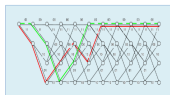
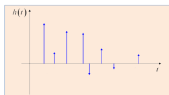


Reliable Data Transport

6.02 Fall 2013 Lecture 22



INTRODUCTION TO BECS II
**DIGITAL
COMMUNICATION
SYSTEMS**

Today's Plan

- ▶ Tools:
 - ▶ sequence number
 - ▶ time stamp
 - ▶ acknowledgements
 - ▶ retransmission
- ▶ Basic protocols:
 - ▶ stop-and-wait
 - ▶ sliding window
- ▶ Throughput analysis
- ▶ Round-trip time statistics

Reliable Data Transport: Objectives and Challenges

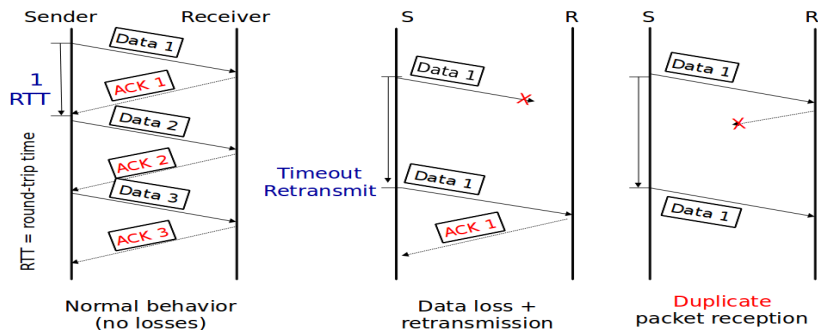
- ▶ sender sends a sequence of packets (DATA) to receiver
- ▶ receiver sends acknowledgements (ACK) of receipt
- ▶ packets/acknowledgements may be lost arbitrarily
- ▶ packets/acknowledgements may be reordered arbitrarily
- ▶ packet/acknowledgements delays are variable (queueing)
- ▶ packets may even be duplicated
- ▶ sender wants to know which data was received
- ▶ receiver wants to assemble a correct sequence of all packets

- ▶ Transmitter
 - ▶ receive packets in sequence for transmission
 - ▶ attach sequence numbers and time stamps before transmission
 - ▶ keep "transmission time, packet sequence number" record
 - ▶ keep "packet acknowledged" and "round-trip time" records
 - ▶ periodically re-transmit long-unacknowledged packets

- ▶ Receiver:
 - ▶ send acknowledgements for received packet sequence numbers
 - ▶ deliver packets in sequence

The "Stop-and-Wait" Protocol

- ▶ transmit next packet only after receiving ACK (for the previous one)
- ▶ re-transmit unacknowledged packet in time T_o (timeout) (after sending out its last copy)
- ▶ adjust T_o using round-trip time and packet loss statistics

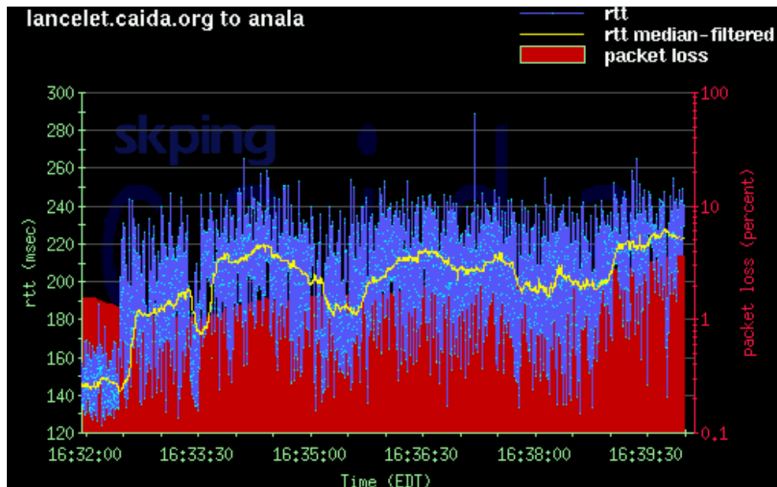


Choosing timeout T_o

- ▶ **Too small:**
unnecessary re-transmissions of acknowledged packets
- ▶ **Too large:**
poor throughput waiting for lost packets' acknowledgements

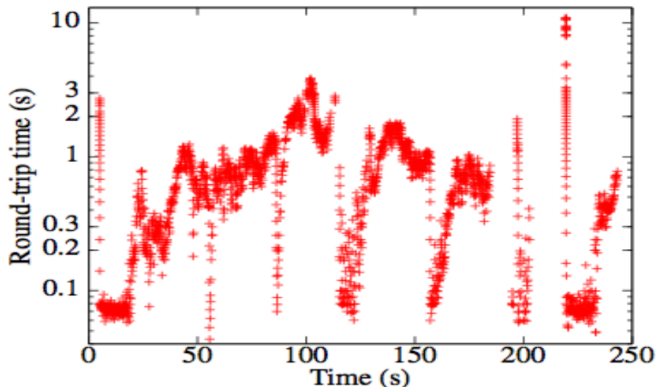
- ▶ Analysis depends on network properties: too tricky
- ▶ Trying to get insight based on simplistic models

Round-Trip Time as a Random Variable



Round-Trip Time as a Random Variable

Figure 1: Round-trip time during a TCP download on the Verizon LTE network in Cambridge, Mass., Oct. 14, 2011 at 3 p.m.



<http://nms.csail.mit.edu/papers/index.php?detail=208>

Two Simplistic Performance Numbers

- (a) Assume round-trip time T_r is a random variable, but nothing is lost. Then $\mathbf{P}(\text{re-transmission}) = \mathbf{P}(T_r > T_o)$ should be small enough. Since $\mathbf{P}(T_r > T_o)$ decreases as T_o increases, T_o must be large enough
- (b) Assume round-trip time $T_r < T_o$ is fixed, but packets are lost with probability p , causing time T_a to receiving acknowledgement to be random. Then average time per packet $T = \mathbf{E}[T_s]$ should be small enough. Since $T = (1 - p)T_r + p(T + T_o)$ implies $T = T_r + \frac{pT_o}{1-p}$, T_o must be small enough
- ▶ Use (a) as a guide to get T_o from the statistics of T_r
 - ▶ Otherwise, use (b) to keep T_o as small as possible

Markov Inequality as a Guide

How do you find a threshold γ such that $\mathbf{P}(X \geq \gamma) \leq q$ when we do not know much about the distribution of X ?

If $X \geq 0$ and $\gamma \geq 0$ then $\gamma \mathbf{P}(X \geq \gamma) \leq \mathbf{E}[X]$

- ▶ Apply with $X = |T_r - \mathbf{E}[T_r]|^2$: **Chebyshev inequality**
- ▶ Apply with $X = |T_r - \mathbf{E}[T_r]|$: common in traffic control

$$T_o = \mathbf{E}[T_r] + \frac{\mathbf{E}[|T_r - \mathbf{E}[T_r]|]}{q}.$$

How do we get $\mathbf{E}[T_r]$ and $\mathbf{E}[|T_r - \mathbf{E}[T_r]|]$?

Estimating $\hat{T}_r = \mathbf{E}[T_r]$ and $\hat{V}_r = \mathbf{E}[|T_r - \mathbf{E}[T_r]|]$

The "time-invariant" case:

$$\hat{T}_r = \frac{T_{r1} + T_{r2} + \dots + T_{rm}}{m}$$

$$\hat{V}_r = \frac{|T_{r1} - \hat{T}_r| + |T_{r2} - \hat{T}_r| + \dots + |T_{rm} - \hat{T}_r|}{m}$$

with m round-trip measurements T_{r1}, \dots, T_{rm}

When m is large, this becomes very slow to adapt to changes in $\hat{T}_r = \mathbf{E}[T_r]$ and $\hat{V}_r = \mathbf{E}[|T_r - \mathbf{E}[T_r]|]$

Exponentially Weighted Moving Average

To adapt to changes in T_r distribution:

$$\begin{aligned}\hat{T}_r^+ &= (1 - \alpha)\hat{T}_r + \alpha T_r \\ \hat{V}_r^+ &= (1 - \beta)\hat{V}_r + \beta|T_r - \hat{T}_r|\end{aligned}$$

$0 < \alpha, \beta < 1$ (TCP uses $\alpha = 1/8$, $\beta = 1/4$)
previous slide is the "limit as $\alpha, \beta \rightarrow 0$ "

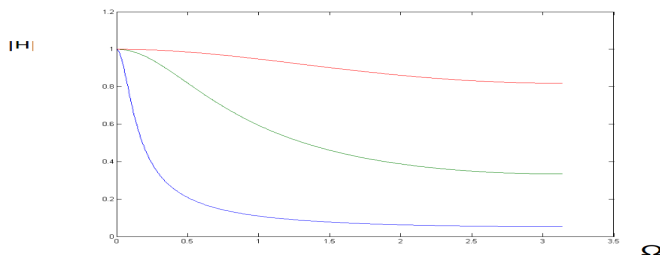
Meaning: $1/\alpha$, $1/\beta$ are the **time constants** of the network

EWMA: What Is Going On

LTI model: $y[n + 1] = (1 - \alpha)y[n] + \alpha x[n]$

Step response: $y_s[n] = 1 - (1 - \alpha)^n \quad (n \geq 0)$

Frequency response: $H(\Omega) = \frac{\alpha}{e^{j\Omega} - 1 + \alpha}$



Which color corresponds to the smallest α ?

Example: Stop-and-Wait Performance With Constant T_r

Recall:

$$T = T_r + \frac{pT_o}{1-p}$$

If bottleneck link can support 100 packets/sec, $T_r = 100ms$, and $T_o = T_r + \epsilon$ then, using stop-and-wait, the maximum throughput is at most only 10 packets/sec.

Only 10 percent utilization:

We need a better reliable transport protocol

Sliding Window Protocol

- ▶ Allow up to W unacknowledged packets
- ▶ Packet k acknowledged – send out packet $k + W$
- ▶ Keep a buffer of out-of-order packets at the receiver

