

First, a few general thoughts regarding this unit on operational amplifiers (op-amps).

How do engineers (and others) deal with design and analysis of large, complex systems?

Break large systems into [relatively] independent subsystems  
Sometimes called "modules," or "blocks," or "layers."

This happens all the time.

Divide automobile into engine, transmission, power steering, braking, electrical  
Different cross-sections depending on questions asked  
Electrical contains elements from engine, transmission, etc.  
Reference is "Zen and the Art of Motorcycle Maintenance  
By Robert Persig.

In software design, divide software into layers  
e.g. BIOS, then DOS or Windows (op sys), then word processor (app)  
In hardware design, divide circuit into blocks (block diagram)  
Radio has antenna, RF, LO, mixer, IF, detector, amp, PA.

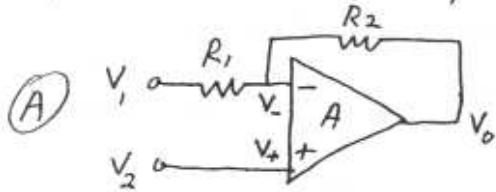
Many mechanical designs use high gain amplifier plus negative feedback

Power steering  
Cruise control  
Control of many biological processes  
PEOPLE (you and me)  
Catching a baseball  
Wheelchair tennis  
Lifting your arm to a set position (we'll try this in class!)

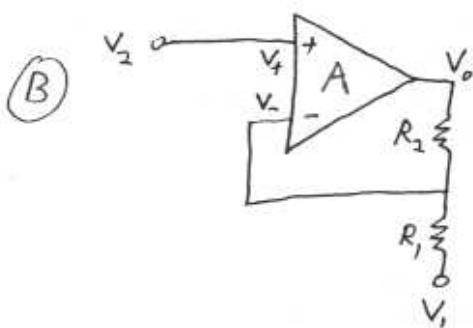
Development of integrated circuits led to design of integrated op-amps

Credited to Bob Pease, MIT '61, in late '60's  
Devices were 702, 709, 741 (still used!)  
Pease still at National Semiconductor, still writes informative columns  
Excellent example of compartmentalization  
Could achieve result with fewer transistors but  
Gain block is easy to design with  
Transistors are "cheap" to incorporate on IC  
Mass production is efficient  
Feedback allows consistent transfer function despite op-amp inaccuracies  
(see homework problem 10.1)

Quick review of simple op-amp configurations



With  $V_2 = 0$ , this is an inverting amplifier  
 For  $A \gg \frac{R_2}{R_1}$ ,  $V_- \approx V_+$  and  $V_o = -\frac{R_2}{R_1} V_i$



With  $V_1 = 0$ , this is a non-inverting amplifier

For  $A \gg \frac{R_1 + R_2}{R_1}$ ,  $V_- \approx V_+$  and  $V_o = V_i + \frac{R_2}{R_1} V_i$

$$V_o = \left(1 + \frac{R_2}{R_1}\right) V_i$$

↓                      ↓  
 from voltage      from voltage  
 across  $R_1$       across  $R_2$

What if we use (A) with  $V_1 = 0$  and input is  $V_2$ ?

Then it's the identical circuit to (B),  
 just drawn differently

What if we use (B) with  $V_2 = 0$  and input is  $V_1$ ?

Then it's the identical circuit to (A),  
 just drawn differently

By superposition

$$V_o = -\frac{R_2}{R_1} V_1 + \left(1 + \frac{R_2}{R_1}\right) V_2$$

Actual op-amp circuits have output resistance

[Show 741 schematic diagram]

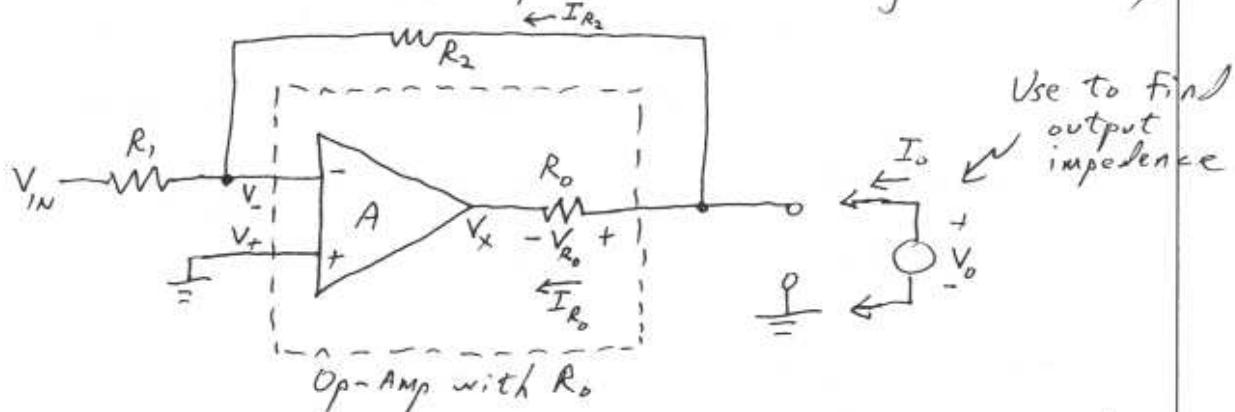
But the negative feedback causes op-amp to do

"whatever it takes" to achieve  $-\frac{R_2}{R_1} V_{IN}$  (inverting case)

This significantly reduces the effective output resistance

[but not under all conditions, as we shall demonstrate]

Let's examine op-amp with negative feedback  
 Will use external / output resistor to gain visibility



Can make Thevenin equivalent

With  $V_{IN}=0$ , connect  $V_o$  to output and calculate  $I_o$

$$V_o \text{ at output} \rightarrow \frac{R_1}{R_1 + R_2} V_o \text{ at } V_-$$

Which produces  $-A \frac{R_1}{R_1 + R_2} V_o$  at  $V_x$

$$\text{So } V_{R_o} = V_o - \left[ -A \frac{R_1}{R_1 + R_2} V_o \right] = V_o \left[ 1 + A \frac{R_1}{R_1 + R_2} \right]$$

$$\text{and } I_{R_o} = \frac{V_o}{R_o} \left[ 1 + A \frac{R_1}{R_1 + R_2} \right]$$

$$I_o = I_{R_o} + I_{R_2} = \frac{V_o}{R_o} \underbrace{\left[ 1 + A \frac{R_1}{R_1 + R_2} \right]}_{\approx A \frac{R_1}{R_2}} + \underbrace{\frac{V_o}{R_2}}_{\text{small}}$$

$$\text{So } \frac{V_o}{I_o} \approx \frac{R_o}{A \left[ \frac{R_1}{R_2} \right]} \quad \text{inverse gain}$$

What is going on?

$V_o$  at output pulls right end of  $R_o$  "up" by  $V_o$  volts

But this pulls  $V_+$  up by  $\frac{R_1}{R_1+R_2}$  volts, which

is approx the inverse gain of the amplifier

This ~~pulse~~ is amplified by the op-amp, pulling  
the left side of  $R_o$  down by  $A \times [\text{inverse gain}]$

If gain = 100 and  $A = 10^5$

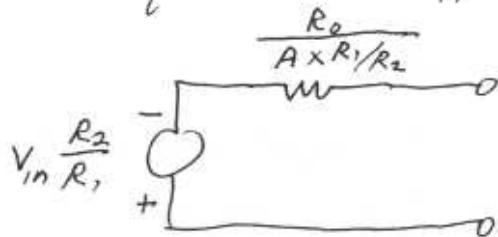
left side of  $R_o$  goes down by 1000  $V_o$

So  $R_o$  pulls 1001 times the current that it  
would pull if connected to ground

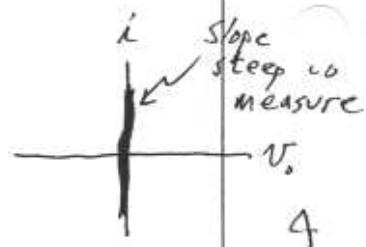
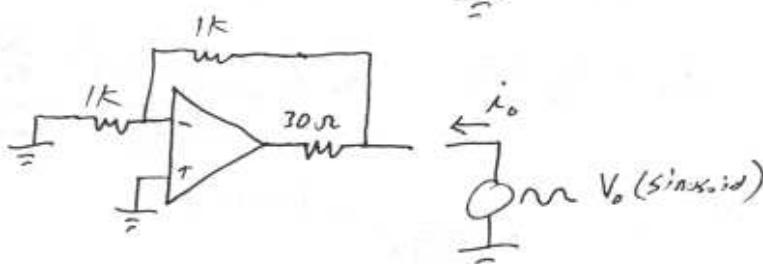
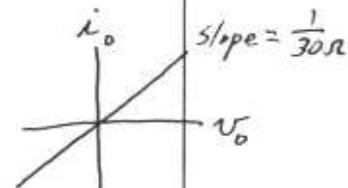
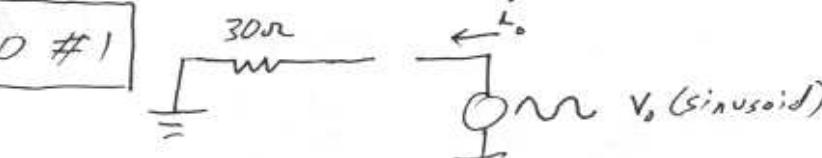
Feedback makes  $R_o$  act like  $\frac{R_o}{1001}$

$30\Omega \rightarrow 30 \text{ milliohms}$

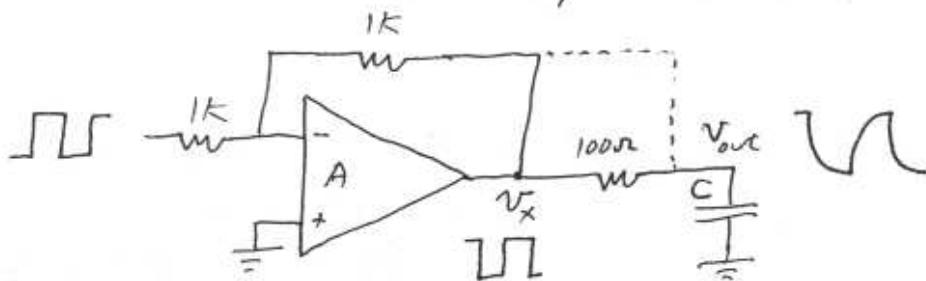
Thevenin equivalent is approx



DEMO #1



What if we use an op-amp with square wave  $V_{IN}$  to drive a capacitor? Start with 100Ω "output resistance" outside the feedback loop



Now connect the feedback directly to the capacitor, as shown by the dotted line

If  $A = 10^6$ , should reduce output impedance from 100Ω to 200nΩ

Would expect this to force square wave at capacitor, right?

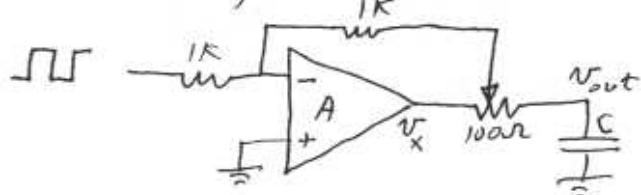
Wrong!

[Student Fill in waveform here] →

Why is this?

[Discussion in class]

What if we gradually move feedback from  $V_X$  to  $V_{out}$



$V_{out}$  starts as  $\sim\sim$  and improves to  $\sim\sim$

$V_X$  starts as  $\square\square$  and moves to  $\nearrow\nearrow$  to provide additional charging current to C

But eventually the  $V_X$  peaks hit the op-amp voltage limits

6.002 Lecture Notes  
Thursday 4/24/03  
Joel Schindall

## Op-Amp circuit analysis

Start with what you know

(input voltage, etc.)

Move where circuit constraints "help" you

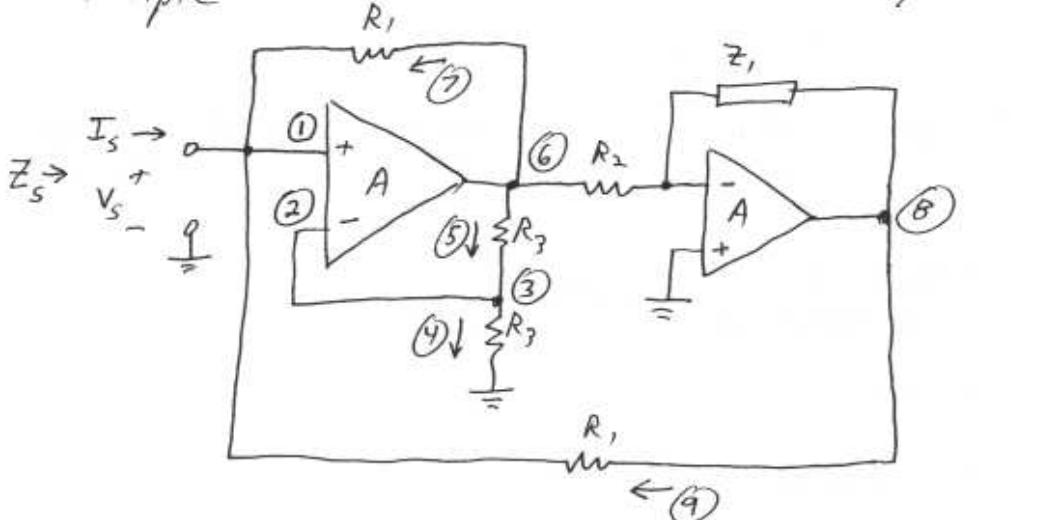
$$v_+ = v_- \quad i_m = 0 \quad \text{at op-amp}$$

(in active region with feedback)

It's like the game of Minesweeper

[ describe ]

### Example



Flow is from ① to ② to ... to ⑨

Every step is easy