# Lecture 18 - The Bipolar Junction Transistor (II)

#### REGIMES OF OPERATION

April 19, 2001

#### **Contents**:

- 1. Regimes of operation.
- 2. Large-signal equivalent circuit model.
- 3. Output characteristics.

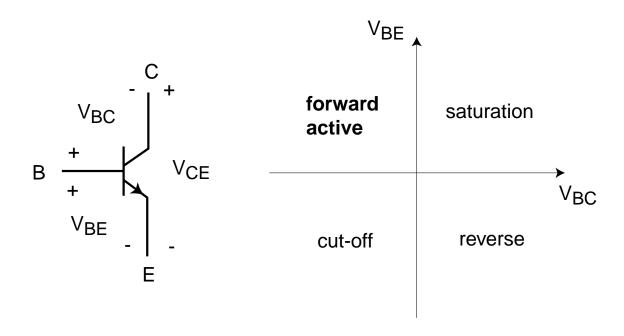
## Reading assignment:

Howe and Sodini, Ch. 7, §§7.3, 7.4

## **Key questions**

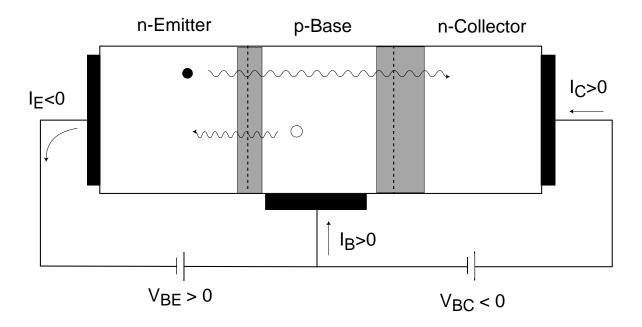
- What other regimes of operation are there for the BJT?
- What is unique about each regime?
- How do equivalent circuit models for the BJT look like?

#### 1. Regimes of operation

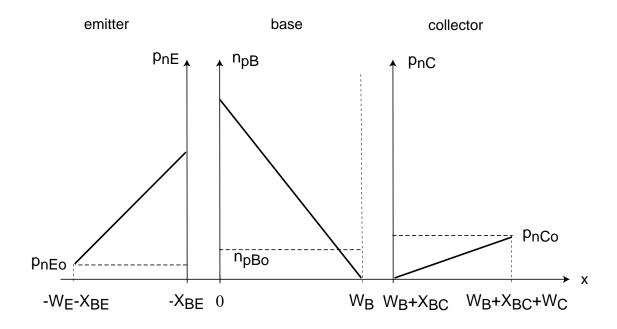


- forward active: device has good isolation and high gain; most useful regime;
- saturation: device has no isolation and is flooded with minority carriers ⇒ takes time to get out of saturation; avoid
- reverse: poor gain; not useful;
- *cut-off*: negligible current: nearly an open circuit; useful.

# $\square$ Forward-active regime: $V_{BE} > 0, V_{BC} < 0$



Minority carrier profiles (not to scale):



• Emitter injects electrons into base, collector collects electrons from base:

$$I_C = I_S \exp \frac{qV_{BE}}{kT}$$

• Base injects holes into emitter, recombine at emitter contact:

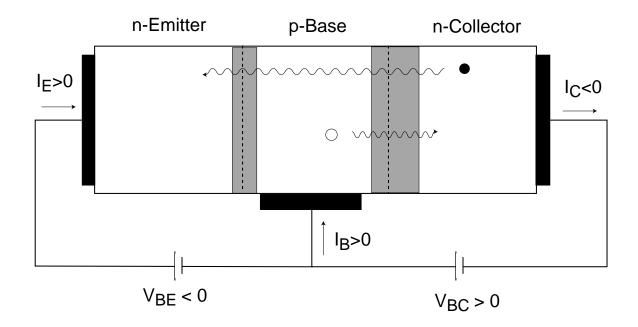
$$I_B = \frac{I_S}{\beta_F} (\exp \frac{qV_{BE}}{kT} - 1)$$

• Emitter current:

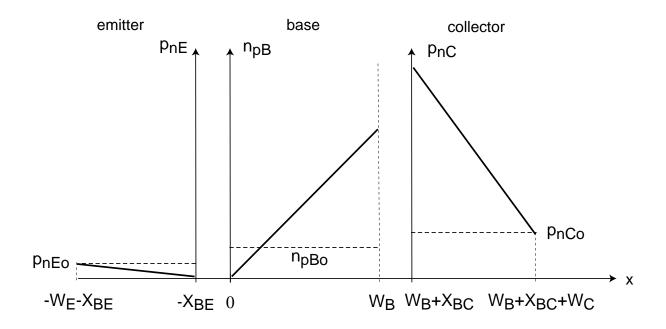
$$I_E = -I_C - I_B = -I_S \exp \frac{qV_{BE}}{kT} - \frac{I_S}{\beta_F} (\exp \frac{qV_{BE}}{kT} - 1)$$

- State-of-the-art IC BJT's today:  $I_C \sim 0.1-1~mA$ ,  $\beta_F \simeq 50-300$ .
- $\beta_F$  hard to control tightly  $\Rightarrow$  circuit design techniques required to be insensitive to variations in  $\beta_F$ .

# $\square$ Reverse regime: $V_{BE} < 0, V_{BC} > 0$



#### Minority carrier profiles:



• Collector injects electrons into base, emitter collects electrons from base:

$$I_E = I_S \exp \frac{qV_{BC}}{kT}$$

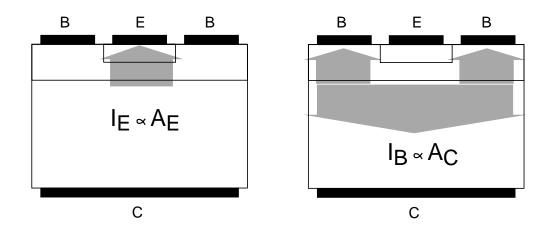
• Base injects holes into collector, recombine at collector contact and buried layer:

$$I_B = \frac{I_S}{\beta_R} (\exp \frac{qV_{BC}}{kT} - 1)$$

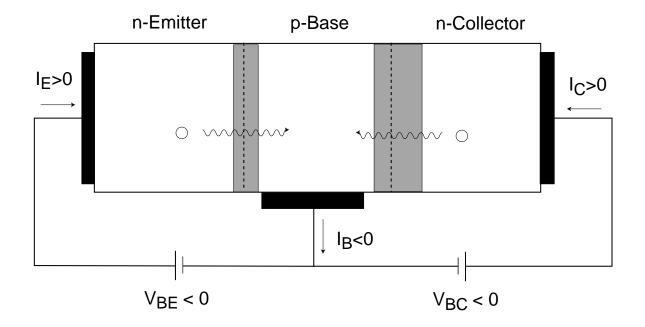
• Collector current:

$$I_C = -I_E - I_B = -I_S \exp \frac{qV_{BC}}{kT} - \frac{I_S}{\beta_R} (\exp \frac{qV_{BC}}{kT} - 1)$$

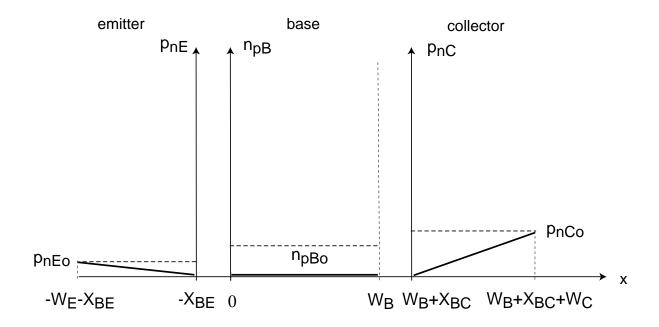
• Typically,  $\beta_R \simeq 0.1 - 5 \ll \beta_F$ .



$$\square$$
 Cut-off:  $V_{BE} < 0, V_{BC} < 0$ 



## Minority carrier profiles:



• Base extracts holes from emitter:

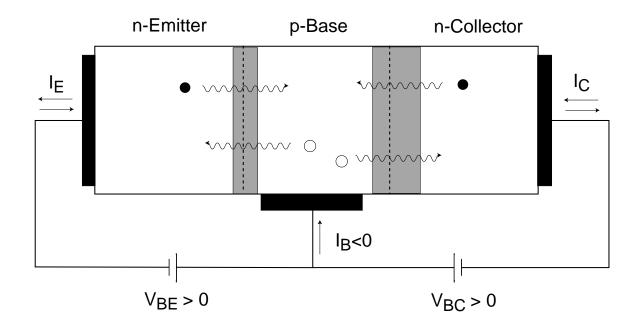
$$I_{B1} = -\frac{I_S}{\beta_F} = -I_E$$

• Base extracts holes from collector:

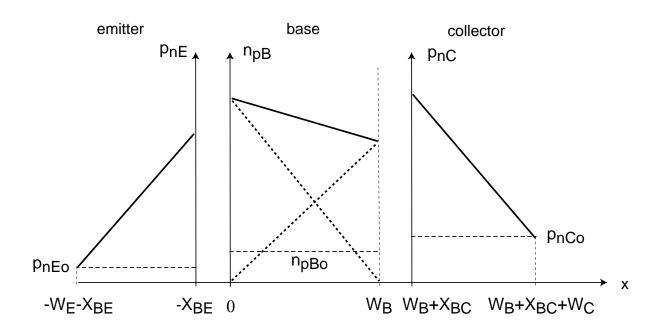
$$I_{B2} = -\frac{I_S}{\beta_R} = -I_C$$

• These are tiny leakage currents ( $\sim 10^{-12} A$ ).

# $\square$ Saturation: $V_{BE} > 0, V_{BC} > 0$



## Minority carrier profiles:



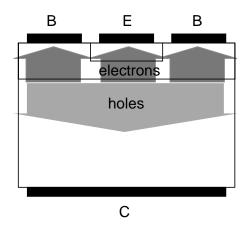
Saturation is superposition of forward active + reverse:

$$I_{C} = I_{S}(\exp \frac{qV_{BE}}{kT} - \exp \frac{qV_{BC}}{kT}) - \frac{I_{S}}{\beta_{R}}(\exp \frac{qV_{BC}}{kT} - 1)$$

$$I_{B} = \frac{I_{S}}{\beta_{F}}(\exp \frac{qV_{BE}}{kT} - 1) + \frac{I_{S}}{\beta_{R}}(\exp \frac{qV_{BC}}{kT} - 1)$$

$$I_{E} = -\frac{I_{S}}{\beta_{F}}(\exp \frac{qV_{BE}}{kT} - 1) - I_{S}(\exp \frac{qV_{BE}}{kT} - \exp \frac{qV_{BC}}{kT})$$

- $I_C$  and  $I_E$  can have either sign, depending on relative magnitude of  $V_{BE}$  and  $V_{BC}$ , and  $\beta_F$  and  $\beta_R$ .
- $\bullet$  In saturation, collector and base flooded with excess minority carriers  $\Rightarrow$  takes lots of time to get transistor out of saturation.



#### 2. Large-signal equivalent circuit model

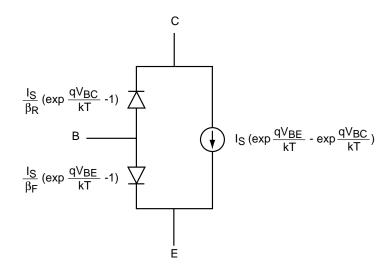
System of equations that describes BJT operation:

$$I_{C} = I_{S}(\exp \frac{qV_{BE}}{kT} - \exp \frac{qV_{BC}}{kT}) - \frac{I_{S}}{\beta_{R}}(\exp \frac{qV_{BC}}{kT} - 1)$$

$$I_{B} = \frac{I_{S}}{\beta_{F}}(\exp \frac{qV_{BE}}{kT} - 1) + \frac{I_{S}}{\beta_{R}}(\exp \frac{qV_{BC}}{kT} - 1)$$

$$I_{E} = -\frac{I_{S}}{\beta_{F}}(\exp \frac{qV_{BE}}{kT} - 1) - I_{S}(\exp \frac{qV_{BE}}{kT} - \exp \frac{qV_{BC}}{kT})$$

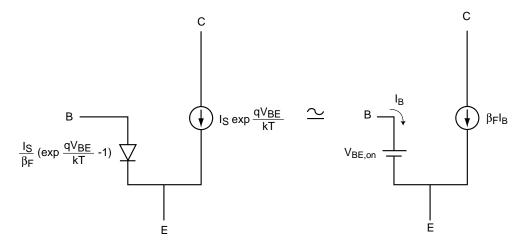
Equivalent-circuit model representation:  $Non-Linear\ Hybrid-\pi\ Model$ 



Three parameters in this model:  $I_S$ ,  $\beta_F$ , and  $\beta_R$ . Model equivalent to Ebers-Moll model in text.

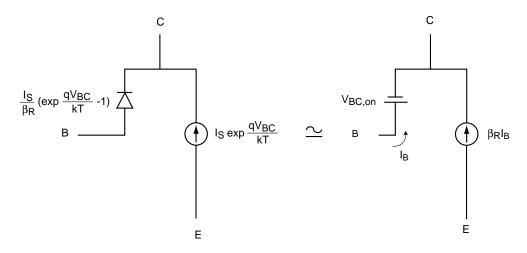
#### Simplifications of equivalent-circuit model:

• Forward-active regime:  $V_{BE} > 0, V_{BC} < 0$ 



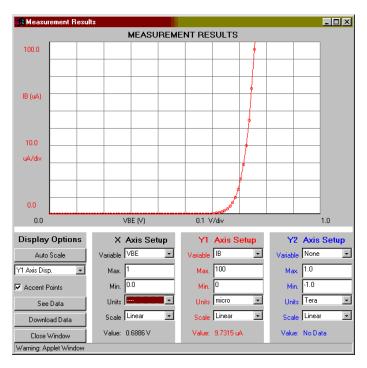
For today's technology:  $V_{BE,on} \simeq 0.7 \ V$ .  $I_B$  depends on outside circuit.

• Reverse:  $V_{BE} < 0, V_{BC} > 0$ 

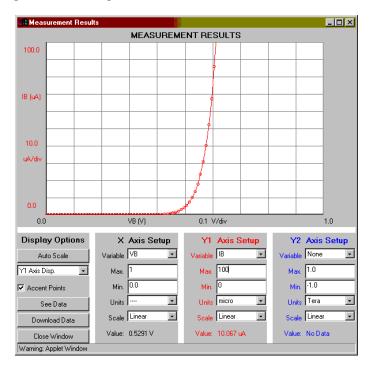


For today's technology:  $V_{BC,on} \simeq 0.5 \ V$ .  $I_B$  also depends on outside circuit.

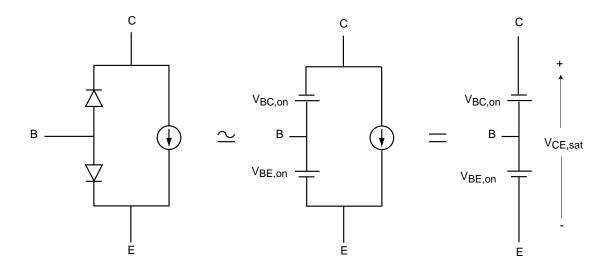
 $I_B$  vs.  $V_{BE}$  for  $V_{CE} = 2.5 V$ :



 $I_B$  vs.  $V_{BC}$  for  $V_{EC} = 2.5 V$ :

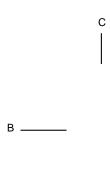


## • Saturation: $V_{BE} > 0, V_{BC} > 0$



Today's technology:  $V_{CE,sat} = V_{BE,on} - V_{BC,on} \simeq 0.2 \ V$ .  $I_B$  and  $I_C$  depend on outside circuit.

• Cut-off:  $V_{BE} < 0, V_{BC} < 0$ 

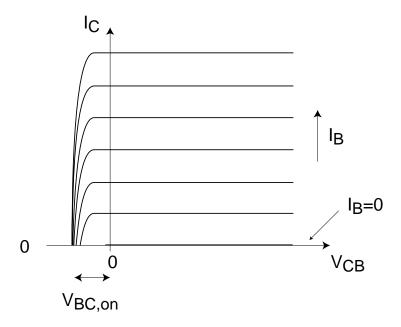


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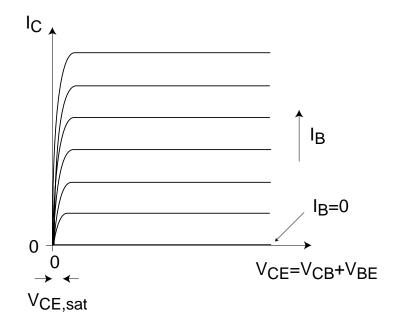
Only negligible leakage currents.

# 3. Output characteristics

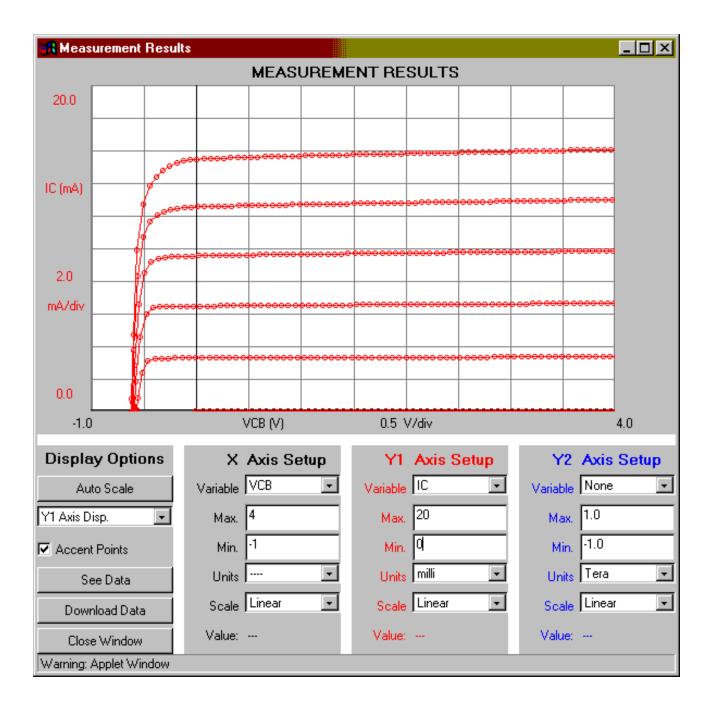
First, common-base output characteristics:



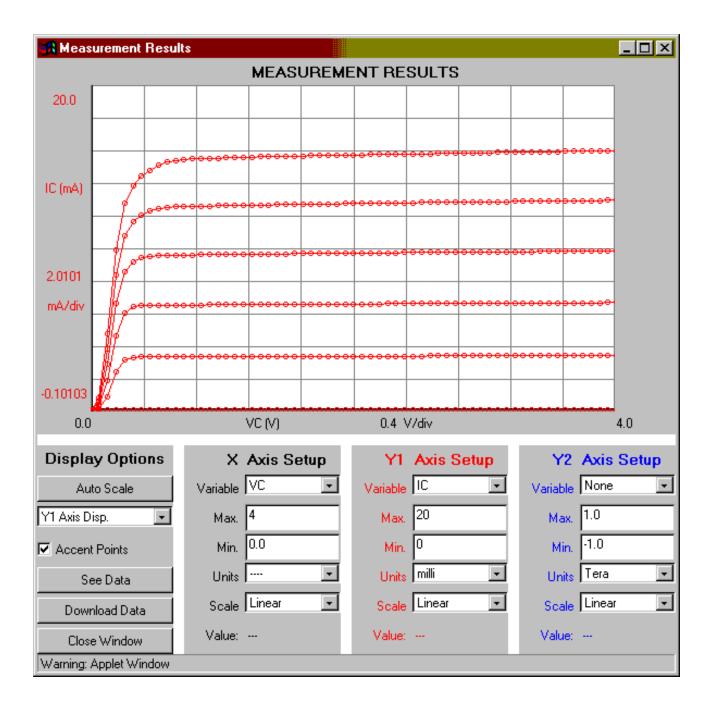
Next, common-emitter output characteristics:



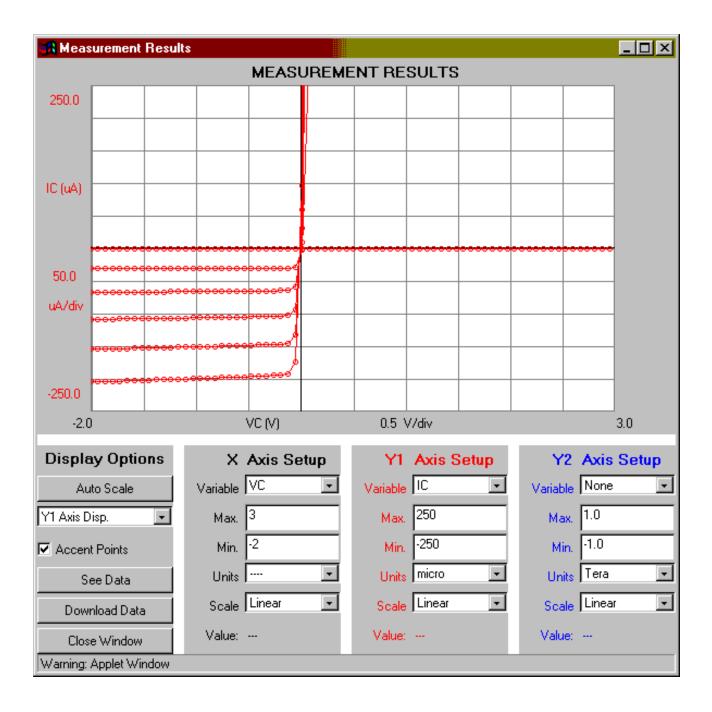
## $I_C$ vs. $V_{CB}$ for $0 \le I_B \le 100 \ \mu A$ :



## $I_C$ vs. $V_{CE}$ for $0 \le I_B \le 100 \ \mu A$ :

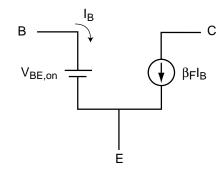


## $I_C$ vs. $V_{CE}$ for $0 \le I_B \le 100 \ \mu A$ :

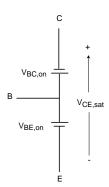


#### **Key conclusions**

• Forward-active regime: most useful, device has gain and isolation. For bias calculations:



• Saturation: device flooded with minority carriers. Not useful. For bias calculations:



• Cut-off: device open. Useful. For bias calculations:

