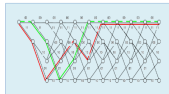


# Routing Algorithms

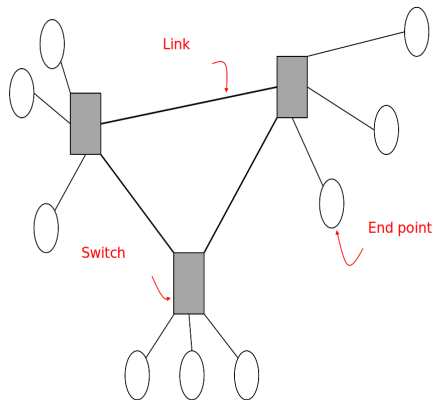
6.02 Fall 2013 Lecture 20



INTRODUCTION TO EECS II  
**DIGITAL  
COMMUNICATION  
SYSTEMS**

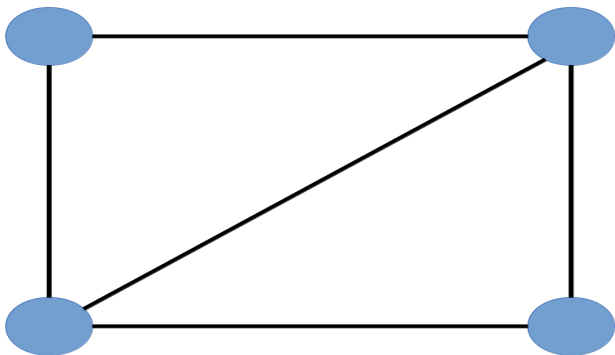
## Routing Algorithms:

- ▶ Addressing, Forwarding, Routing
- ▶ Distance-Vector Algorithms
- ▶ Link-State Algorithms



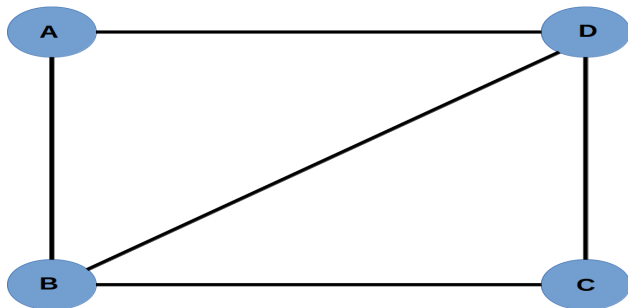
# Network Model

Some nodes, some links . . .



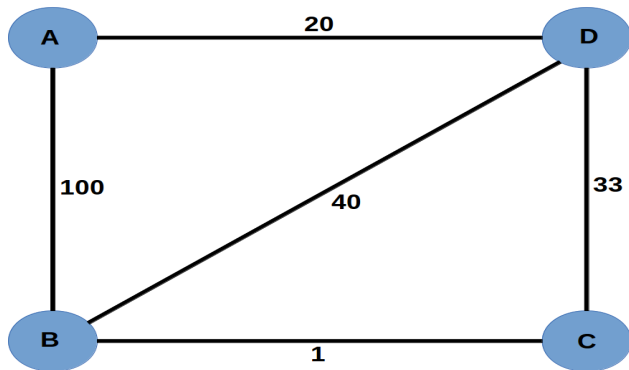
# Network Model

- ▶ node names, i.e. **addresses**: A, B, C, D
- ▶ link names:  $\rightarrow A$  (from B or D),  $\rightarrow B$  (from A, D, or C), etc.



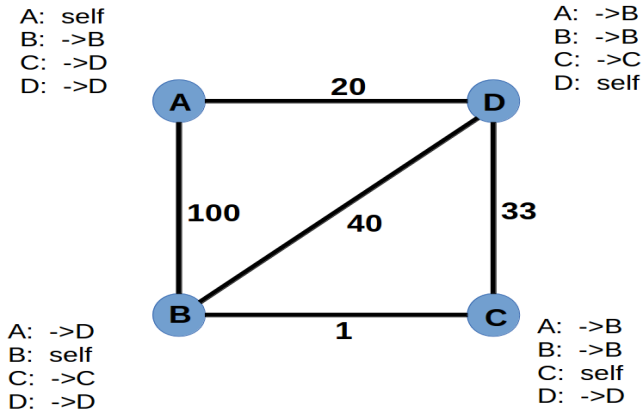
# Network Model

Link costs: A->B is 100, D->B is 40, etc.



# Network Model

Forwarding table: **incorrect**

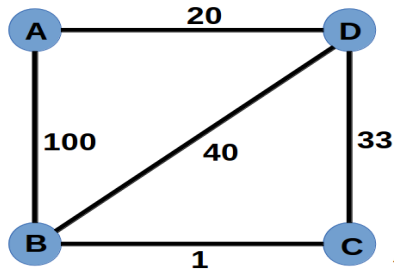


# Network Model

Forwarding table: **correct**

A: self  
B: ->B  
C: ->D  
D: ->D

A: ->A  
B: ->B  
C: ->C  
D: self

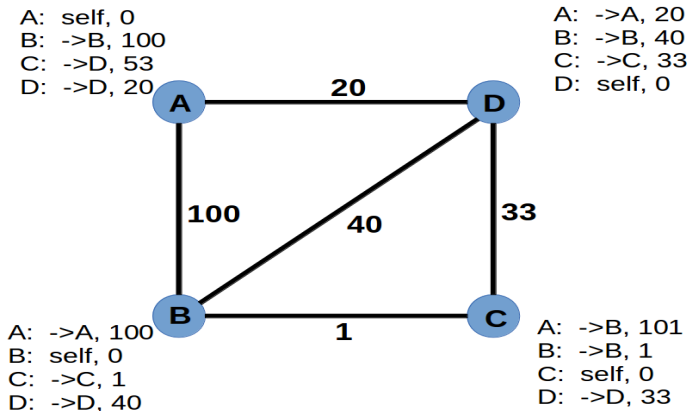


A: ->A  
B: self  
C: ->C  
D: ->D

A: ->B  
B: ->B  
C: self  
D: ->D

# Network Model

Routing table: correct forwarding table with total costs



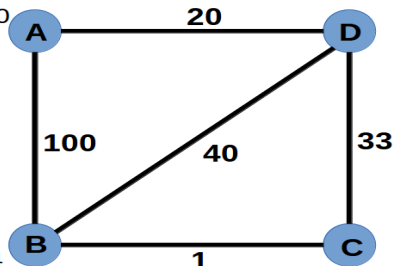


# Network Model

Forwarding table: **optimal**

A: self, 0  
B: ->D, 54  
C: ->D, 53  
D: ->D, 20

A: ->A, 20  
B: ->C, 34  
C: ->C, 33  
D: self, 0



A: ->C, 54  
B: self, 0  
C: ->C, 1  
D: ->C, 34

A: ->D, 53  
B: ->B, 1  
C: self, 0  
D: ->D, 33

# Routing Algorithms

## Nodes

- ▶ know (current) neighbor links and costs (HELLO protocol)
- ▶ exchange simple info, repeatedly
- ▶ aim to establish optimal routing ASAP

## Basic ideas:

- ▶ **distance-vector algorithms:**  
maintain/exchange w/neighbors your routing distance tables
- ▶ **link-state algorithms:**  
memorize and forward neighbor/cost info for every node

# Distance-Vector Algorithms

- ▶ each node maintains its own **distance vector**, i.e. a list of best available upper bounds for the distance to every **known** node on the network, as well as its neighbors' distance vectors
- ▶ distance vector (or just its **updates**) are sent to all neighbors regularly
- ▶ distance vector updates from neighbors may cause an update of node's own distance vector

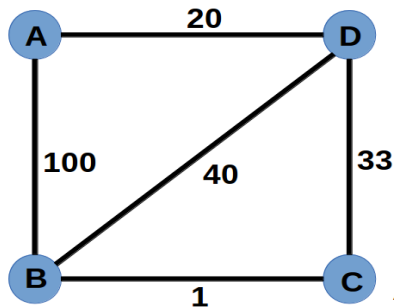
Bellman-Ford integration:

if node A is linked directly to node B at cost  $x$ , and the cost from node B to node C is not larger than  $y$  then the minimal cost from A to C is not larger than ...

# Distance-Vector: Initialization

A: 0  
B: inf  
C: inf  
D: inf

A: inf  
B: inf  
C: inf  
D: 0



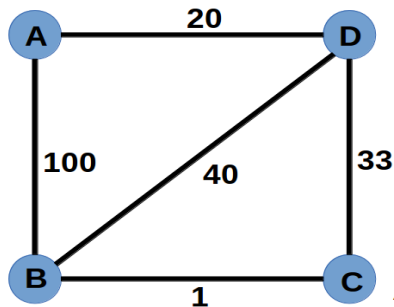
A: inf  
B: 0  
C: inf  
D: inf

A: inf  
B: inf  
C: 0  
D: inf

# Distance-Vector: After First Step

A: 0  
B: 60  
C: 53  
D: 20

A: 20  
B: 34  
C: 33  
D: 0



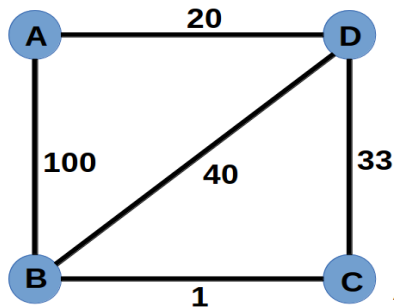
A: 60  
B: 0  
C: 1  
D: 34

A: 53  
B: 1  
C: 0  
D: 33

# Distance-Vector: After Second Step, or Steady-State

A: 0  
B: 54  
C: 53  
D: 20

A: 20  
B: 34  
C: 33  
D: 0



A: 54  
B: 0  
C: 1  
D: 34

A: 53  
B: 1  
C: 0  
D: 33

# Distance-Vector Algorithms: Formally

$$\text{cost}^+(a, c) = \min_{\text{neighbor } b} \{ \text{cost}(a, b) + \text{cost}(b, c) \}$$

- ▶ **convergence guarantee:** if network configuration remain constant, upper bounds of the cost eventually stop increasing (after a time equal to the maximal number of hops in an optimal path)
- ▶ **optimality guarantee:** if network configuration remain constant, upper bounds of the cost eventually become equal to the true minimal cost
- ▶ **correctness guarantee:** once the upper bounds are exact, forwarding to the neighbor with the minimal cost to the destination is correct and optimal (correctness relies on assuming that **all link costs are positive**)

# Link-State Algorithms

- ▶ nodes send out info about their links to neighbors, with costs (**LSA – link-state advertising**)
- ▶ nodes forward all LSAs they receive (only once)
- ▶ in time equal to the **diameter** of the network (measured in **hops**) all nodes will have all LSAs
- ▶ once a node has all LSAs from all nodes, it can optimize routing on its own (e.g., using the **Dijkstra algorithm**)

**LSA:** [node, (neighbor1,cost1), ..., (neighborN,costN)]



# Dijkstra's Shortest Path Algorithm

## Initialize:

- ▶ **nodeset**: [all nodes] (the set of nodes to be processed)
- ▶ **costs**:  $\text{costs}[\text{me}] = 0$ ,  $\text{costs}[\text{other}] = \text{inf}$  (costs to node, upper bounds)
- ▶ **routes**:  $\text{routes}[\text{me}] = \text{me}$ ,  $\text{routes}[\text{other}] = \text{None}$  (forwarding table)

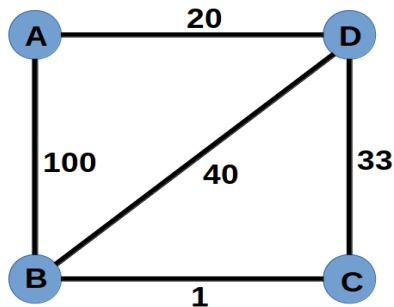
## Step (while **nodeset** isn't empty):

- ▶ find **u**, the node in nodeset with smallest **cost[u]**
- ▶ remove **u** from nodeset
- ▶ for all neighbors **v** of **u**:  
if  $\text{cost}[\text{v}] > \text{cost}[\text{u}] + \text{cost}(\text{u}, \text{v})$ :  
     $\text{cost}[\text{v}] = \text{cost}[\text{u}] + \text{cost}(\text{u}, \text{v})$   
     $\text{routes}[\text{v}] = \text{routes}[\text{u}]$  if  $u \neq \text{me}$ ,  $v \neq \text{me}$

# Dijkstra's Algorithm: Initialization

0: A

Inf: None



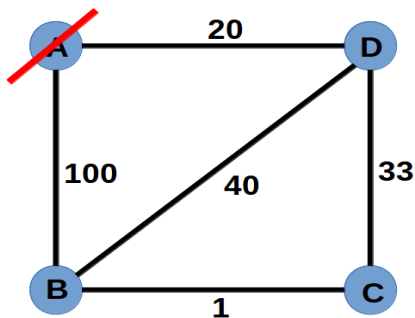
Inf: None

Inf: None

# Dijkstra's Algorithm: First Step

0: A

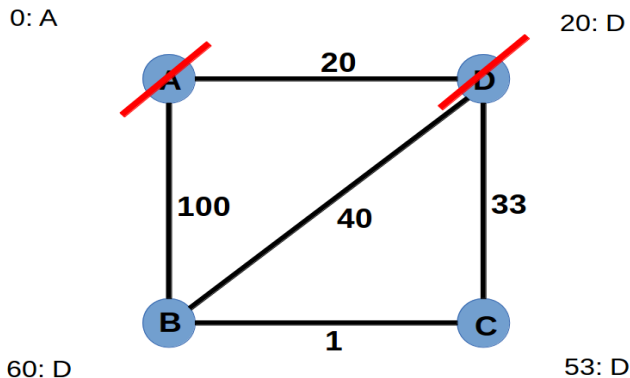
20: D



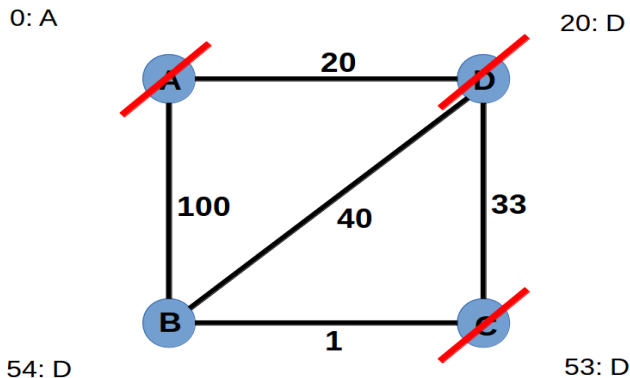
100: B

Inf: None

# Dijkstra's Algorithm: Second Step



# Dijkstra's Algorithm: Third Step



# Dijkstra's Shortest Path Algorithm: Complexity

Parameters:

- ▶ **N**: number of nodes
- ▶ **L**: number of links

Complexity:

- ▶ finding **u**: **N** times:  **$O(\log N)$**  each time, total  **$O(N \log N)$**
- ▶ updating **costs**:  **$O(L)$** , since each link appears twice