

# Analog Building Blocks

- Sampling theorem
- Undersampling, antialiasing
- FIR digital filters
- Quantization noise, oversampling
- OpAmps, DACs, ADCs

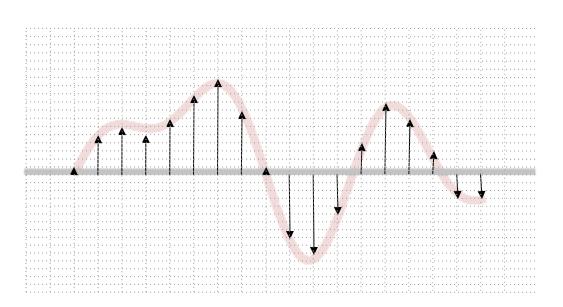
Thu: Lab 4 Checkoff

## Digital Representations of Analog Waveforms

Continuous time Continuous values

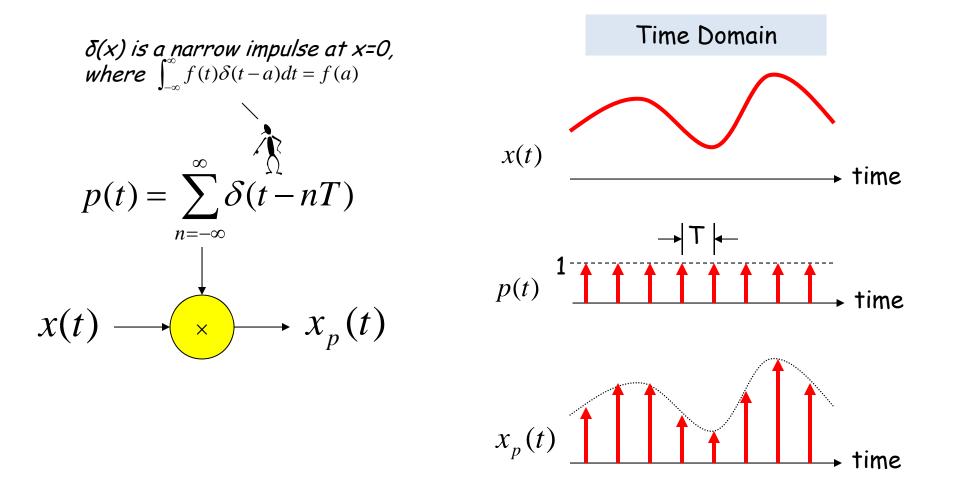


Discrete time Discrete values



#### **Discrete** Time

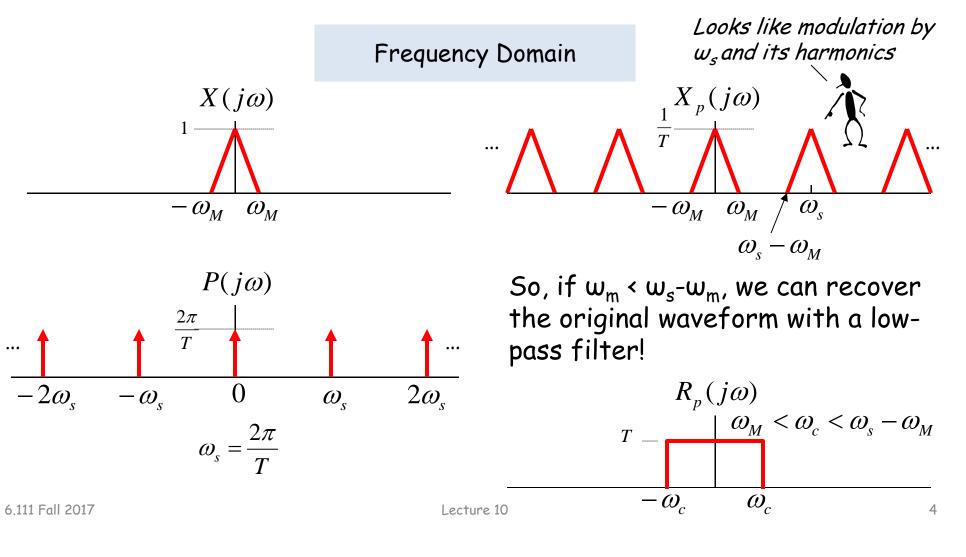
Let's use an impulse train to sample a continuous-time function at a regular interval T:



#### Reconstruction

Is it possible to reconstruct the original waveform using only the discrete time samples?

$$x_p(t) \longrightarrow \mathbb{R}_p \longrightarrow x(t)$$



#### Sampling Theorem

Let x(t) be a band-limited signal, ie, X(jw)=0 for  $|w| > w_M$ . Then x(t) is uniquely determined by its samples x(nT), n = 0, ±1, ±2, ..., if

ω<sub>s</sub> > 2ω<sub>M</sub>

 $2w_{M}$  is called the "Nyquist rate" and  $w_{s}/2$  the "Nyquist frequency"

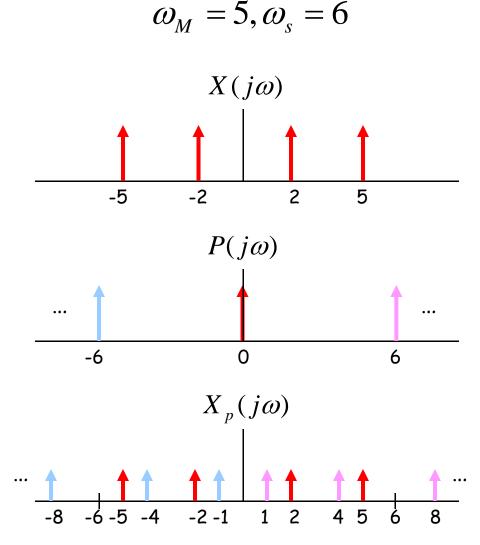
where

 $\omega_s = \frac{2\pi}{T}$ 

Given these samples, we can reconstruct x(t) by generating a periodic impulse train in which successive impulses have amplitudes that are successive sample values, then passing the train through an ideal LPF with gain T and a cutoff frequency greater than  $w_M$  and less than  $w_s$ - $w_M$ .

## $\textbf{Undersampling} \rightarrow \textbf{Aliasing}$

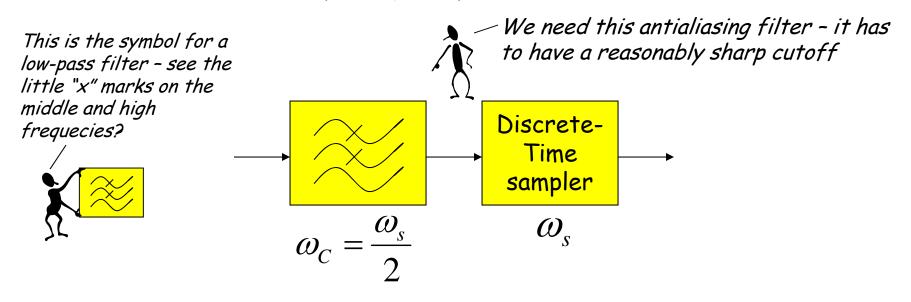
If  $w_s \leq 2w_M$  there's an overlap of frequencies between one image and its neighbors and we discover that those overlaps introduce additional frequency content in the sampled signal, a phenomenon called aliasing.



There are now tones at 1 (= 6 - 5) and 4 (= 6 - 2) in addition to the original tones at 2 and 5.

## Antialias Filters

If we wish to create samples at some fixed frequency  $w_s$ , then to avoid aliasing we need to use a low-pass filter on the original waveform to remove any frequency content  $\geq w_s/2$ .



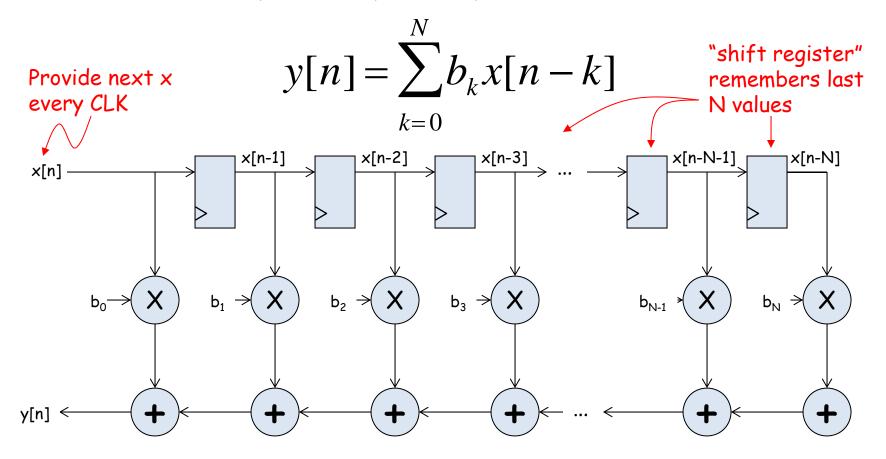
The frequency response of human ears essentially drops to zero above 20kHz. So the "Red Book" standard for CD Audio chose a 44.1kHz sampling rate, yielding a Nyquist frequency of 22.05kHz. The 2kHz of elbow room is needed because practical antialiasing filters have finite slope...

*f*s = (3 samples/line)(490 lines/frame)(30 frames/s) = 44.1 kHz

More info: http://www.cs.columbia.edu/~hgs/audio/44.1.html

## **Digital Filters**

Equation for an N-tap finite impulse response (FIR) filter:



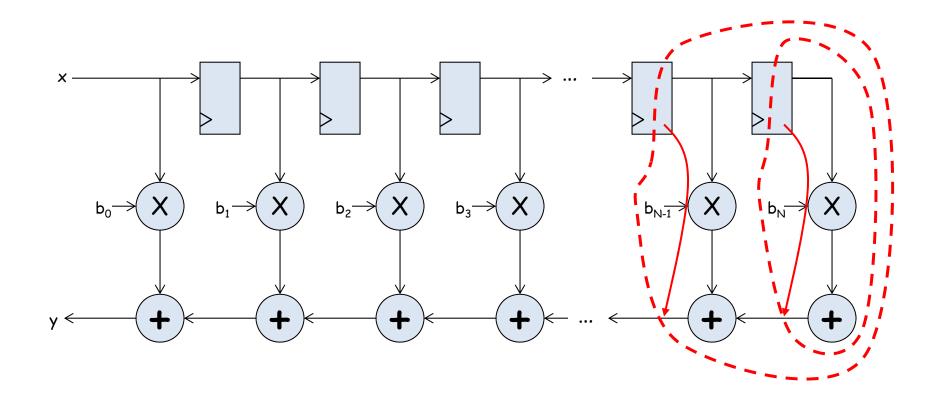
What components are part of the  $t_{PD}$  of this circuit? How does  $t_{PD}$  grow as N gets larger?

## Filter coefficients

- Use Matlab command: b = fir1(N, $\omega_c/(\omega_s/2)$ )
  - N is the number of taps (we'll get N+1 coefficients). Larger N gives sharper roll-off in filter response; usually want N to be as large as reasonably possible.
  - $\omega_c$  is the cutoff frequency (3kHz in Lab 5)
  - $\omega_s$  is the sample frequency (48kHz in Lab 5)
  - The second argument to the fir1 command is the cutoff frequency as a fraction of the Nyquist frequency (i.e., half the sample rate).
  - By default you get a lowpass filter, but can also ask for a highpass, bandpass, bandstop.
- The b coefficients are real numbers between 0 and 1. But since we don't want to do floating point arithmetic, we usually scale them by some power of two and then round to integers.
  - Since coefficients are scaled by 2<sup>s</sup>, we'll have to re-scale the answer by dividing by 2<sup>s</sup>. But this is easy - just get rid of the bottom S bits!

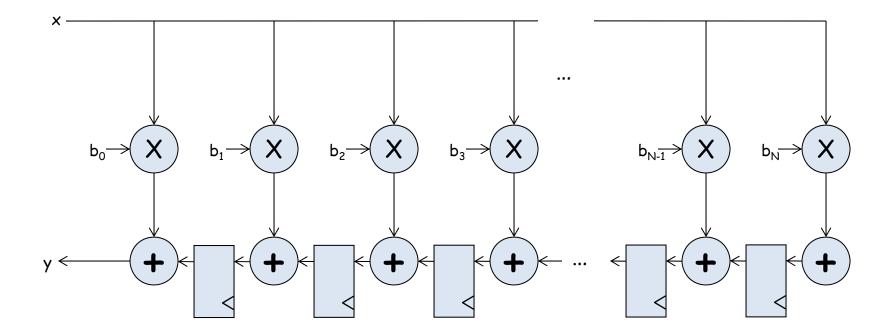
## Retiming the FIR circuit

Apply the cut-set retiming transformation repeatedly...



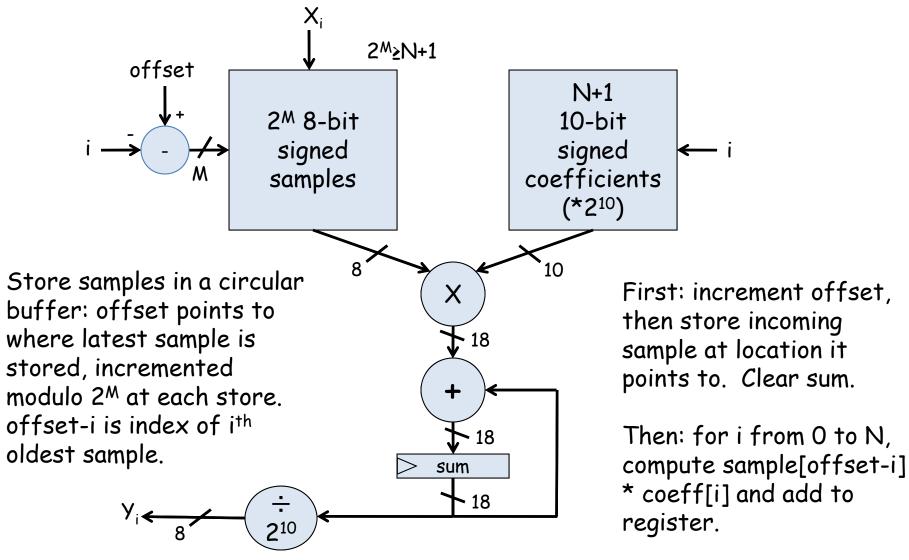
## **Retimed FIR filter circuit**

"Transposed Form" of a FIR filter



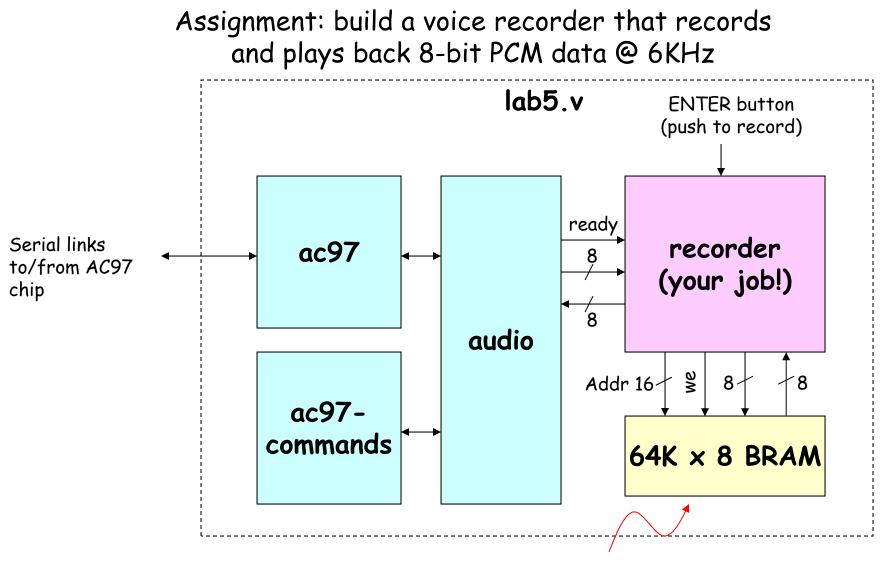
What components are part of the  $t_{PD}$  of this circuit? How does  $t_{PD}$  grow as N gets larger?

## N-tap FIR: less hardware, N+1 cycles...

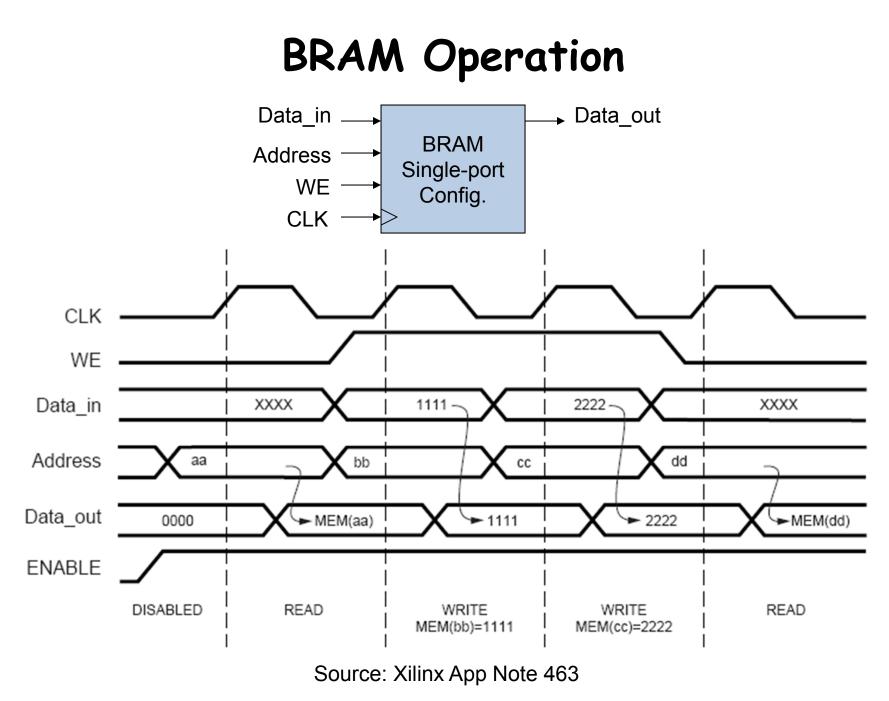


Finally: result in sum

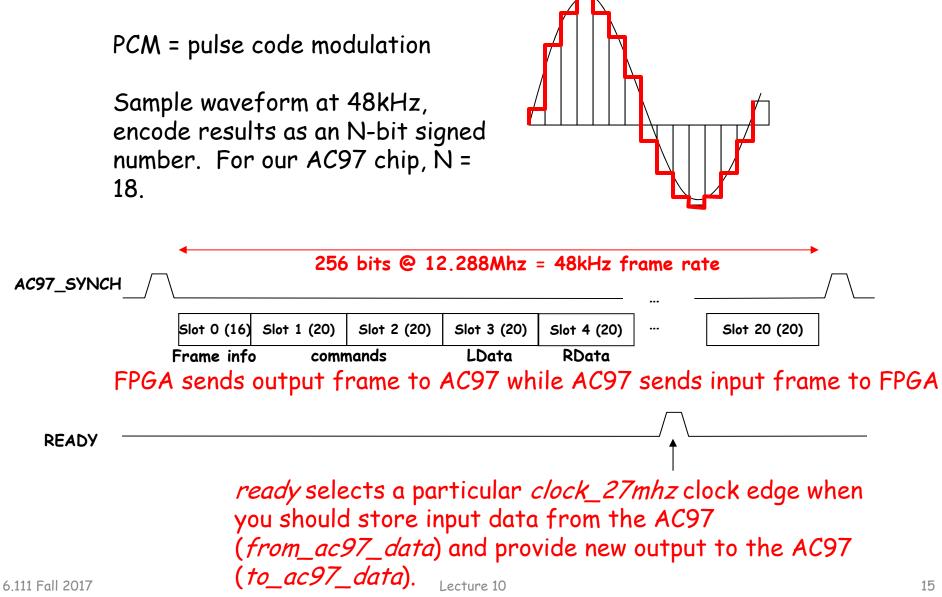
#### Lab 5A overview



#### About 11 seconds of speech @ 6KHz



## AC97: PCM data

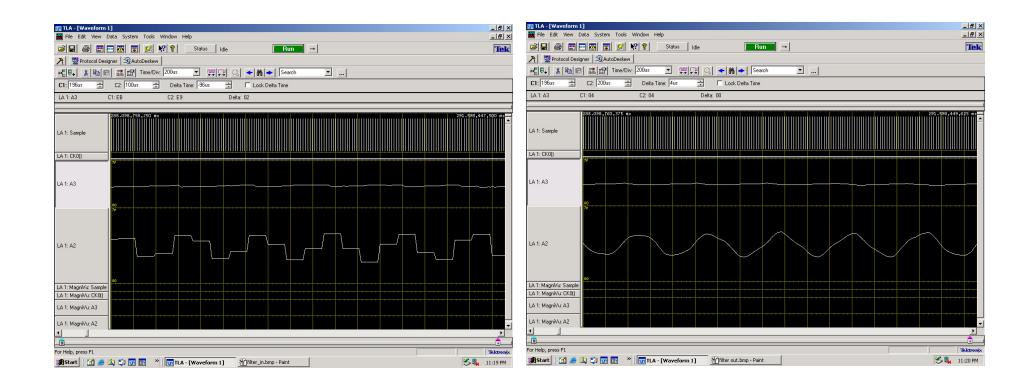


## Lab 5a\* w/ FIR filter

• Since we're down-sampling by a factor of 8, to avoid aliasing (makes the recording sound "scratchy") we need to pass the incoming samples through a low-pass antialiasing filter to remove audio signal above 3kHz (Nyquist frequency of a 6kHz sample rate).

• We need a low-pass reconstruction filter (the same filter as for antialiasing!) when playing back the 6kHz samples. Actually we'll run it at 48kHz and achieve a 6kHz playback rate by feeding it a sample, 7 zeros, the next sample, 7 more zeros, etc.

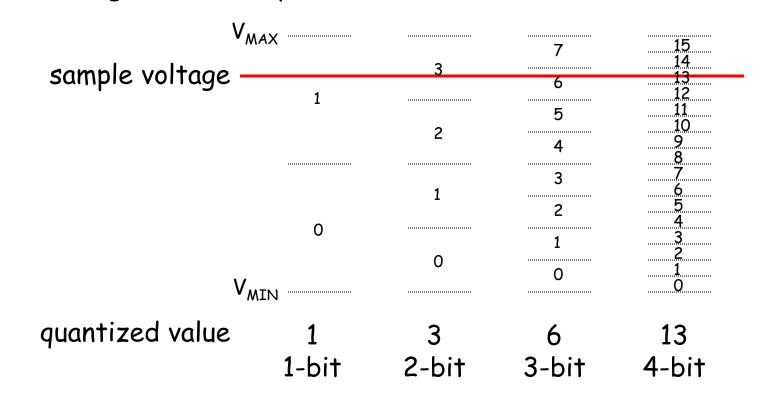
#### **FIR Filter**



#### **Discrete Values**

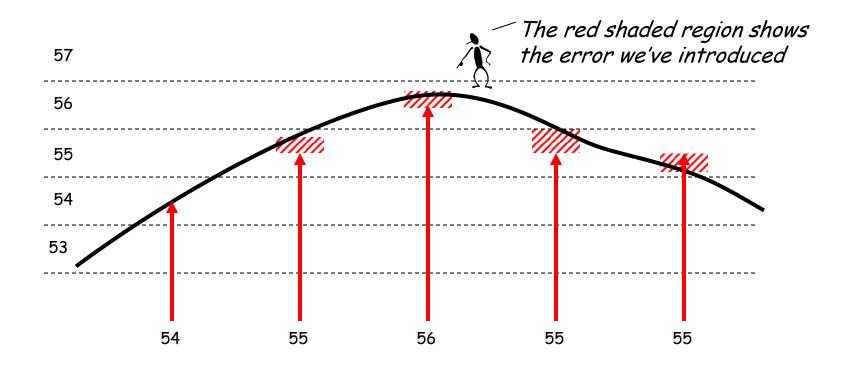
If we use N bits to encode the magnitude of one of the discrete-time samples, we can capture  $2^N$  possible values.

So we'll divide up the range of possible sample values into  $2^N$  intervals and choose the index of the enclosing interval as the encoding for the sample value.

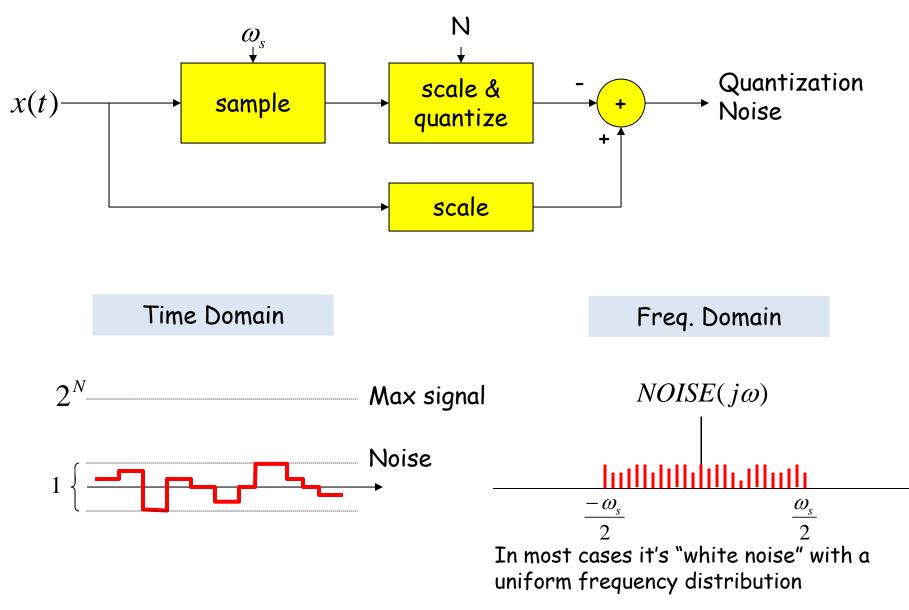


#### **Quantization Error**

Note that when we quantize the scaled sample values we may be off by up to  $\pm \frac{1}{2}$  step from the true sampled values.



#### **Quantization** Noise



#### Decibel (dB) - 3dB point

$$dB = 20 \log \left(\frac{V_o}{V_i}\right)$$

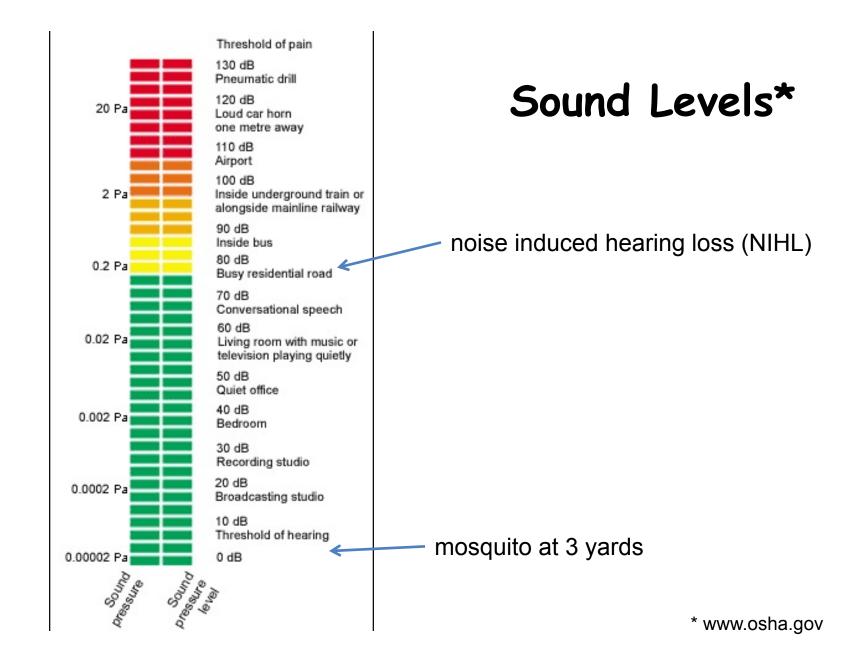
$$dB = 10 \log \left(\frac{P_o}{P_i}\right)$$

 $\log_{10}(2) = .301$ 

3 dB point = ? half power point  $100 dB = 100,000 = 10^{5}$   $80 dB = 10,000 = 10^{4}$   $60 dB = 1,000 = 10^{3}$  $40 dB = 100 = 10^{2}$ 

## **Common Decibel Units**

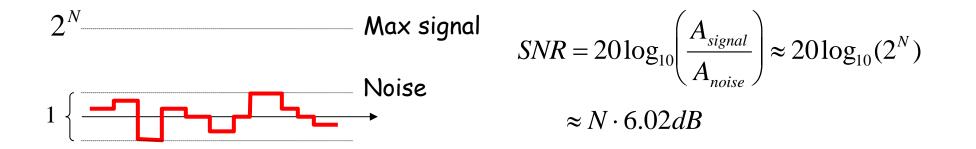
dB UNIT	reference	application
dbV	1 Volt rms	routine voltage measurements [comparisons!]
dBm	1 mW into 50Ω [0.224V] or 600Ω [0.775V]	radio-frequency [50 $\Omega$ ] or audio [600 $\Omega$ ] power measurements [in England, the dBu is used to mean 0.775V reference without regard to impedance or power]
dB mV	1 millivolt rms	signal levels in cable systems
dbW	1 Watt	audio power amplifier output [usually into 8, 4, or $2\Omega$ impedances]
dBf	1 femtowatt [10 <sup>-15</sup> watt]	communications and stereo receiver sensitivity [usually $50\Omega$ , $75\Omega$ unbalanced, or $300\Omega$ balanced antenna input impedances]
dB (SPL)	$0.0002\mu$ bar, = $20\mu$ Pa [=Pascals] [1 bar = $10^6$ dynes/cm <sup>2</sup> ~1AT]	



#### SNR: Signal-to-Noise Ratio

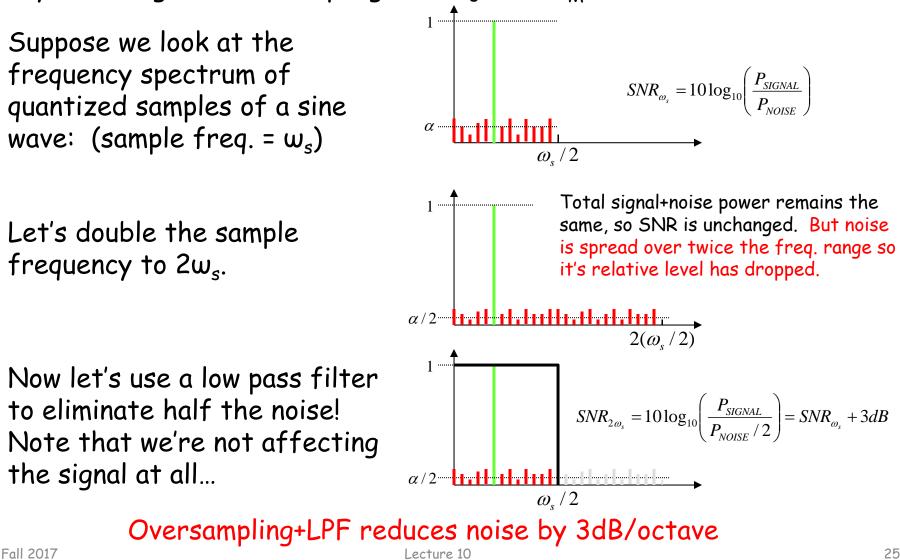
$$SNR = 10\log_{10}\left(\frac{P_{SIGNAL}}{P_{NOISE}}\right) = 10\log_{10}\left(\frac{A_{SIGNAL}^2}{A_{NOISE}^2}\right) = 20\log_{10}\left(\frac{A_{SIGNAL}}{A_{NOISE}}\right)$$
  
$$\swarrow RMS \text{ amplitude}$$

SNR is measured in decibels (dB). Note that it's a logarithmic scale: if SNR increases by 3dB the ratio has increased by a factor 2. When applied to audible sounds: the ratio of normal speech levels to the faintest audible sound is 60-70 dB.



## Oversampling

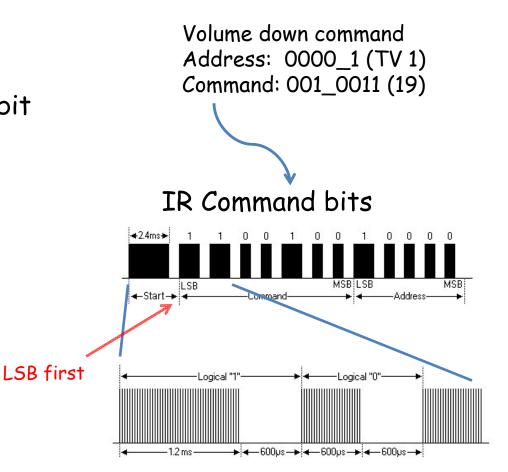
To avoid aliasing we know that  $w_s$  must be at least  $2w_M$ . Is there any advantage to oversampling, i.e.,  $w_s = K \cdot 2w_M$ ?



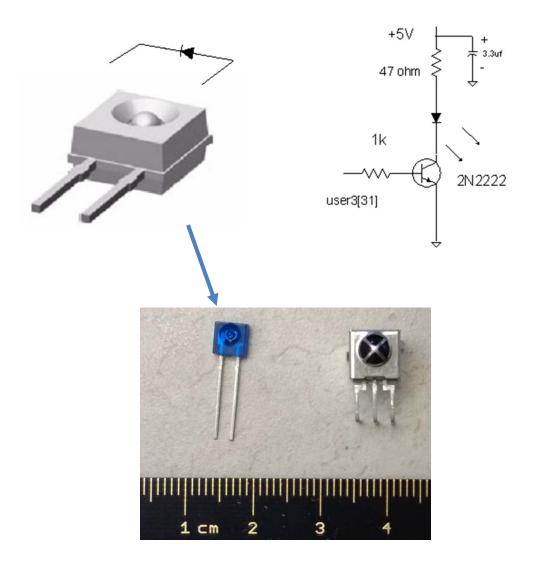
#### Lab 5b Overview

Assignment: build a digital system to "learn" four Sony Infrared Command (SIRC) and use it to control a Sony television.

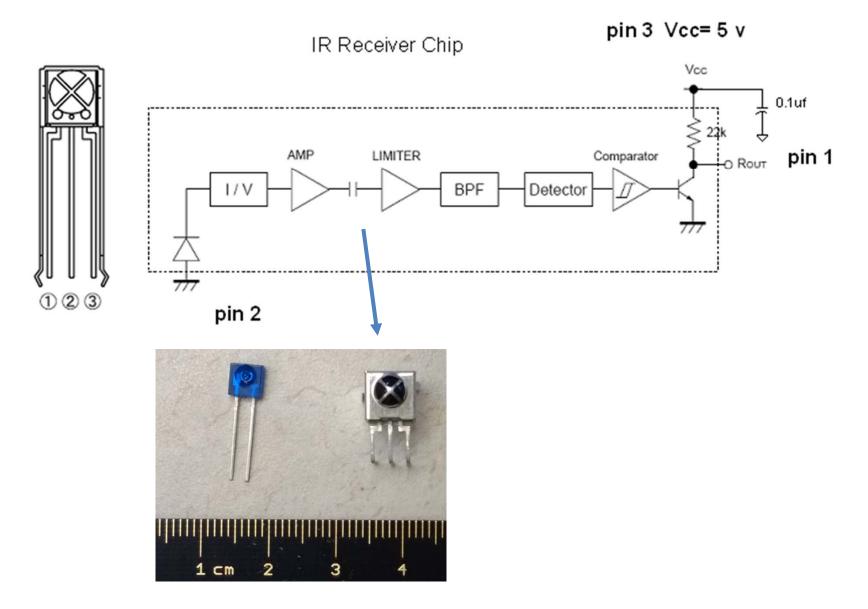
- Data sent via 950nm IR modulated at 40khz.
- Data width: 12, 15 or 20 bit protocol (use 12 bit).
- Start bit: 2400us High: 1200us Low: 600us
- Transmit FSM provided
- Learn/store remote commands



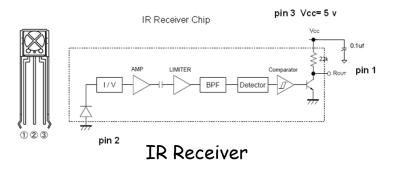
#### **IR** Transmitter



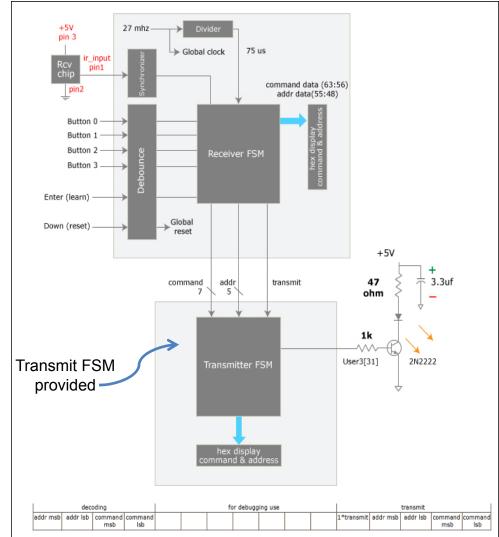
#### **RPM7140 IR Receiver**



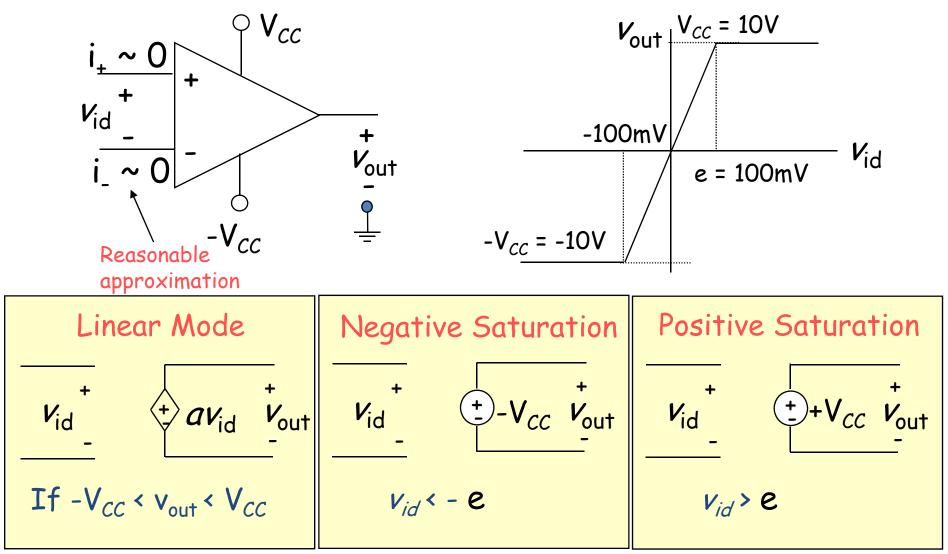
## Lab 5b Block Diagram



- IR receiver demodulates signal and provides input into labkit - powered by 5V from labkit.
- 2N2222 BJT used to power IR transmitter (note bypass caps) - power from labkit
- Command code and channel displayed on hex display

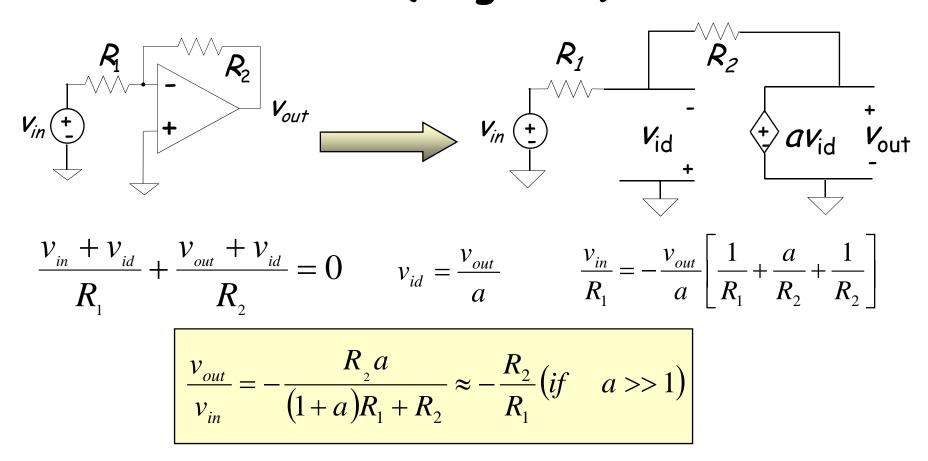


#### Our Analog Building Block: OpAmp



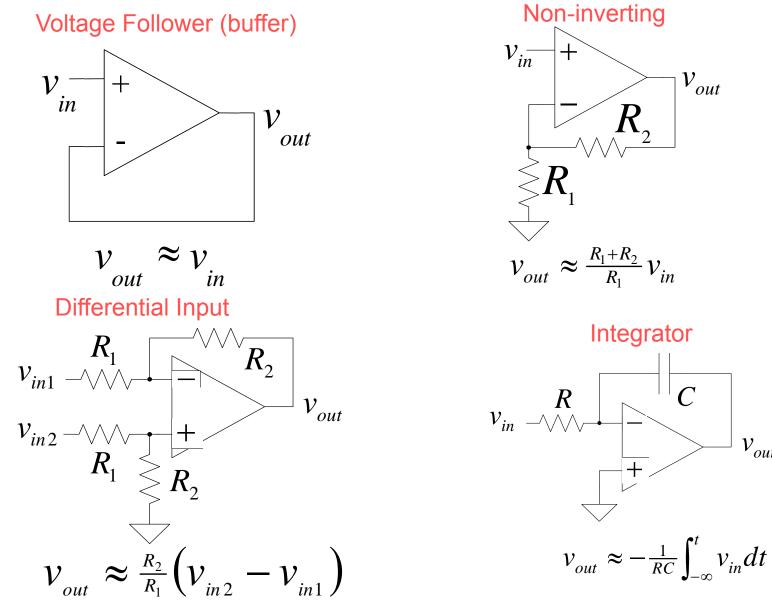
Very small input range for "open loop" configuration

## The Power of (Negative) Feedback



- Overall (closed loop) gain does not depend on open loop gain
- Trade gain for robustness
- Easier analysis approach: "virtual short circuit approach"
  - v<sub>+</sub> = v<sub>-</sub> = 0 if OpAmp is linear

#### **Basic OpAmp Circuits**



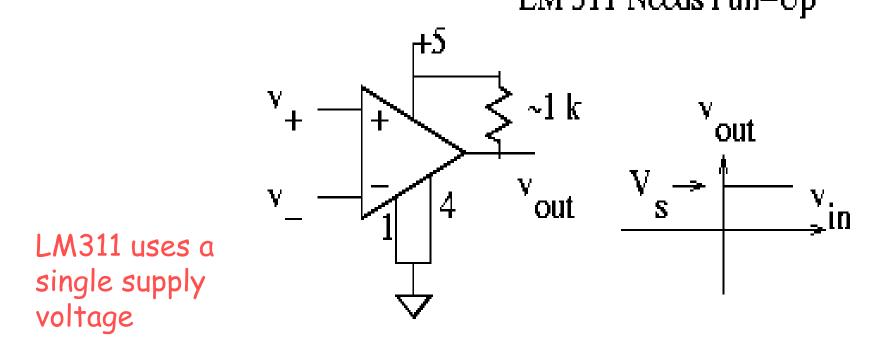
6.111 Fall 2017

 $V_{out}$ 

#### **OpAmp** as a Comparator

Analog Comparator: Is V+ > V-? The Output is a DIGITAL signal

> Analog Comparator: Analog to TTL LM 311 Needs Pull–Up

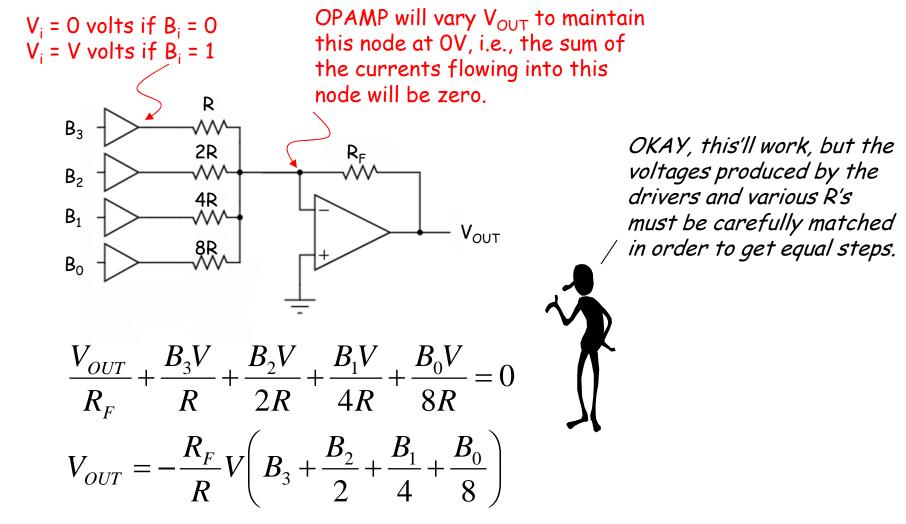


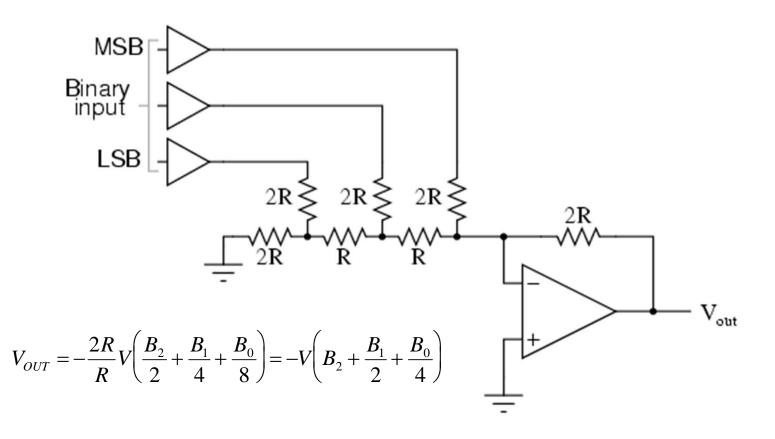
# Digital to Analog

- Common metrics:
  - Conversion rate DC to ~500 MHz (video)
  - # bits up to ~24
  - Voltage reference source (internal / external; stability)
  - Output drive (unipolar / bipolar / current) & settling time
  - Interface parallel / serial
  - Power dissipation
- Common applications:
  - Real world control (motors, lights)
  - Video signal generation
  - Audio / RF "direct digital synthesis"
  - Telecommunications (light modulation)
  - Scientific & Medical (ultrasound, ...)

#### DAC: digital to analog converter

How can we convert a N-bit binary number to a voltage?

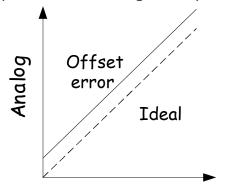




# R-2R Ladder achieves large current division ratios with only two resistor values

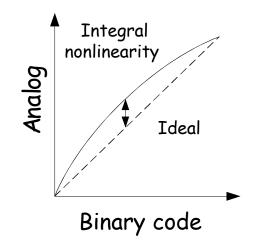
## Non-idealities in Data Conversion

Offset - a constant voltage offset that appears at the output when the digital input is 0

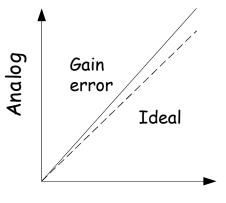


Binary code

Integral Nonlinearity - maximum deviation from the ideal analog output voltage

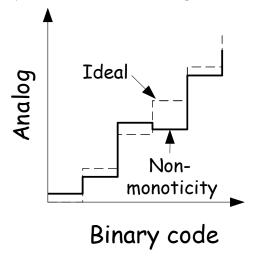


Gain error - deviation of slope from ideal value of 1

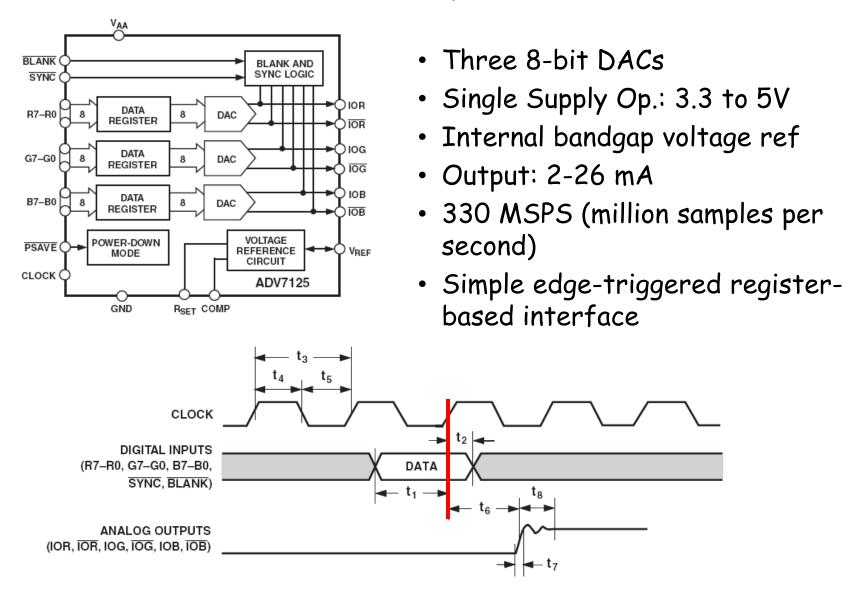


Binary code

Differential nonlinearity - the largest increment in analog output for a 1-bit change

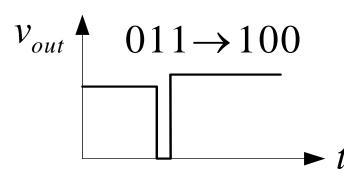


# Labkit: ADV7125 Triple Out Video DAC

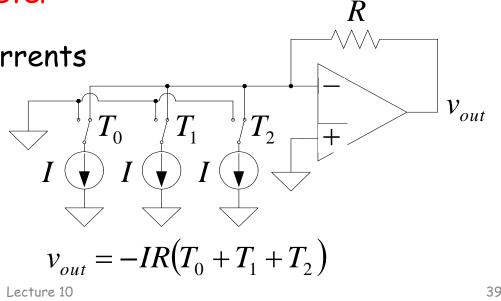


# Glitching and Thermometer D/A

- Glitching is caused when switching times in a D/A are not synchronized
- Example: Output changes from 011 to 100 - MSB switch is delayed
- Filtering reduces glitch but • increases the D/A settling time
- One solution is a thermometer • code D/A - requires  $2^{N}$  - 1 switches but no ratioed currents



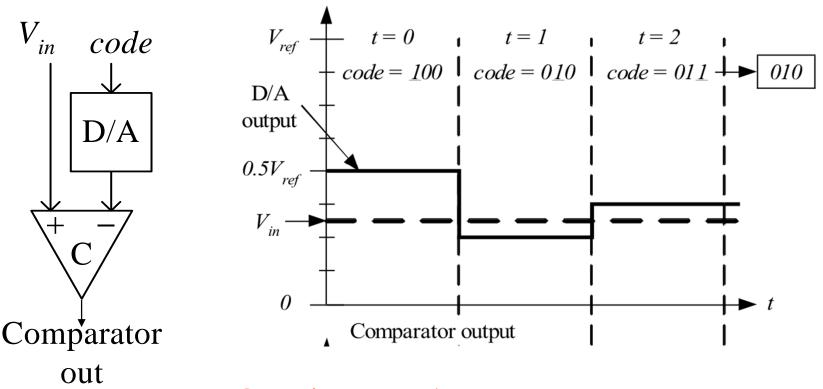
Binary		Thermometer		
0	0	0	0	0
0	1	0	0	1
1	0	0	1	1
1	1	1	1	1



# Successive-Approximation A/D

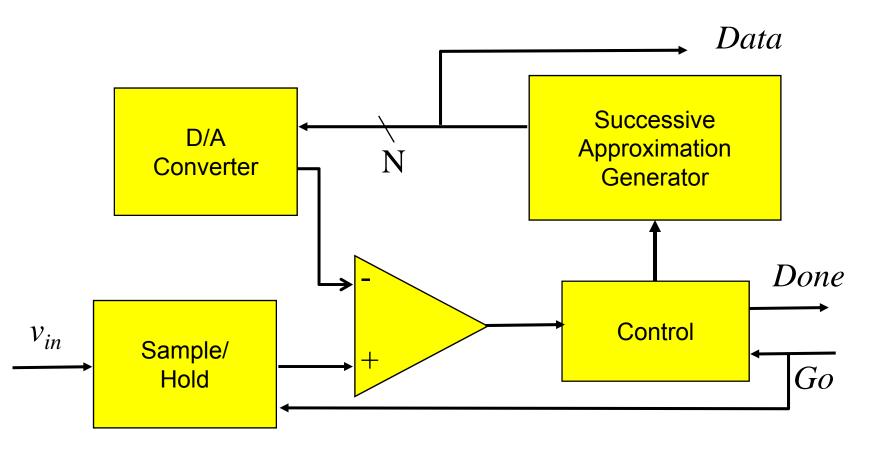
D/A converters are typically compact and easier to design. Why not A/D convert using a D/A converter and a comparator?

- DAC generates analog voltage which is compared to the input voltage
- If DAC voltage > input voltage then set that bit; otherwise, reset that bit
- This type of ADC takes a fixed amount of time proportional to the bit length



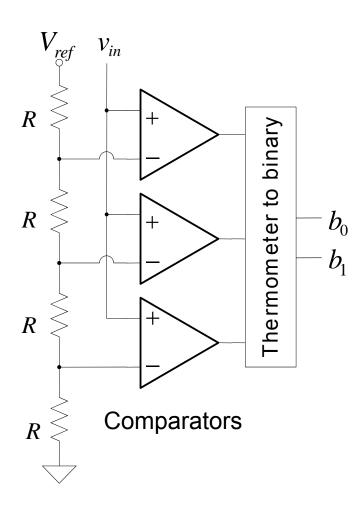
Example: 3-bit A/D conversion, 2 LSB < Vin < 3 LSB

# Successive-Approximation A/D



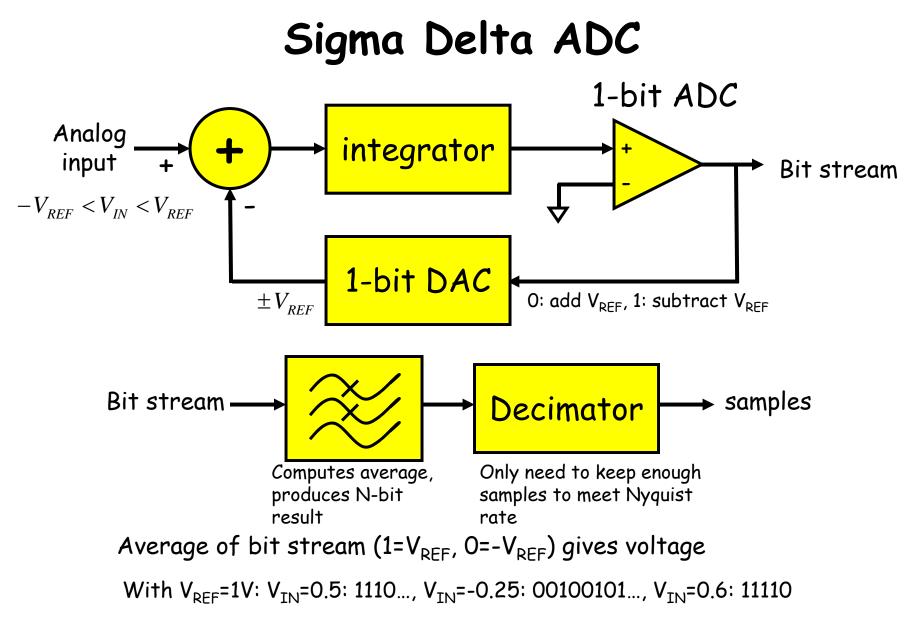
Serial conversion takes a time equal to  $N(t_{D/A} + t_{comp})$ 

# Flash A/D Converter



- Brute-force A/D conversion
- Simultaneously compare the analog value with every possible reference value
- Fastest method of A/D conversion
- Size scales exponentially with precision

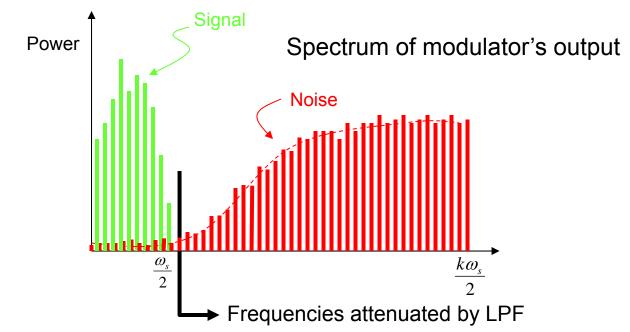
(requires 2<sup>N</sup> comparators)



http://designtools.analog.com/dt/sdtutorial/sdtutorial.html#instructions

# So, what's the big deal?

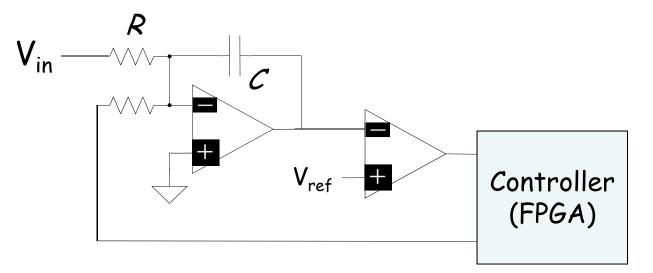
- Can be run at high sampling rates, oversampling by, say, 8 or 9 octaves for audio applications; low power implementations
- Feedback path through the integrator changes how the noise is spread across the sampling spectrum.



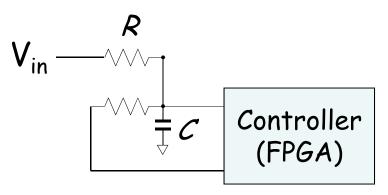
• Pushing noise power to higher frequencies means more noise is eliminated by LPF:  $N^{th}$  order  $\Sigma\Delta$  SNR = (3+N\*6)dB/octave

### Sigma Delta ADC

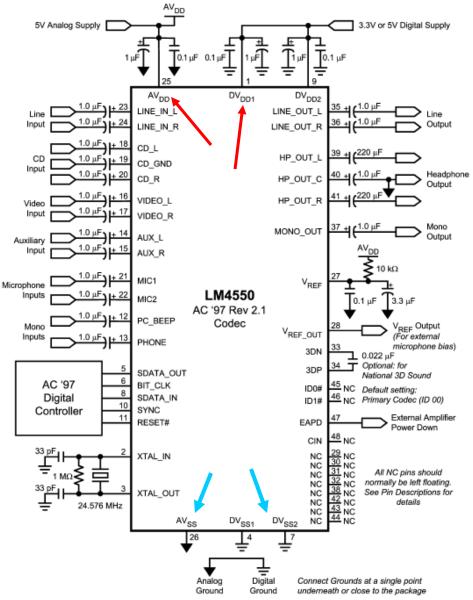
• A simple ADC:



Poor Man's ADC:



#### AD Supply Voltages Consideration

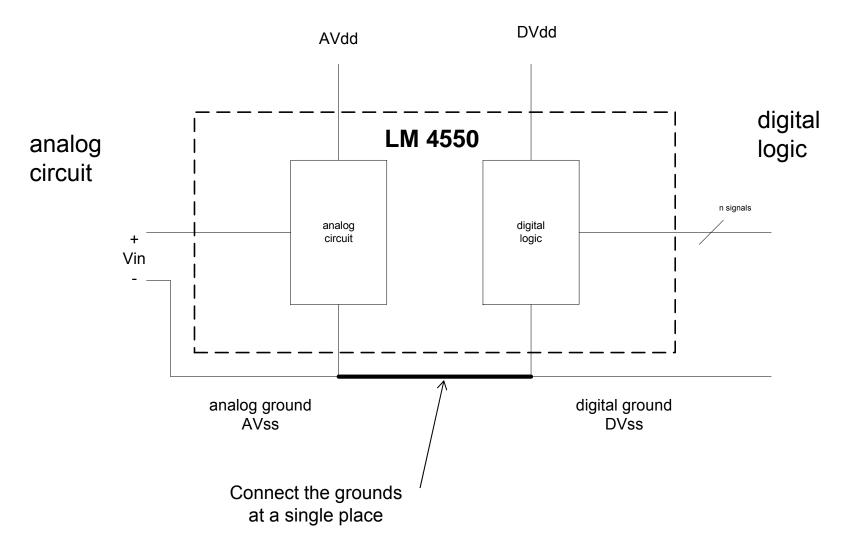


Noise caused by current spikes in fast switching digital circuits:

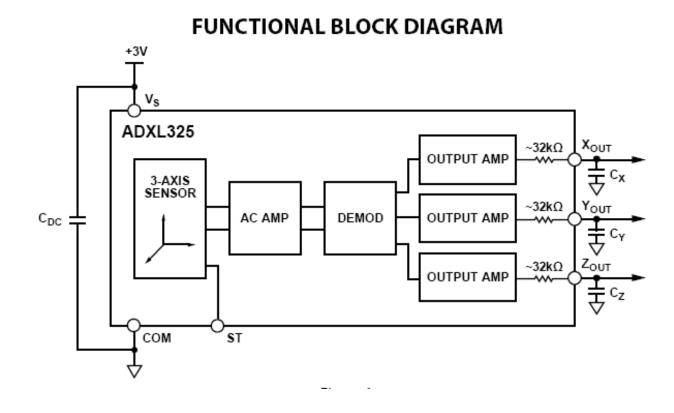
$$i_c = c \frac{dv}{dt}$$

- AV<sub>DD</sub> Positive Analog Supply Voltage
- $AV_{ss}$  Analog Ground
- DV<sub>DD</sub> Positive Digital Supply Voltage
- DV<sub>ss</sub> Digital Ground

#### Digital/Analog Grounds



#### Sensors



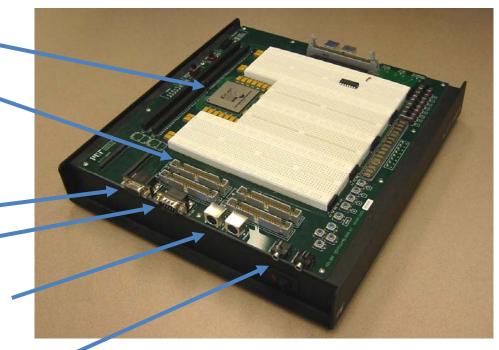
3 Axis 5G accelerometer

- Many sensors have native analog outputs: thermocouples, accelerometers, pressure gauge, ..
- 3-axis

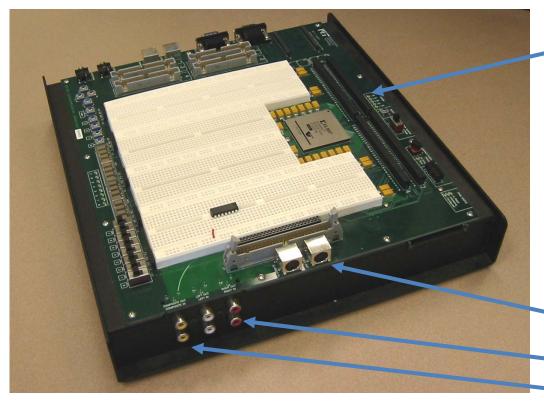
   accelerometer
   now used in cell
   phones, games,
   iPods, laptops,
   6.111 projects

# Labkit Hardware

- Xilinx FPGA
- Logic analyzer pods
  - 4 banks/pods of 16 data lines
  - (analyzerN\_clock) and
     a 16-bit data bus
     (analyzerN\_data[15:0])
     N=1,2,3,4
- VGA video output
- RS-232 Serial IO
- PS/2 keyboard and mouse input
- AC97 audio input/output
  - Intel standard for PC audio systems
  - codec's ADCs and DACs operate at a 48kHz sample rate, with 18 bits of precision
- 128Mbits Flash memory, (2) 512k x 36 ZBT SRAM



### Labkit Hardware



- Bidirectional user
  - general purpose I/O, such as connecting to devices on the breadboards
  - bidirectional (inout)
     signals user1[31:0]
     through user4[31:0]
- TV Video
  - S video input/output
    - Audio input/output
    - Composite video input/output

# Upload Lab 4 Verilog

- Submit by Monday
- Grading
  - Proper use of blocking and non-blocking assignments
  - <u>Readable Code (reformatted)</u> with comments and consistent indenting [use emacs or vim]
  - Use of default in case statement
  - Use of parameter statements for symbolic name and constants (state==5 vs state==DATA\_READY)
  - Parameterized modules when appropriate
  - Readable logical flow, properly formatted (see "Verilog Editors")
  - No long nested if statements.
  - Score 1 to 3 (3 perfect); 1/2 point off for each occurrence.