

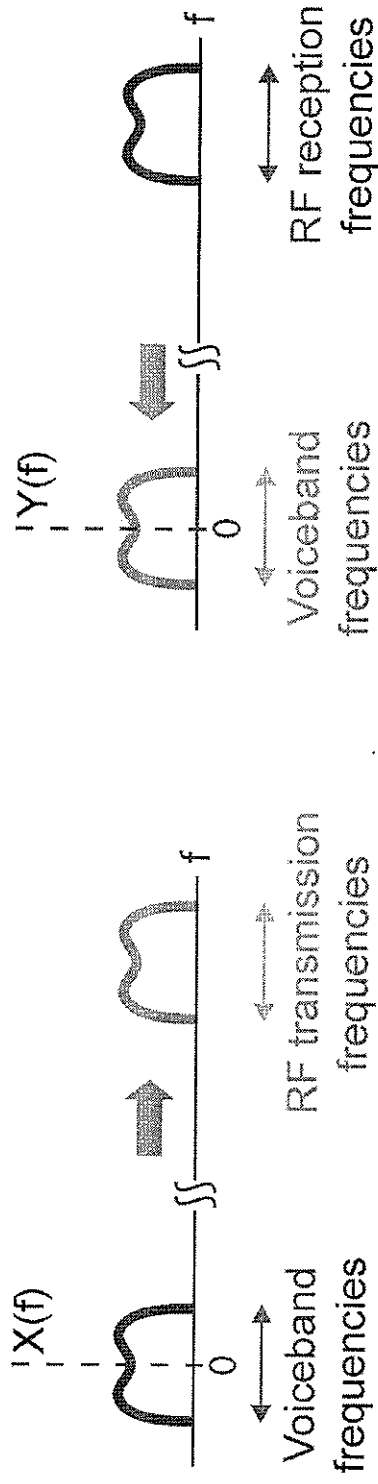
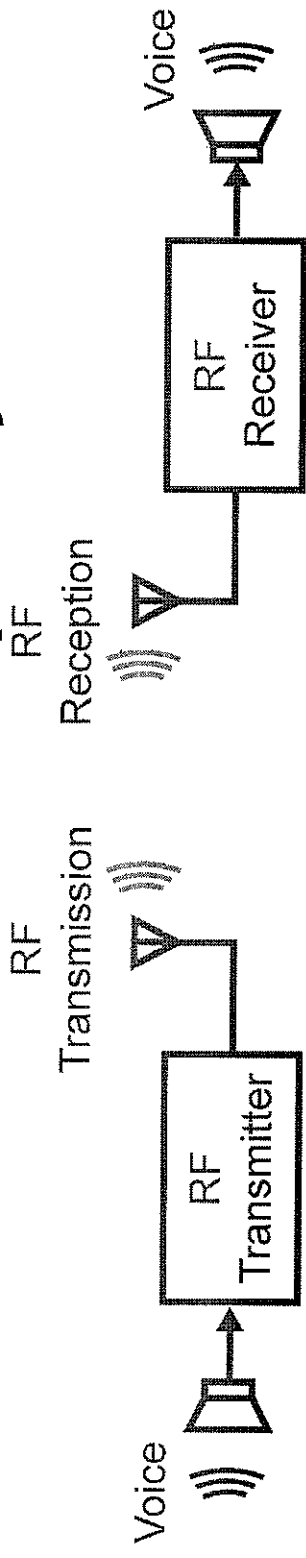
INTRODUCTION TO EACS II

# DIGITAL COMMUNICATION SYSTEMS

## 6.02 Spring 2009 Lecture #16

- Modulation Step-by-Step
- Phase Coherency Issue

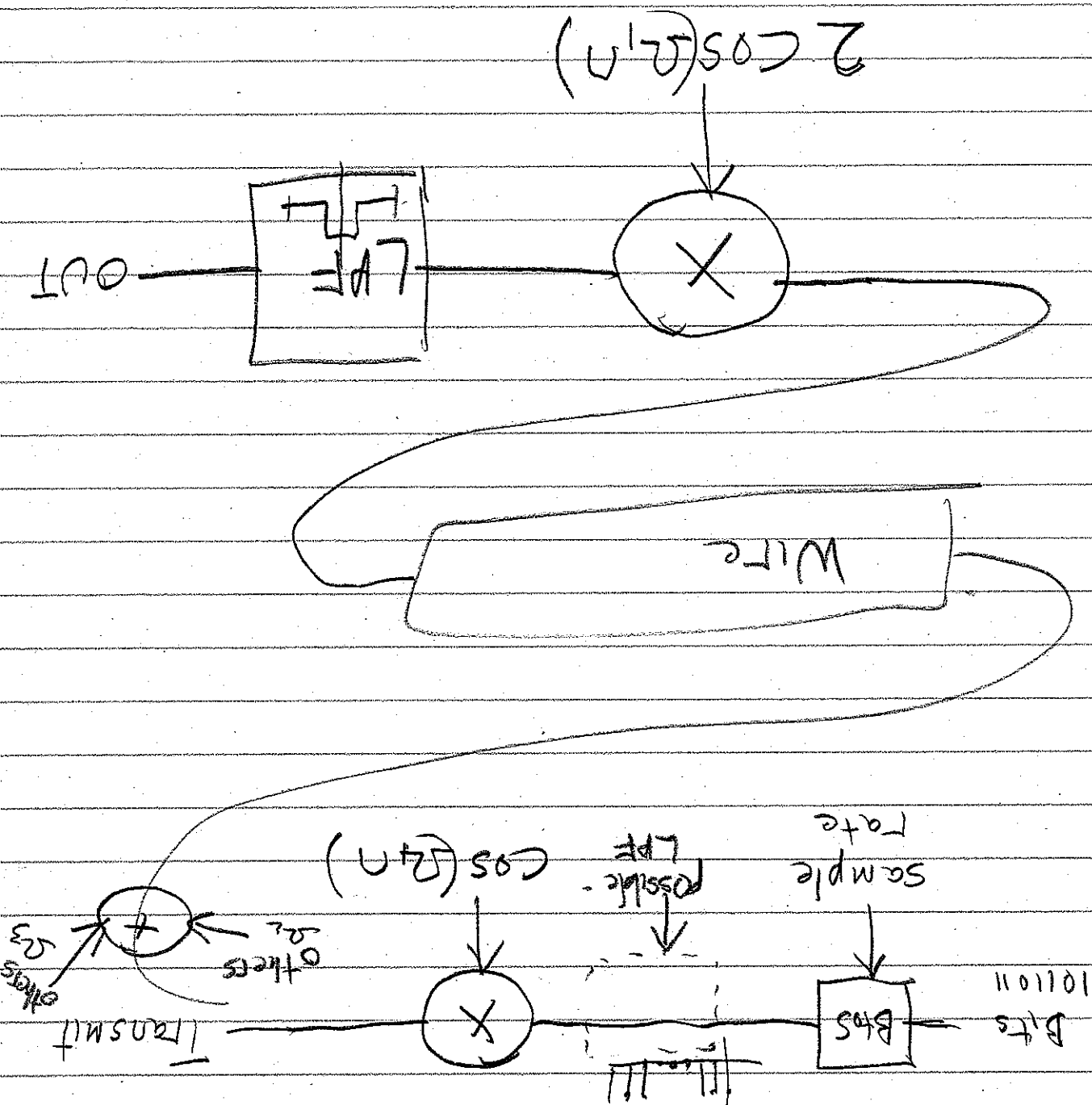
# Motivation for High Frequency Modulation



- Modulation is used to change the frequency band of a signal
  - Enables RF communication in different frequency bands
    - Used in cell phones, AM/FM radio, WLAN, cable TV, ....
  - Note: higher frequencies lead to smaller antennas
    - 3GHz, 10cm wavelength, 2.5cm antenna ( $1/4$  wavelength)

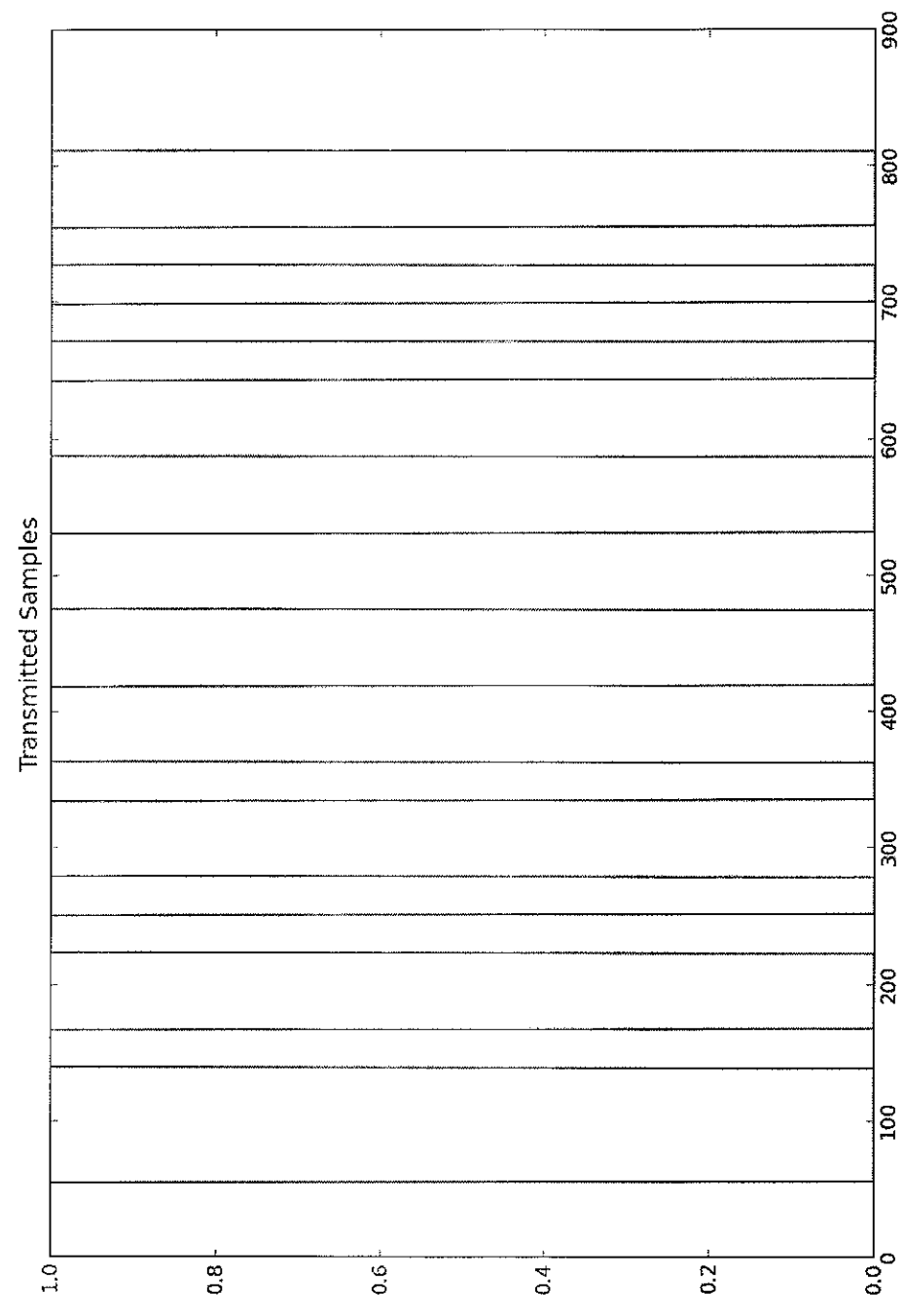
# Block Diagram of Modulation

2



④

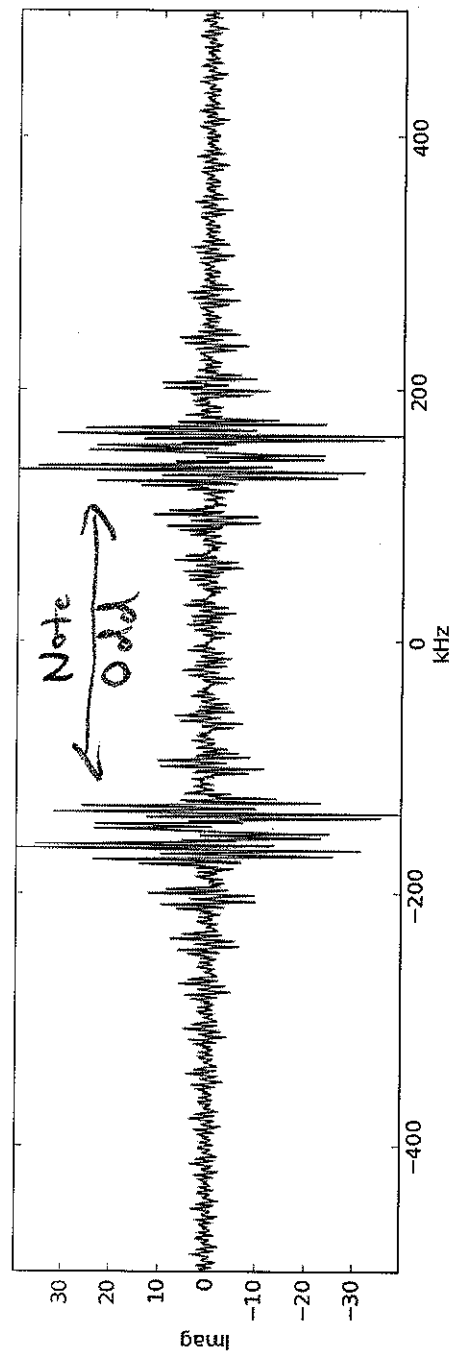
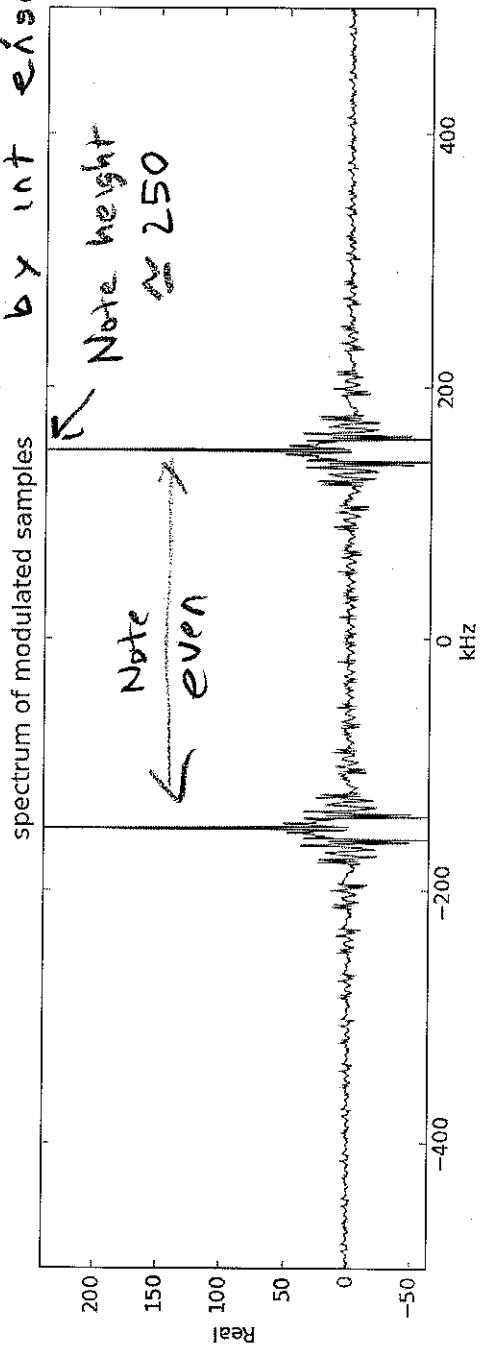
# 35000 Bits/Sec, 1M samples/sec



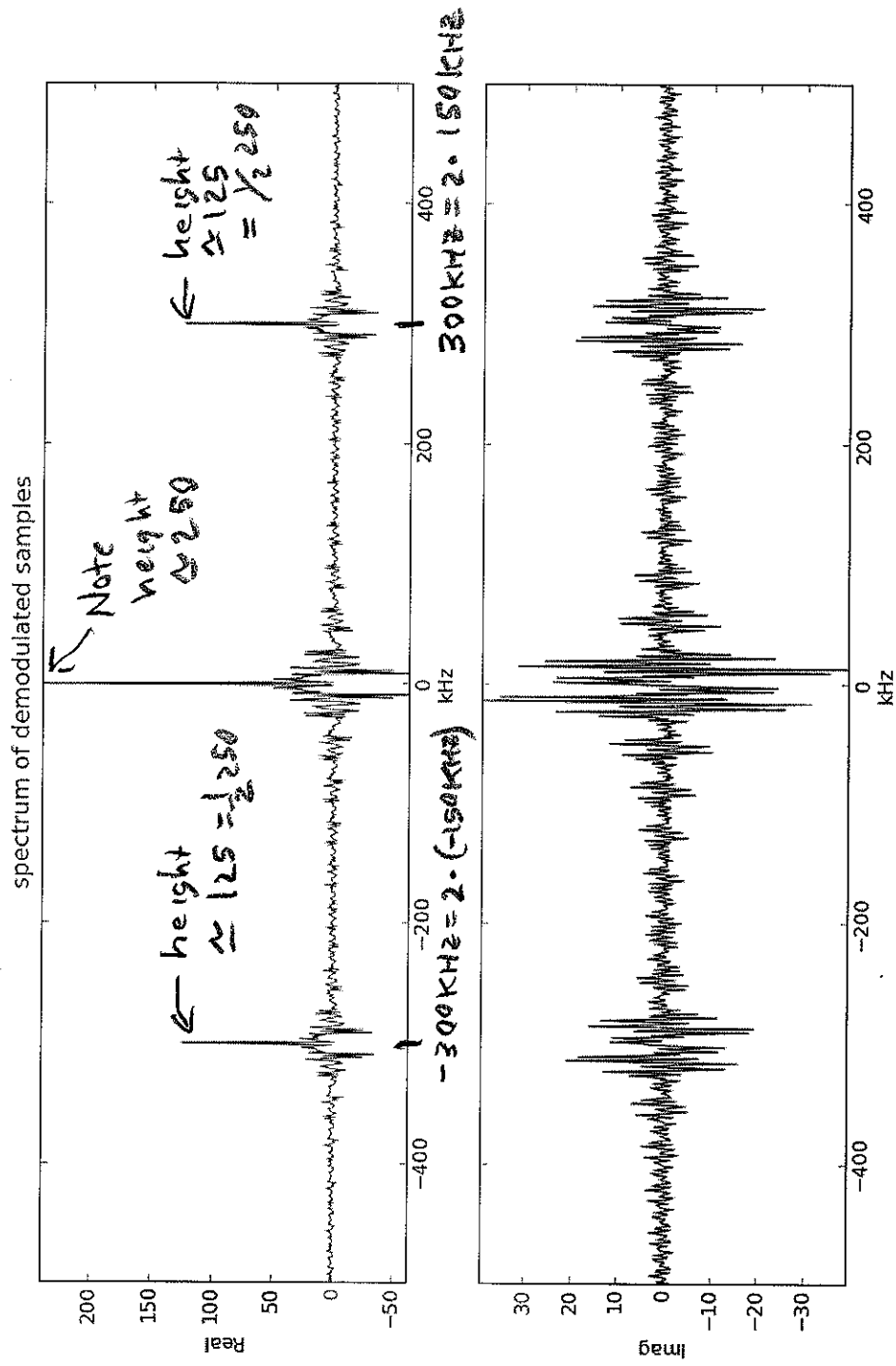
5

# Post 150Khz Modulation (1M Sample Rate)

Note  $N=1099001$  DFT used 50 150KHz approximated as  $\text{int}(\frac{150000}{1M} N) \cdot (1M/N)$ . The rounding performed by int ensures an actual DFT frequency.

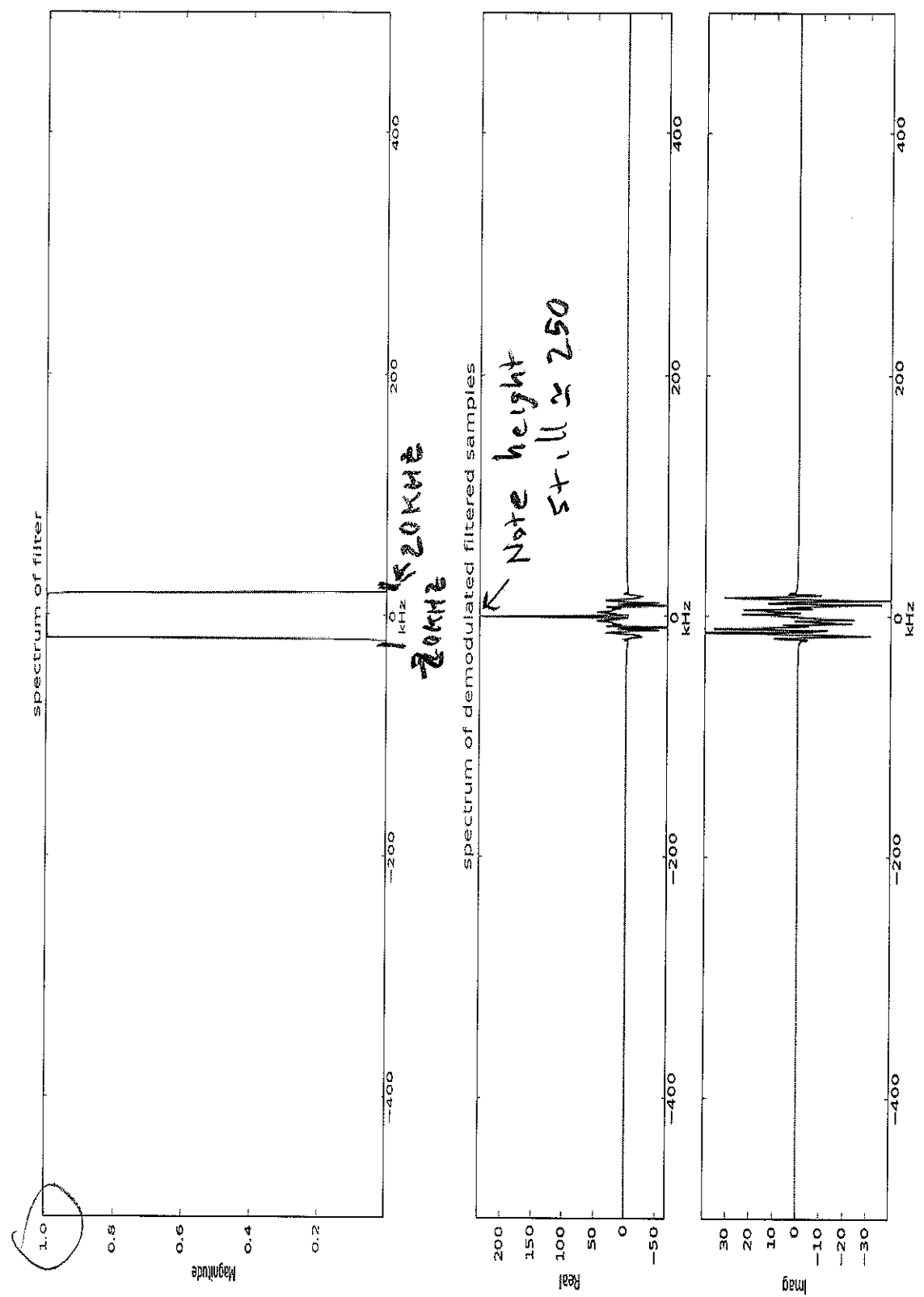


# Spectrum of Demodulated Signal



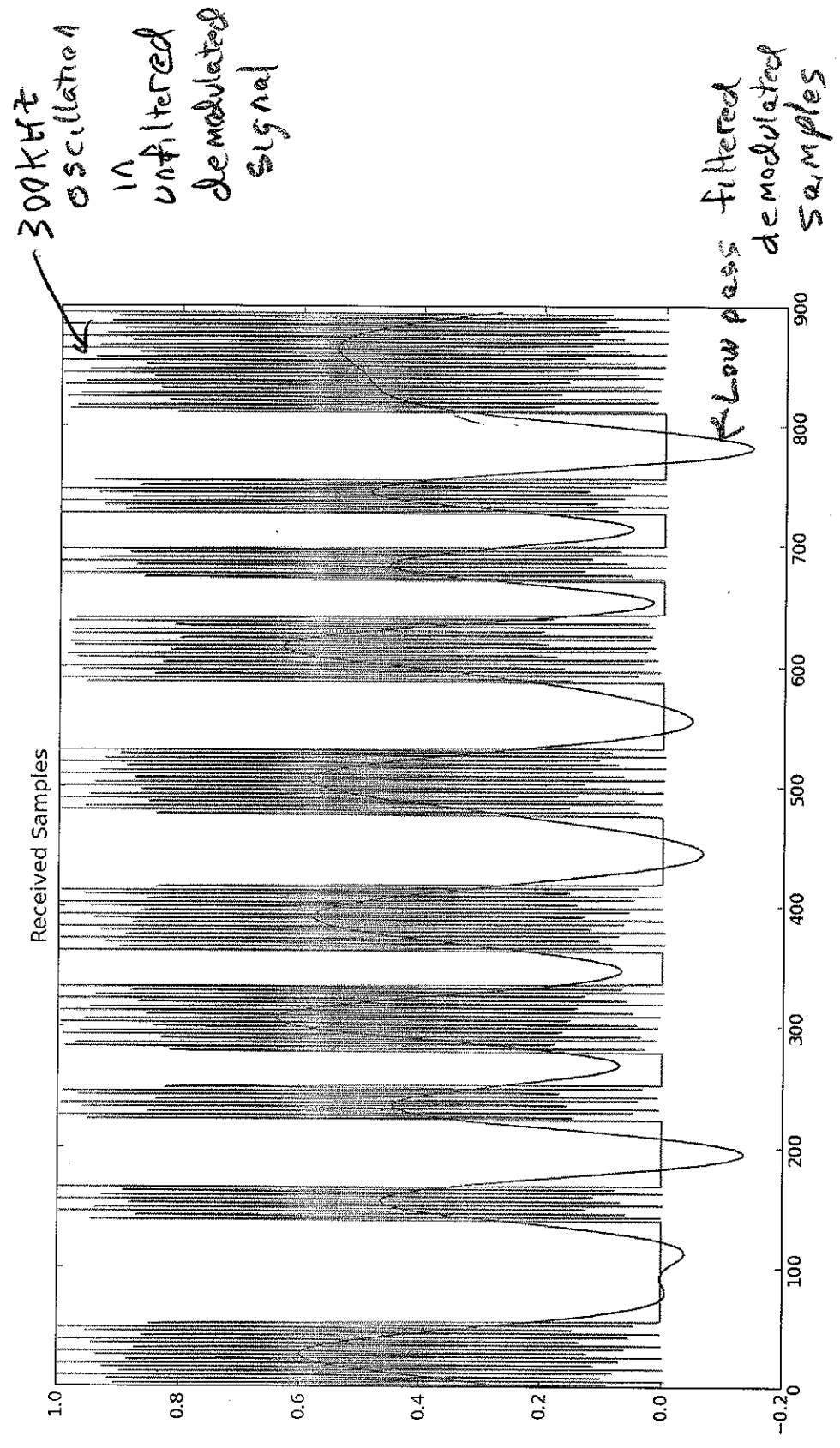
⑦

# LPF and Spectrum After LPF



8

# Received samples pre and post LPF

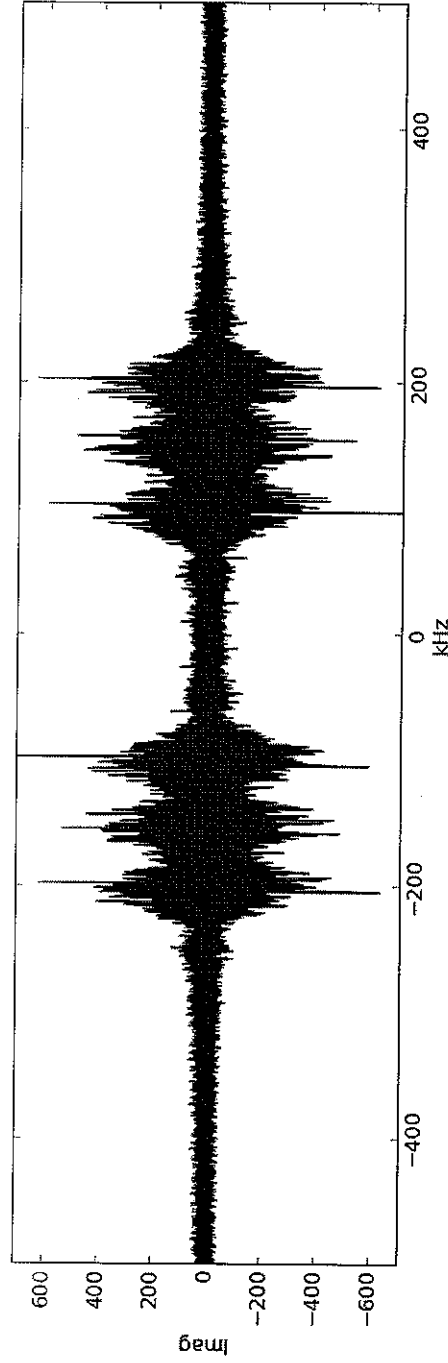
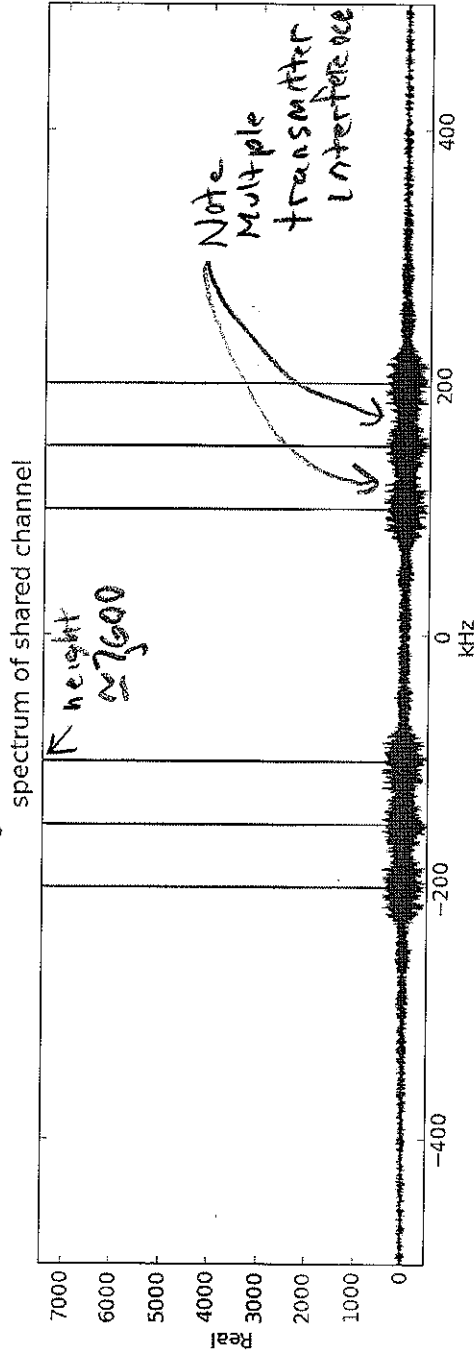




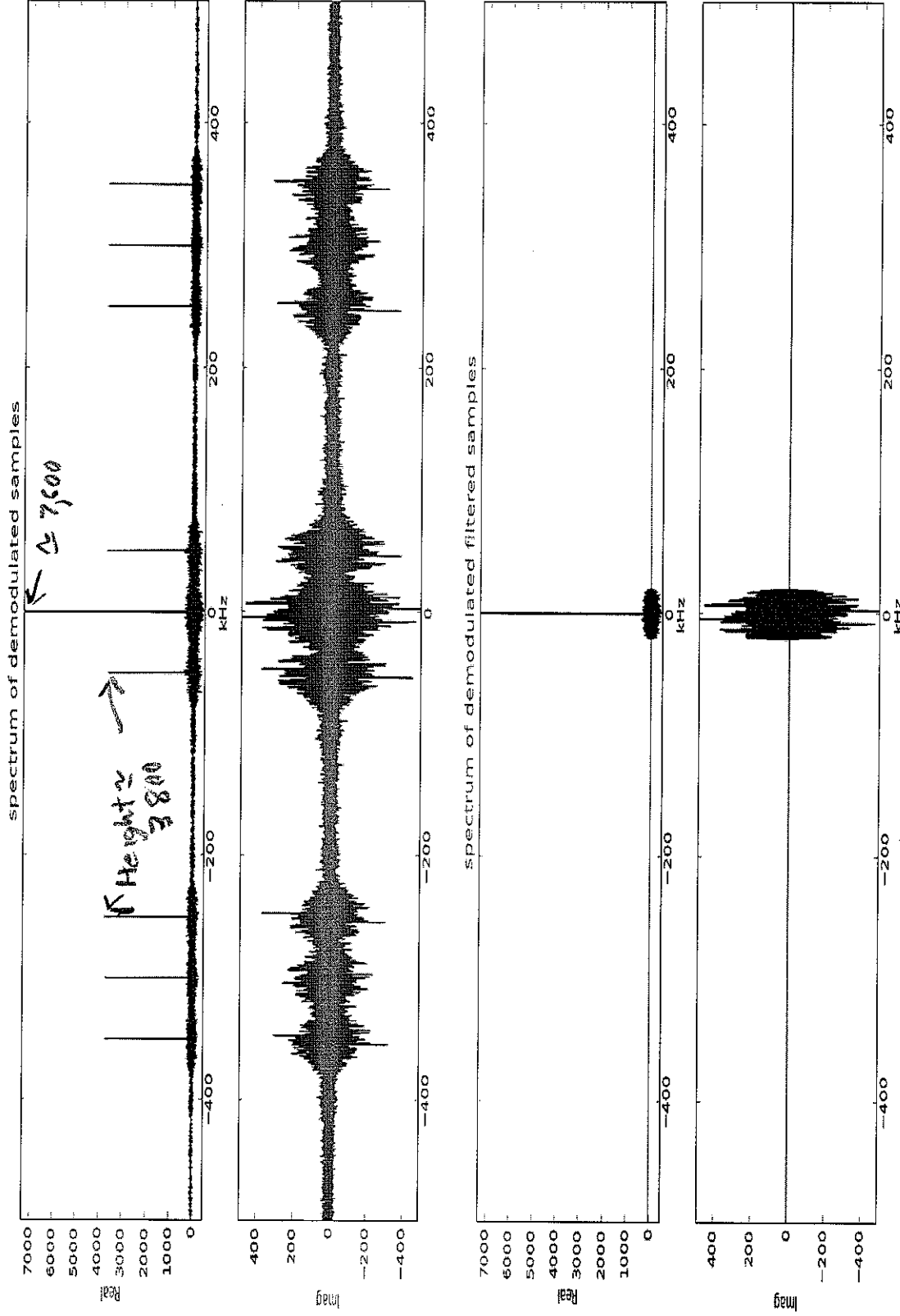
9

# Spectrum: 100, 150, 200Khz transmitters

Again, aligned to nearest  $f_k = \frac{K}{N} \cdot 1M$

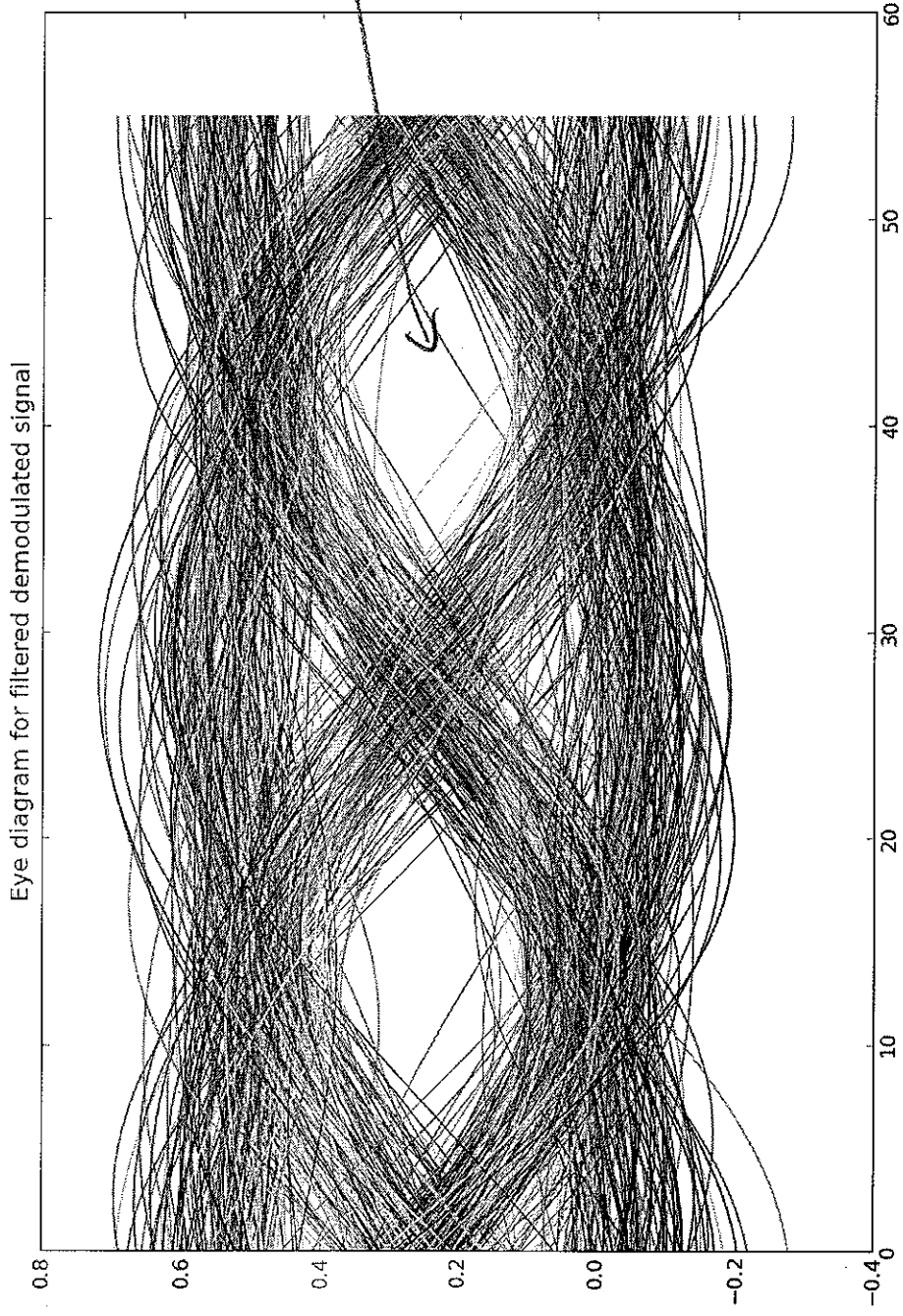


# Demod Spectrum Before and After LPF



11

# Eye Diagram for Received Bits

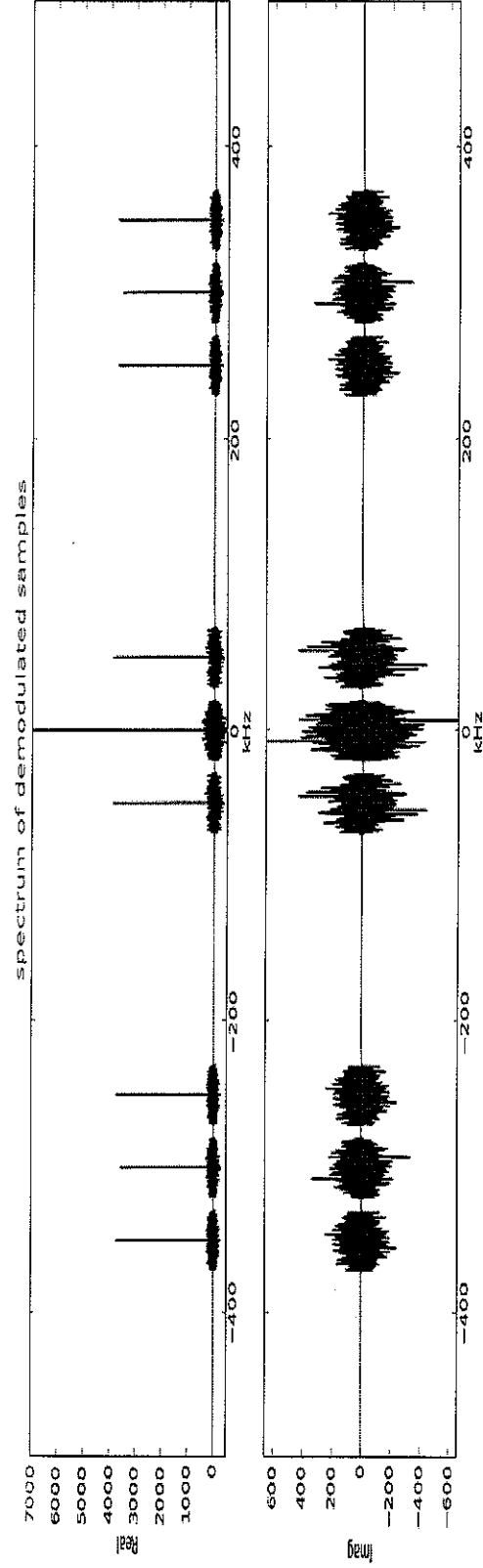
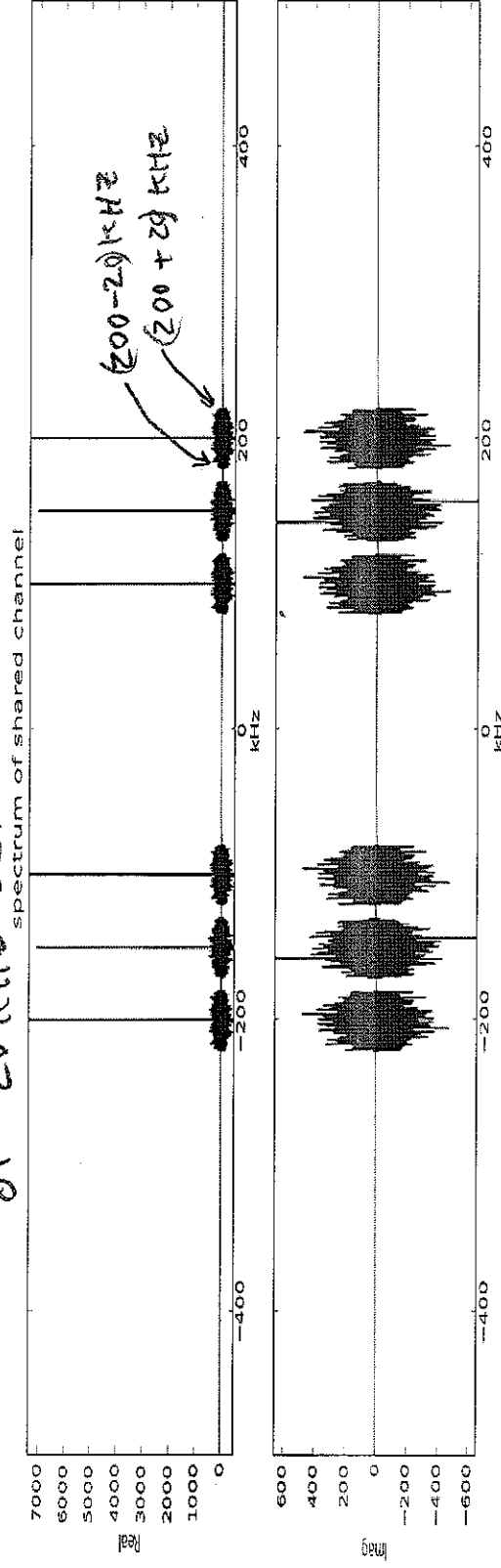


Includes  
interference  
from other  
transmitters  
and  
intersymbol  
interference,

12

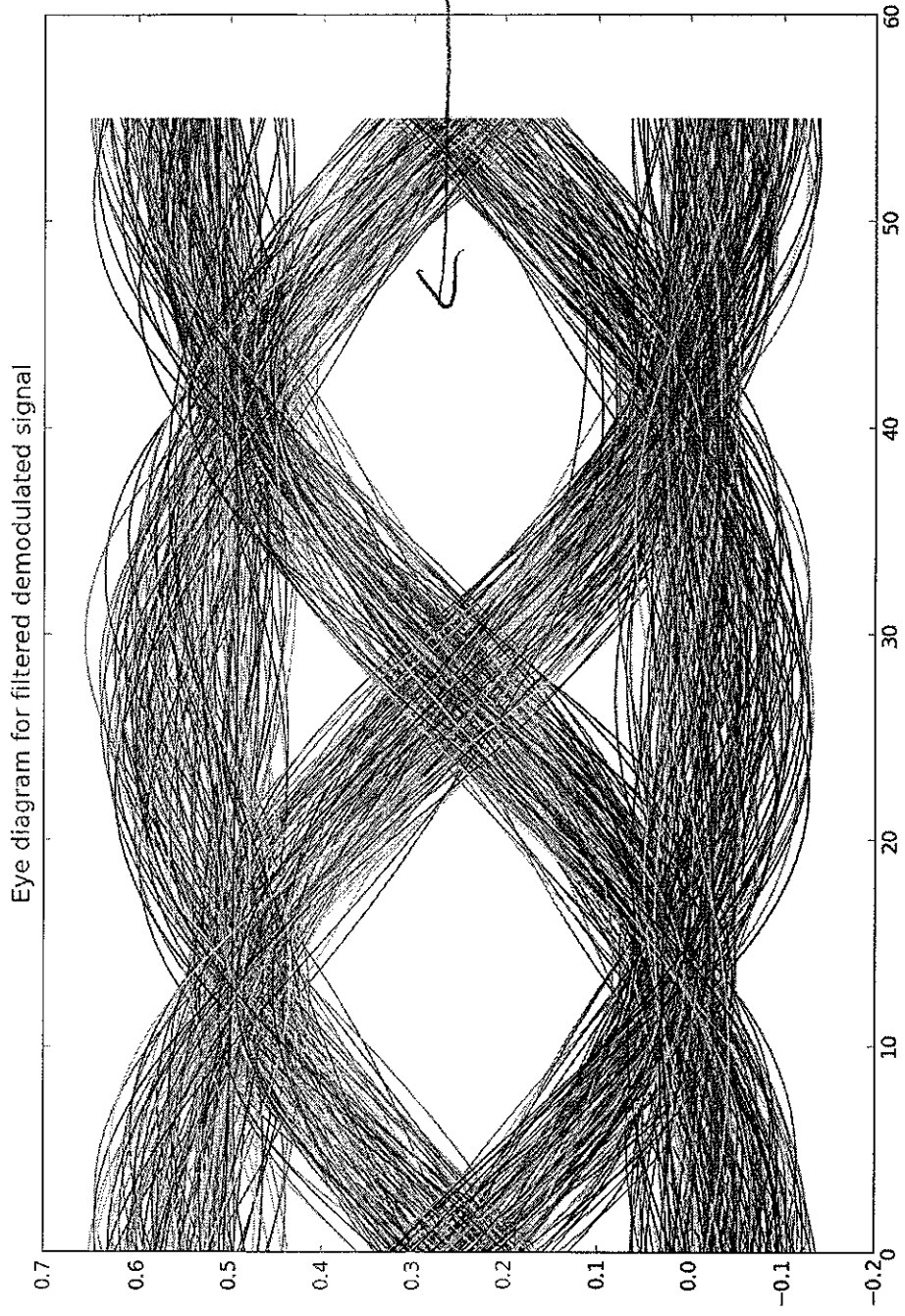
# Transmit Filtered Spectrum, Pre/Post Demod

Each signal is filtered with a cutoff frequency of 20 kHz before modulation



13

# Eye Diagram received bits, transmit filters



Note  
eye  
diagram  
Improvement,  
There is  
still  
intersymbol  
interference,  
but little  
multiple  
transmitter  
interference

$$+ \left( \frac{1}{2} e^{-j\omega n} + \frac{1}{2} e^{j\omega n} \right)$$

$$+ \frac{1}{2} e^{-j\omega n} e^{j\omega n} + \frac{1}{2} e^{j\omega n} e^{-j\omega n}$$

$$\left( \frac{1}{2} e^{-j\omega n} e^{j\omega n} + \frac{1}{2} e^{j\omega n} e^{-j\omega n} \right) \left( \frac{1}{2} e^{j\omega n} + \frac{1}{2} e^{-j\omega n} \right)$$

Consider the modulation SN=1

$$= \left( \frac{1}{2} e^{-j\omega n} e^{j\omega n} + \frac{1}{2} e^{j\omega n} e^{-j\omega n} \right) s[n-D]$$

$$s[n-D] \cos(\omega(n-D))$$

Received signal

$D = \# \text{ samples of delay}$

Modulated and delayed signal

$$s[n] \cos(\omega n) = s[n] \left( \frac{1}{2} e^{j\omega n} + \frac{1}{2} e^{-j\omega n} \right)$$

Modulated signal

Adding white delay

(14)

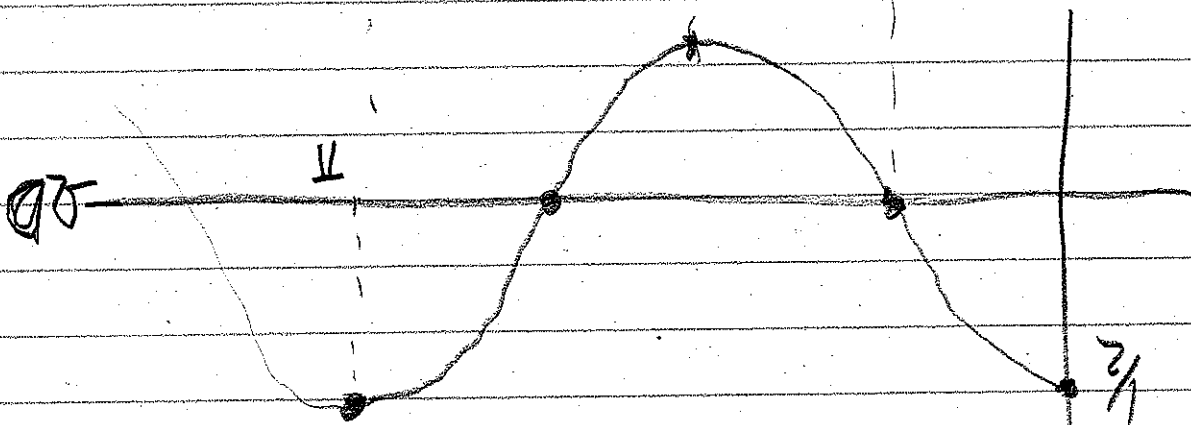
Demod by Sine

$$\left( \frac{1}{2} e^{-j\omega t} + \frac{1}{2} e^{j\omega t} \right) \left( \frac{1}{2} e^{-j\omega t} + \frac{1}{2} e^{j\omega t} \right)$$

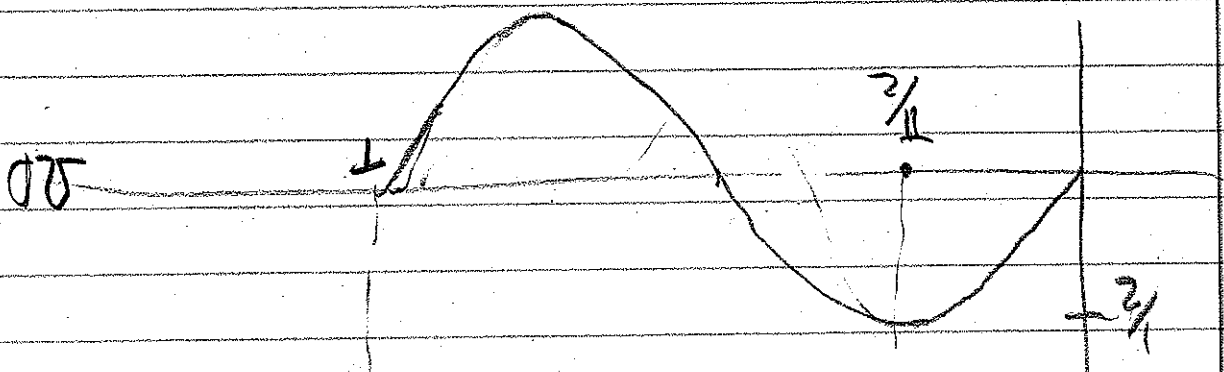
$$= \frac{1}{4} e^{-j\omega t} e^{-j\omega t} + \frac{1}{4} e^{-j\omega t} e^{j\omega t} + \frac{1}{4} e^{j\omega t} e^{-j\omega t} + \frac{1}{4} e^{j\omega t} e^{j\omega t}$$

$$+ \frac{1}{4} (e^{-j2\omega t} - e^{-j\omega t})$$

Cosine output after LPF  $S(t)=1$

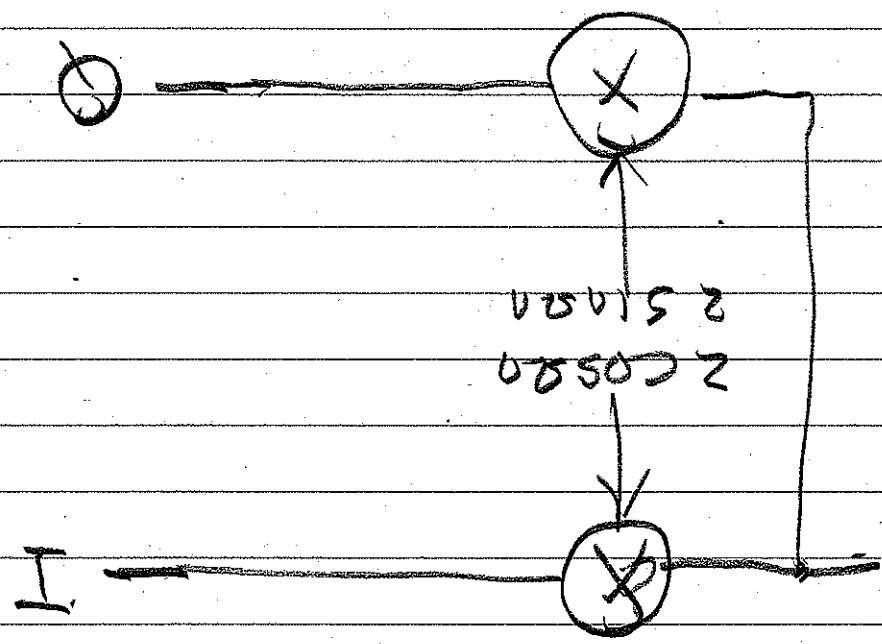


Sine output after LPF  $S(t)=1$



Suppose  $S(t) = 1$  V

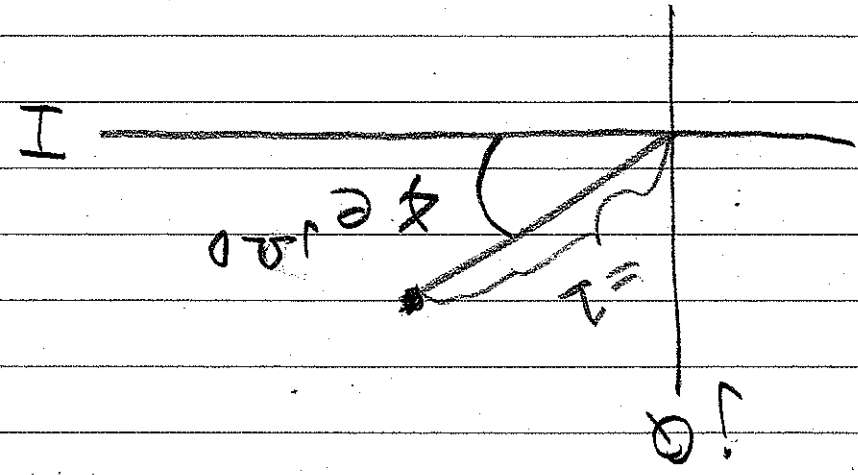
Note



$$|I|^2 + |0|^2 = 1$$

$$\cos^2 20t + \sin^2 20t$$

Regardless of delay

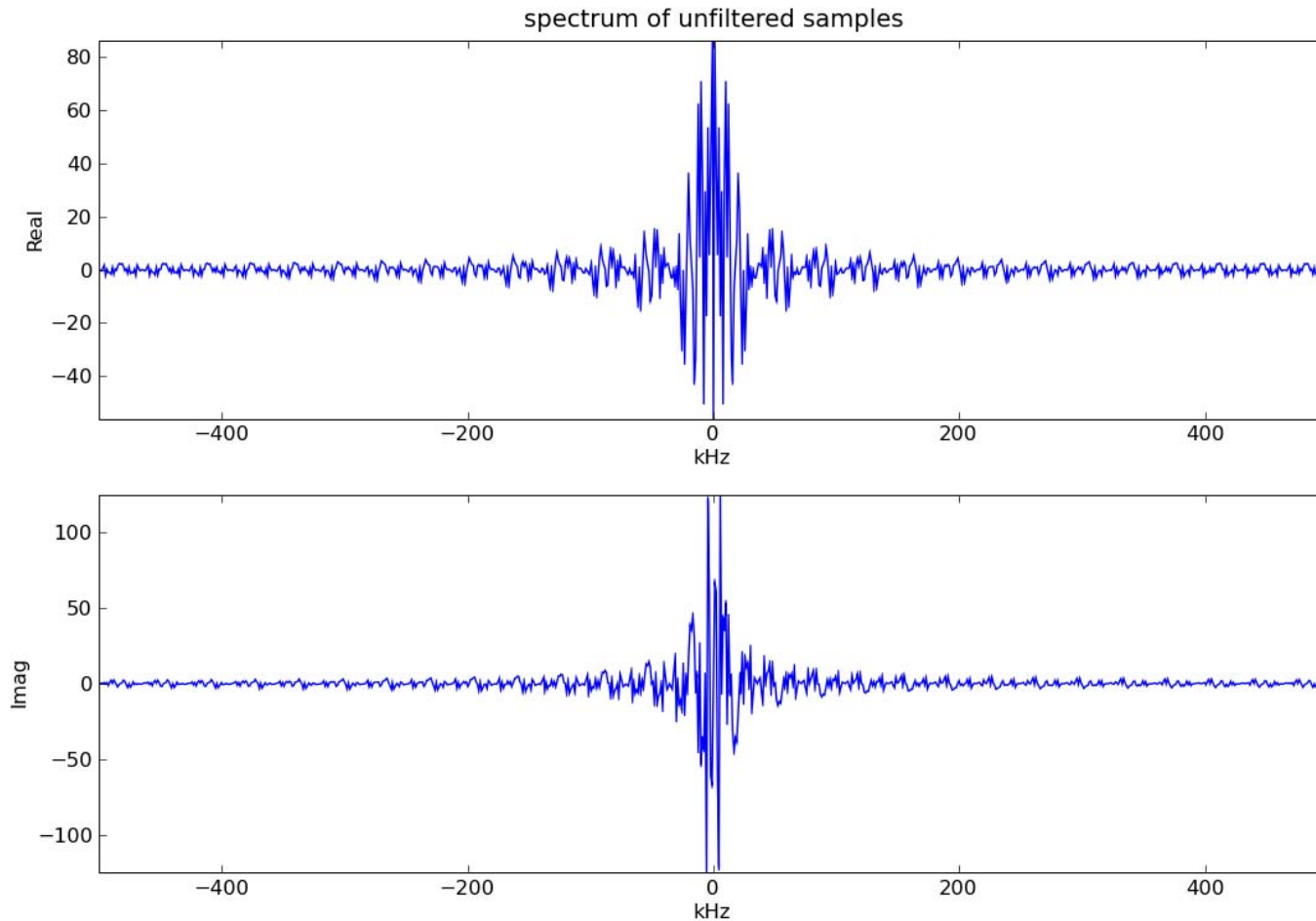




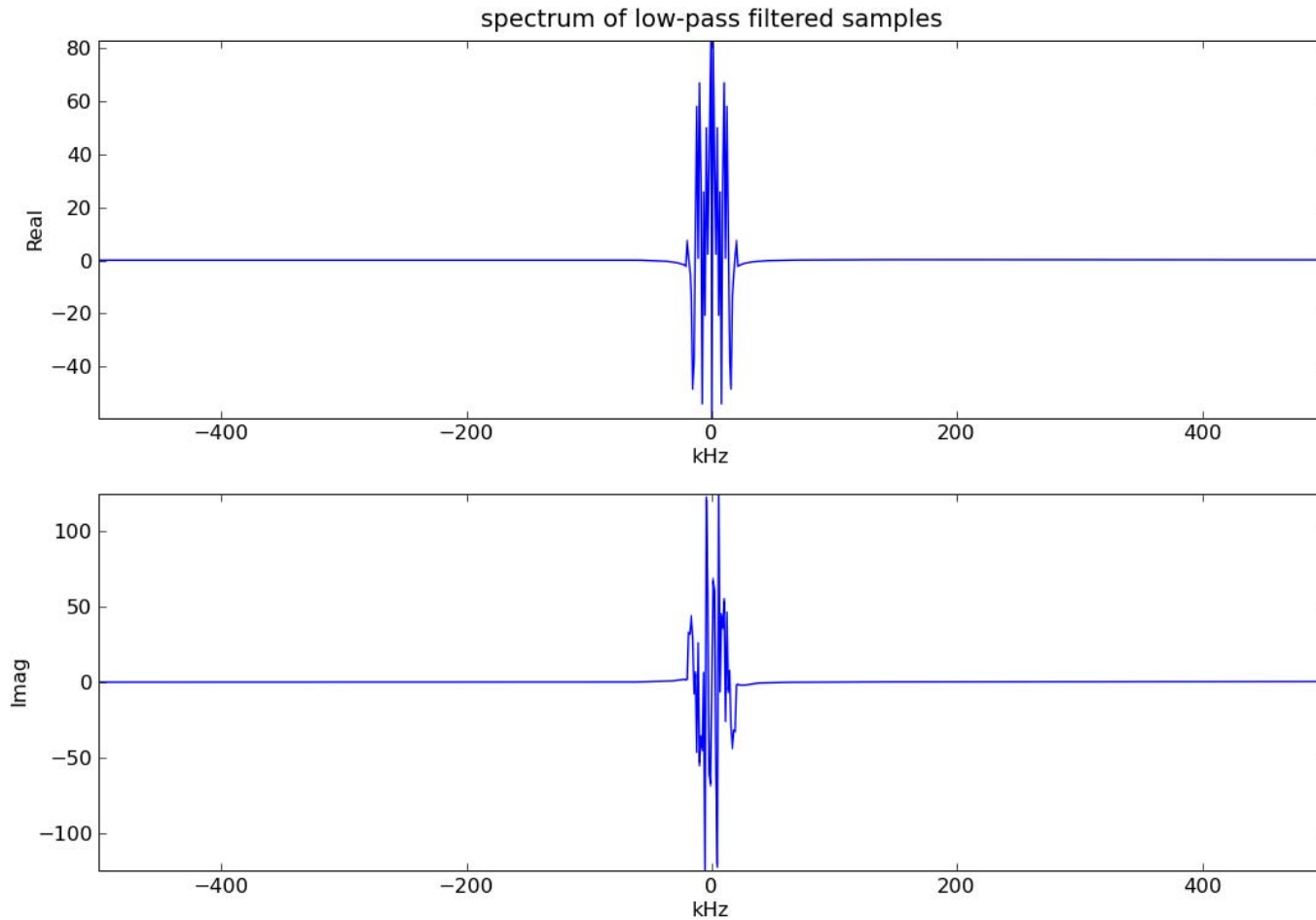
In the following single sideband modulation example,  $1e6$  samples/sec and 35000 bits/sec are used. A signal is low-pass filtered (with 20kHz cutoff frequency) is modulated with a cosine at 200Khz. Then the signal is high-pass filtered with a filter cutoff frequency of 200kHz to produce a single side-band like spectrum and then demodulated with a cosine to recover the signal.

Note: In this example, the samples are using -0.5volts for zero and 0.5volts for one. This eliminates a large component at DC, and removes an ambiguity with the single side-band like signal (If there is a large DC component, then after modulation there will be a large component of the spectrum at exactly 200kHz that has to be divided in half for the single side-band to work properly).

# Spectrum of unfiltered samples

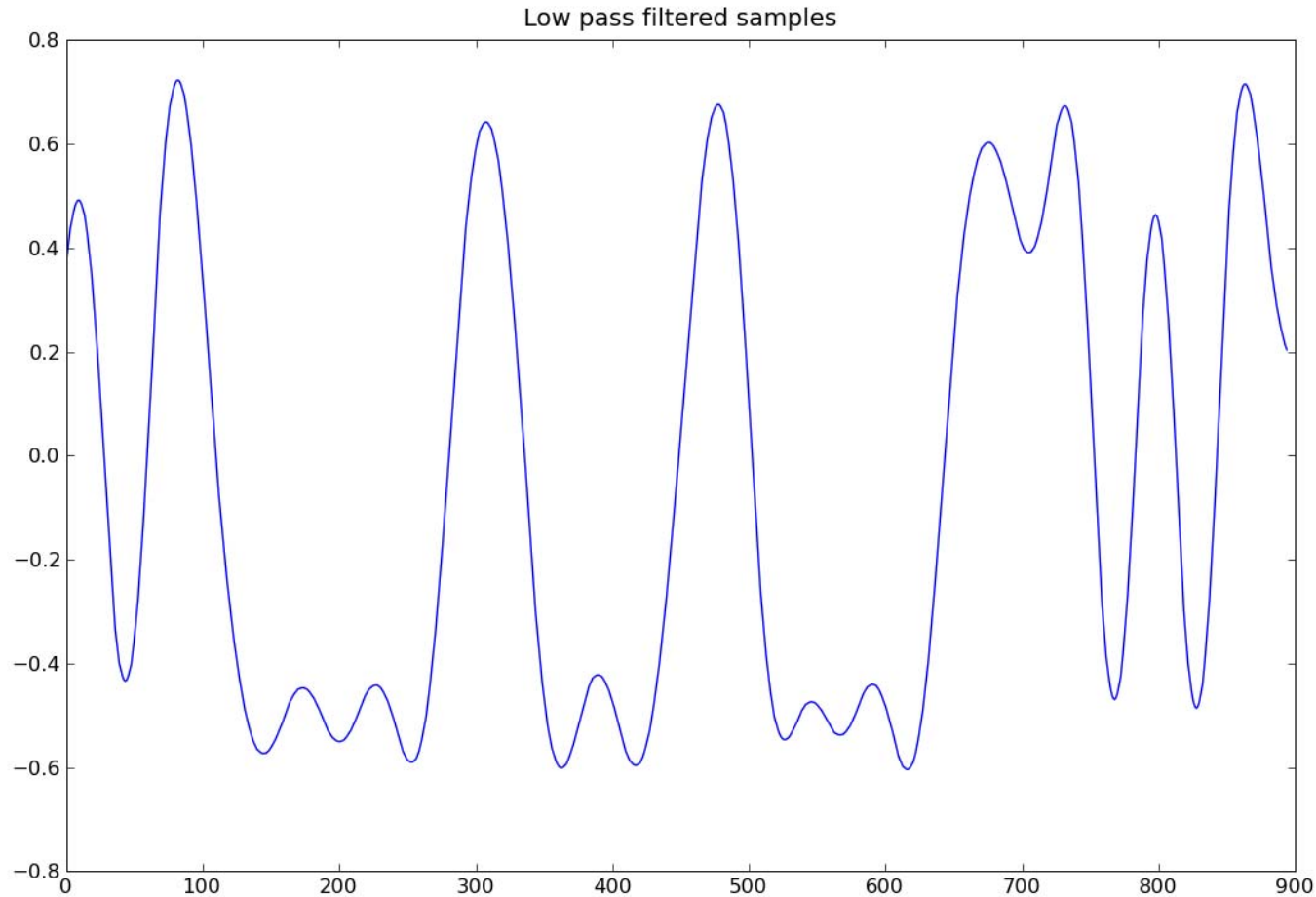


# Spectrum of LPF samples

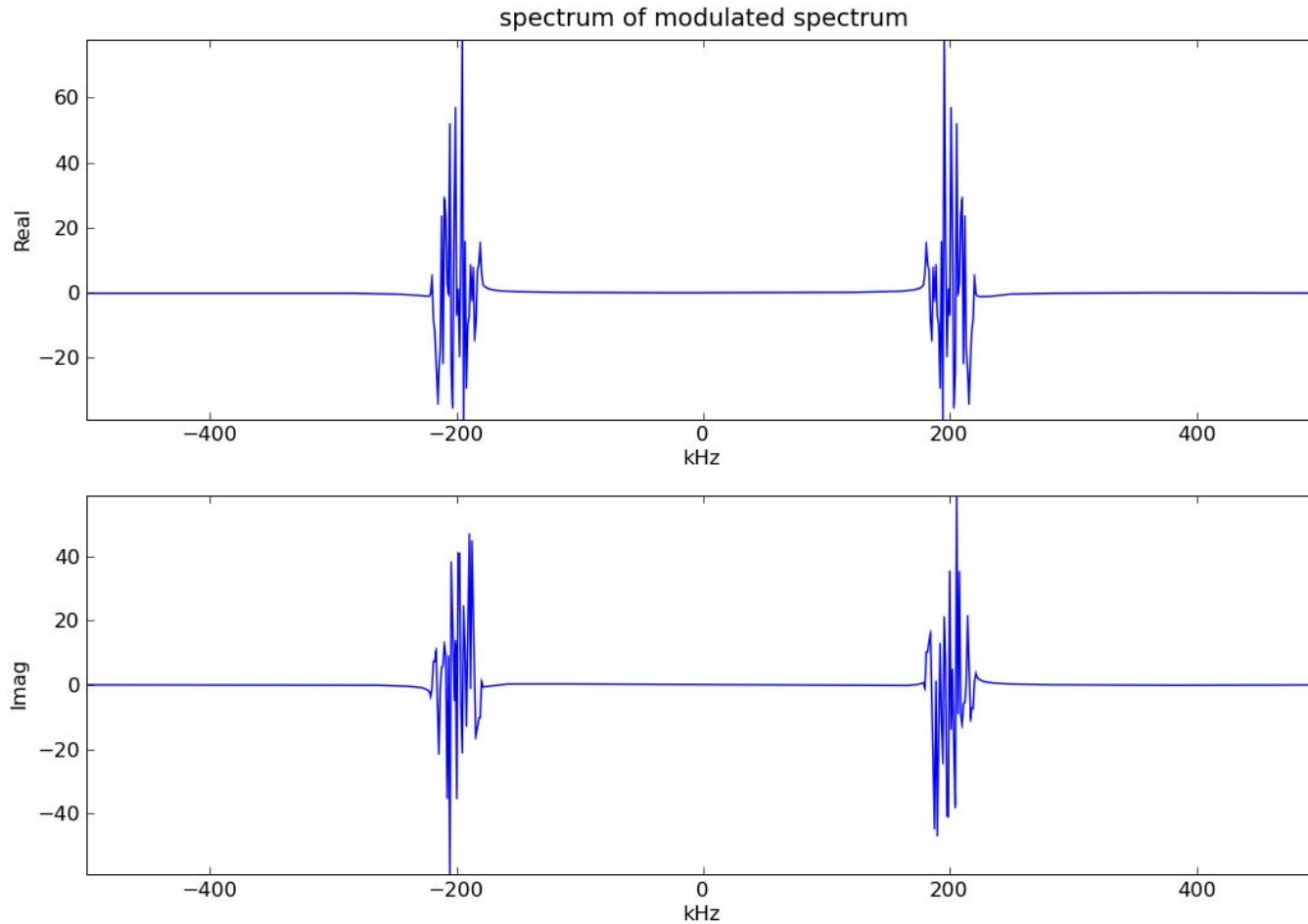


# Time-domain Plot of LPF samples (32 bits)

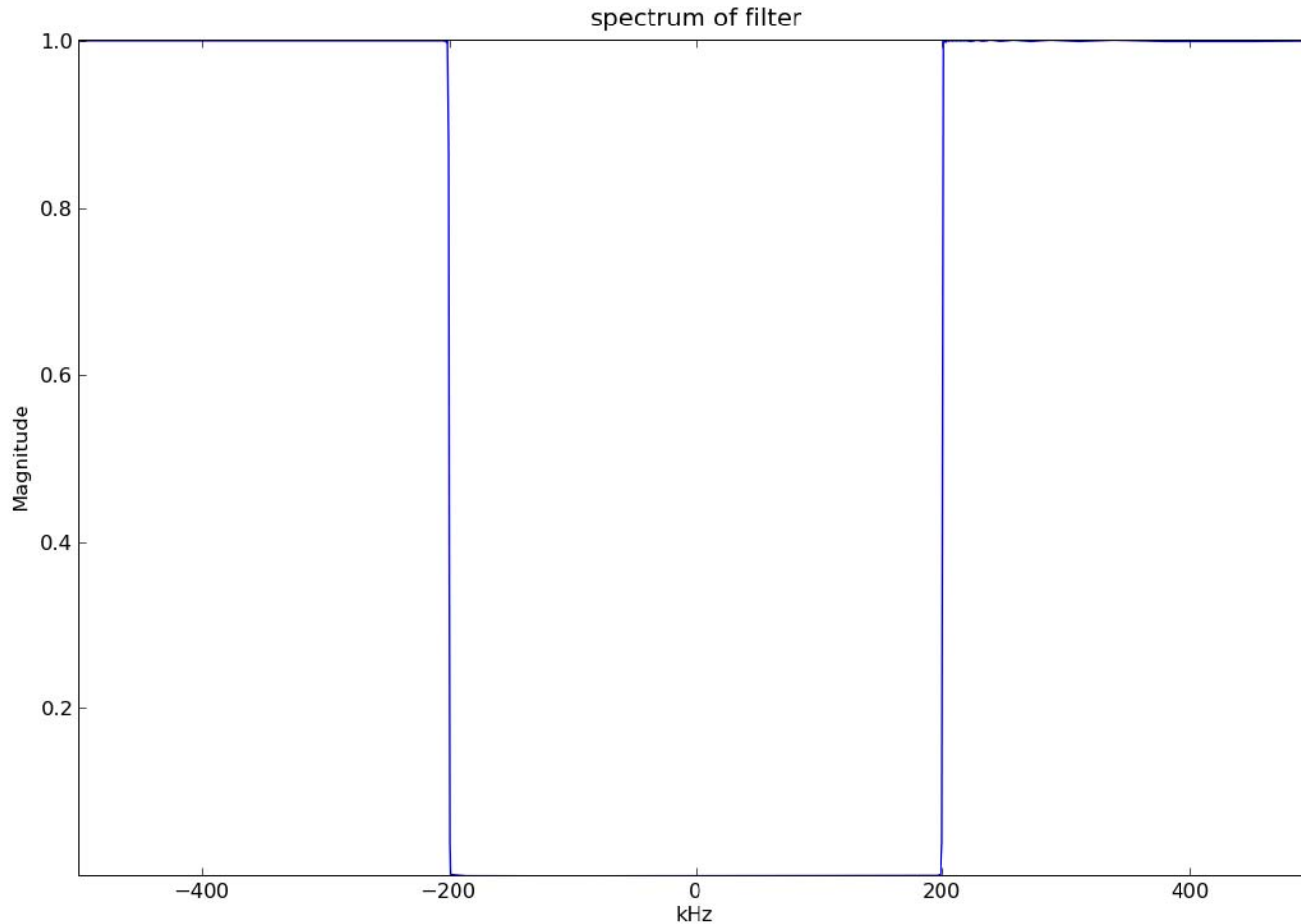
## Note Voltage range (-0.5 to 0.5)



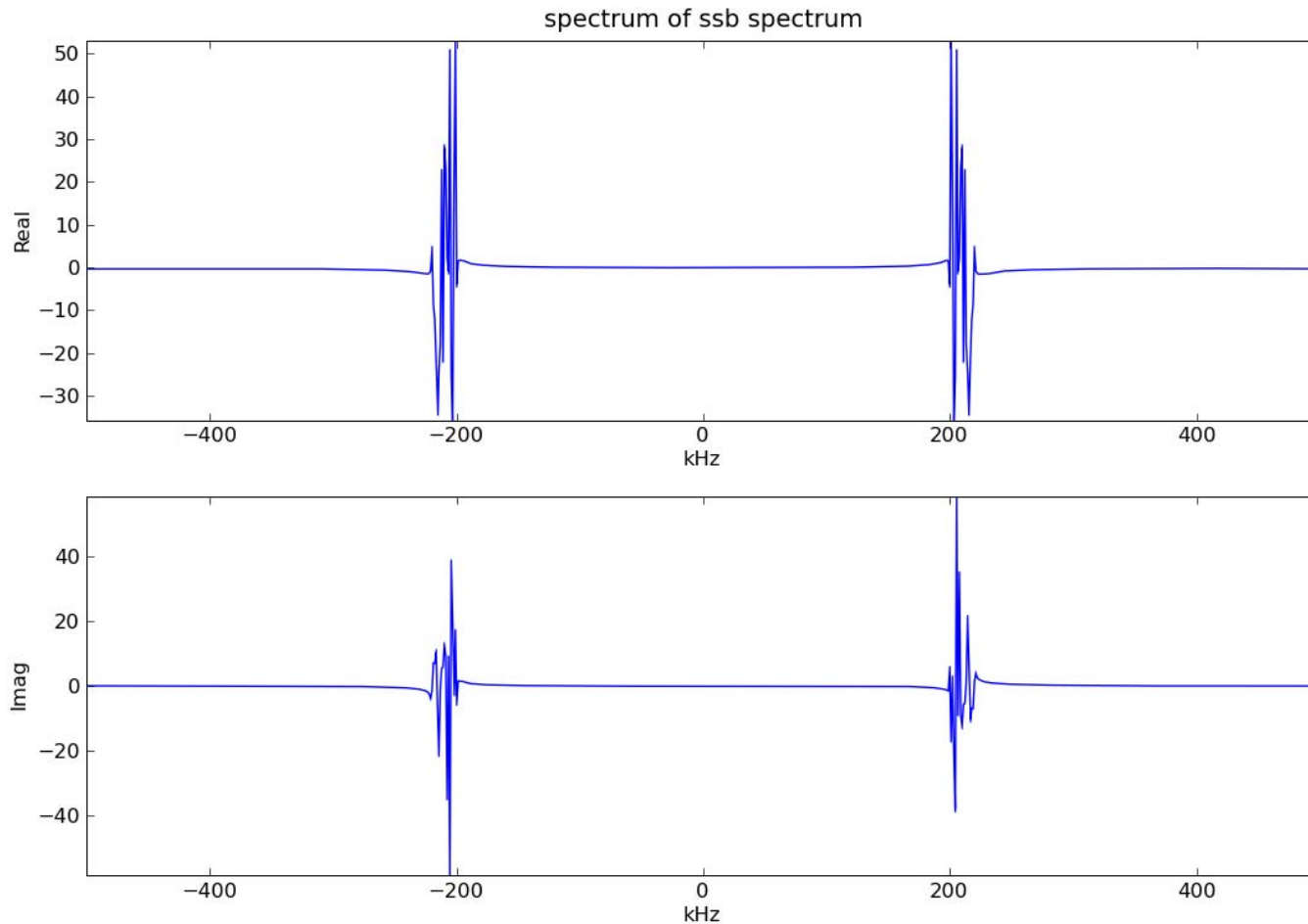
# Plot of the modulated LPF'd spectrum



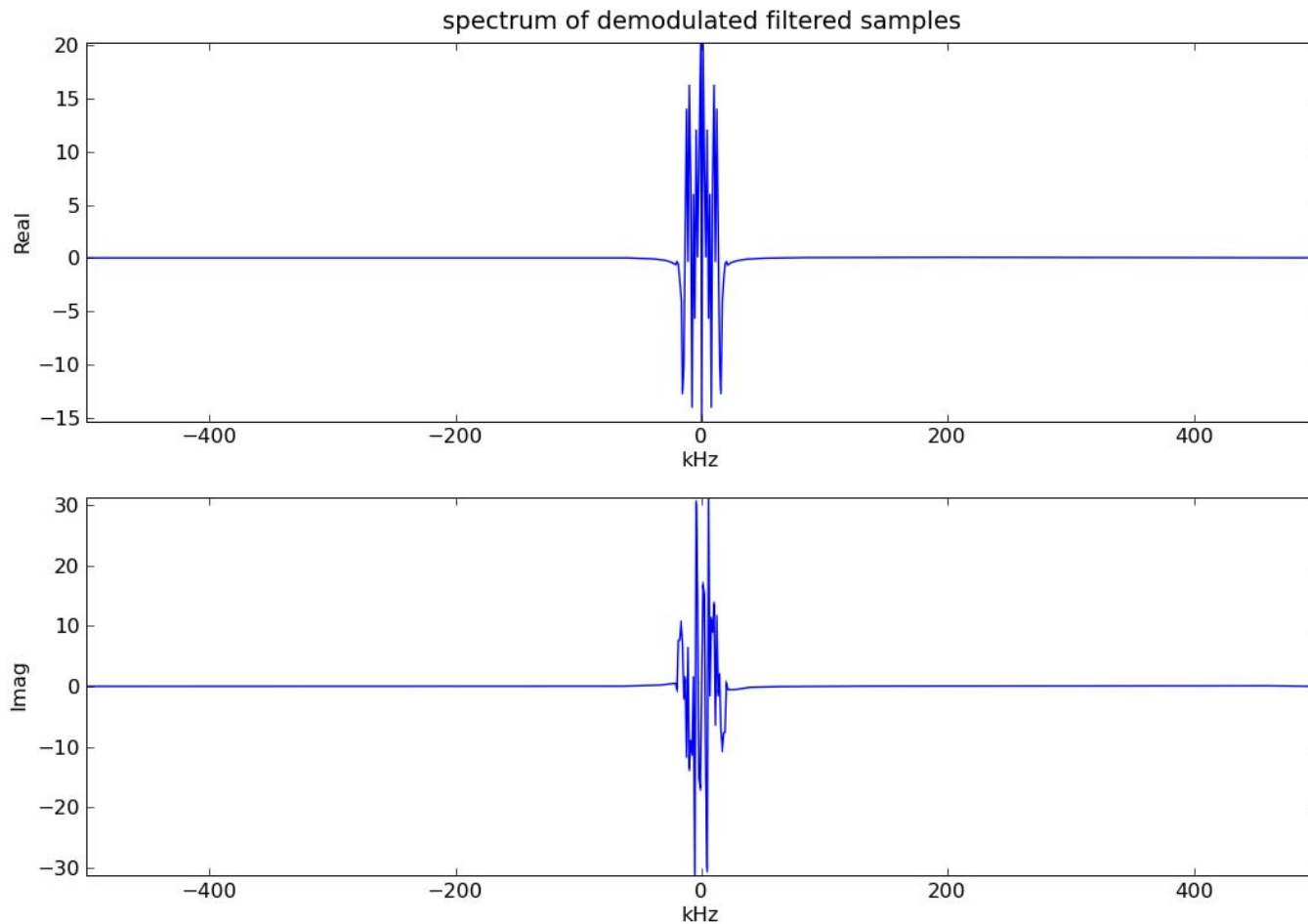
# High pass filter used to generate ssb



# High pass filtered Modulated signal

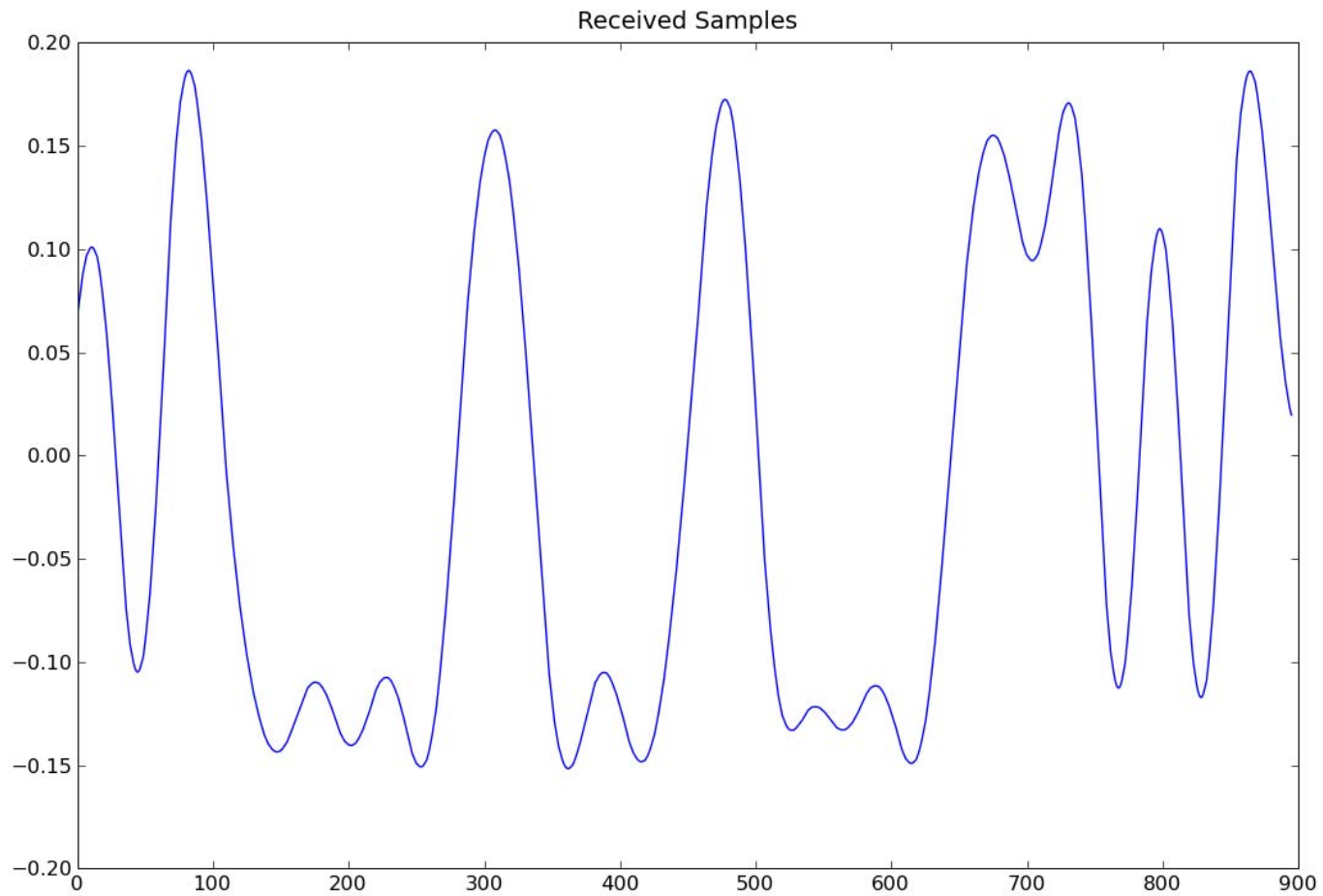


# LPF Demodulated Signal





# Received Signal in Time



In this next example, consider using sine and cosine demodulation of cosine modulated signal  $s[n]$  where there is a delay. In, particular, for the case where

$$N = 1001$$

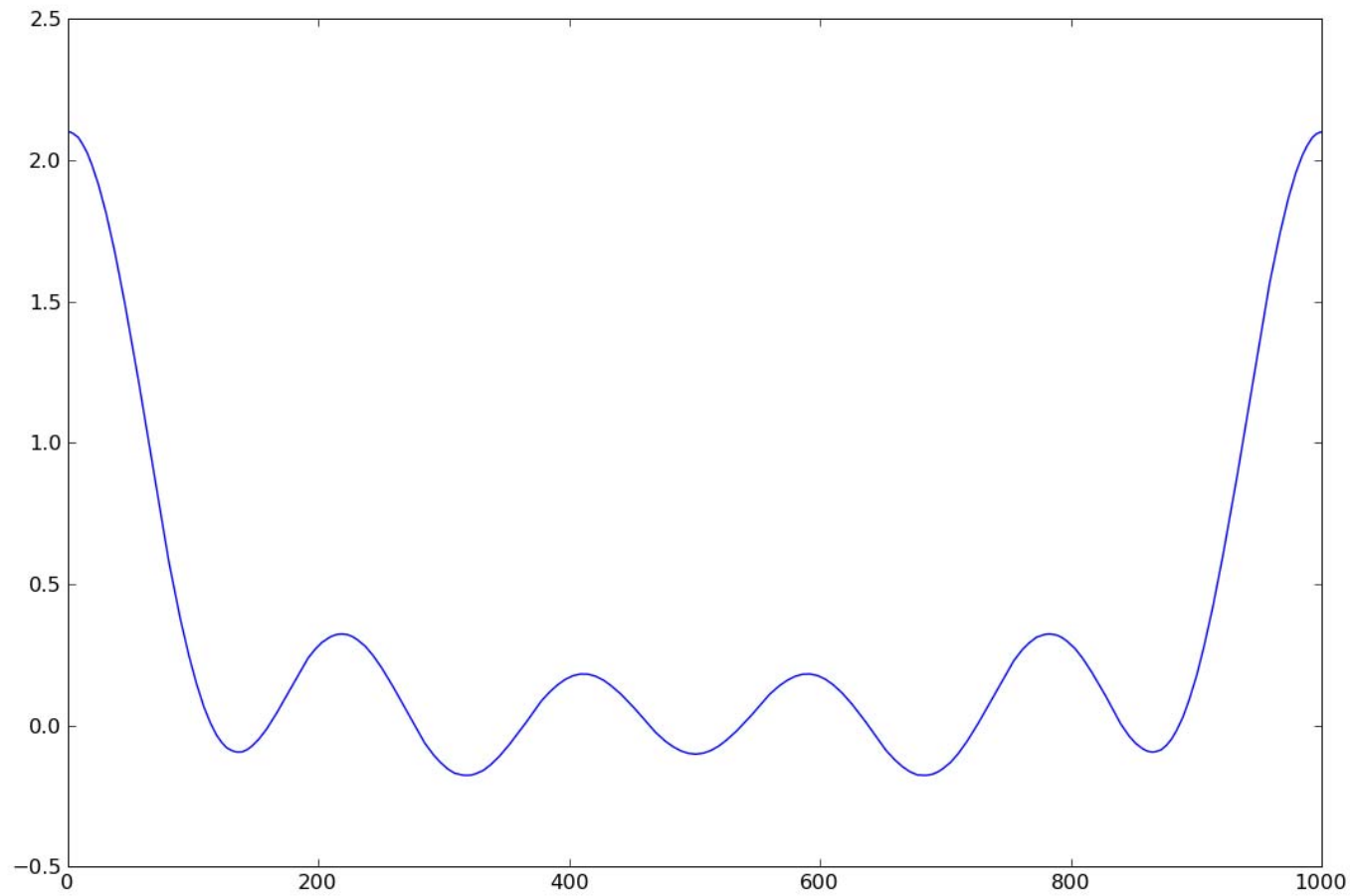
$$\Omega_1 = \frac{2 * \pi}{1001}$$

$$s[n] = 0.3 + 0.5 \cos \Omega_1 n + 0.4 \cos 2\Omega_1 n + 0.3 \cos 3\Omega_1 n + 0.3 \cos 4\Omega_1 n + 0.3 \cos 5\Omega_1 n$$

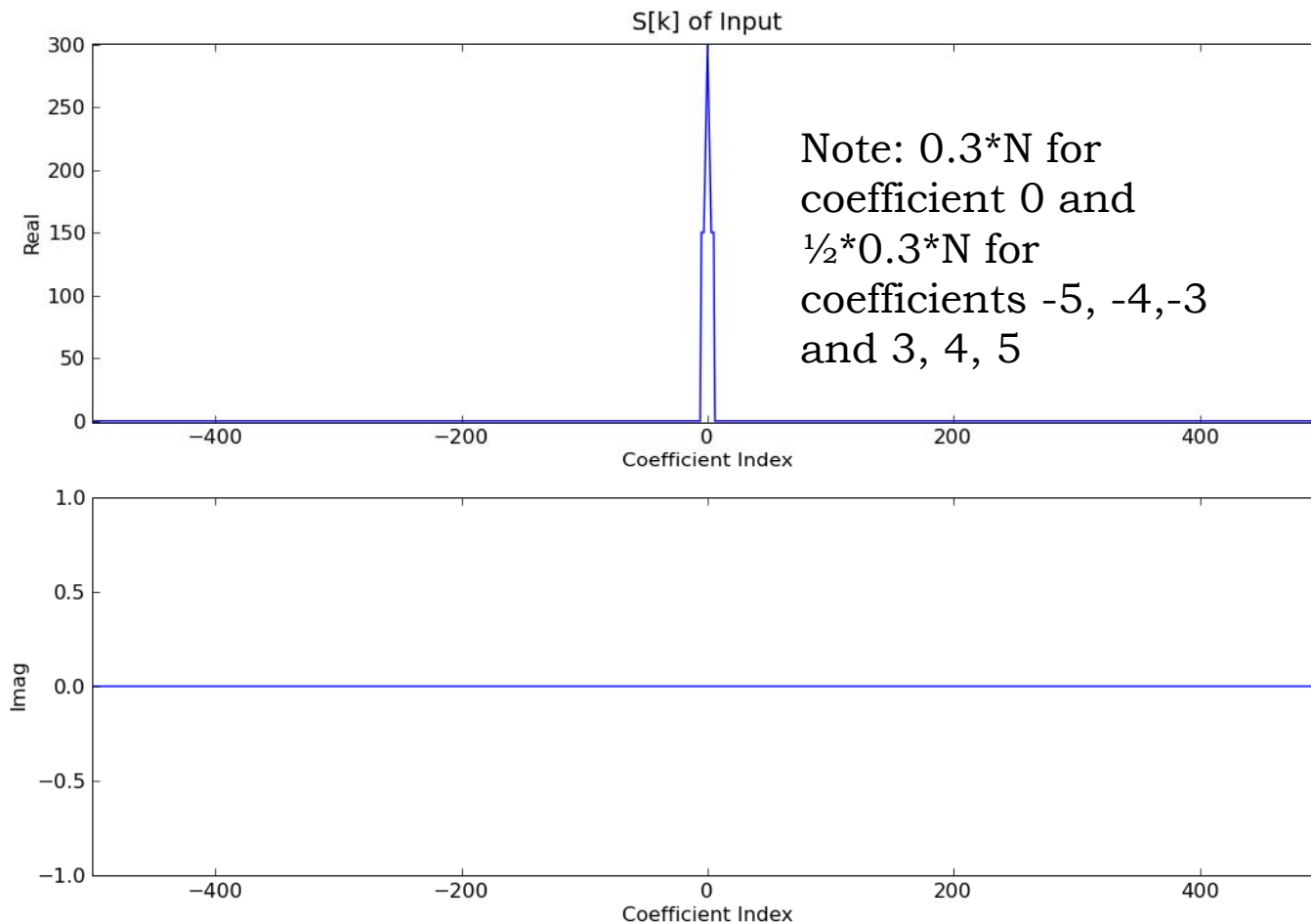
consider a delay of 5 samples (so that  $25 * \Omega_1 * D$  is almost  $\pi/4$ ) in the modulated signal.

The following plots show the impact of a 5 sample delay on modulation and demodulation at four different carrier frequencies (but the same delay). The different carrier frequencies will change the phase shift introduced by the the delay, and generate different outputs from sine and cosine demodulation. In particular, the carrier frequencies considered are 25, 50, 75 and 100 times  $\Omega_1$ .

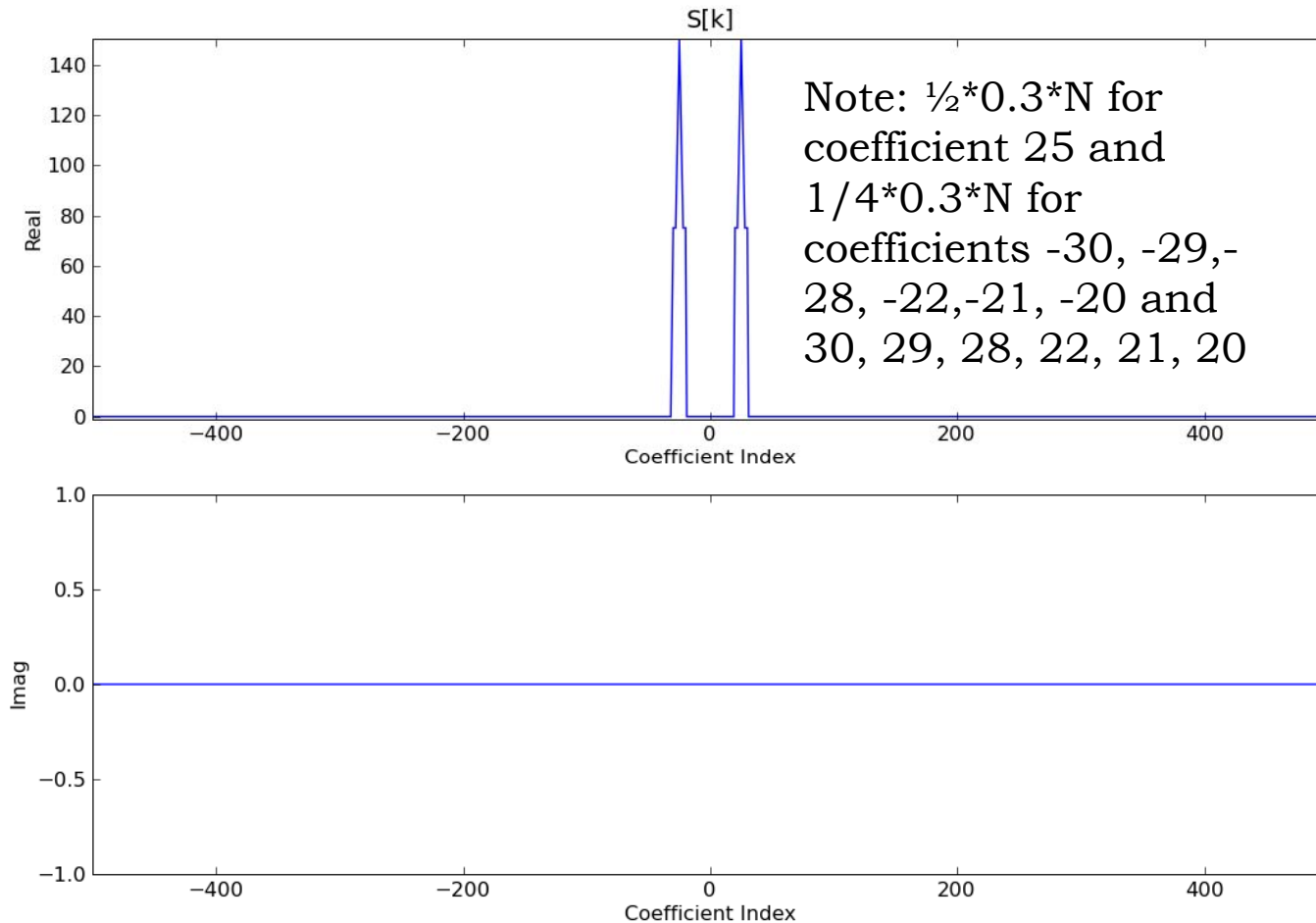
# Plot of $s[n]$



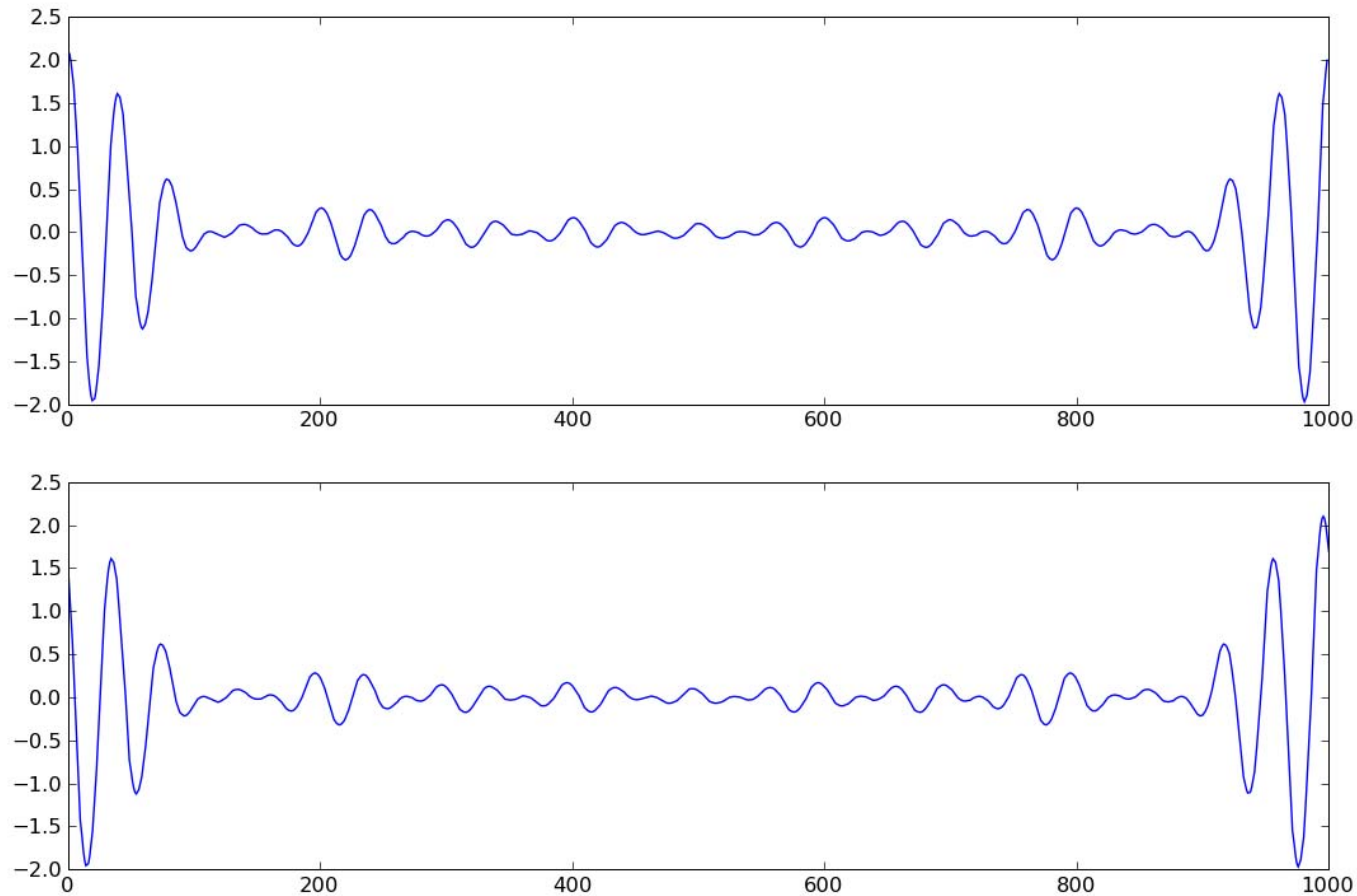
# Plot of DFT Coefficients for $s[n]$



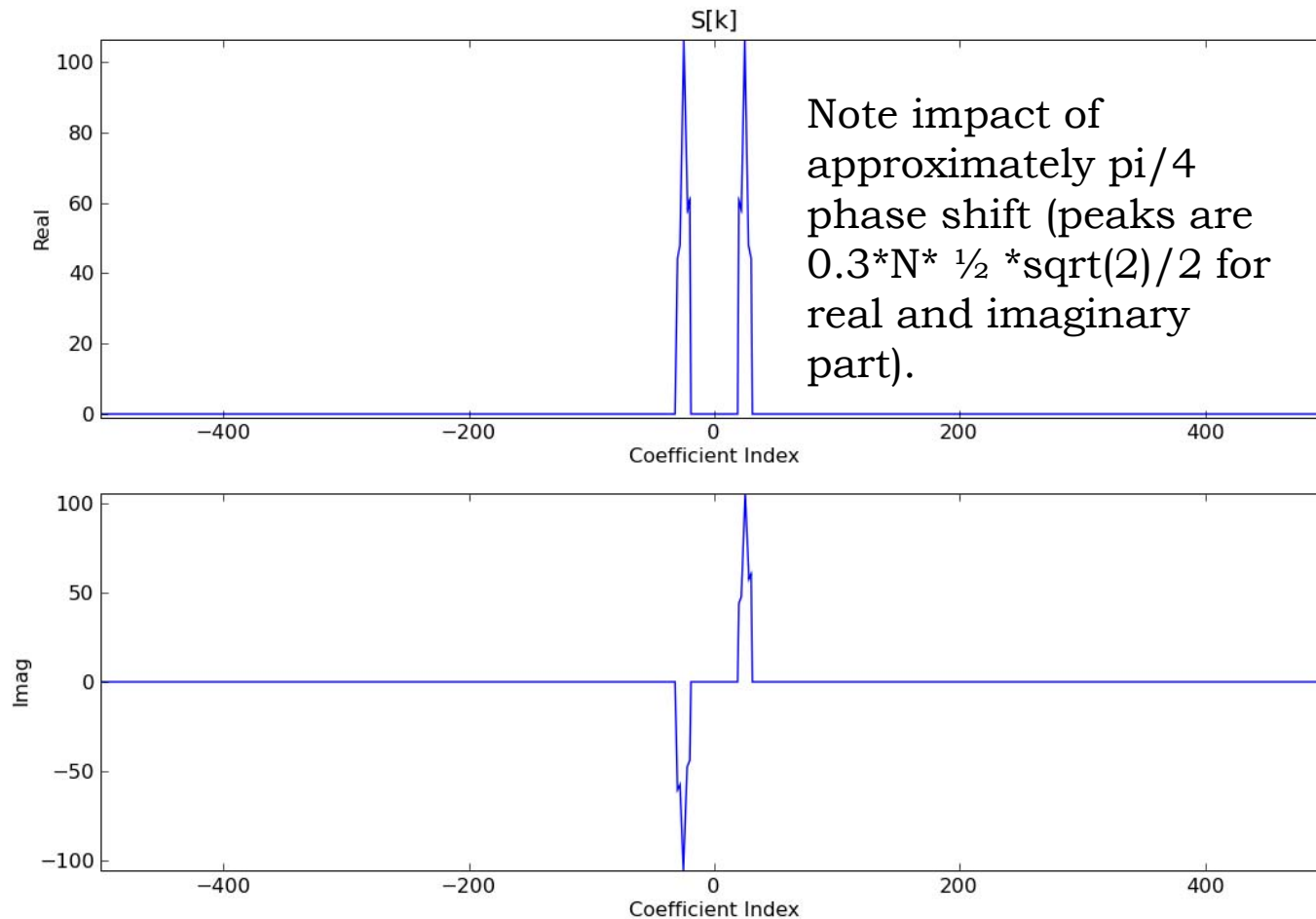
# Cos25 Omega\_1 n modulated s[n]



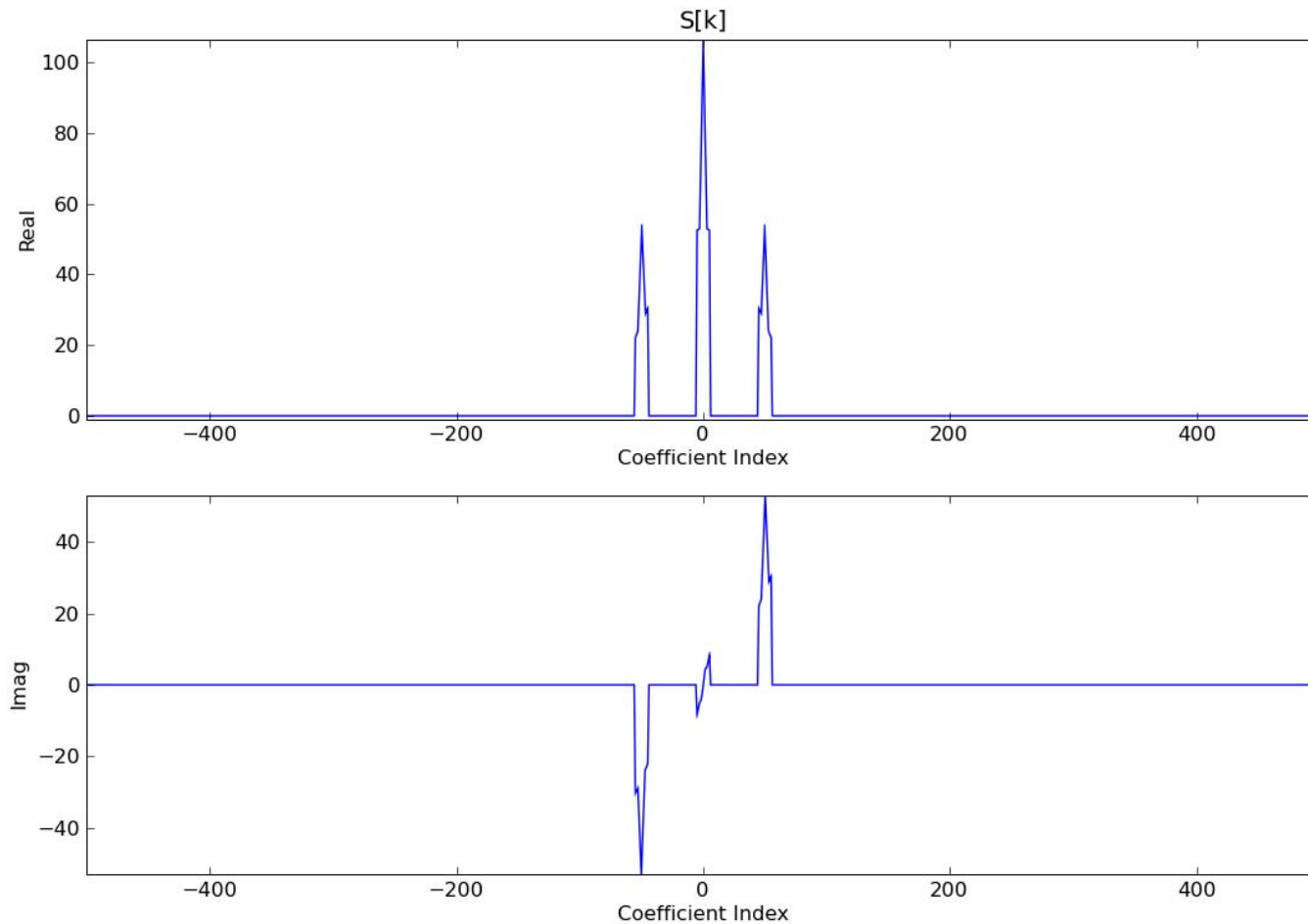
# Plots of modulated $s[n]$ and $s[n-5]$ (note periodicity!)



# Cos25 Omega\_1 n modulated s[n] after 5 sample delay

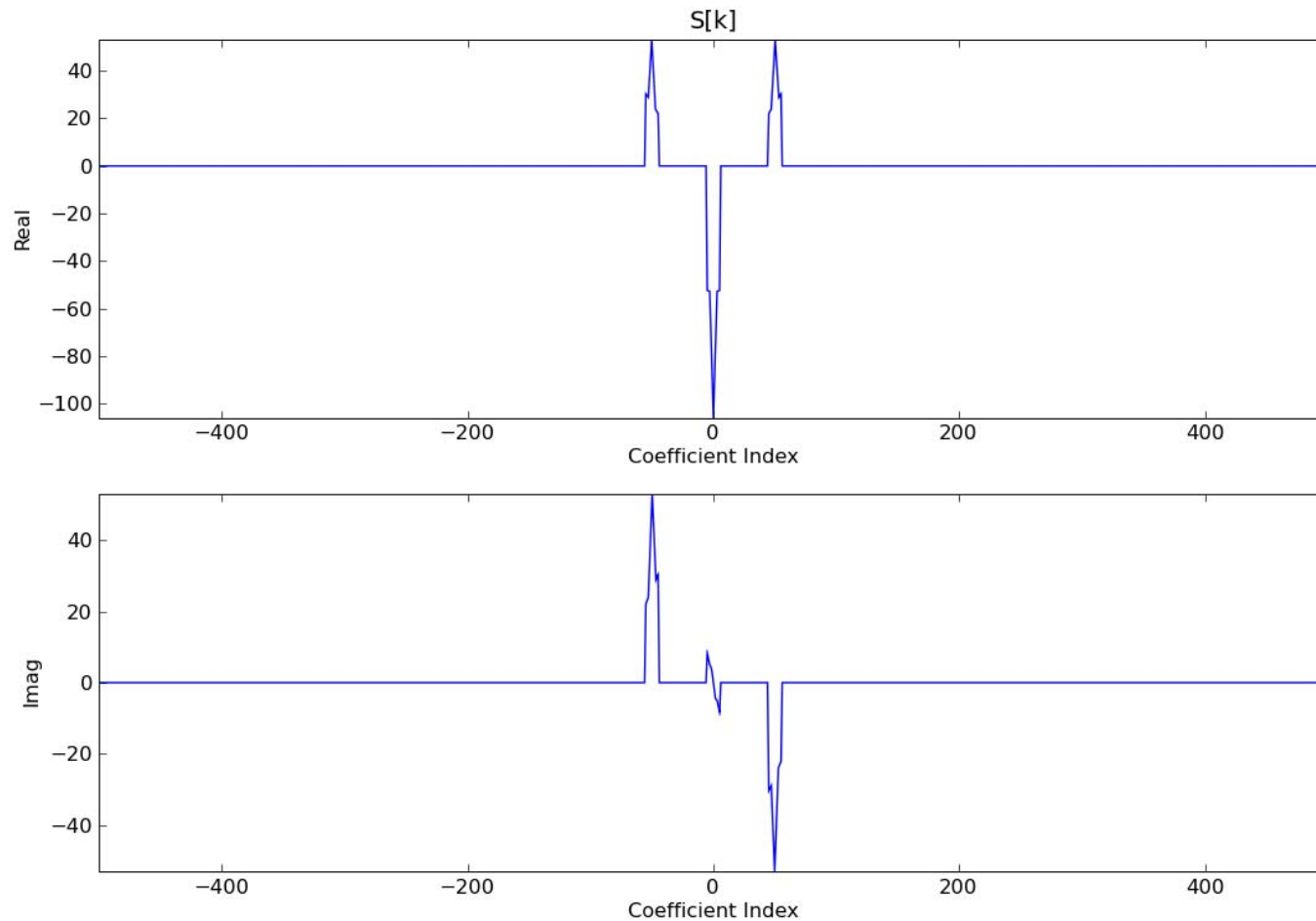


# Cos25 Omega\_1 n demod after delay

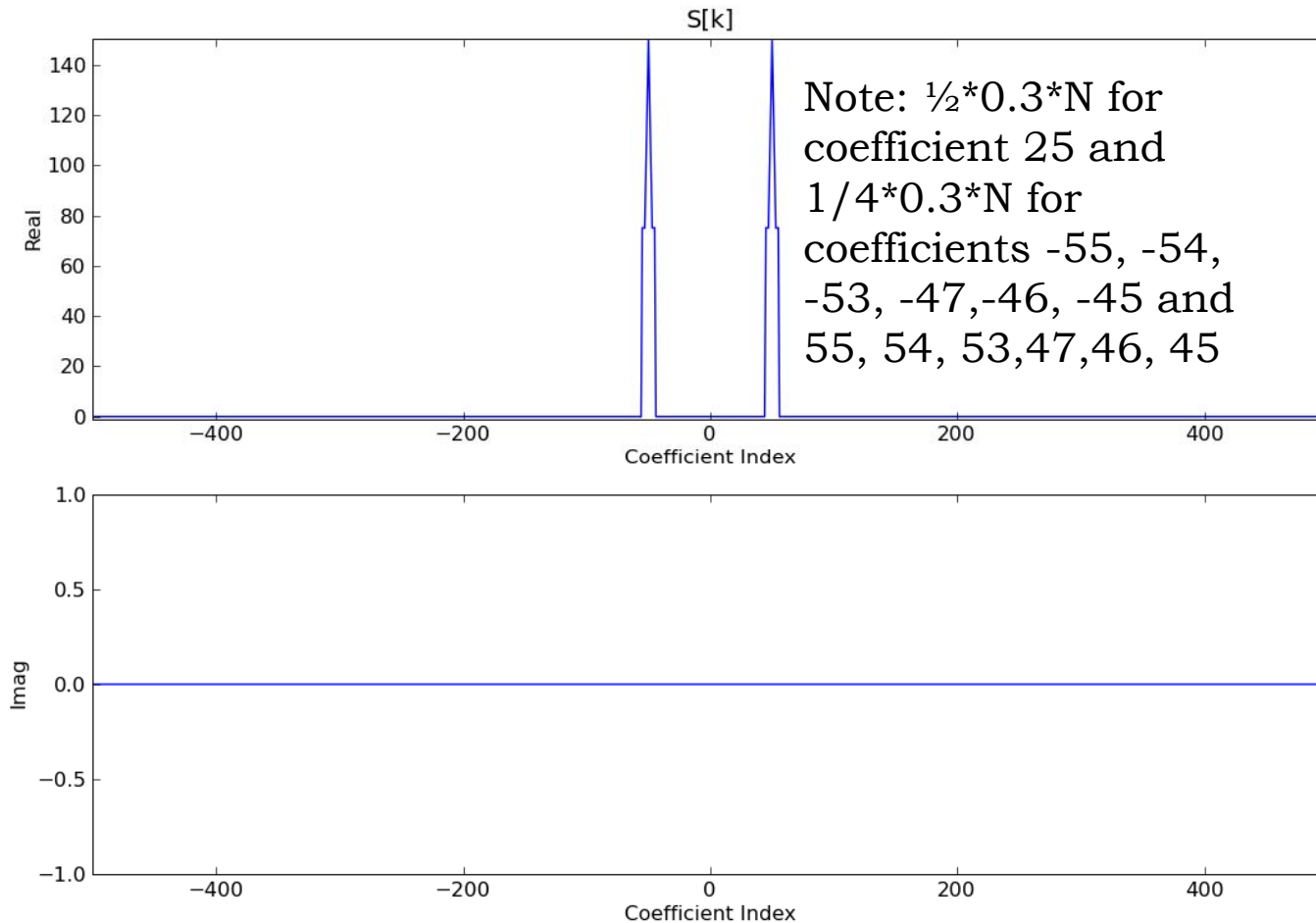




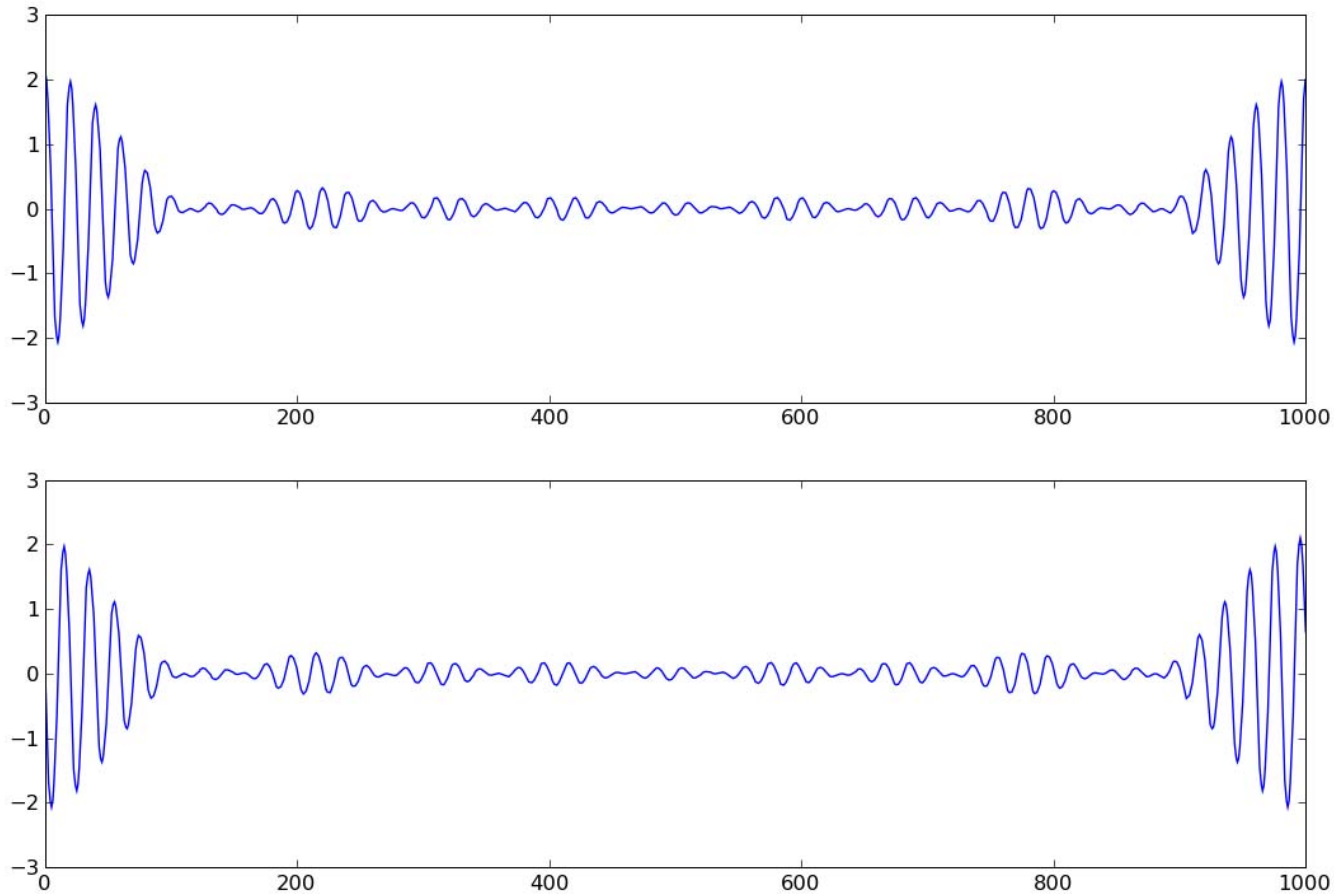
# Sin 25 Omega\_1 n demod after delay



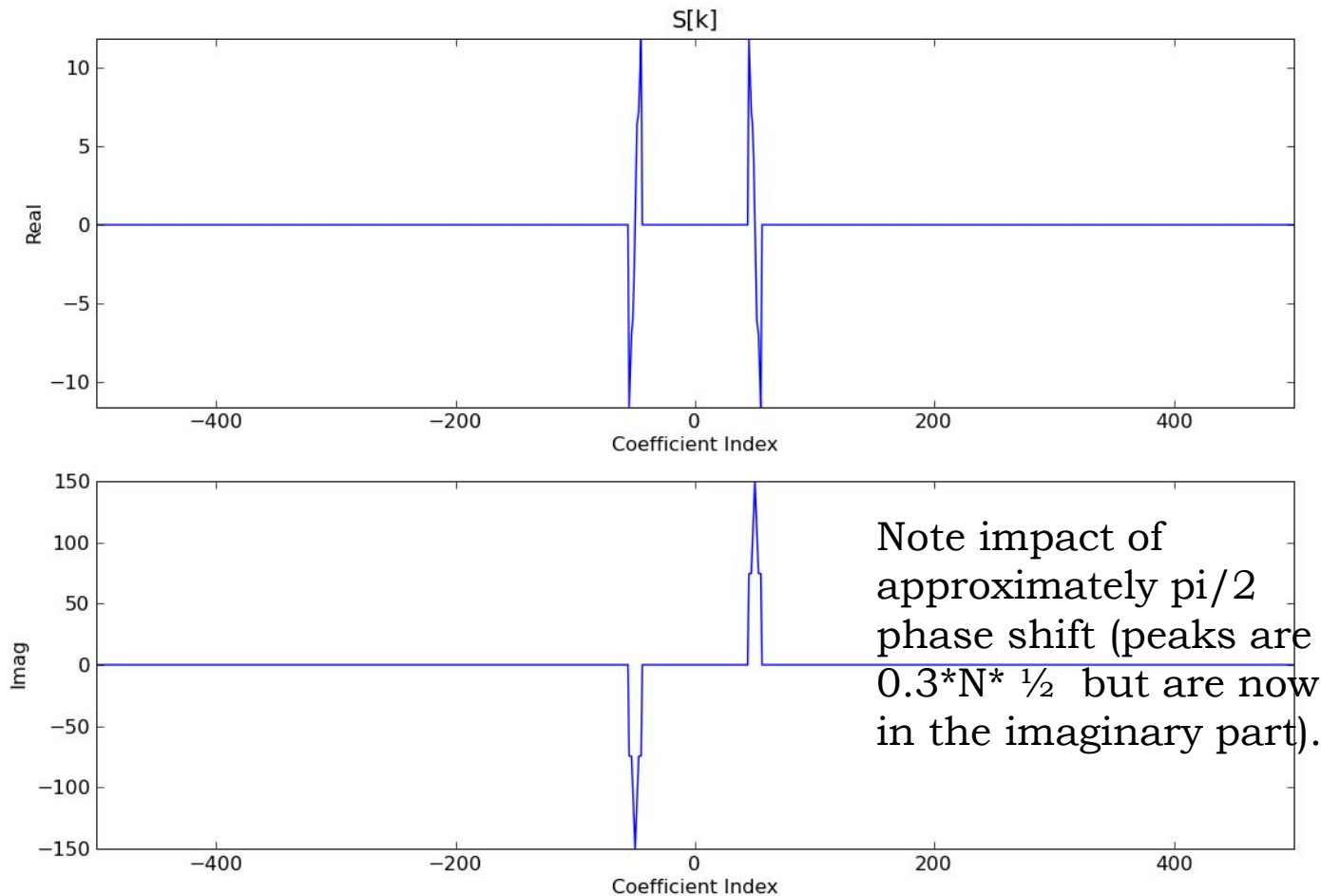
# Cos50 Omega\_1 n modulated s[n]



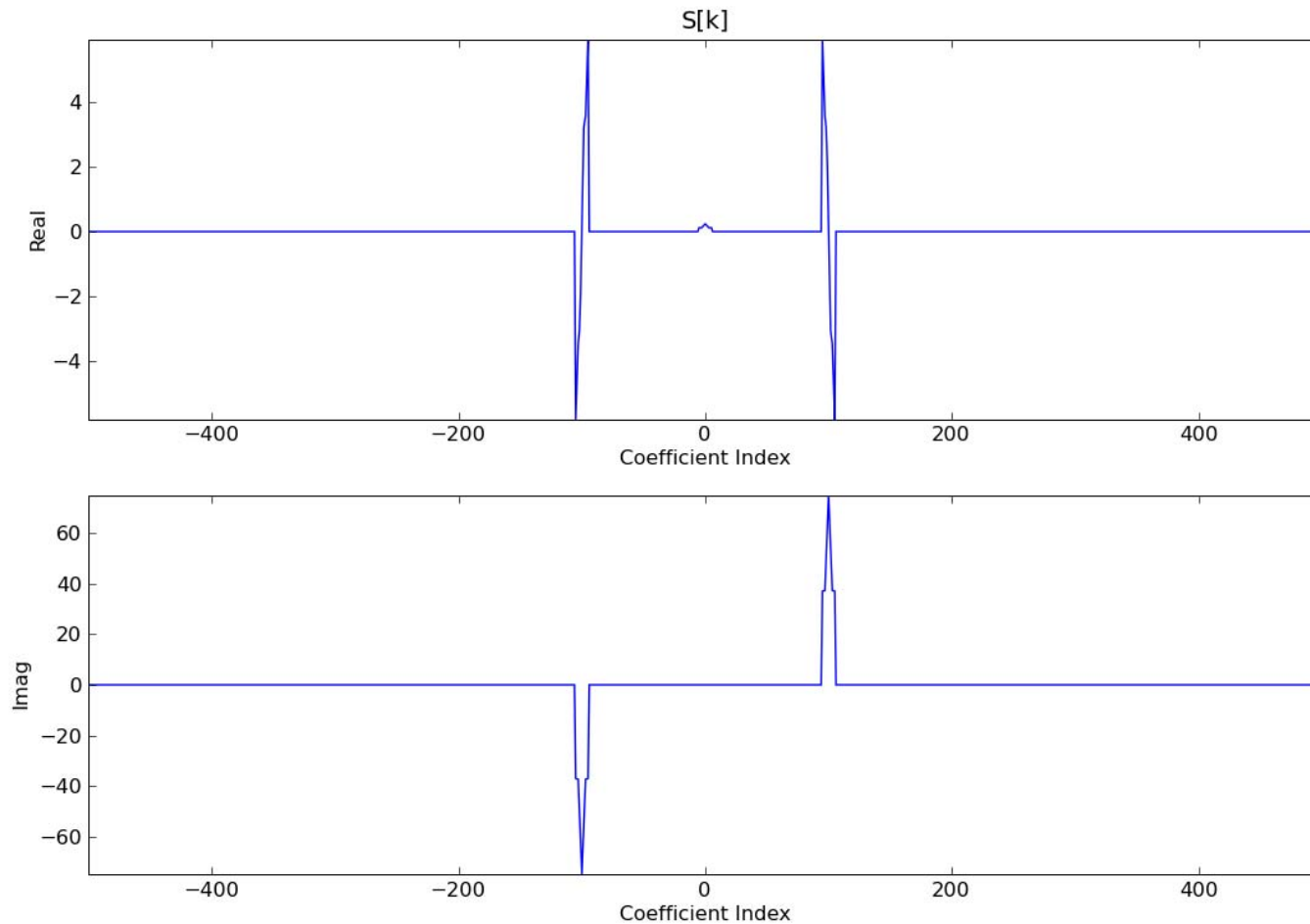
# Plots of $\cos(50\Omega_1 n)$ modulated $s[n]$ and $s[n-5]$ (note periodicity!)



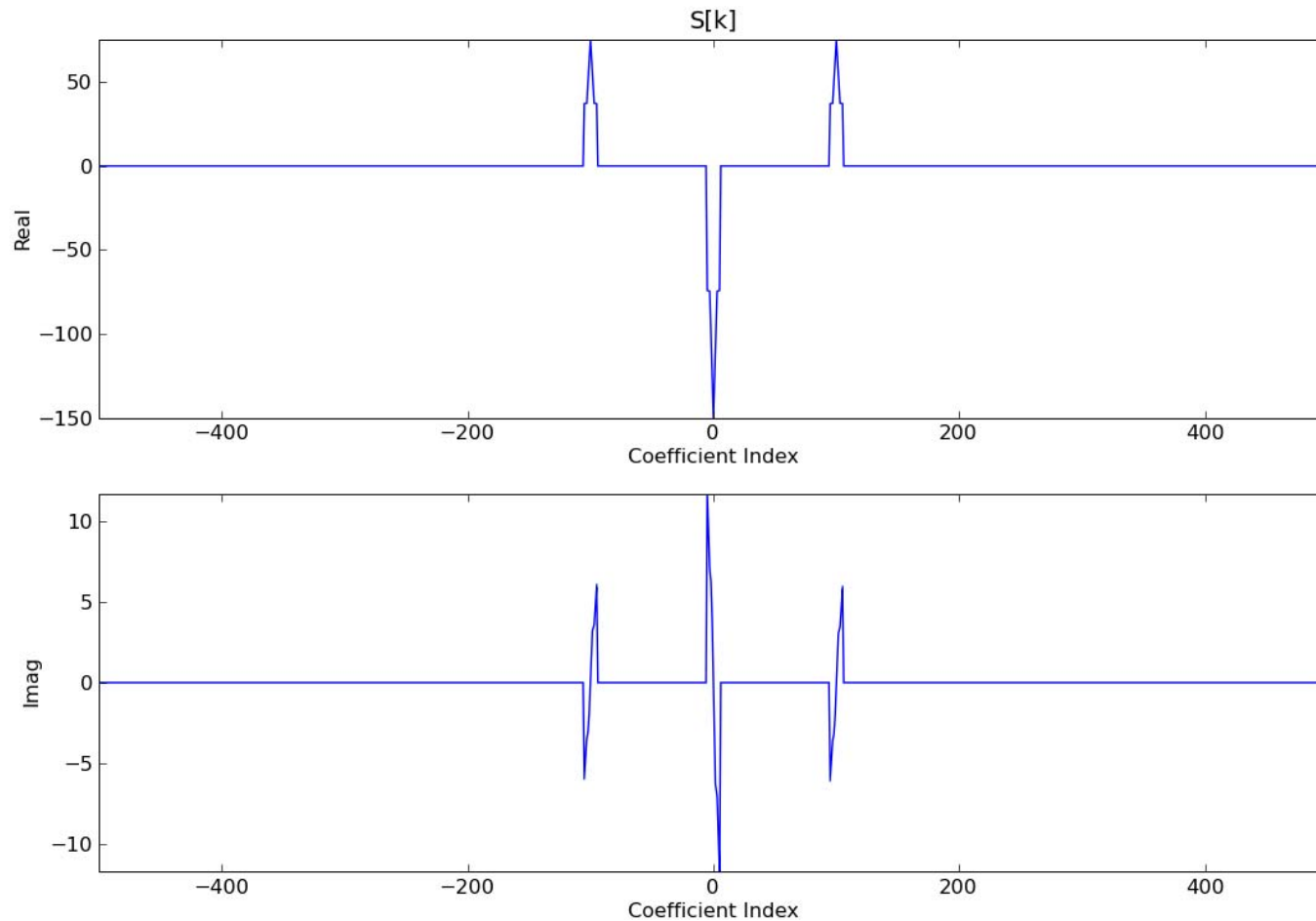
# Cos50 Omega\_1 n modulation after 5 sample delay



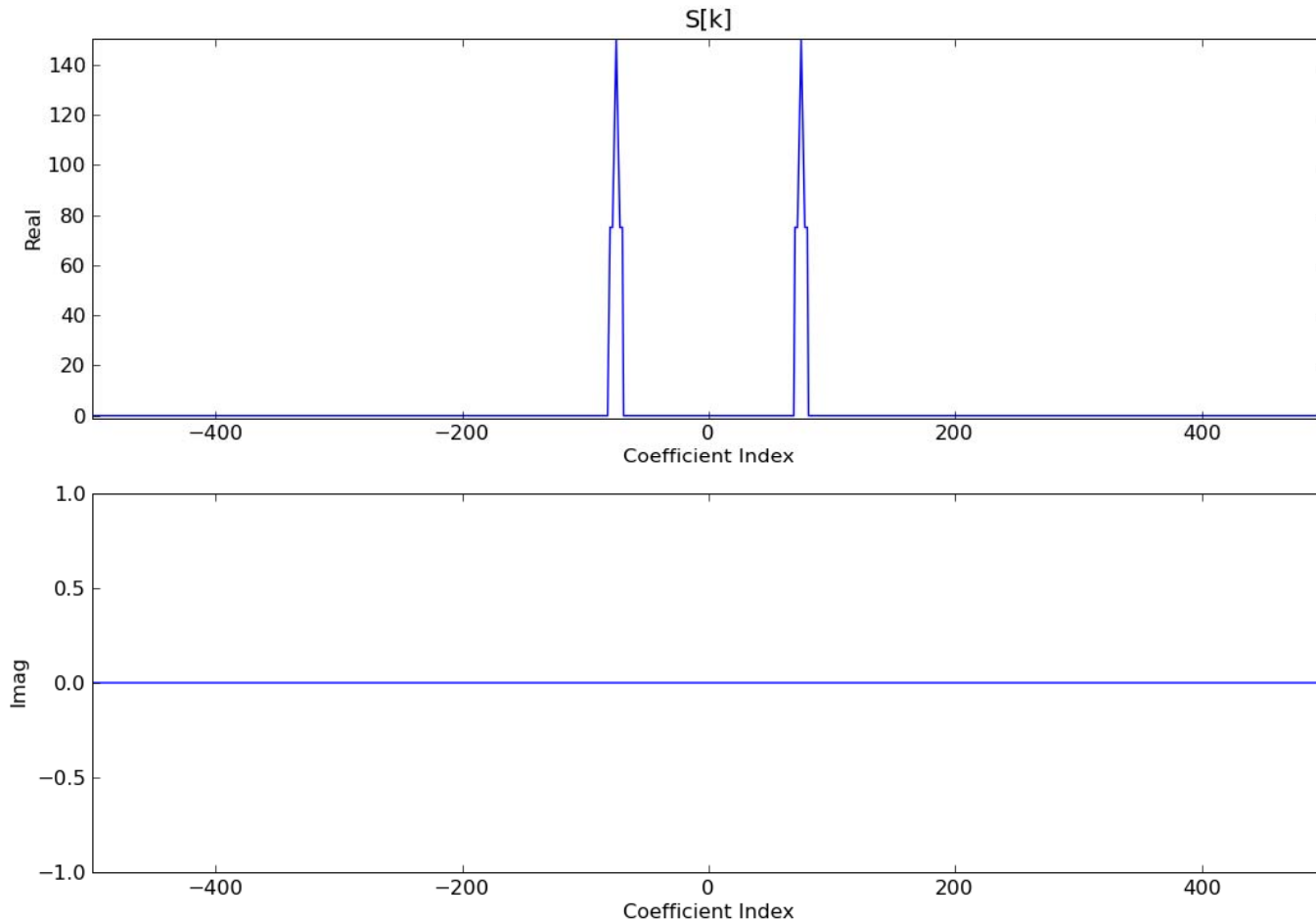
# Cos50 Omega\_1 n demod after delay



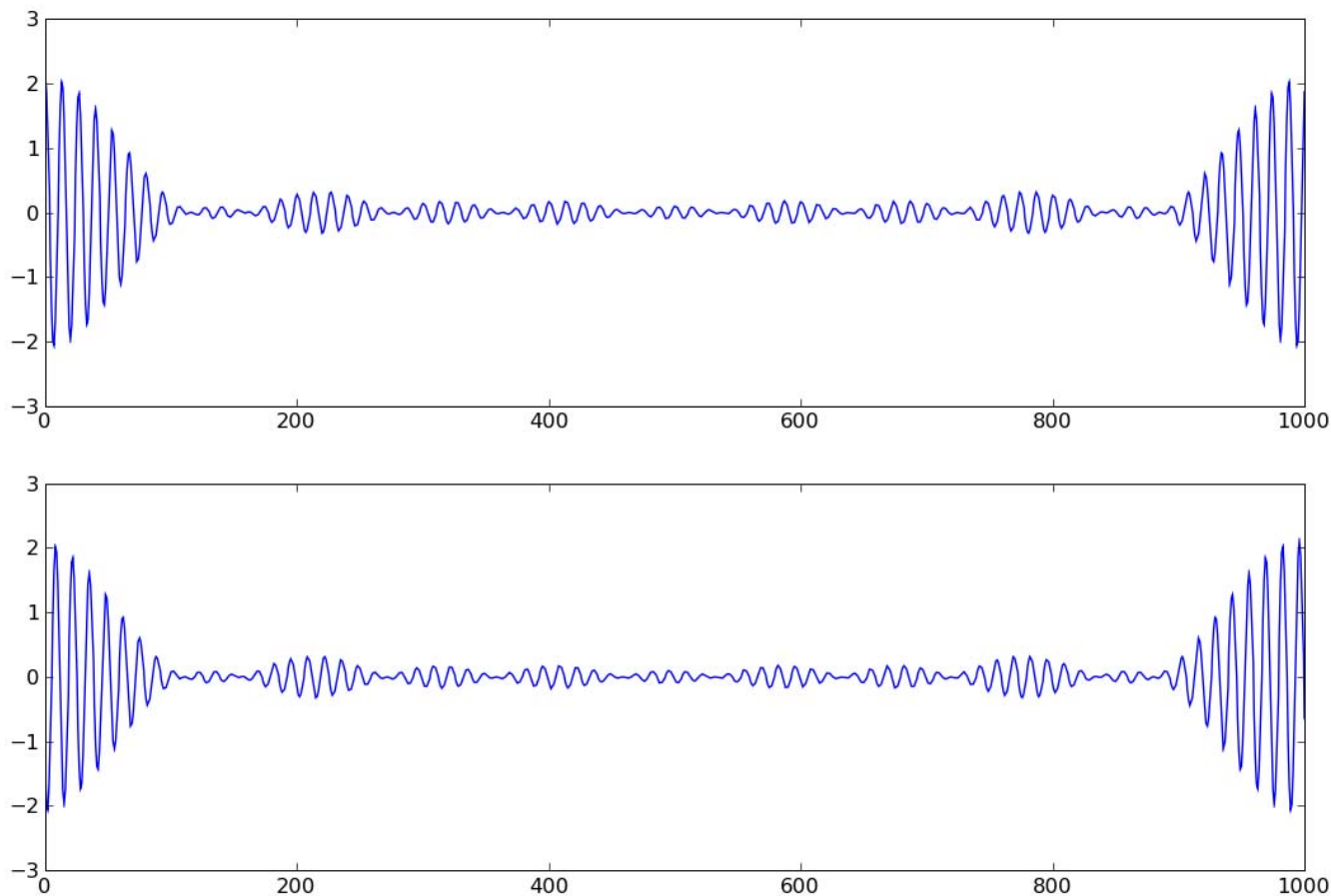
# Sin 50 Omega\_1 n demod after delay



# Cos75 Omega\_1 n modulated s[n]

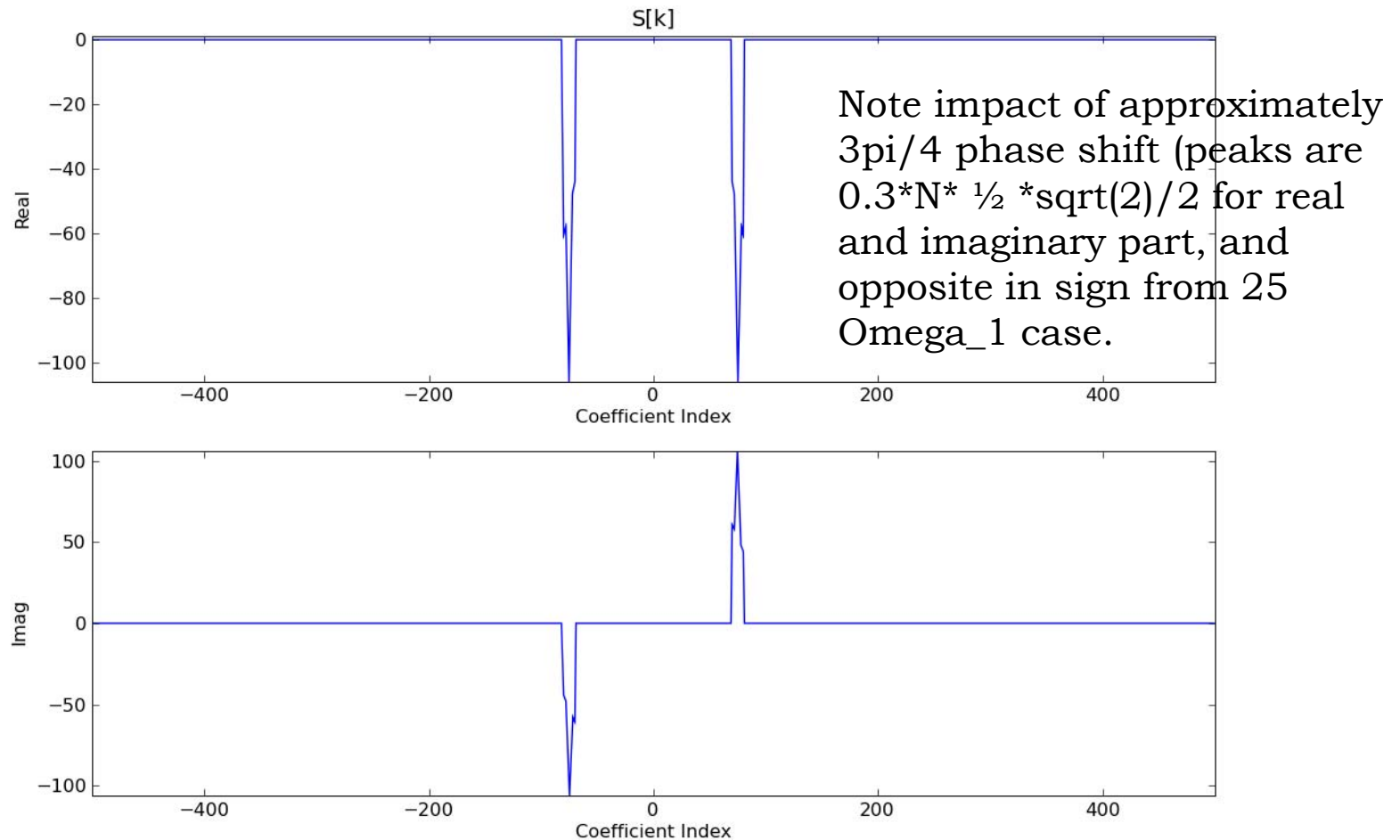


# Plots of $s[n]$ and $s[n-5]$ (note periodicity!)

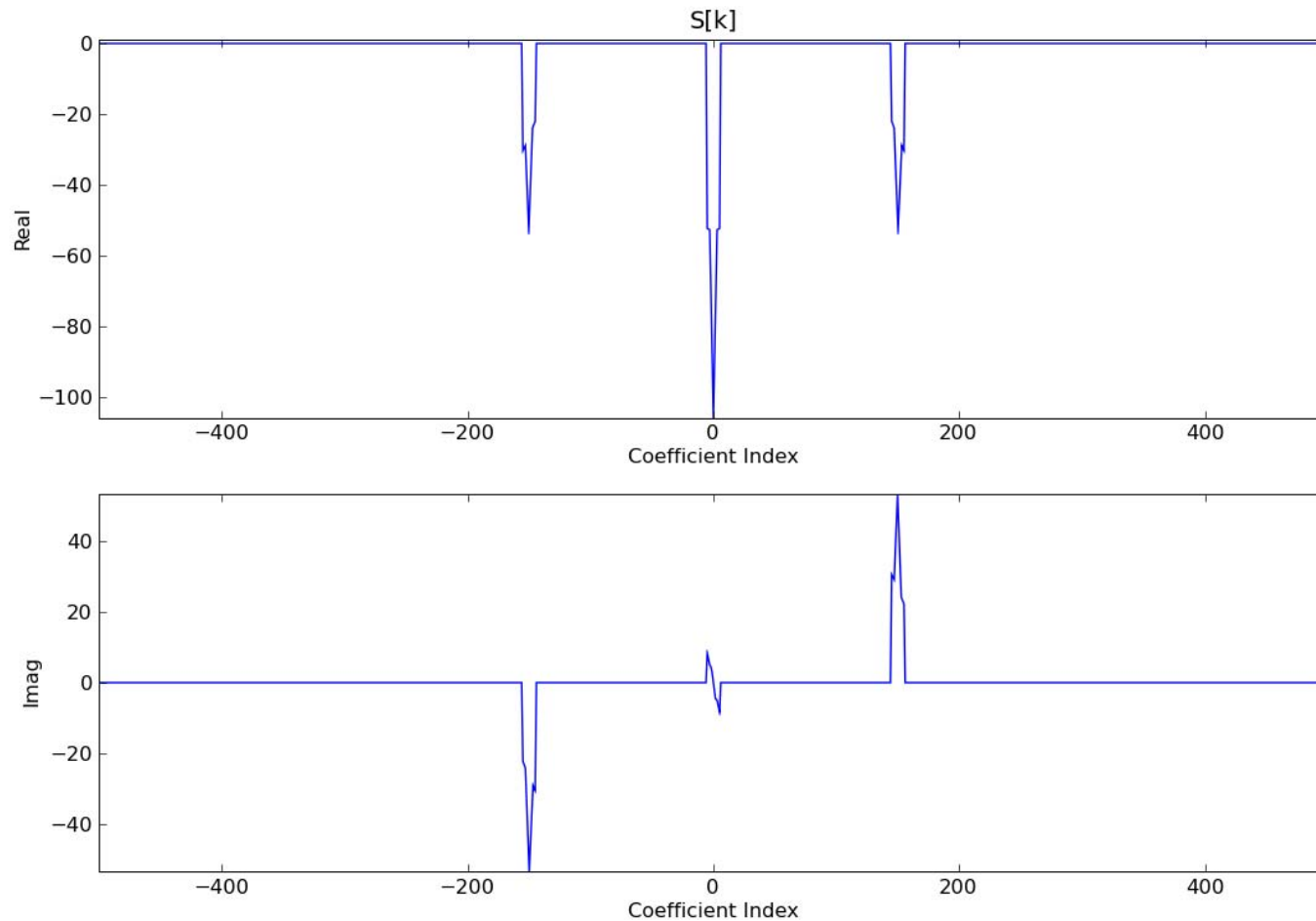




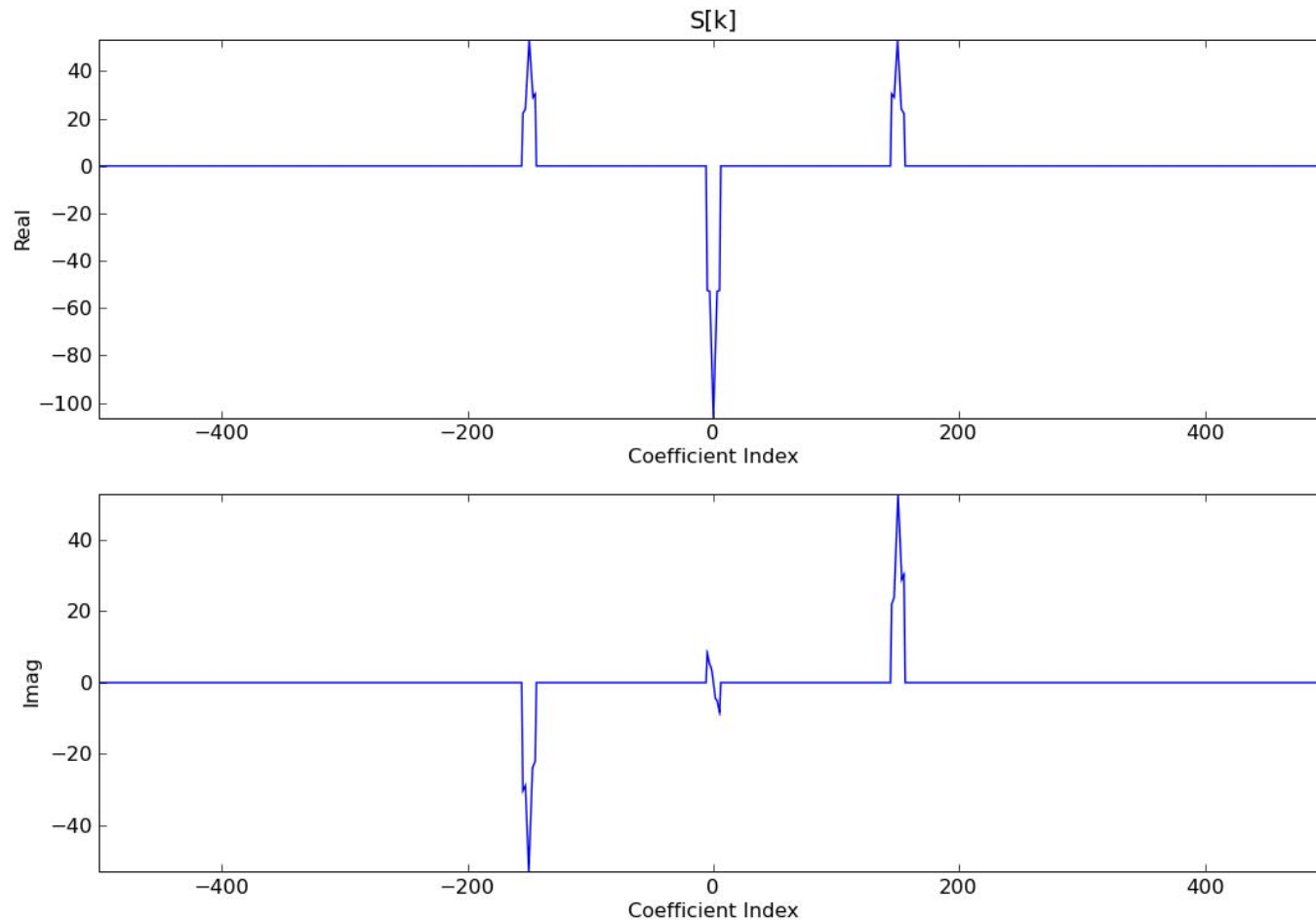
# Cos 75 Omega\_1 n modulated s[n] after 5 sample delay



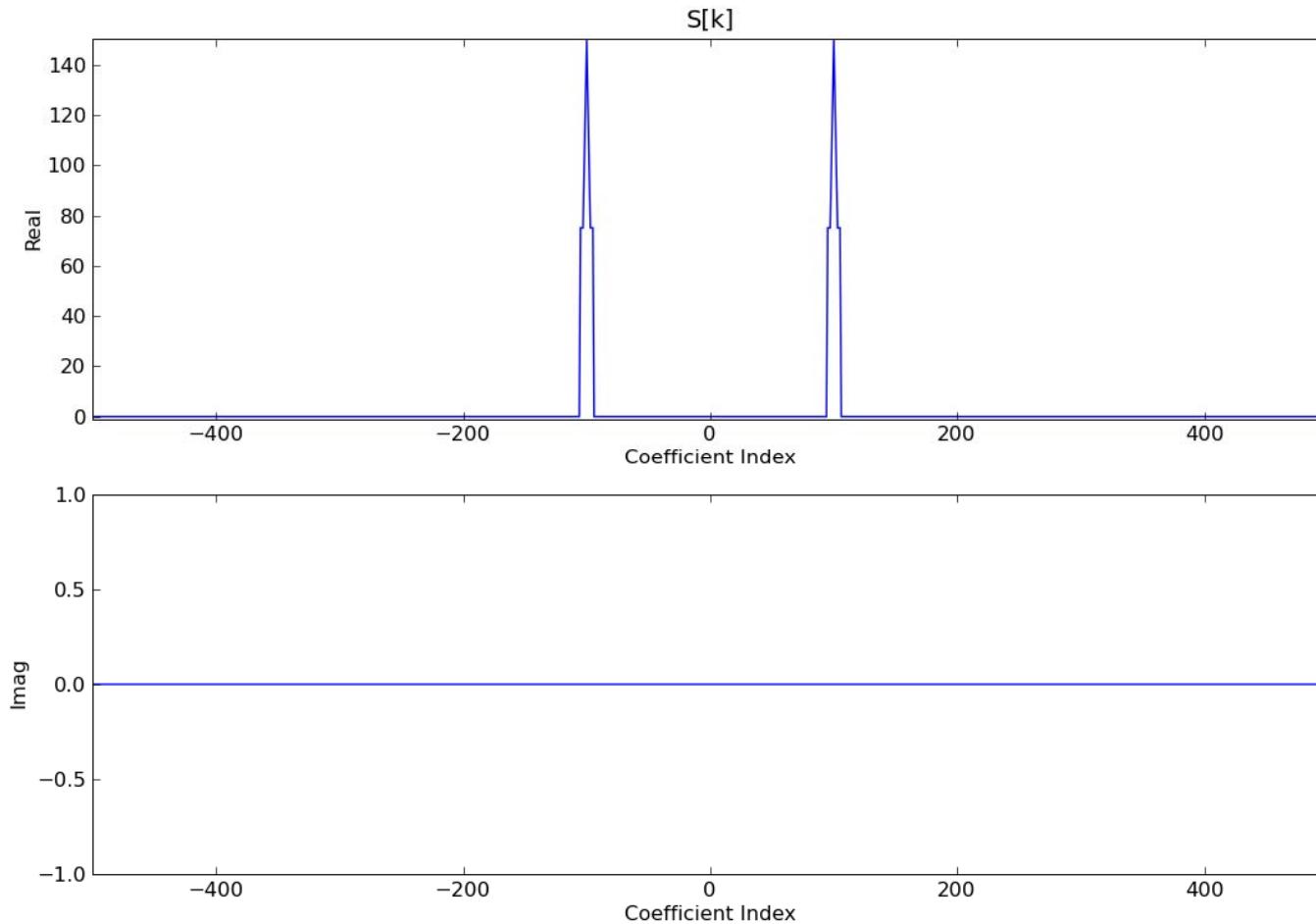
# Cos75 Omega\_1 n demod after delay



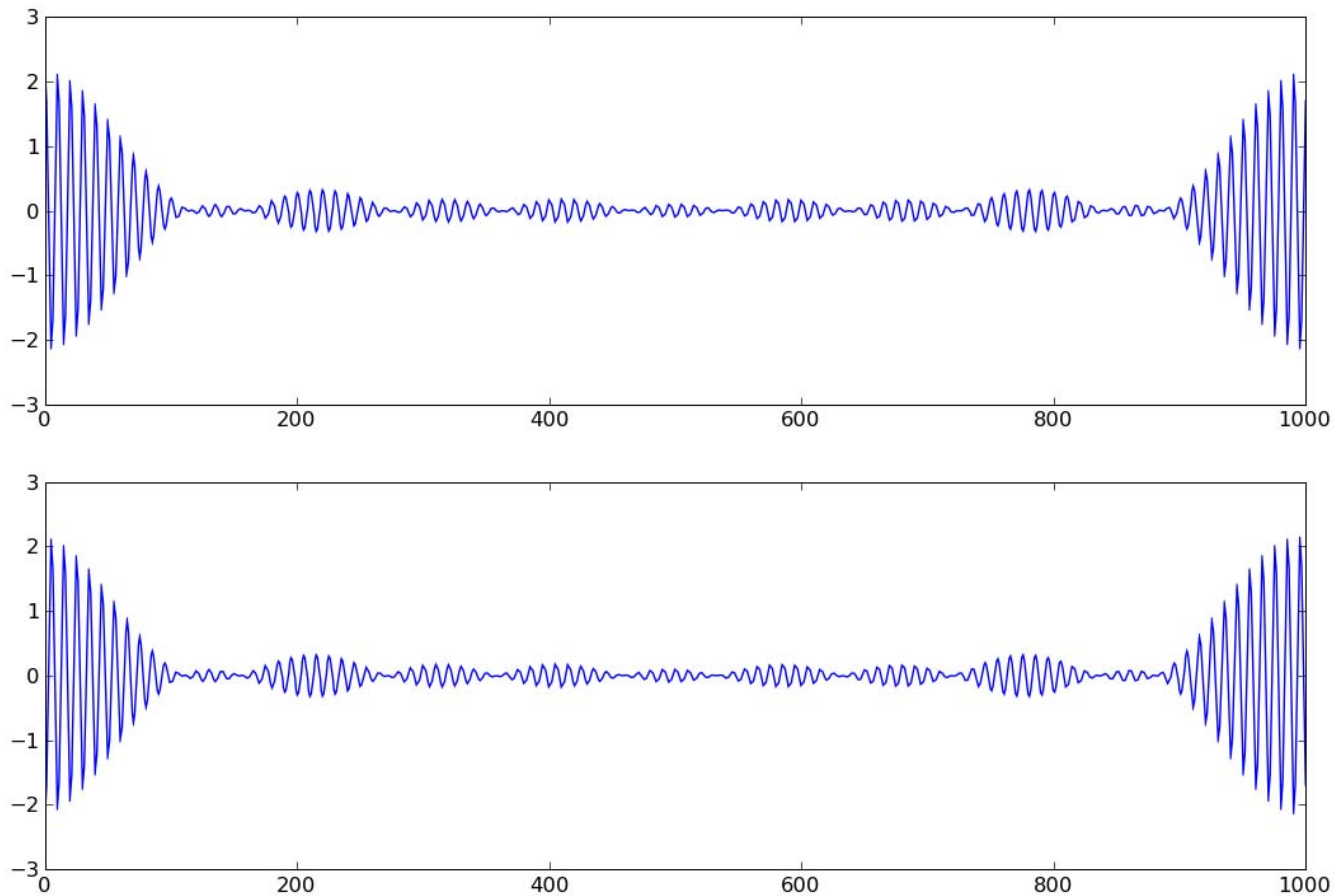
# Sin 75 Omega\_1 n demod after delay



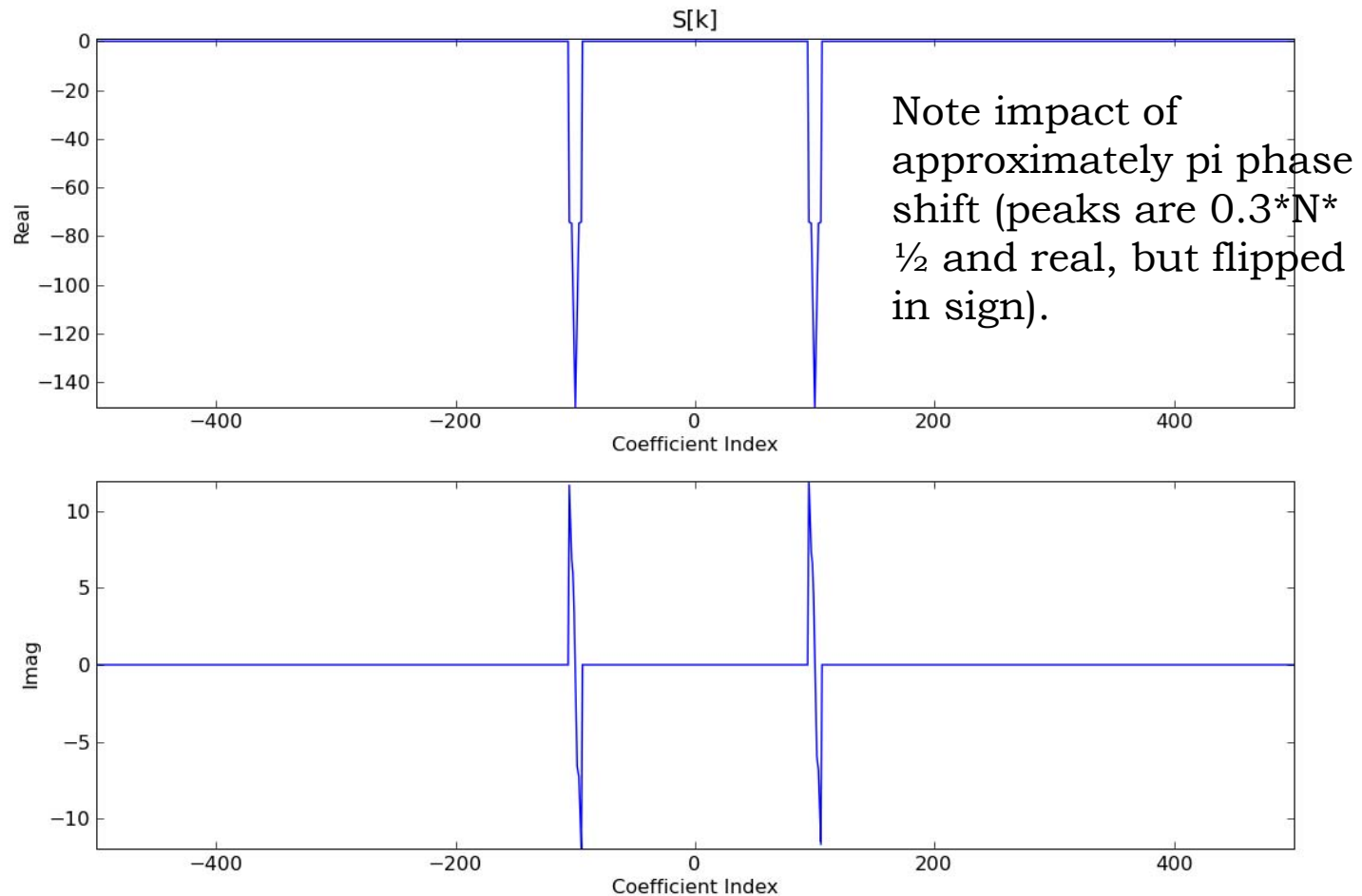
# Cos100 Omega\_1 n modulation



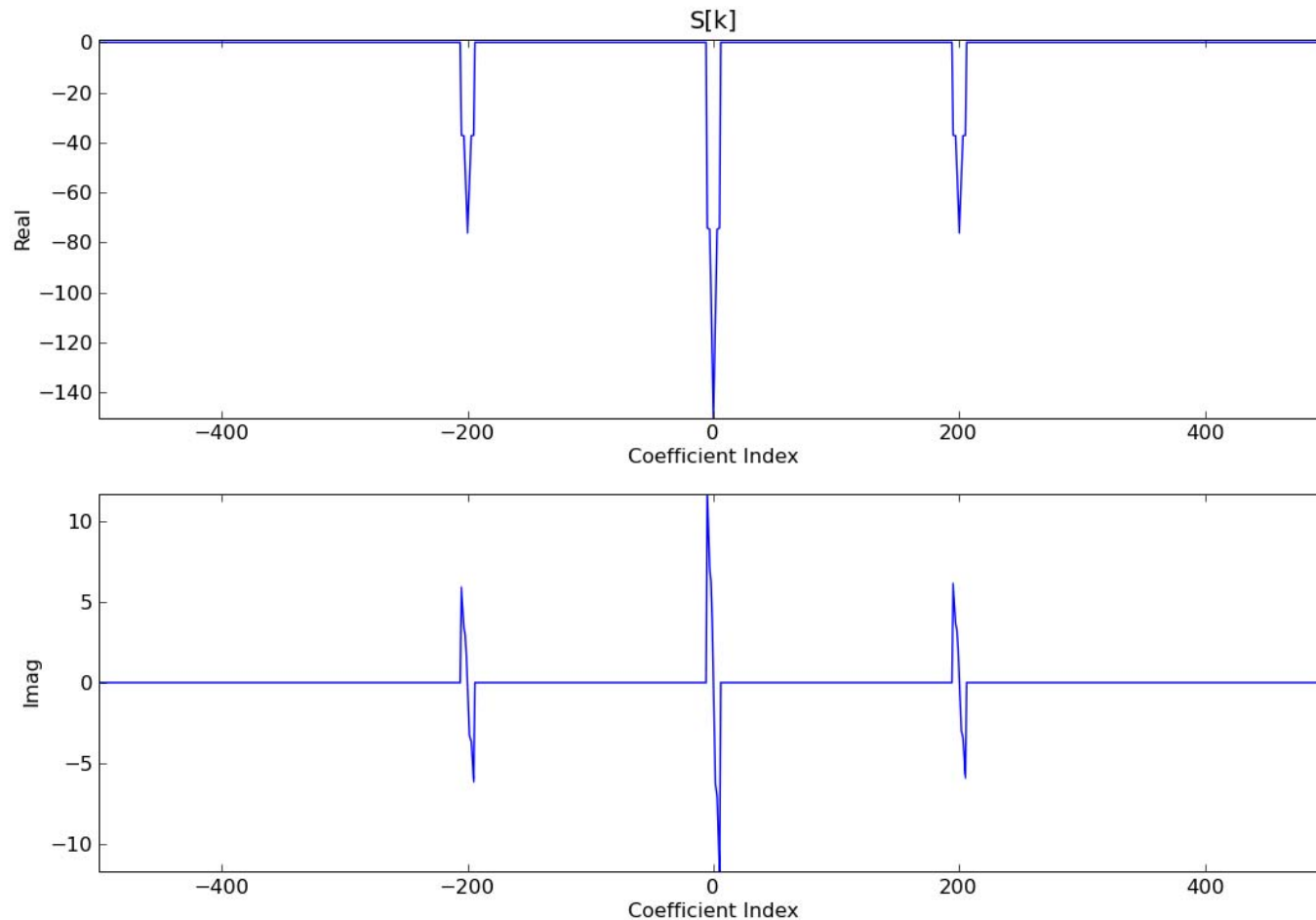
# Plots of $s[n]$ and $s[n-5]$ (note periodicity!)



# Cos 100 Omega\_1 n modulation after 5 sample delay



# Cos100 Omega\_1 n demod after delay



# Sin 100 Omega\_1 n demod after delay

