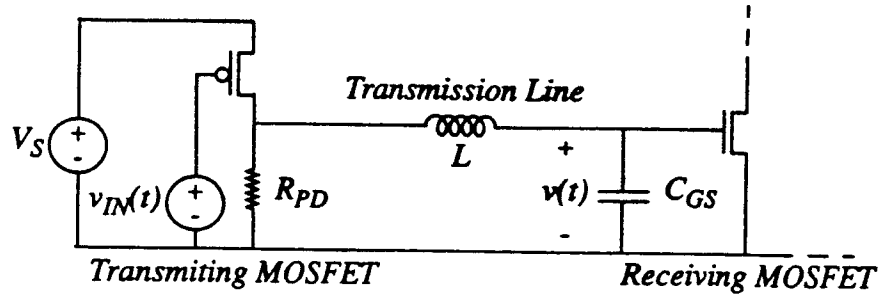


Problem 3 - 20%

In this problem a MOSFET and pull-down resistor having resistance R_{PD} are used to transmit digital data down a transmission line having inductance L as shown below. At the end of the transmission line is a receiving MOSFET having gate-to-source capacitance C_{GS} . Model the transmitting MOSFET with a switch-resistor model having on-state resistance R_{ON} .



- (3A) Assume that v_{IN} turns the transmitting MOSFET off at $t = 0$ after it was on for a very long time. In this case, derive *but do not solve* the differential equation that describes the evolution of $v(t)$, the gate-to-source voltage of the receiving MOSFET. Also provide the corresponding initial conditions in terms of $v(t)$ and its derivatives at $t = 0$.

Eqn:

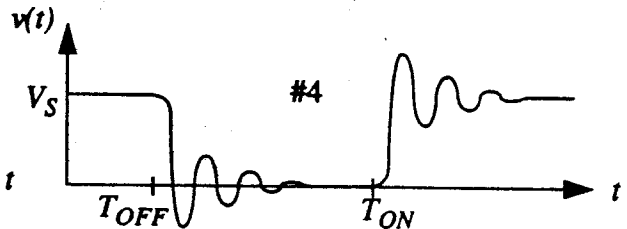
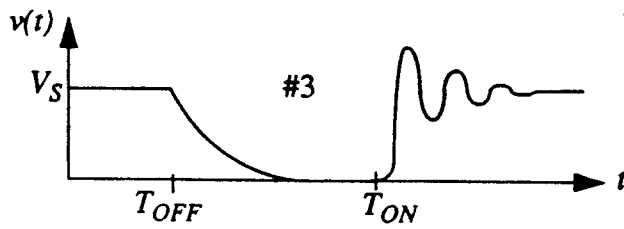
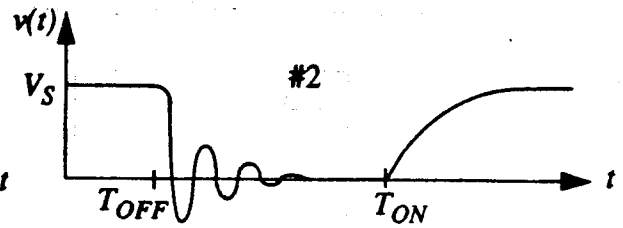
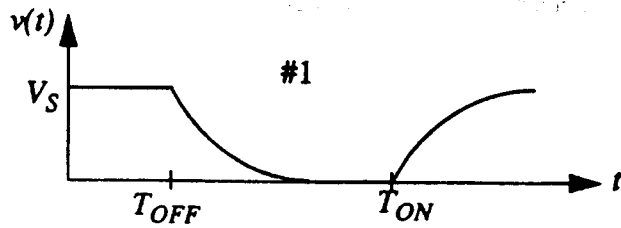
IC:

- (3B) Assume that v_{TN} turns the transmitting MOSFET on at $t = 0$ after it was off for a very long time. In this case, derive *but do not solve* the differential equation that describes the evolution of $v(t)$, the gate-to-source voltage of the receiving MOSFET. Also provide the corresponding initial conditions in terms of $v(t)$ and its derivatives at $t = 0$.

Eqn:

IC:

(3C) Assume that $R_{ON} \ll \sqrt{L/C_{GS}} \ll R_{PD}$. In this case, which of the following sketches best describes the evolution of $v(t)$ given that the transmitting MOSFET turns on at T_{ON} and off at T_{OFF} ? Why?

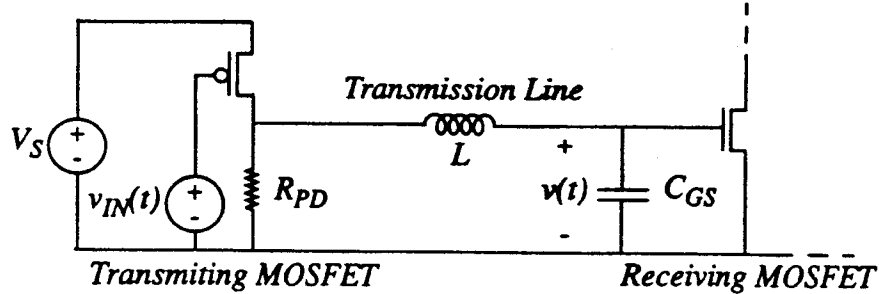


Sketch:

Why?

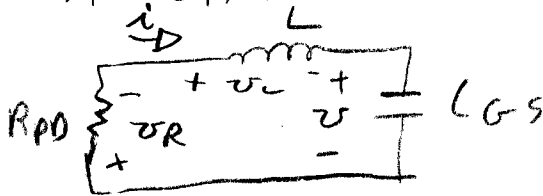
Problem 3 - 20%

In this problem a MOSFET and pull-down resistor having resistance R_{PD} are used to transmit digital data down a transmission line having inductance L as shown below. At the end of the transmission line is a receiving MOSFET having gate-to-source capacitance C_{GS} . Model the transmitting MOSFET with a switch-resistor model having on-state resistance R_{ON} .



- (3A) Assume that v_{IN} turns the transmitting MOSFET off at $t = 0$ after it was on for a very long time. In this case, derive but do not solve the differential equation that describes the evolution of $v(t)$, the gate-to-source voltage of the receiving MOSFET. Also provide the corresponding initial conditions in terms of $v(t)$ and its derivatives at $t = 0$.

mosfet off:



$$v + v_L + v_R = 0$$

$$\frac{1}{C} \int i dt + L \frac{di}{dt} + R i = 0$$

$$i = C \frac{dv}{dt}$$

$$\Rightarrow v + LC \frac{d^2v}{dt^2} + RC \frac{dv}{dt} = 0$$

init, $L = \text{short}$, $C = \text{open}$, DC steady state

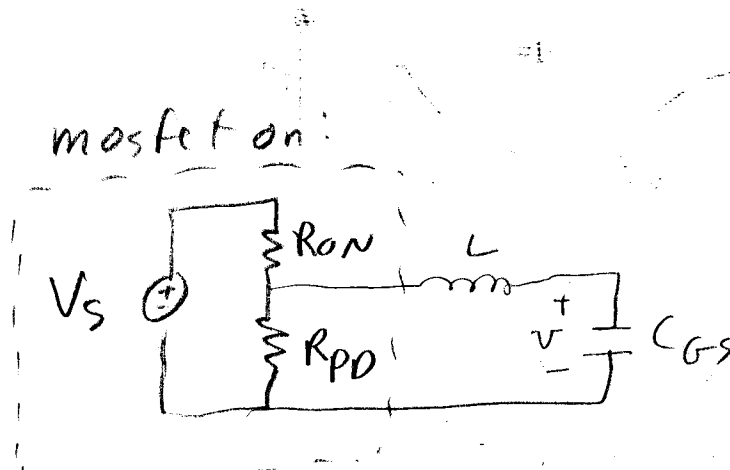
$$v(0) = \frac{V_S R_{PD}}{R_{PD} + R_{ON}}$$

$$\frac{dv}{dt}(0) = 0$$

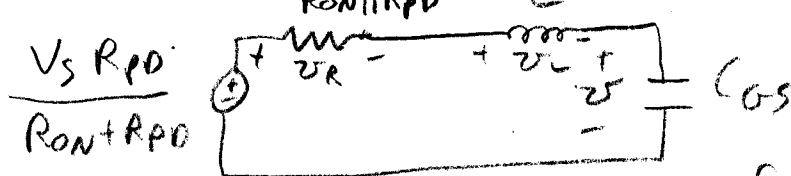
Eqn:
$$\frac{d^2v}{dt^2} + \frac{R_{PD}}{L} \frac{dv}{dt} + \frac{v}{LC} = 0$$

IC:
$$v(0) = V_S \frac{R_{PD}}{R_{PD} + R_{ON}} \quad \frac{dv}{dt}(0) = 0$$

- (3B) Assume that v_{IN} turns the transmitting MOSFET on at $t = 0$ after it was off for a very long time. In this case, derive but do not solve the differential equation that describes the evolution of $v(t)$, the gate-to-source voltage of the receiving MOSFET. Also provide the corresponding initial conditions in terms of $v(t)$ and its derivatives at $t = 0$.



Thev equiv: $R_{on} || R_{pd} = R$



$$v + v_L + v_R = \frac{V_s R_{pd}}{R_{on} + R_{pd}}$$

From part A:

$$v + LC \frac{d^2 v}{dt^2} + R \frac{dv}{dt} = \frac{V_s R_{pd}}{R_{on} + R_{pd}}$$

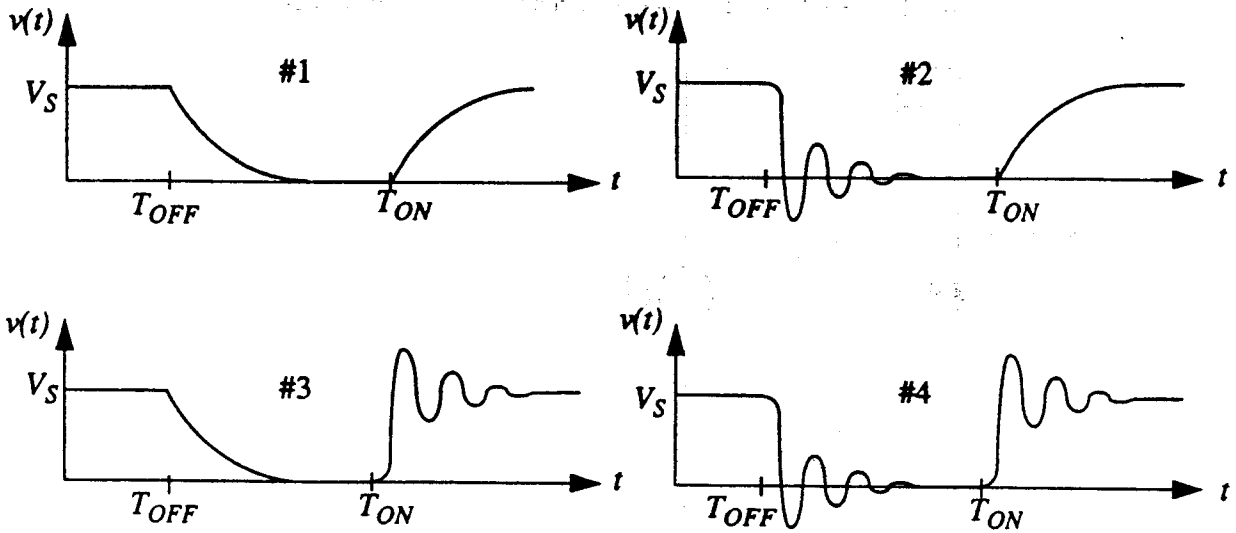
init, $L = \text{short}$, $C = \text{open}$, DC steady state

$$v(0) = 0, \quad \frac{dv}{dt}(0) = 0$$

Eqn:
$$\frac{d^2 v}{dt^2} + \frac{(R_{on} || R_{pd})}{L} \frac{dv}{dt} + \frac{v}{LC} = \frac{1}{LC} \frac{V_s R_{pd}}{R_{on} + R_{pd}}$$

IC:
$$v(0) = 0, \quad \frac{dv}{dt}(0) = 0$$

(3C) Assume that $R_{ON} \ll \sqrt{L/C_{GS}} \ll R_{PD}$. In this case, which of the following sketches best describes the evolution of $v(t)$ given that the transmitting MOSFET turns on at T_{ON} and off at T_{OFF} ? Why?



$$\frac{d^2 v}{dt^2} + 2\alpha \frac{dv}{dt} + \omega_0^2 v = V$$

oscillate if $\alpha < \omega_0$
 don't if $\alpha \geq \omega_0$

Sketch: # 3 Why?

Off oscillates if $\frac{R_{PD}}{2L} < \sqrt{\frac{1}{LC}}$
 or $\frac{R_{PD}}{2} < \sqrt{\frac{L}{C}}$, but $R_{PD} \gg \sqrt{\frac{L}{C}}$
 so no oscillation

On oscillates if $\frac{R_{ON} || R_{PD}}{2} < \sqrt{\frac{L}{C}}$
 and $R_{ON} \ll \sqrt{\frac{L}{C}}$, so oscillates.