Massachusetts Institute of Technology Department of Electrical Engineering and Computer Science

6.002 – Electronic Circuits Fall 2002

Homework #11 Solutions

Introduction

This homework assignment focuses on the analysis and design of a system for playing back a digitally-stored audio signal. Additionally, this assignment serves as the pre-lab exercises for Lab #4, which will involve the construction, testing and demonstration of the audio playback system. Consequently, you should save a copy of your results for use during Lab #4.

A block diagram of the audio playback system is shown in Figure 1. At the center of the system is a digital memory in which 32,768 samples of the audio signal are stored. Each sample in the memory has a unique numerical address between 0 and 32,767, inclusive. Consecutive samples are stored at consecutive addresses.

To obtain 32,768 consecutive samples of the audio signal, 4.096 seconds of continuous analog audio signal are first sampled at an 8-kHz rate. The analog audio samples are then digitized by an 8-bit analog-to-digital converter. That is, the samples are quantized to take on one of 256 possible discrete digital values between 0 and 255, inclusive. Here, the digital value of 0 corresponds to the most positive signal voltage, and the digital value of 255 corresponds to the most negative signal voltage. The resulting digital data is then written into the memory.

To retrieve the stored audio signal samples in sequence at the proper rate, the memory is addressed by a counter which counts from 0 to 32,767 at an 8-kHz rate established by an external clock. After counting to 32,767 the counter returns to 0, and the retrieval process repeats itself. As the memory address increments, the corresponding data appears at the memory output. This data is converted back to an analog voltage in a piecewise constant manner by a digital-to-analog converter.

During the course of recording and playing back the analog audio signal, the signal is sampled in time, quantized in amplitude, and reconstructed in a piecewise constant manner. As you will learn in 6.003, this process introduces undesirable high-frequency components into the signal. To

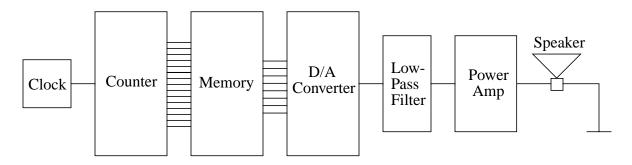


Figure 1: block diagram of the audio playback system.

minimize the perceived impact of these components, the signal is filtered by a low-pass filter after it is reconstructed by the digital-to-analog converter. Finally, the signal is amplified by a power amplifier which in turn drives a speaker. The power amplifier is necessary because the low-pass filter is not capable of driving the speaker directly.

In the course of this homework assignment you will analyze and design four of the functional blocks shown in Figure 1. These blocks are the clock, the digital-to-analog converter, the low-pass filter and the power amplifier. In Lab #4, you will construct these blocks and verify that they perform as desired. Then, you will combine them with the counter, the read-only memory and the speaker to construct and demonstrate the entire audio play-back system. Since you will construct the system from the components in your 6.002 lab kit, your design of the blocks must account for the fact that the available components are limited.

Problem 1: The Clock

The circuit shown in Figure 2 is the system clock, which is a square-wave oscillator followed by a CMOS inverter; the inverter functions only as a buffer. The oscillator is constructed from another CMOS inverter, a resistor and a capacitor. Both inverters are powered between the positive supply voltage $V_{\rm S}$ and ground, and both exhibit the hysteretic input-output characteristic defined in the figure. The inverters are otherwise ideal.

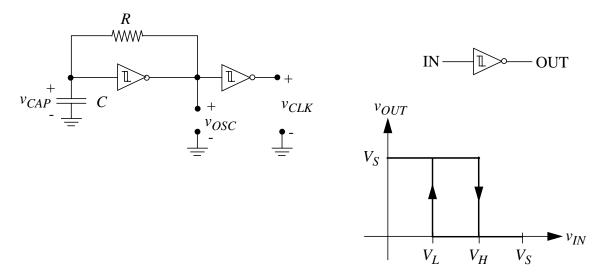


Figure 2: the system clock.

(A) Assume that v_{CAP} has just charged up to V_{H} so that v_{OSC} has just switched to 0 V. How much time elapses before v_{CAP} decays to V_{L} , which in turn causes v_{OSC} to switch to V_{S} ?

ANSWER: As shown in the figure below, the capacitor now begins to discharge from $V_{\rm H}$ toward zero. The capacitor voltage is given by

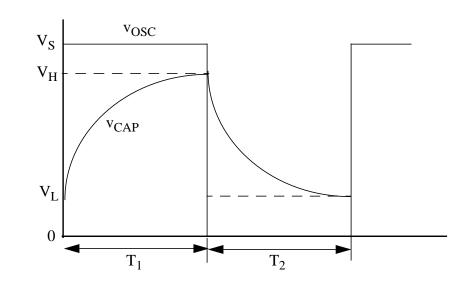
$$v_{\rm CAP} = V_H \cdot e^{-t/RC}$$

We want to solve for the time at which $v_{\text{CAP}} = V_L$. This time is denoted by T_2 in the figure.

$$V_{\rm L} = V_{\rm H} \cdot e^{-T_2/RC}$$

Solve to get:

$$T_2 = RC \cdot ln \frac{V_{\rm H}}{V_{\rm L}}$$



(B) Assume that v_{CAP} has just decayed to V_{L} so that v_{OSC} has just switched to V_{S} . How much time elapses before v_{CAP} charges up to V_{H} , which in turn causes v_{OSC} to switch to 0 V?

ANSWER: Now the capacitor starts to charge from $V_{\rm L}$ toward $V_{\rm S}$. The solution for the capacitor voltage is:

$$v_{\rm CAP} = V_{\rm S} + (V_{\rm L} - V_{\rm S}) \cdot e^{-t/RC}$$

We want to solve for the time at which v_{CAP} reaches V_{H} . This time is denoted by T_1 in the figure.

$$V_H = V_{\rm S} + (V_{\rm L} - V_{\rm S}) \cdot e^{-T_1/RC}$$

Solve to get

$$T_1 = RC \cdot ln \frac{V_{\rm S} - V_{\rm L}}{V_{\rm S} - V_{\rm H}}$$

(C) Determine the frequency of the oscillator in terms of $R, C, V_{\rm L}, V_{\rm H}$ and $V_{\rm S}$.

ANSWER: The period T of the oscillator is

$$T = T_1 + T_2 = RC \cdot ln \frac{(V_{\rm S} - V_{\rm L})V_{\rm H}}{(V_{\rm S} - V_{\rm H})V_{\rm L}}$$

The frequency f is the inverse of the period and is given by

$$f = \frac{1}{T} = \frac{1}{RC \cdot ln \frac{(V_{\rm S} - V_{\rm L})V_{\rm H}}{(V_{\rm S} - V_{\rm H})V_{\rm L}}}$$

(D) Assume that $V_{\rm L} = 1.8$ V, $V_{\rm H} = 3.0$ V and $V_{\rm S} = 5.0$ V. Choose values for R and C so that the oscillator oscillates at or very near 8-kHz. Since oscillator frequency alone under specifies R

and C, there is no single correct choice. Therefore, choose values for R and C that are easily implemented with the components in the 6.002 lab kit.

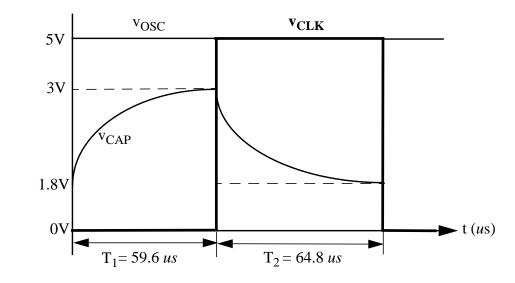
ANSWER: f = 8KHz is equivalent to $T = 1/f = 125\mu s$. Pick $C = .0047\mu F$, we solve for R using the equation in part (C):

$$R = \frac{T}{C \cdot ln \frac{(V_{\rm S} - V_{\rm L})V_{\rm H}}{(V_{\rm S} - V_{\rm H})V_{\rm L}}} = 27K\Omega$$

which is a standard resistor value.

(E) For the choice of R and C from Part (D), sketch and clearly label a single graph that displays v_{CAP} , v_{OSC} and v_{CLK} as a function of time over one period of oscillation.

ANSWER: Using equations developed in (A) and (B) we get $T_1 = 59.6\mu s$ and $T_2 = 64.8\mu s$. We notice that $T_1 \neq T_2$. This does not affect the operation of the clock because the counter is triggered by either the rising or the falling edge but not both.



Problem 2: The Digital-To-Analog Converter

The circuit shown in Figure 3 is the digital-to-analog converter. The voltage sources v_{DB0} through v_{DB7} represent the voltages supplied by the eight data bits of the digital memory, DB0 through DB7. These voltages will be approximately 5 V when the corresponding data bit is a logical high, and approximately 0 V when the corresponding data bit is a logical low. The voltage v_{OFF} , which is set by a potentiometer, is an offset voltage that is used to center the output of the converter around 0 V. Assume that the op-amp in the converter is ideal.

(A) Determine v_{DAC} as a function of v_{DB0} through v_{DB7} , and v_{OFF} . Hint: use superposition.

Answer:

Set $v_{OFF} = 0$ and compute the current going through R_8 ,

$$i_{-} = \frac{0 - v_{DAC-}}{R_8} = \sum_{i=0}^{7} \frac{v_{DBi}}{R_i}$$

This gives us the portion of the output voltage contributed by the inputs,

$$v_{DAC-} = -\sum_{i=0}^{7} \frac{R_8}{R_i} v_{DBi}$$

Now setting $v_{DBi} = 0$, we get the portion of the output voltage contributed by v_{OFF} ,

$$v_{DAC+} = v_{OFF} \cdot \left(1 + \frac{R_8}{R_-}\right)$$

where $R_{-} = R_0 ||R_1||...||R_7$.

The total output voltage is

$$v_{DAC} = v_{DAC-} + v_{DAC+}$$
$$v_{DAC} = -\sum_{i=0}^{7} \frac{R_8}{R_i} v_{DBi} + v_{OFF} \cdot (1 + \frac{R_8}{R_-})$$

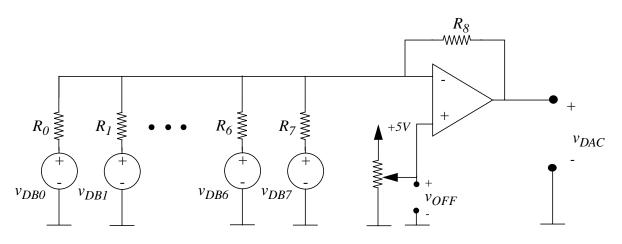


Figure 3: the digital-to-analog converter.

(B) With $v_{\text{OFF}} = 0$ V, the output of the digital-to-analog converter should span the range of 0 V to -2.5 V. Thus, the output of the converter should be given by

$$v_{\text{DAC}} = -2.5 \text{ V} \sum_{i=0}^{7} \frac{2^i}{255} \text{DB}i$$

where each data bit DB*i* takes on the numerical value of 1 when high and 0 when low. In this manner, each successive data bit from DB0 to DB7 is given a voltage weighting twice that of the preceding data bit, making it possible for the converter to output voltages from 0 V to -2.5 V in steps of -2.5/255 V. Given this, what must be the relationships between the values of R_0 through R_7 , and R_8 ?

The voltage rating of the speaker is approximately ± 1.25 V. Since the low-pass filter and power amplifier between the converter and the speaker both have unity voltage gain over the frequency range of interest, the output range of the analog-to-digital converter must be designed to match the speaker rating. This is why the range is chosen to be 0 V to -2.5 V, with $v_{\rm OFF} = 0$. Note further that the output range of the converter is negative. This is because the converter is based upon the inverting amplifier configuration.

Answer:

$$R_0 = 2R_2 = 4R_2 = \dots = 128R_7$$

Substituting DB0=1, we get

$$\frac{-2.5}{255} = -\frac{R_8}{R_0} 5 \Rightarrow \frac{R_8}{R_0} = \frac{1}{510}$$

(C) The role of v_{OFF} is to offset the output of the digital-to-analog converter so that it is centered around 0 V. That is, with DB0 through DB7 all low, v_{DAC} should be 1.25 V, and with DB0 through DB7 all high, v_{DAC} should be -1.25 V. Given this, what must be the value of v_{OFF} ?

Answer:

$$R_{-} = R_{0}||R_{1}||...||R_{7}$$

= $R_{0}(1||\frac{1}{2}||\frac{1}{4}||...||\frac{1}{128})$
= $R_{0}/(1+2+4+...+128)$
= $R_{0}/255$

We want to have $V_{DAC} = 1.25$ when $V_{DBi} = 0$. This leads to

$$1.25 = v_{OFF} \cdot (1 + \frac{R_8}{R_-}) \\ = v_{OFF} \cdot (1 + 255 \frac{R_8}{R_0}) \\ v_{OFF} = .83V$$

(D) Based on the results of Part (B), choose values for R_0 through R_7 , and R_8 . Since the results of Part (B) under specify R_0 through R_7 , and R_8 , there is no single correct choice. Further, since arbitrary valued resistors are not available, the results of Part (B) can not be satisfied exactly. Therefore, choose values for R_0 through R_7 , and R_8 that are easily implemented with the components in the 6.002 lab kit, and that satisfy the results of Part (B) as best as possible.

Answer:

The following is a set of possible values.

Resistor	ideal value(Ω)	actual values (Ω)
R_0	$154 \mathrm{K}$	$150 \mathrm{K}$
R_1	$76.8 \mathrm{K}$	82K
R_2	$38.4\mathrm{K}$	39K
R_3	$19.2 \mathrm{K}$	18K
R_4	$9.6\mathrm{K}$	10K
R_5	$4.8\mathrm{K}$	$4.7\mathrm{K}$
R_6	$2.4\mathrm{K}$	$2.2\mathrm{K}$
R_7	1.2K	1.2K
R_8	302	$560 \parallel 680$

Problem 3: The Low-Pass Filter

The circuit shown in Figure 4 is the low-pass filter. It is a second-order filter, and is driven by the output of the digital-to-analog converter. Its purpose is to remove the high-frequency components of the audio signal that result from the sampling, quantization and reconstruction of that signal. Assume that the op-amp in the filter is ideal.

(A) Assume that the low-pass filter operates in sinusoidal steady state with $v_{\text{DAC}} = \Re\{\tilde{v}_{\text{DAC}}e^{j\omega t}\}$ and $v_{\text{LPF}} = \Re\{\tilde{v}_{\text{LPF}}e^{j\omega t}\}$ where \tilde{v}_{DAC} and \tilde{v}_{LPF} are complex amplitudes. Find the input-output transfer function $H_{\text{LPF}}(\omega)$ of the filter where $H_{\text{LPF}}(\omega) \equiv \tilde{v}_{\text{LPF}}/\tilde{v}_{\text{DAC}}$.

ANSWER: Unfortunately, there is no simple way to solve this circuit. We are forced to return to the Node Method. There are three nodes in the circuit, but the Ideal Op-Amp Model allows us to assume that $v_+ = v_- = v_{\text{LPF}}$. By using this simplification, we can avoid writing a node equation for the output node. I am defining the internal node as \tilde{e} .

For the v_+ node:

$$\frac{\tilde{v}_{\rm LPF}}{\frac{1}{j\omega C_2}} + \frac{\tilde{v}_{\rm LPF} - \tilde{e}}{R} = 0$$

For the v_{-} node:

$$\frac{\tilde{v}_{\rm LPF} - \tilde{e}}{\frac{1}{j\omega C_1}} + \frac{\tilde{v}_{\rm LPF} - \tilde{e}}{R} + \frac{\tilde{v}_{\rm DAC} - \tilde{e}}{R} = 0$$

We choose to solve the first equation for \tilde{e} and substitute into the second. Mathematically, it is irrelevant how we solve, but practically, it tends to be easier to solve the most simple equation first, and substitute into more and more complicated expressions.

$$\tilde{e} = \tilde{v}_{\text{LPF}}(1 + j\omega RC_2)$$

Substituting in for \tilde{e} and factoring out a \tilde{v}_{LPF} gives us:

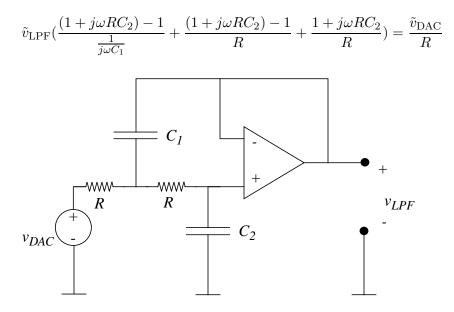


Figure 4: the low-pass filter.

Solving for $\frac{\tilde{v}_{\text{LPF}}}{\tilde{v}_{\text{DAC}}}$ and we have:

$$H_{\rm LPF}(\omega) = \frac{\tilde{v}_{\rm LPF}}{\tilde{v}_{\rm DAC}} = \frac{1}{1 - \omega^2 R^2 C_1 C_2 + 2j\omega R C_2}$$

(B) Using the results of Part (A), find the magnitude and phase of $H_{\rm LPF}(\omega)$.

ANSWER:

$$|H_{\rm LPF}(\omega)| = \frac{1}{\sqrt{(1 - \omega^2 R^2 C_1 C_2)^2 + (2\omega R C_2)^2}}$$

$$\angle H_{\rm LPF}(\omega) = 0 - \arctan \frac{2\omega R C_2}{1 - \omega^2 R^2 C_1 C_2}$$

(C) There is no best design for the low-pass filter to meet the needs of the audio playback system. However, with the appropriate choice of C_1 , C_2 and R, the transfer function of one good design will take the form

$$|H_{\rm LPF}(\omega)| = \frac{1}{1 + (\omega/\omega_{\rm LPF})^2}$$

where ω_{LPF} is a specified frequency. For this design, show that the low-frequency and high-frequency asymptotes of $|H_{\text{LPF}}(\omega)|$ intersect at $\omega = \omega_{\text{LPF}}$, and therefore that ω_{LPF} is the frequency that delineates the pass band of the low-pass amplifier.

ANSWER: The low and high frequency asymptotes are calculated by including only the lowest and highest order ω terms respectively. Continue to simplify in this manner until you are left with only one term containing ω .

For $\omega \ll \omega_{\text{LPF}}$ we drop the ω term because it is much less than 1. The result is very simple:

$$H_{\rm LPF}(\omega \ll \omega_{\rm LPF}) \approx 1$$

For $\omega \gg \omega_{\rm LPF}$ we drop the 1 term because it is much less than ω . The result is still simple:

$$H_{\rm LPF}(\omega \ll \omega_{\rm LPF}) \approx \frac{1}{(\omega/\omega_{\rm LPF})^2}$$

Solving for the intercept of these equations gives the expected $\omega = \omega_{\text{LPF}}$. This is known as the cut-off frequency.

(D) What constraints must be imposed on C_1 , C_2 and R to obtain the low-pass filter transfer function described in Part (C)?

ANSWER: Our current equation for $|H_{LPF}(\omega)|$ does not look much like our desired result, but let's try multiplying out the denominator.

$$|H_{\rm LPF}(\omega)| = \frac{1}{\sqrt{1 - 2\omega^2 R^2 C_1 C_2 + (\omega^2 R^2 C_1 C_2)^2 + 4\omega^2 R^2 C_2^2}}$$

If we let $C_1 = C_2 = C$, then we can easily factor that equation.

$$|H_{\rm LPF}(\omega)| = \frac{1}{\sqrt{1 + 2\omega^2 R^2 C^2 + (\omega^2 R^2 C^2)^2}} = \frac{1}{\sqrt{(1 + \omega^2 R^2 C^2)^2}} = \frac{1}{1 + \omega^2 R^2 C^2}$$

This final form looks a lot more like what we want. We can see that $\omega_{\text{LPF}} = 1/(RC)$

(E) Given that the low-pass filter is to be designed as described in Part (C), use the results of Part (D) to choose values for C_1 , C_2 and R so that $\omega_{\text{LPF}} \approx 2\pi \times 4000 \text{ rad/s}$. Since the results of Part (D) under specify C_1 , C_2 and R, there is no single correct choice. Therefore, choose C_1 , C_2 and R so that they are easily implemented with the components in the 6.002 lab kit.

ANSWER: We see that $RC = 1/(2\pi \times 4000) \approx 3.98 \times 10^{-5}$. To choose a good value for R and C we need to consider the parasitic elements in the circuit and the device non-idealities.

There are parasitic capacitances between the pins in the protoboard. Those tend to be on the order of single picofarads. We need our C value to be much larger than that to be resistant to interference.

The resistor choice is effected by the presence of source resistances and input and output resistances of the op-amps. In addition there are parasitic inductances. If the resistance is too small, the parasitic RLC circuits may be under-damped and cause ringing. In general we choose a resistance of a few $k\Omega s$. We have an $R = 3.9k\Omega$ lets try that.

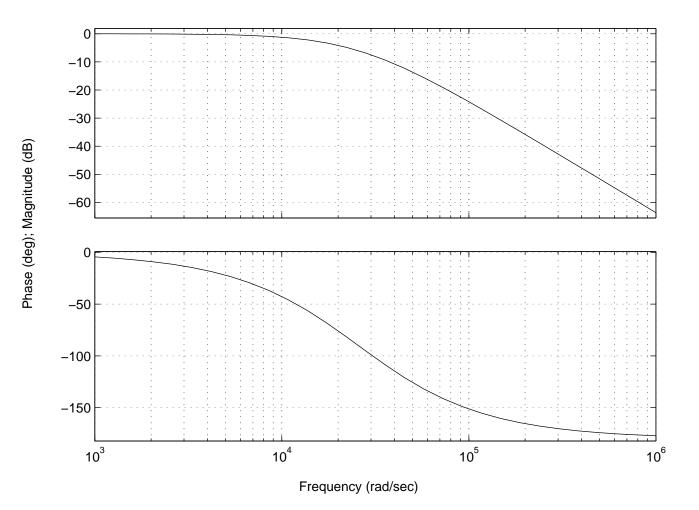
 $R = 3.9k\Omega$ requires that $C = .0102\mu F$. Since this is much larger than a picofarad, and we have a $.01\mu F$ capacitor in our kit, it seems that these values are a good choice.

Just to check, we see that our $RC = 3.9 \times 10^{-5}$. This is about 2 % off of the desired frequency, which is much less than the error of either the resistor or the capacitor.

(F) Given the choice of C_1 , C_2 and R from Part (E), determine ω_{LPF} , and plot both the logmagnitude and phase of $H_{\text{LPF}}(\omega)$ against log-frequency for $2\pi \times 10^1$ rad/s $\leq \omega \leq 2\pi \times 10^5$ rad/s.

ANSWER: From above we see that $\omega_{\text{LPF}} = 2.56 \times 10^4 = 2\pi \times 4081 rad/s$.

Bode Diagrams



Problem 4: The Power Amplifier

Figure 5 shows the output of the low-pass filter driving the power amplifier, which in turn drives the speaker. The power amplifier is constructed from a high-power op-amp, and is necessary because an ordinary low-power op-amp can not supply the current, and hence the power, required to drive the speaker.

Because there exists a coupling capacitor at its input, the power amplifier behaves like a highpass filter. In this way, the amplifier is designed to prevent a possibly damaging DC voltage from being applied to the speaker. Such a voltage component could be present in $v_{\rm LPF}$ if, for example, $v_{\rm OFF}$ in the analog-to-digital converter is not properly adjusted to balance the output of the converter.

(A) Assume that the power amplifier operates in sinusoidal steady state with $v_{\text{LPF}} = \Re\{\tilde{v}_{\text{LPF}}e^{j\omega t}\}$ and $v_{\text{OUT}} = \Re\{\tilde{v}_{\text{OUT}}e^{j\omega t}\}$ where \tilde{v}_{LPF} and \tilde{v}_{OUT} are complex amplitudes. Find the inputoutput transfer function $H_{\text{AMP}}(\omega)$ of the power amplifier where $H_{\text{AMP}}(\omega) \equiv \tilde{v}_{\text{OUT}}/\tilde{v}_{\text{LPF}}$.

ANSWER: We can use the equation for an inverting op-amp to write down the answer directly.

$$H_{\rm AMP}(\omega) = \frac{\tilde{v}_{\rm OUT}}{\tilde{v}_{\rm LPF}} = \frac{-R_2}{R_1 + \frac{1}{j\omega C}} = \frac{-j\omega R_2 C}{1 + j\omega R_1 C}$$

Remember that this comes from assuming that $v_{-} = v_{+} = 0$ and that the current into $v_{-} = 0$. (B) Using the result of Part (A), find the magnitude and phase of $H_{AMP}(\omega)$.

ANSWER:

$$|H_{\rm LPF}(\omega)| = \frac{\omega R_2 C}{\sqrt{1 + \omega^2 R_1^2 C^2}}$$

$$\angle H_{\rm LPF}(\omega) = -\pi/2 - \arctan \frac{\omega R_1 C}{1}$$

(C) Let ω_{AMP} be the frequency at which the low-frequency and high-frequency asymptotes of $|H_{AMP}(\omega)|$ intersect. Determine ω_{AMP} in terms of R_1 , R_2 and C.

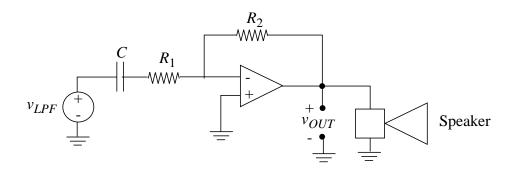


Figure 5: the power amplifier.

ANSWER: This problem can be approached just as in Problem 3C:

For $\omega \ll R_1 C$ we drop the ω term because it is much less than 1. The result is simple:

$$H_{\rm LPF}(\omega \ll R_1 C) \approx \omega R_2 C$$

Which goes to zero as ω goes to zero. This matches our intuition that the capacitor becomes an open circuit at low frequencies.

For $\omega \gg R_1 C$ we drop the 1 because it is much less than ω . The result is what we expect from noticing that the capacitor behaves like a short at high frequencies:

$$H_{\rm LPF}(\omega \ll R_1 C) \approx \frac{R_2}{R_1}$$

Solving for the intercept of these equations gives the expected $\omega = \frac{1}{R_1 C} = \omega_{AMP}$.

(D) Choose values for R_1 , R_2 and C so that $\omega_{AMP} \leq 2\pi \times 100$ Hz, and $|H_{AMP}(\omega)| = 1$ for $\omega \gg \omega_{AMP}$. Since these conditions alone under specify R_1 , R_2 and C, there is no single correct choice. Therefore, choose values for R_1 , R_2 and C that are easily implemented with the components in the 6.002 lab kit.

ANSWER: $|H_{AMP}(\omega)| = 1$ requires that $R_1 = R_2 = R$. So now we only need to choose two values, R and C. The key here is that $RC > 1/(2\pi \times 100) \approx 1.59 \times 10^{-3}$

Using the same criteria as in the previous problem, one possible combination is:

$$R_1 = R_2 = 15k\Omega$$
$$C = 0.1\mu F$$

.

To check: $\omega = 1/(RC) = 666.7 rad/s = 2\pi \times 106 Hz$

(E) If the original analog signal is recorded with a reduced amplitude, then the power amplifier must compensate by providing greater than unity gain. To provide this gain, R_2 is implemented with a fixed resistor in series with a potentiometer. Design such a modification that provides a variable gain of 1 to 2. Note that the 6.002 lab kit has a limited number of potentiometers.

ANSWER: When we choose values for the potentiometer and R, we still need to obey the restriction above that $RC > 1/(2\pi \times 100) \approx 1.59 \times 10^{-3}$.

Let's use a 10 k Ω potentiometer, as it's close to the 15 k Ω we found above. We know that the series resistor R_2 and the input resistor R_1 must also be 10 k Ω . To satisfy the condition from Part (D), let $C = 0.2\mu$ F. We can implement this with 2 0.1μ F capacitors in parallel. When the potentiometer is at one extreme of its travel, its resistance is zero, and the circuit has a gain of one. At the other end, it has a resistance of 10 k Ω , and the gain of the circuit is two.

Problem 5: Connecting The Blocks

In the complete audio playback system the output of the digital-to-analog converter is connected directly to the input of the low-pass filter, and the output of the low-pass filter is connected directly to the input of the power amplifier, as shown in Figure 1. Thus, the filter loads the converter, and the amplifier loads the filter. Explain why this loading could be ignored in Problems 2, 3 and 4. That is, explain why the converter, filter and amplifier may each be analyzed and designed in isolation.

ANSWER: The key to this simplicity is the op-amp. Using the ideal model of the opamp (which turns out to be a relatively accurate model) we see that the output of each stage is independent of the amount of current supplied. That is to say, the op-amp in the digital-toanalog converter has the same output value no matter how much current the low-pass filter draws. Similarly, the op-amps in the low-pass filter and output stage maintain the same output voltage regardless of the current drawn.

Of course none of the op-amps are completely ideal. The reason we have the final power stage is precisely because the 741 op-amp we are using for the other stages cannot supply enough current to drive the speaker. Even the power op-amp will show some output resistance, e.g. the output will change when the speaker is attached. However, within their designed region of operation, the op-amps will be highly insensitive to loading.