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6.012 Problem Set #1 Solutions - Fall 2000

Problem #1: E2.1

At RT, $n_i = 10^{10} \text{ cm}^{-3}$

a) Since $N_A \gg n_i$, $n_0 = N_A = 10^{15} \text{ cm}^{-3}$

b) $p_0 = \frac{n_i^2}{n_0} = \frac{10^{20}}{10^{15}} = 10^5 \text{ cm}^{-3}$

Problem #2: E2.4

a) Since $N_A > N_D$, holes are the majority carrier. Thus is a compensated p-type Si.

b) Since $N_A - N_D \gg n_i$, $p_0 = N_A - N_D = 5 \times 10^{16} \text{ cm}^{-3}$

c) $n_0 = \frac{n_i^2}{N_A - N_D} = 2 \times 10^3 \text{ cm}^{-3}$

Problem #3: E2.5

Wafer initially doped with $N_A = 10^{14} \text{ cm}^{-3}$ ($p_0 = 10^{14} \text{ cm}^{-3}$). Must be compensated with N_D to yield $p_0 = 10^{13} \text{ cm}^{-3}$.

$p_0 = N_A - N_D$
 $N_D = 9 \times 10^{13} \text{ cm}^{-3}$

Problem #4: E2.6 \Rightarrow Low doping - need to include thermal generation

$8n_0 = n_0 = \frac{N_D}{2} + \frac{N_A}{2} \left[1 + \frac{4n_i^2}{N_D^2} \right] \Rightarrow \frac{n_i^2}{n_0} + N_D - n_0 = 0$

$N_D = 7.875 n_i$ At RT, $N_D = 7.875 \times 10^{10} \text{ cm}^{-3}$

Not taking thermal generation into account results in $\frac{0.115}{7.875} = 1.6\%$ error.

Problem #5: E2.7

$n_0 = 5 \times 10^{14} \text{ cm}^{-3}$

$p_0 = \frac{n_i^2}{n_0} = 2 \times 10^5 \text{ cm}^{-3}$

$L_{pn} = 10^{-4} \text{ cm}$
 $L_{pp} = 10^{-12} \text{ cm}^3$

e⁻ in $1 \mu\text{m}^3$ volume = 500 electrons
h⁺ in $1 \mu\text{m}^3$ volume = 2×10^{-7} holes

As the dimensions are scaled down, the number of carriers decrease as the cube of the linear dimension, but's can be compensated by increasing the doping.

Problem #6: P2.2

3 impurities: As: 10^{16} cm^{-3} (Group V $\rightarrow N_D$)

B: $1.15 \times 10^{16} \text{ cm}^{-3}$ (Group III $\rightarrow N_A$)

P: $2.5 \times 10^{15} \text{ cm}^{-3}$ (Group V $\rightarrow N_D$)

$n_0 = N_A n_{As} + N_{Dp} - N_{As} = 10^{15} \text{ cm}^{-3}$
 $p_0 = \frac{n_i^2}{n_0} = 10^5 \text{ cm}^{-3}$

Problem #7: P2.4

Temp (C)	n_i (cm ⁻³)	$T^{3/2}$	$\ln(n_i)$	$\ln(T)$
-65	218.15	2.32E+08	3223.054	1.99E+16
0	273.15	1.42E+08	4514.416	1.40318E+02
70	343.15	2.82E+11	6368.616	2.77604E+05
125	398.15	5.08E+12	7944.584	0.000491389

$\Rightarrow N_A = 1.02 \times 10^{16} \text{ cm}^{-3}$

At 300 K $\Rightarrow n_i = 1.44 \times 10^{10} \text{ cm}^{-3}$

Temp at which $n_i = 2.88 \times 10^{10} \text{ cm}^{-3}$:

$2.88 \times 10^{10} = A T^{3/2} e^{-6608.7/T} \rightarrow T \ln(2.88 \times 10^{10}) - \ln(A) = 3/2 T \ln(T) - 6608$

$T = 517.21 - 0.1174 T \ln(T) \rightarrow T_0$ solve, make a guess & iterate.
 $T = 305 \rightarrow 312.38 \rightarrow 306.55 \rightarrow 311.16 \rightarrow 307.51 \rightarrow 310.14 \rightarrow 308.1 \rightarrow 309.9 \rightarrow 308.5 \rightarrow 309.16 \rightarrow 308.7 \rightarrow 309.4 \rightarrow 308.9 \rightarrow 309.3 \rightarrow 309 \rightarrow 309.25 \rightarrow 309.10 \rightarrow 309.20 \rightarrow 309.06 \rightarrow 309.17 \rightarrow 309.09 \rightarrow 309.15 \rightarrow 309.1$
 Finally converges to 309.1 K.

Problem #7: P2-4 (cont.)

Repeat same procedure to get T when $n_i = 7.2 \times 10^9 \text{ cm}^{-3}$

$$T (\ln(7.2 \times 10^9) - \ln(1)) = \frac{3}{2} T \ln(T) - 6608.2$$

$$T = 466.59 - 0.1059 T \ln(T) \Rightarrow \text{Converges to } T = 291.4 \text{ K}$$

so,

T	n_i
291.4 K	$7.2 \times 10^9 \text{ cm}^{-3}$
300 K	$1.44 \times 10^{10} \text{ cm}^{-3}$
309.1 K	$2.88 \times 10^{10} \text{ cm}^{-3}$

Problem #8:

For Ge:

T (C)	$n_i \text{ (cm}^{-3}\text{)}$
27	2.1×10^{13}
150	2.5×10^{15}
500	1.5×10^{18}

(From Graph)

@ 27°C $(N_a - N_d) \gg n_i$ so, $p_o = N_a - N_d = 5 \times 10^{15} \text{ cm}^{-3}$
 $n_o = \frac{n_i^2}{p_o} = 8.82 \times 10^{10} \text{ cm}^{-3}$

@ 150°C $(N_a - N_d) \approx n_i \rightarrow$ Must take thermal generation into account.

$$p_o = \frac{N_a - N_d}{2} + \frac{N_a - N_d}{2} \sqrt{1 + \frac{4n_i^2}{(N_a - N_d)^2}} = 6.04 \times 10^{15} \text{ cm}^{-3}$$

$$n_o = \frac{n_i^2}{p_o} = 1.03 \times 10^{15} \text{ cm}^{-3}$$

@ 500°C $(N_a - N_d) \ll n_i$

$$n_o = p_o = n_i = 1.5 \times 10^{18} \text{ cm}^{-3}$$