

**Massachusetts Institute of Technology**  
**Electrical Engineering and Computer Science Department**

**6.002 Electronic Circuits**

**Homework #6**  
**Handout F00-031**

**Issued: Oct. 12, 2000 - Due: Oct. 20, 2000**

**Read Sections 9.1 - 9.2**

**Exercise 6-1:** Exercise 1 from Chapter 9

**Exercise 6-2:** Exercise 2 from Chapter 9

**Problem 6-1:** (Exercise 5 from Chapter 9 with part e omitted)

Consider again the MOSFET amplifier shown in Figure 9.44 (See Notes). Assume as before that the amplifier is operated under the saturation discipline.

- a) What is the range of valid input voltages for the amplifier? What is the corresponding range of valid output voltages?
- b) Assuming we desire to use voltages of the form  $A\sin(\omega t)$  as AC inputs to the amplifier, determine the input bias point  $V_I$  for the amplifier which will allow for the maximum input swing under the saturation discipline. What is the corresponding output bias point voltage  $V_O$ ?
- c) What is the largest value of  $A$  that will allow the saturation region operation for the bias point determined in (b)?
- d) What is the small signal gain of the amplifier for the bias point determined in (b)?

**Problem 6-2:** (Problem 1 from Chapter 9 with part c omitted)

This problem studies the small-signal analysis of the MOSFET amplifier discussed in Problem 3 (Figure 8.40) in the previous chapter.

- a) First consider the biasing the amplifier. Determine  $V_{IN}$ , the bias component of  $v_{IN}$ , so that  $v_{OUT}$  is biased to  $V_{OUT}$  where  $0 < V_{OUT} < V_S$ . Find  $V_{MID}$ , the bias component of  $v_{MID}$  in the process.
- b) Next, let  $v_{IN} = V_{IN} + v_{in}$  where  $v_{in}$  is considered to be a small perturbation of  $v_{IN}$  around  $V_{IN}$ . Make the substitution for  $v_{IN}$  and linearize the resulting expression for  $v_{OUT}$ . Your answer should take the form  $v_{OUT} = V_{OUT} + v_{out}$ , where  $v_{out}$  takes the form  $v_{out} = Av_{in}$ . Note that  $v_{out}$  is the small-signal output and  $A$  is the small-signal gain. Derive an expression for  $A$ .

**Problem 6-3:** (Problem 2 from Chapter 9 with parts e and f omitted)

Consider again the buffer described in Problem 5 (Figure 8.41) in the previous chapter. Perform a small-signal analysis of this circuit according to the following steps. Assume that the MOSFET operates in its saturation region and continue to use the SCS MOSFET model.

- a) Draw the small-signal circuit model of the buffer.
- b) Show that the small-signal transconductance  $g_m$  of the MOSFET is given by

$$g_m = K(V_{IN} - V_{OUT} - V_T)$$

where  $V_{IN}$  and  $V_{OUT}$  are the bias, or operating-point, input and output voltages, respectively.

- c) Determine the small-signal gain of the buffer. That is, determine the ratio  $v_{out}/v_{in}$ .
- d) Determine the small-signal output resistance of the buffer. That is determine the equivalent resistance of the buffer at the output port of its small-signal model with  $v_{in} = 0$ . (Hint: This is the Thevenin equivalent resistance of the small-signal circuit looking into the output port.)

- e) Determine the small-signal input resistance of the buffer. That is determine the equivalent resistance of the buffer at the input port of its small-signal model. (Hint: This is the Thevenin equivalent resistance of the small-signal circuit looking into the input port.)