The Problem: Distributed Methods for Finding Paths in Networks

- Addressing (how to name nodes?)
  - Unique identifier for global addressing
  - Link name for neighbors
- Forwarding (how does a switch process a packet?)
- Routing (building and updating data structures to ensure that forwarding works)
- Functions of the network layer

Link costs:

11 13 19
7 5 13

Shortest Path Routing

- Each node wants to find the path with minimum total cost to other nodes
  - We use the term “shortest path,” even though we’re interested in min cost (and not min #hops)
- Several possible distributed approaches
  - Vector protocols, esp. distance vector (DV)
  - Link-state protocols (LS)
Routing Table Structure

<table>
<thead>
<tr>
<th>Destination</th>
<th>Link (next-hop)</th>
<th>Cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>ROUTE L1</td>
<td>18</td>
</tr>
<tr>
<td>B</td>
<td>Self</td>
<td>0</td>
</tr>
<tr>
<td>C</td>
<td>L1</td>
<td>11</td>
</tr>
<tr>
<td>D</td>
<td>L2</td>
<td>4</td>
</tr>
<tr>
<td>E</td>
<td>ROUTE L1</td>
<td>16</td>
</tr>
</tbody>
</table>

Routing table @ node B

Distributed Routing: A Common Plan

- Determining live neighbors
  - Common to both DV and LS protocols
  - HELLO protocol (periodic)
    - Send HELLO packet to each neighbor to let them know who’s at the end of their outgoing links
    - Use received HELLO packets to build a list of neighbors containing an information tuple for each link: (timestamp, neighbor addr, link)
    - Repeat periodically. Don’t hear anything for a while → link is down, so remove from neighbor list.
- Advertisement step (periodic)
  - Send some information to all neighbors
  - Used to determine connectivity & costs to reachable nodes
- Integration step
  - Compute routing table using info from advertisements
  - Dealing with stale data

Distance-Vector Routing

- DV advertisement
  - Send info from routing table entries: (dest, cost)
  - Initially just (self,0)
- DV integration step [Bellman-Ford]
  - For each (dest,cost) entry in neighbor’s advertisement
    - Account for cost to reach neighbor: (dest,my_cost)
    - my_cost = cost_in_advertisement + link_cost
  - Are we currently sending packets for dest to this neighbor?
    - See if link matches what we have in routing table
    - If so, update cost in routing table to be my_cost
  - Otherwise, is my_cost smaller than existing route?
    - If so, neighbor is offering a better deal! Use it...
    - update routing table so that packets for dest are sent to this neighbor

DV Example: round 2

Node A: update routes to B, D, E
Node B: update routes to A, C
Node C: no updates
Node D: update routes to A
Node E: update routes to A, B, C
DV Example: round 3

Node A: (L0, 0), Node B: (L1, 18), Node C: (L1, 7), Node D: (L1, 22), Node E: (L1, 12)

Node A: (L0, 0), Node B: (L1, 18), Node C: (L1, 7), Node D: (L1, 22), Node E: (L1, 12)

Node A: (None, 0), Node B: (None, 0), Node C: (None, 0), Node D: (None, 0), Node E: (None, 0)

Node A: Update cost to B
Node B: Update routes to A
Node C: Update routes to B
Node D: No updates
Node E: No updates

DV Example: Break a Link

Update cost

When link breaks: eliminate routes that use that link.

DV Example: round 4

Node A: (None, 0), Node B: (L0, 4), Node C: (None, 0), Node D: (L2, 15), Node E: (None, 0)

Node A: (None, 0), Node B: (L0, 4), Node C: (None, 0), Node D: (L2, 15), Node E: (None, 0)

Node A: Update cost to B
Node B: Update routes to A, C, D, E
Node C: Update routes to B, D
Node D: No updates
Node E: No updates

DV Example: round 5

Node A: (L0, 12), Node B: (L2, 19), Node C: (None, 0), Node D: (L2, 15), Node E: (None, 0)

Node A: (L0, 12), Node B: (L2, 19), Node C: (None, 0), Node D: (L2, 15), Node E: (None, 0)

Node A: Update cost to B
Node B: Update routes to A, C, D, E
Node C: No updates
Node D: No updates
Node E: No updates
Correctness & Performance

- Optimal substructure property fundamental to correctness of both Bellman-Ford and Dijkstra's shortest path algorithms
  - Suppose shortest path from X to Y goes through Z. Then, the sub-path from X to Z must be a shortest path.
- Proof of Bellman-Ford via induction on number of walks on shortest (min-cost) paths
  - Easy when all costs > 0 and synchronous model (see notes)
  - Harder with distributed async model (not in 6.02)
- How long does it take for distance-vector routing protocol to converge?
  - Time proportional to largest number of hops considering all the min-cost paths

Link-State Routing

- Advertisement step
  - Send information about its links to its neighbors (aka link state advertisement or LSA):
    - [seq#, [(nbhr1, linkcost1), (nbhr2, linkcost2), ...]]
  - Do it periodically (liveness, recover from lost LSAs)
- Integration
  - If seq# in incoming LSA > seq# in saved LSA for source node: update LSA for node with new seq#, neighbor list rebroadcast LSA to neighbors (→ flooding)
  - Remove saved LSAs if seq# is too far out-of-date
- Build routing table
  - Periodically each node runs the same shortest path algorithm over its map (e.g., Dijkstra’s alg)
  - If each node implements computation correctly and each node has the same map, then routing tables will be correct
Integration Step: Dijkstra’s Algorithm (Example)

Suppose we want to find paths from A to other nodes.

Dijkstra’s Shortest Path Algorithm

- Initially
  - nodeset = [all nodes] = set of nodes we haven’t processed
  - spcost = [me:0, all other nodes: ∞] # shortest path cost
  - routes = [me:--, all other nodes: ?] # routing table
- while nodeset isn’t empty:
  - find u, the node in nodeset with smallest spcost
  - remove u from nodeset
  - for v in [u’s neighbors]:
    - d = spcost(u) + cost(u,v) # distance to v via u
    - if d < spcost(v): # we found a shorter path!
      - spcost[v] = d
      - routes[v] = routes[u] (or if u == me, enter link from me to v)
- Complexity: N = number of nodes, L = number of links
  - Finding u (N times): linear search=O(N), using heapq=O(log N)
  - Updating spcost: O(L) since each link appears twice in neighbors

Another Example

Finding shortest paths from A:

<table>
<thead>
<tr>
<th>Step</th>
<th>Nodeset</th>
<th>spcost</th>
<th>route</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>[A,B,C,D,E]</td>
<td>0</td>
<td>--</td>
</tr>
<tr>
<td>1</td>
<td>[B,C,D,E]</td>
<td>19</td>
<td>(B,19) (C, 7)</td>
</tr>
<tr>
<td>2</td>
<td>[B,D,E]</td>
<td>18</td>
<td>(D,4), (C,15), (E,13)</td>
</tr>
<tr>
<td>3</td>
<td>[B,D]</td>
<td>18</td>
<td>(D,4), (C,15), (E,13)</td>
</tr>
<tr>
<td>4</td>
<td>[D]</td>
<td>18</td>
<td>(D,4), (C,15), (E,13)</td>
</tr>
<tr>
<td>5</td>
<td>[]</td>
<td>18</td>
<td>(D,4), (C,15), (E,13)</td>
</tr>
</tbody>
</table>