i \rightarrow$ amplifier “imprecision” current noise



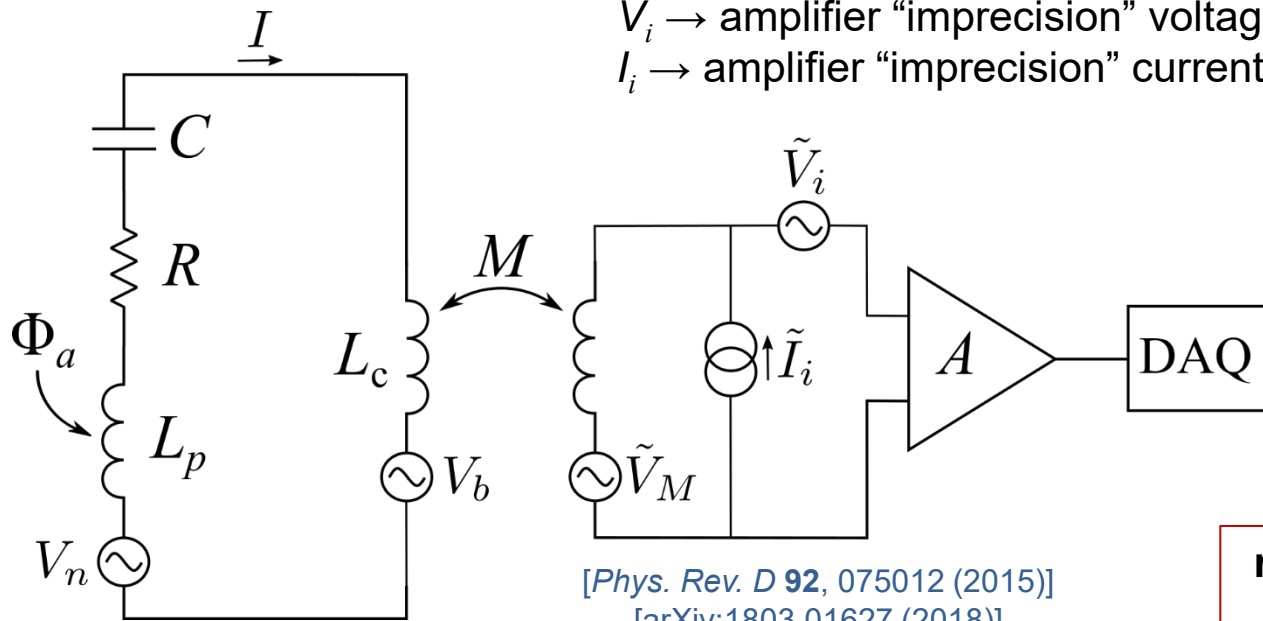
[*Phys. Rev. D* **92**, 075012 (2015)]
[arXiv:1803.01627 (2018)]

resonant pickup circuit → sensitivity is limited by thermal noise;
amplifier imprecision and back-action limits sensitivity bandwidth

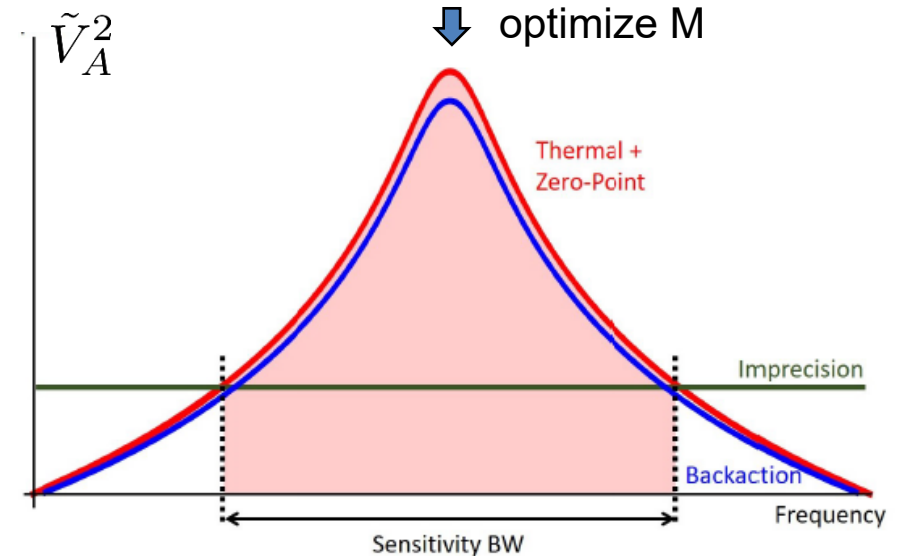
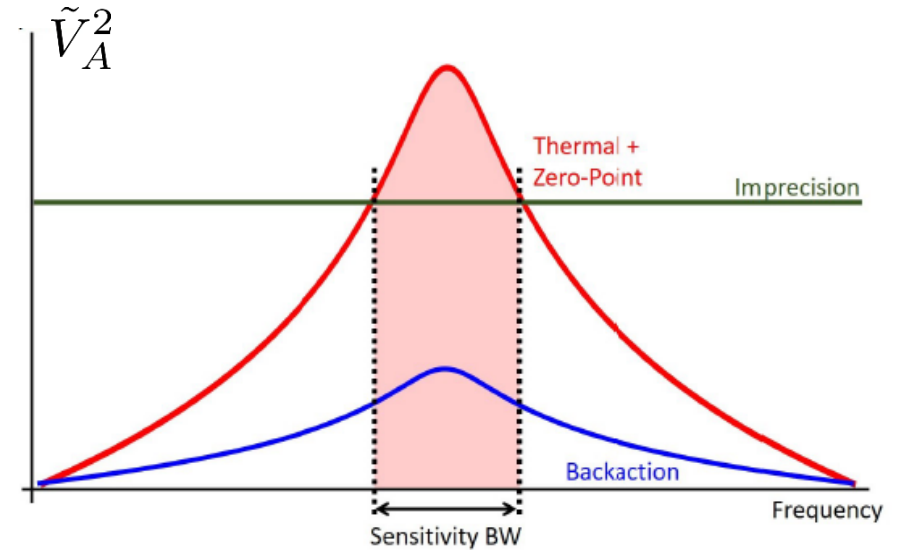
Experimental setup, resonant searches: DM radio



- $V_n \rightarrow$ thermal + quantum noise
- $V_b \rightarrow$ back-action noise
- $V_i \rightarrow$ amplifier "imprecision" voltage noise
- $I_i \rightarrow$ amplifier "imprecision" current noise

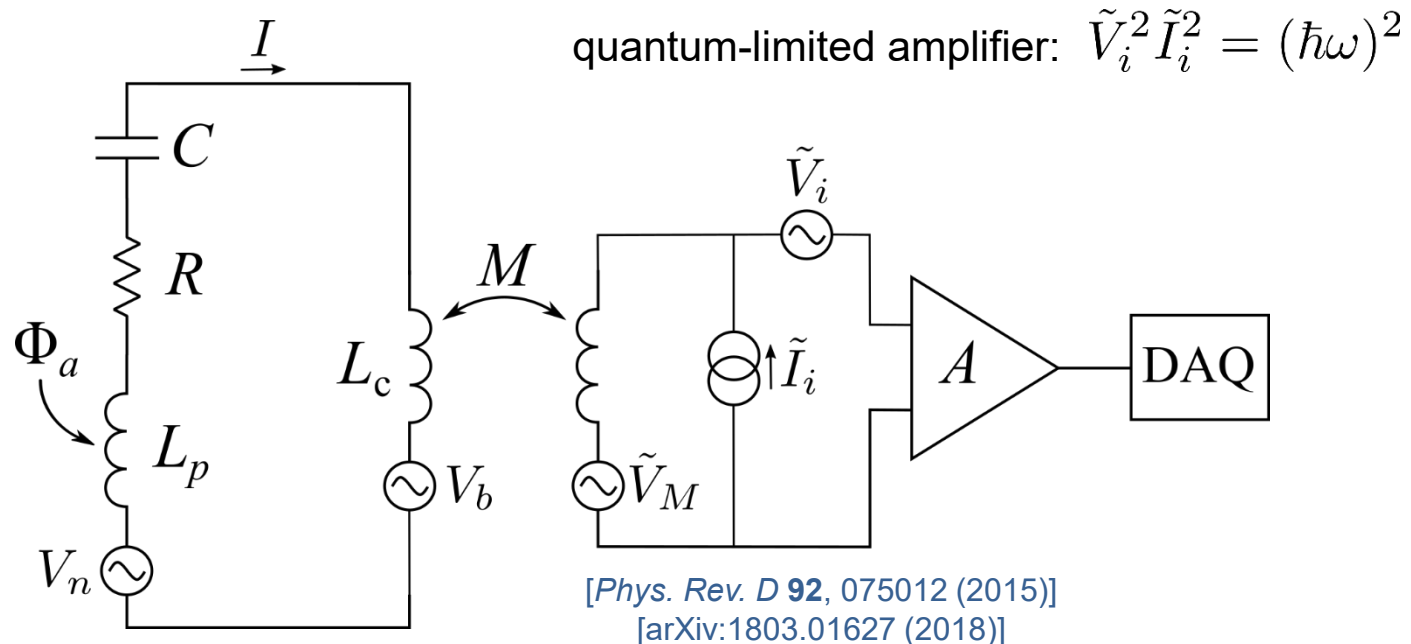
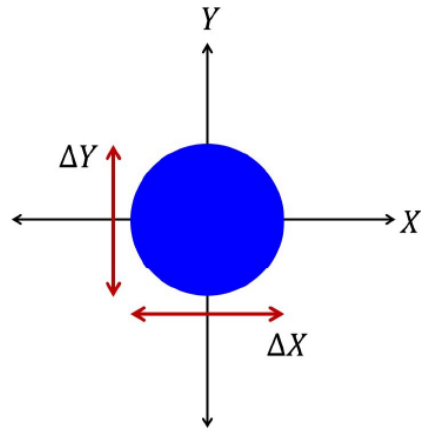
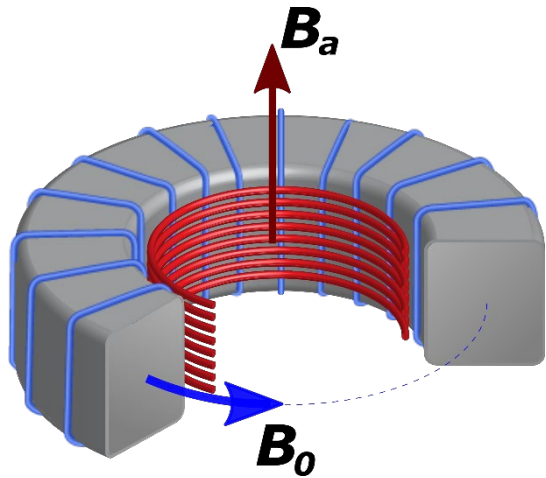


[*Phys. Rev. D* **92**, 075012 (2015)]
[arXiv:1803.01627 (2018)]

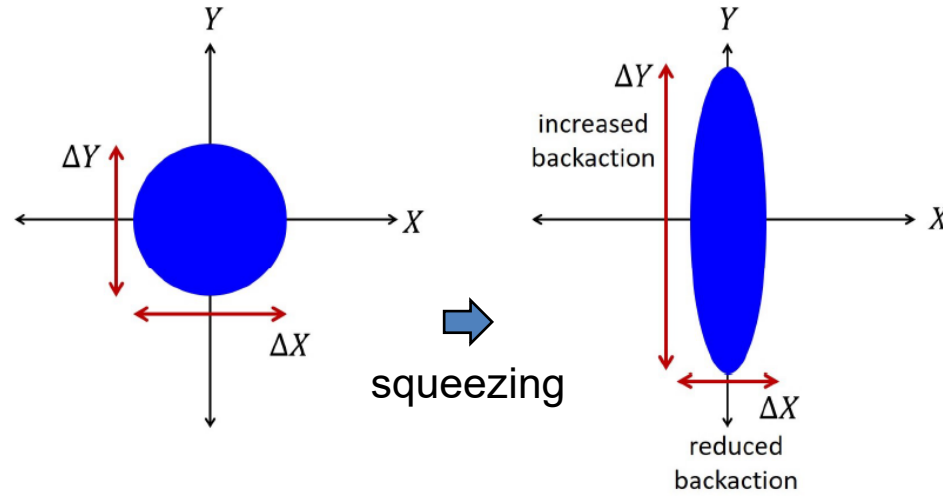
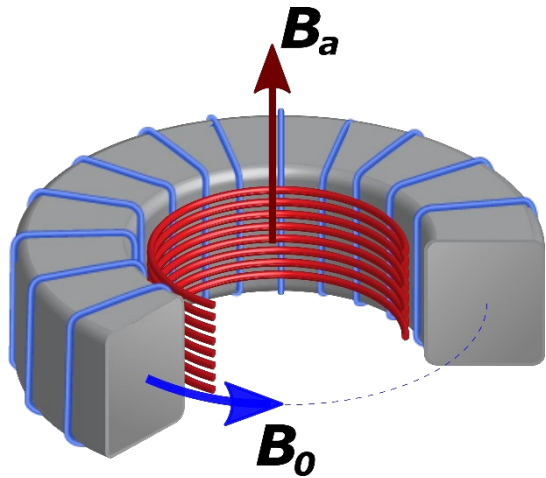


resonant pickup circuit \rightarrow sensitivity is limited by thermal noise;
amplifier imprecision and back-action limits sensitivity bandwidth

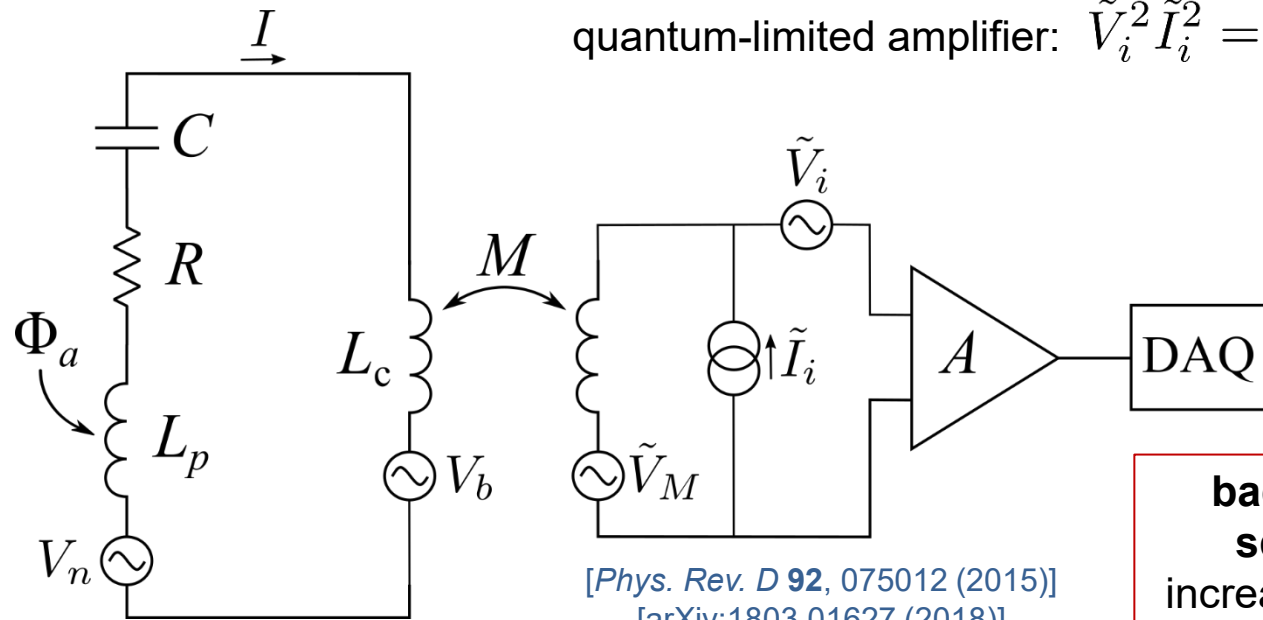
Quantizing the resonant LC circuit → back action evasion



Quantizing the resonant LC circuit → back action evasion

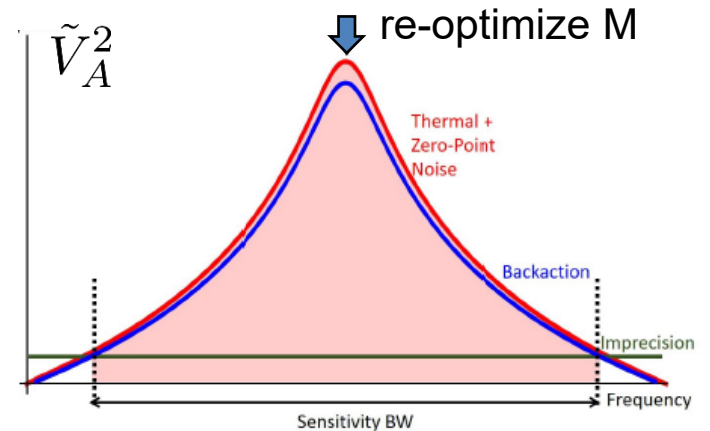
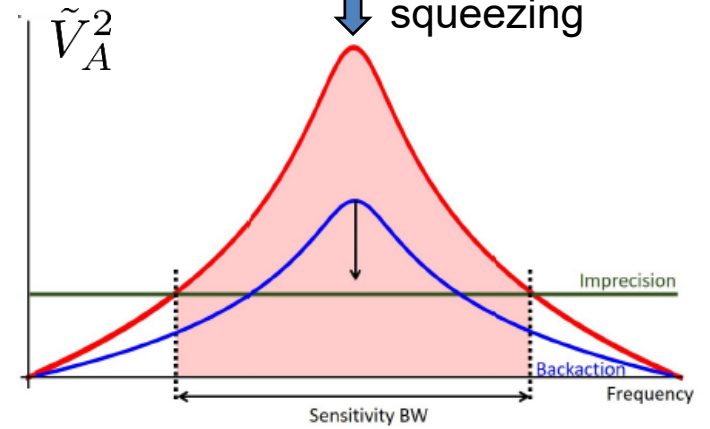
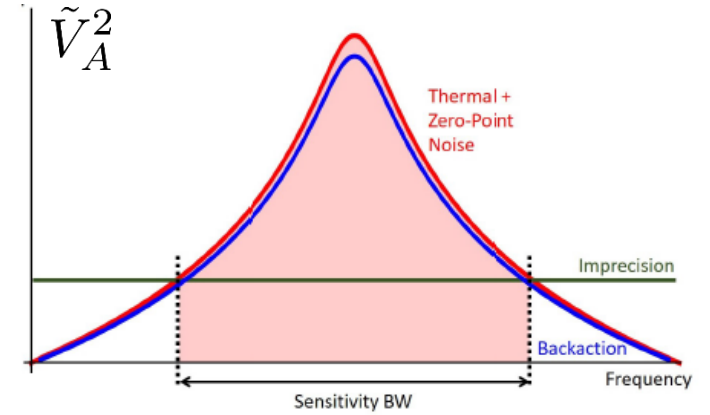


quantum-limited amplifier: $\tilde{V}_i^2 \tilde{I}_i^2 = (\hbar\omega)^2$



[Phys. Rev. D 92, 075012 (2015)]
[arXiv:1803.01627 (2018)]

back action evasion via squeezing can further increase sensitivity bandwidth



Cavity haloscope searches for axion-like dark matter

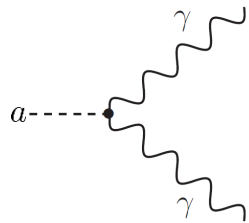
$$a(t) = a_0 \cos \omega_a t$$

goal: search for electromagnetic coupling of axion-like dark matter in mass (frequency) range where experiment size \approx wavelength

interaction with photons:

ALP field amplitude

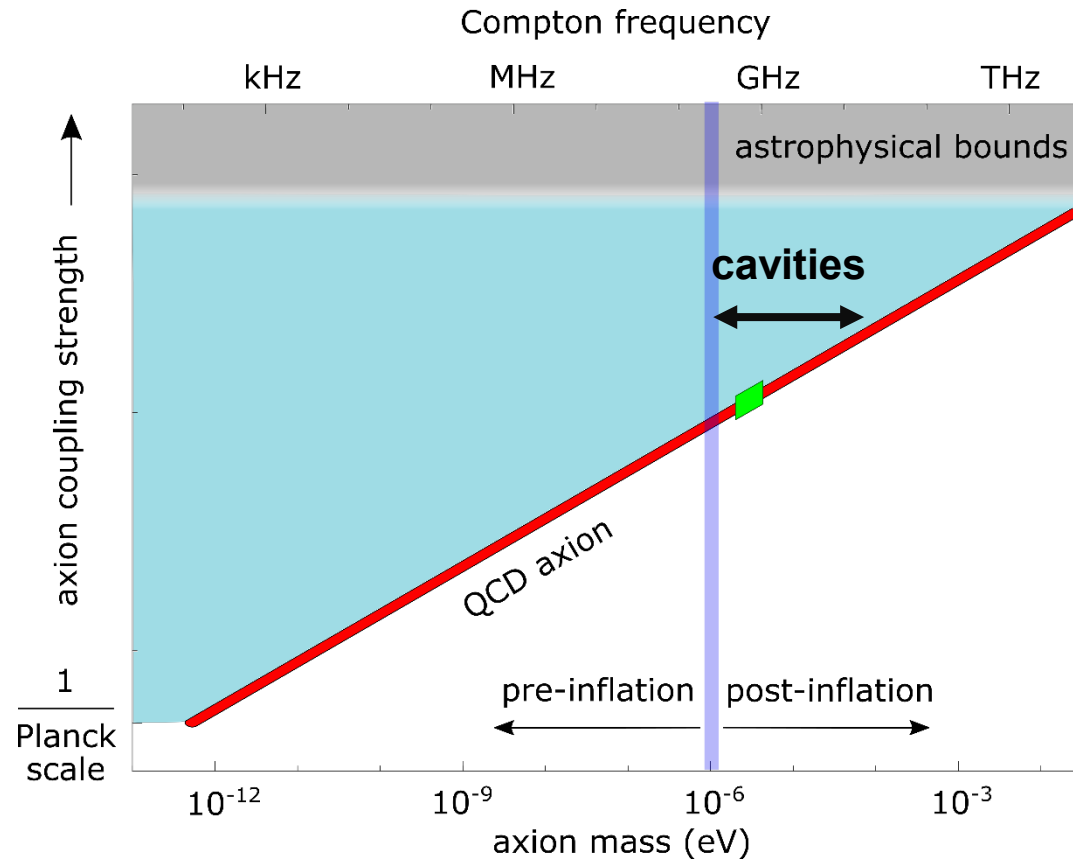
$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



symmetry breaking scale

$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP \leftrightarrow photon conversion in a magnetic field
- precision electromagnetic sensors



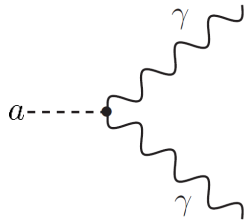
Cavity haloscope searches for axion-like dark matter

goal: search for electromagnetic coupling of axion-like dark matter in in mass (frequency) range where experiment size \approx wavelength

interaction with photons:

ALP field amplitude

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$



symmetry breaking scale

$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP \leftrightarrow photon conversion in a magnetic field
- precision electromagnetic sensors

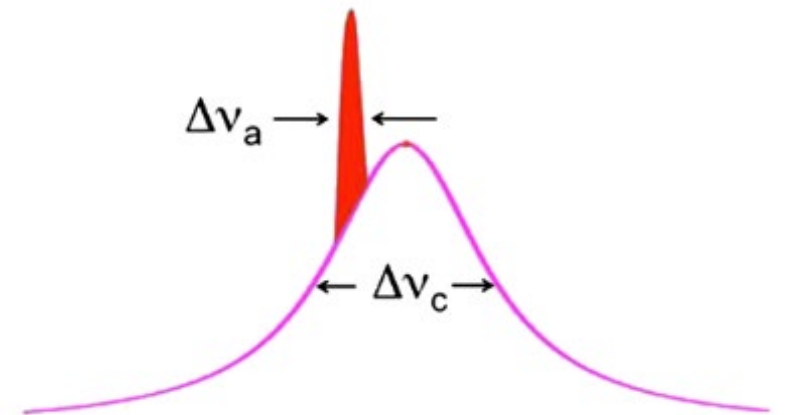
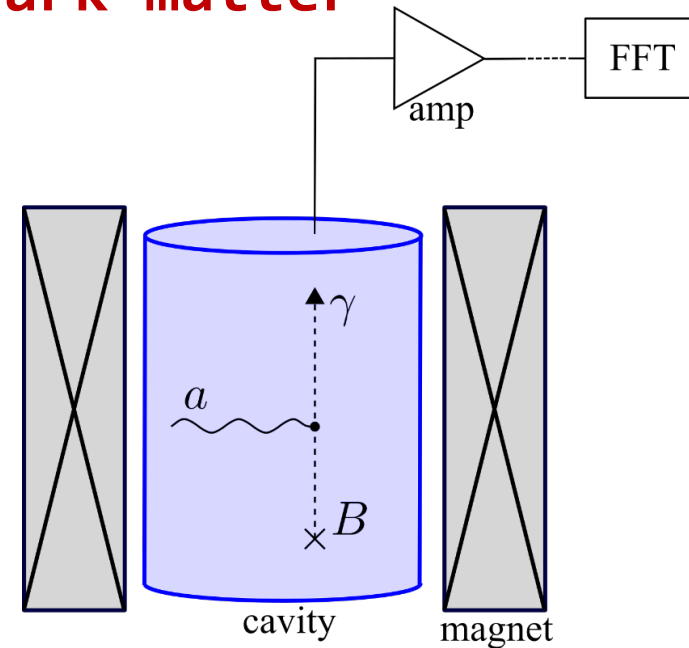
$$\text{axion signal power: } P_{a \rightarrow \gamma} = \frac{g_{a\gamma\gamma}^2 \rho_a}{m_a} \eta C B_0^2 V Q_c$$

$$\eta = \frac{\beta}{1 + \beta}$$

$$\beta = \frac{\text{power output}}{\text{power dissipated}}$$

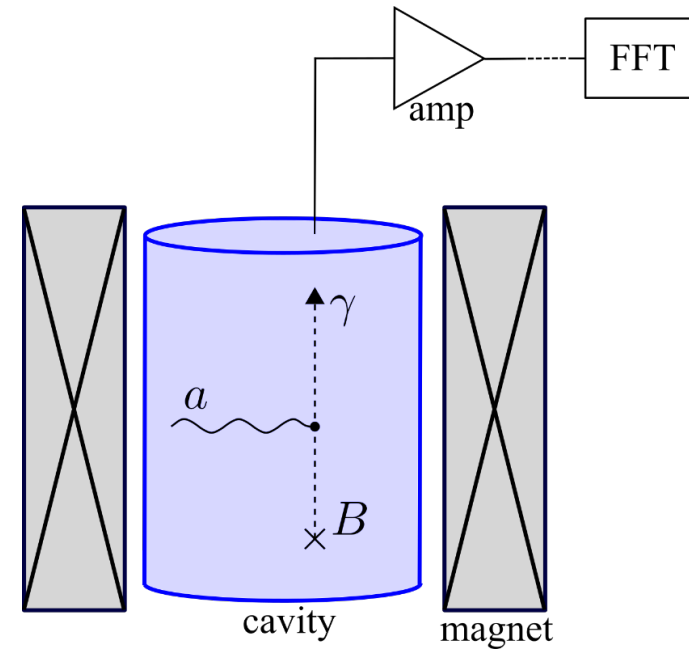
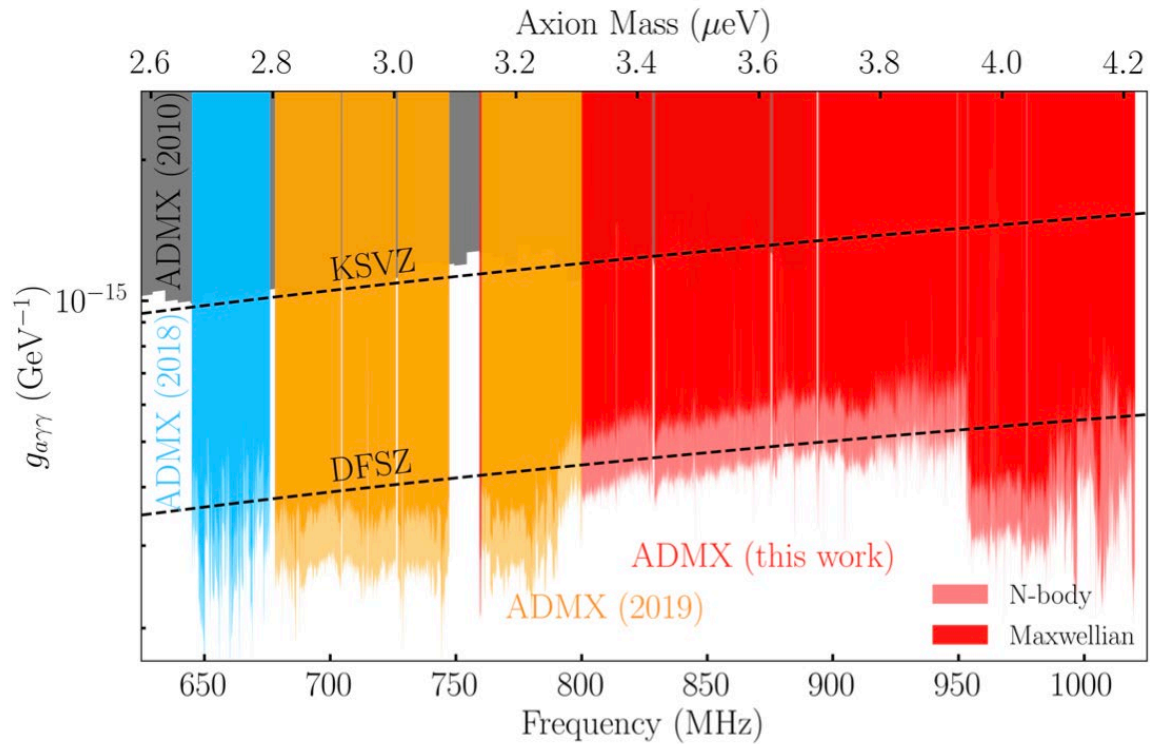
$$Q_c = \frac{Q}{1 + \beta}$$

↑
cavity coupling factor





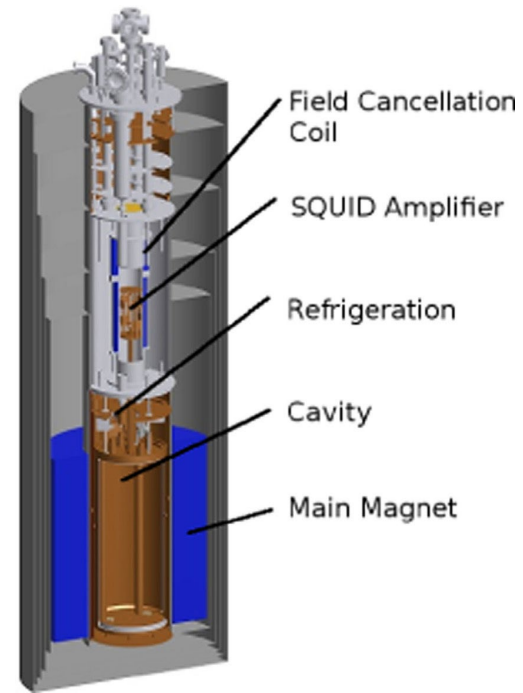
ADMX



axion signal power:
$$P_{a \rightarrow \gamma} = \frac{g_{a\gamma\gamma}^2 \rho_a}{m_a} \eta C B_0^2 V Q_c$$

$P_{a \rightarrow \gamma} \approx 10^{-23} \text{ W}$

sensitivity of a radio receiver $\approx 10^{-15} \text{ W}$

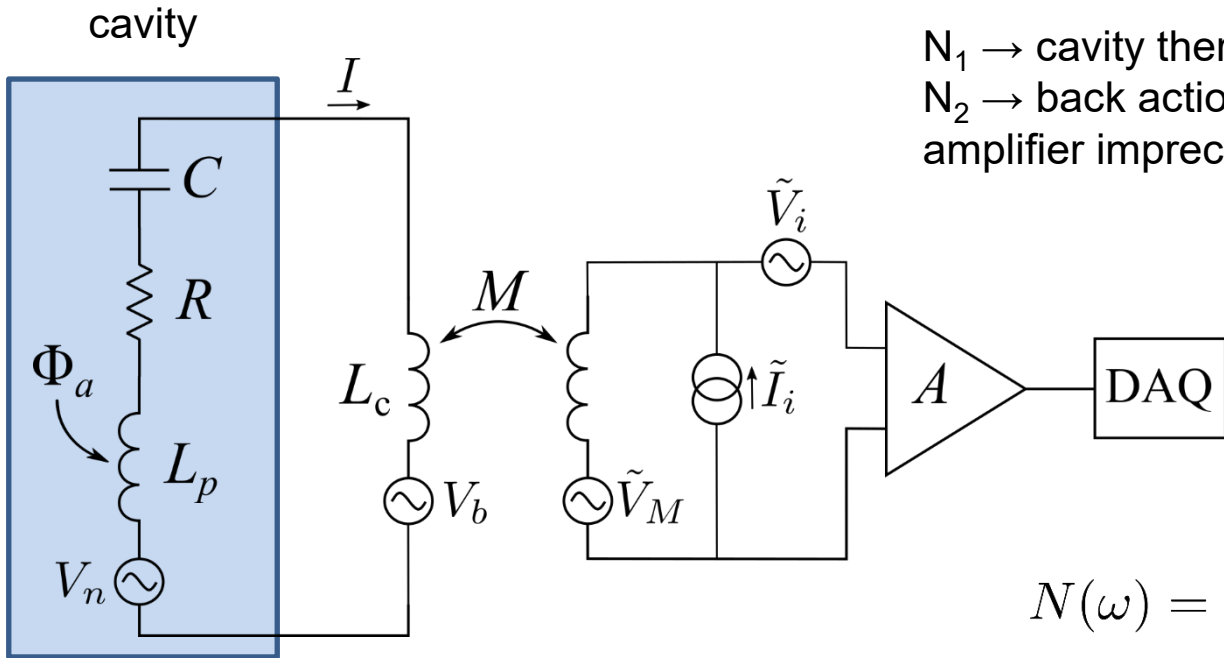


ADMX has started to explore the axion-photon coupling at the level of the QCD axion

[Phys. Rev. Lett. 127, 261803 (2021)]



Noise in cavity haloscopes



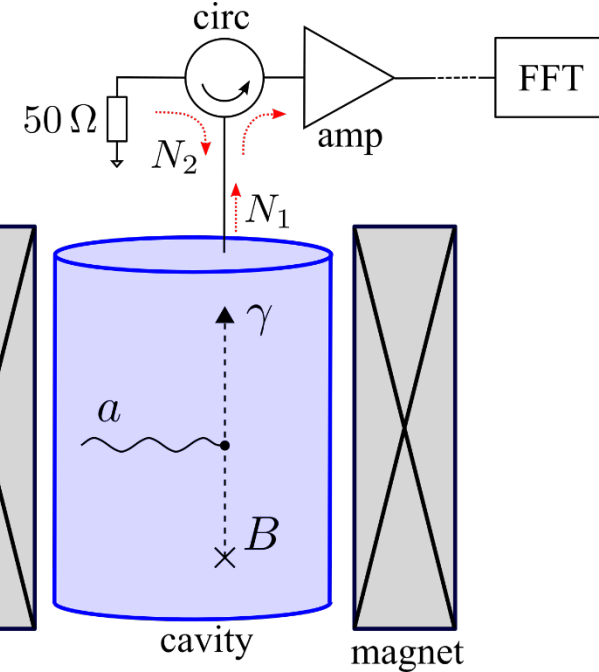
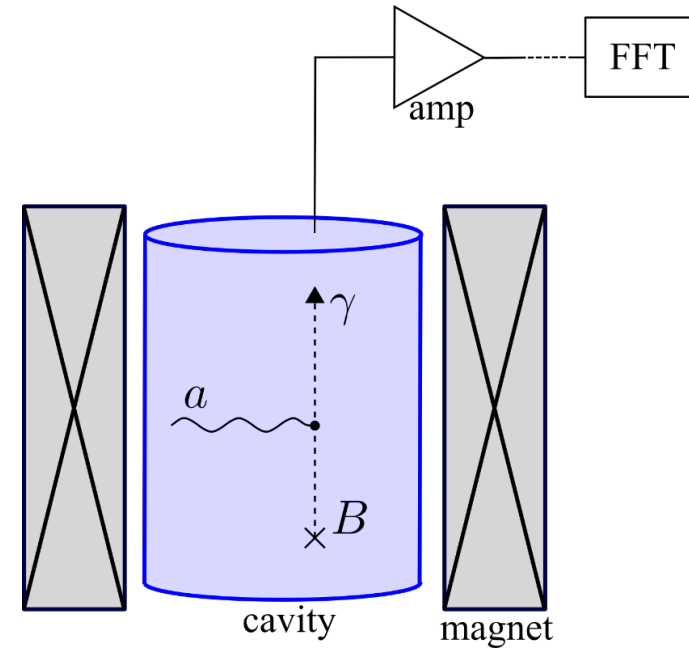
$N_1 \rightarrow$ cavity thermal + zero-point noise $\leftrightarrow V_n$
 $N_2 \rightarrow$ back action $\leftrightarrow V_b$
 amplifier imprecision noise is negligible

$$N(\omega) = \frac{1}{e^{\hbar\omega/k_B T} - 1} + \frac{1}{2}$$

axion signal power: $P_{a \rightarrow \gamma} = \frac{g_{a\gamma\gamma}^2 \rho_a}{m_a} \eta C B_0^2 V Q_c$

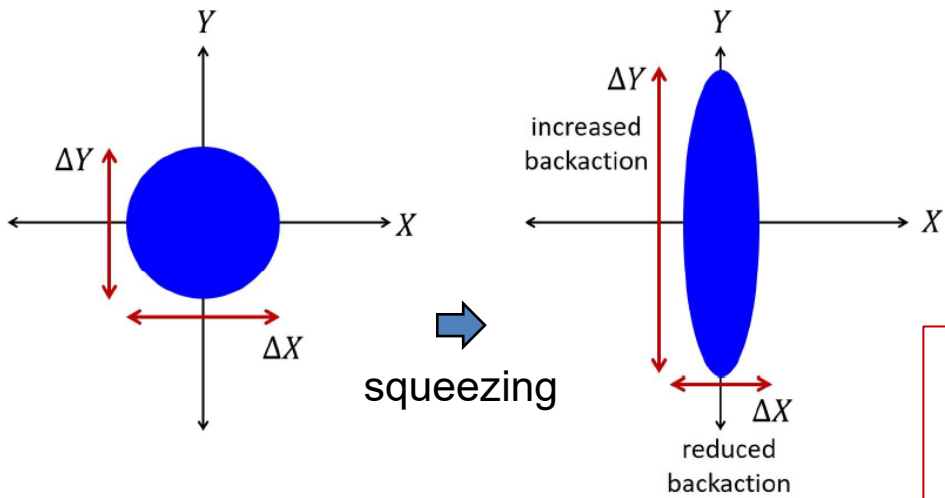
$P_{a \rightarrow \gamma} \approx 10^{-23} \text{ W}$

sensitivity of a radio receiver $\approx 10^{-15} \text{ W}$

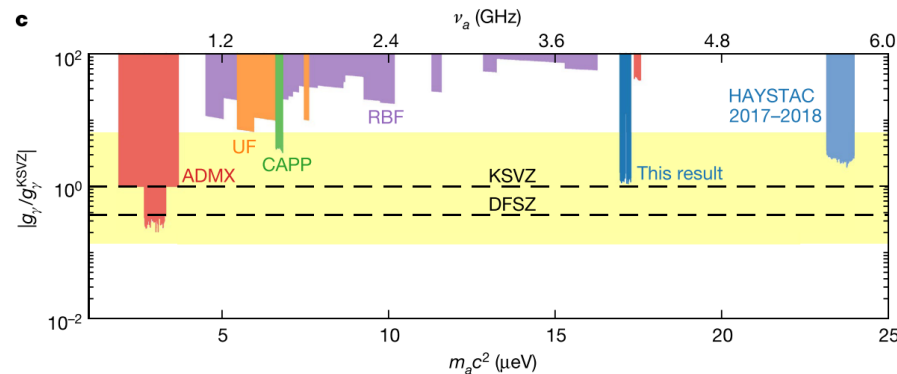
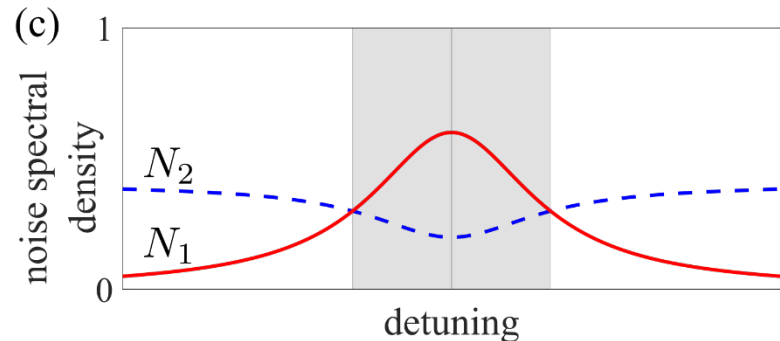
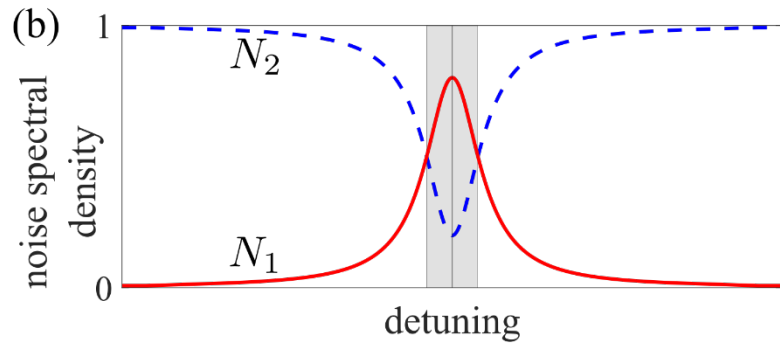




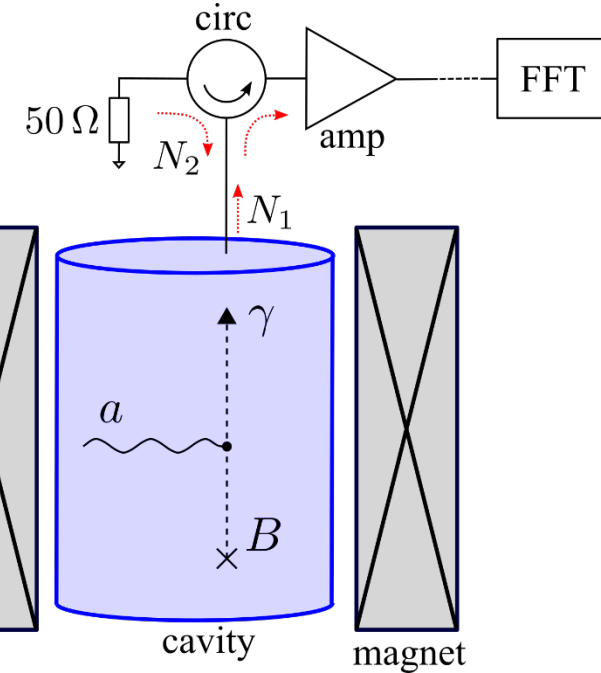
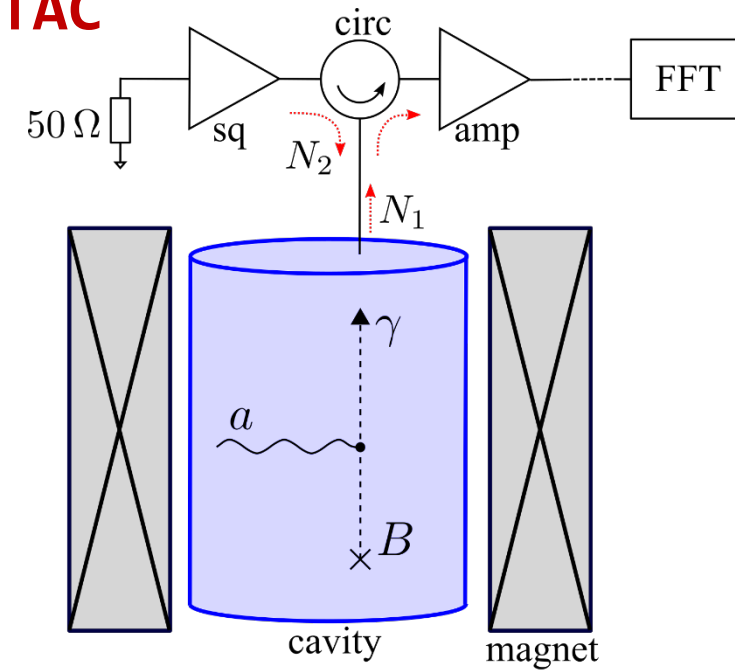
Haloscope At Yale Sensitive To Axion CDM: HAYSTAC



HAYSTAC uses squeezing to increase their sensitivity bandwidth, and thus speed up their cavity scan, by a factor of 1.9 compared to SQL



[K. Backes et al., *Nature* **590**, 238 (2021)]



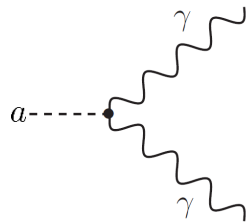
Counting single photons to search for axion-like dark matter

$$a(t) = a_0 \cos \omega_a t$$

interaction with photons:

ALP field
amplitude

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

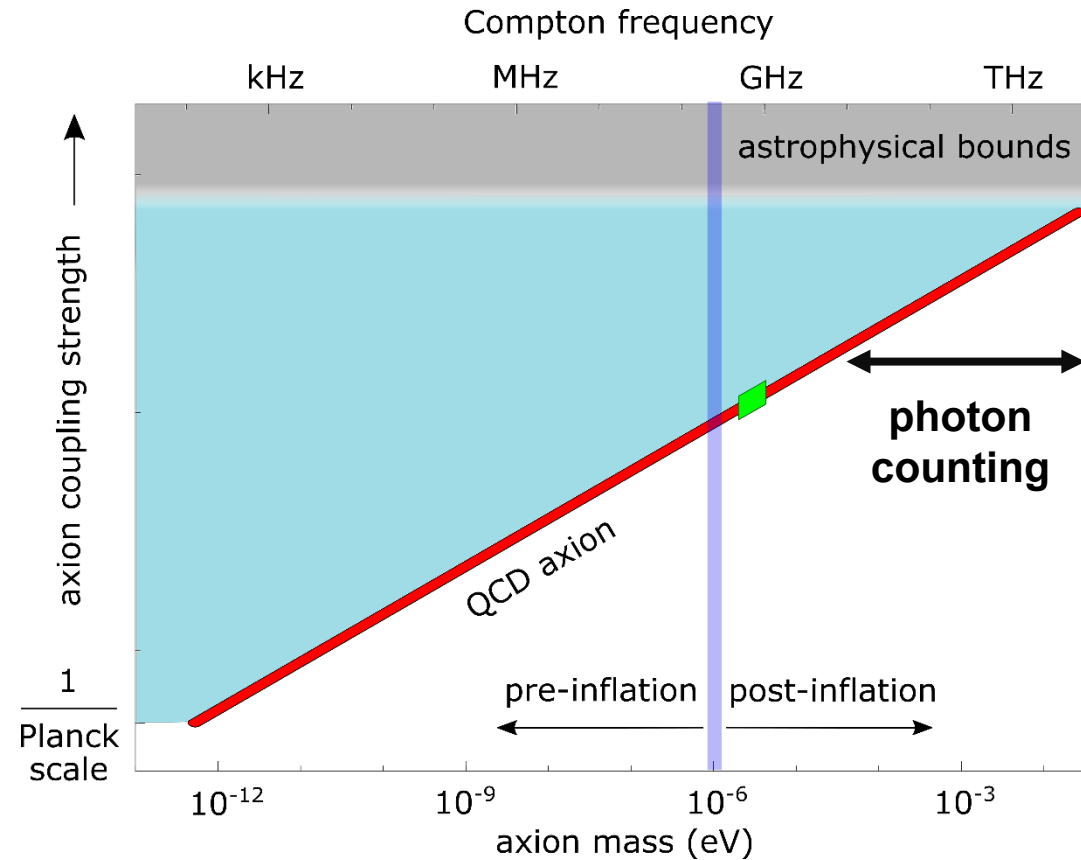


symmetry
breaking
scale

$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

- ALP ↔ photon conversion in a magnetic field
- precision electromagnetic sensors

at Compton frequencies ≥ 10 GHz, single photon counting (bolometric detection) becomes the favourable detection approach



[Phys. Rev. D **88**, 035020 (2013)]

[Phys. Rev. Lett. **126**, 141302 (2021)]

Summary: searches for axion-photon interaction

$$a(t) = a_0 \cos \omega_a t$$

interaction with photons:

ALP field
amplitude

$$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

symmetry
breaking
scale

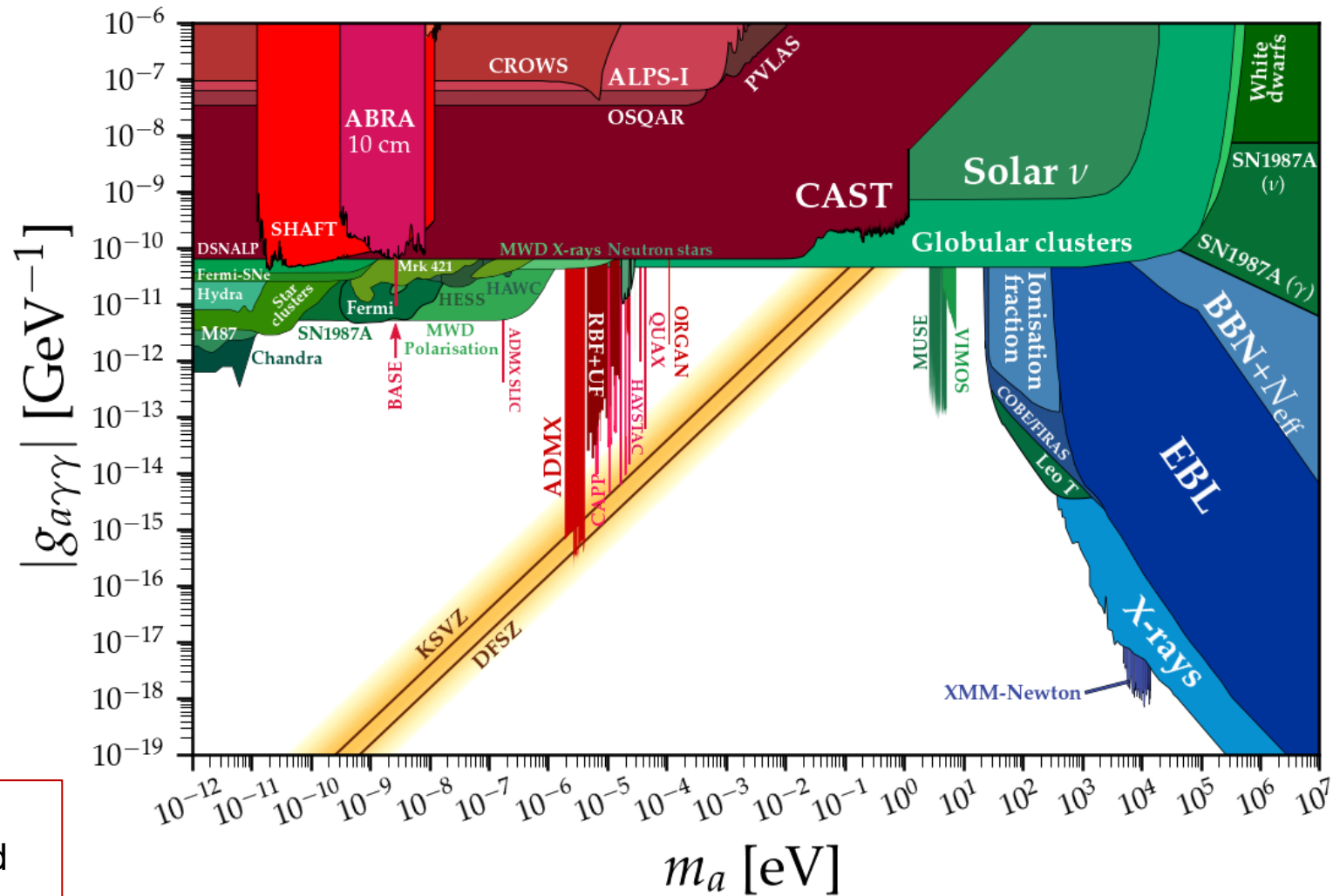
$$\mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$

→ ALP ↔ photon conversion in a magnetic field
→ precision electromagnetic sensors

key experimental parameters:

- magnetic field B → larger is better
- volume V → larger is better
- temperature → colder is better
- sensor noise and back-action

- resonant experiments are most sensitive
- on-resonance sensitivity is limited by thermal and quantum noise
- back-action evasion via squeezing can expand sensitive bandwidth, and thus speed up cavity scan





Tomorrow: searches for interactions of axions with nuclear spins

1. Pseudoscalar light particle: spin = 0, wide range of possible masses [Phys. Rev. D **98**, 035017 (2018)]
2. Proposed to solve the **strong CP problem** of Quantum Chromodynamics [Phys. Rev. Lett. **38**, 1440 (1977)]
3. Axion-like particles (ALPs) arise naturally in string theories, symmetries broken at GUT (10^{16} GeV) or Planck (10^{19} GeV) scales
4. Well-motivated and thoroughly-studied **dark matter** candidate: $a(t) = a_0 \cos \omega_a t$
5. Only 3 possible (non-gravitational) interactions with standard model particles:

interaction with photons:

ALP field amplitude $\rightarrow \frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}$

symmetry breaking scale $\rightarrow \mathcal{L}_{a\gamma\gamma} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$

→ ALP ↔ photon conversion in a magnetic field
→ precision electromagnetic sensors

ADMX, HAYSTAC, DMradio, SHAFT, ABRA,
ALPS, CAST, IAXO, CAPP, ORGAN, BREAD,
SLIC, LC circuit, MADMAX, KLASH, BRASS,
many others

interaction with gluons (strong-CP) defines QCD axion:

$$\frac{a}{f_a} G_{\mu\nu} \tilde{G}^{\mu\nu}$$

$$\mathcal{H}_{\text{EDM}} = g_d a \mathbf{E}^* \cdot \mathbf{I} / I$$

→ nuclear spin \mathbf{I} interacts with an oscillating electric dipole moment (EDM) $d_n = g_d a$ in presence of effective electric field \mathbf{E}^* .

CASPER-electric

interaction with leptons:

$$\frac{\partial_\mu a}{f_a} \bar{\psi}_\ell \gamma^\mu \gamma_5 \psi_\ell$$

$$\mathcal{H}_{aNN} = g_{aNN} \nabla a \cdot \mathbf{I}$$

→ nuclear spin \mathbf{I} interacts with an effective magnetic field ∇a .
co-magnetometers
force mediator → ARIADNE
electron spin → QUAX

CASPER-gradient