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January 10, 2005



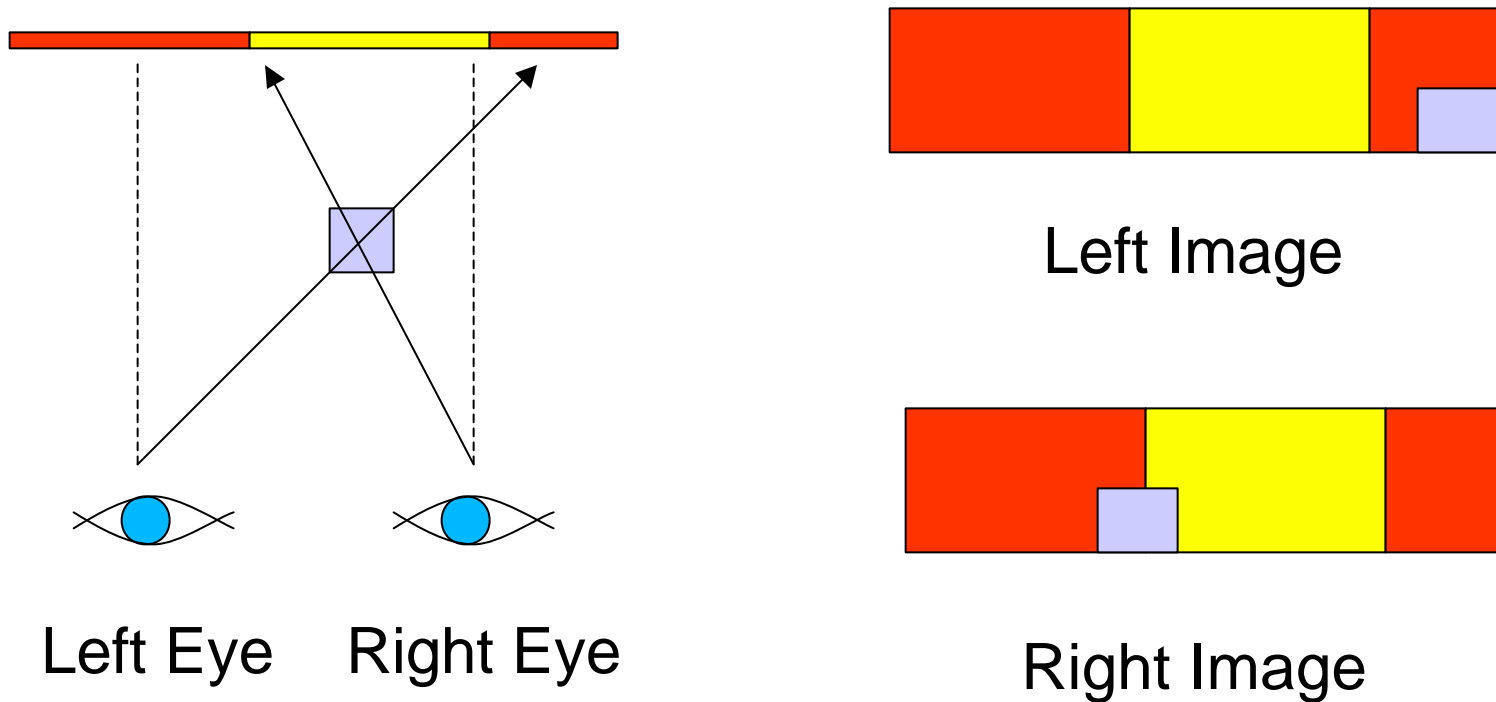
# Agenda

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- ✍ Hodge Podge of Vision Stuff
  - ✍ Stereo Vision
  - ✍ Rigid body motion
  - ✍ Edge Detection
  - ✍ Optical Flow
  - ✍ EM Algorithm to locate objects
- ✍ May not be directly applicable, but we've tried to make it relevant.

# Stereo Vision

- ✍ We can judge distance based on the how much the object's position changes.

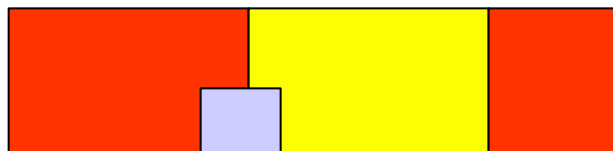


# Stereo Vision

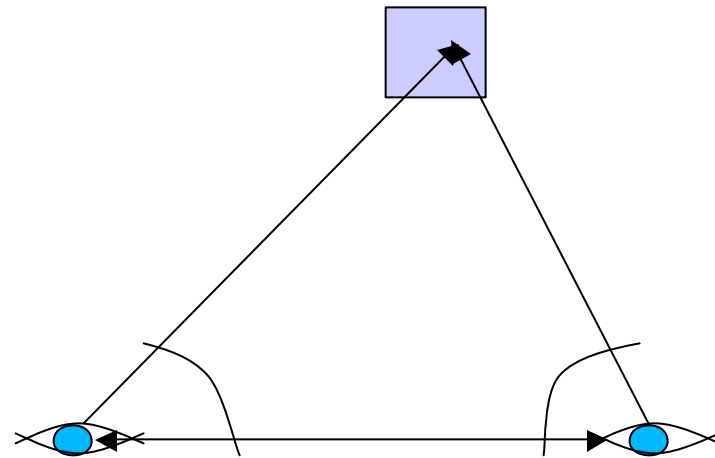
- Use the image to find the angle to the object, then apply some trig:



Left Image



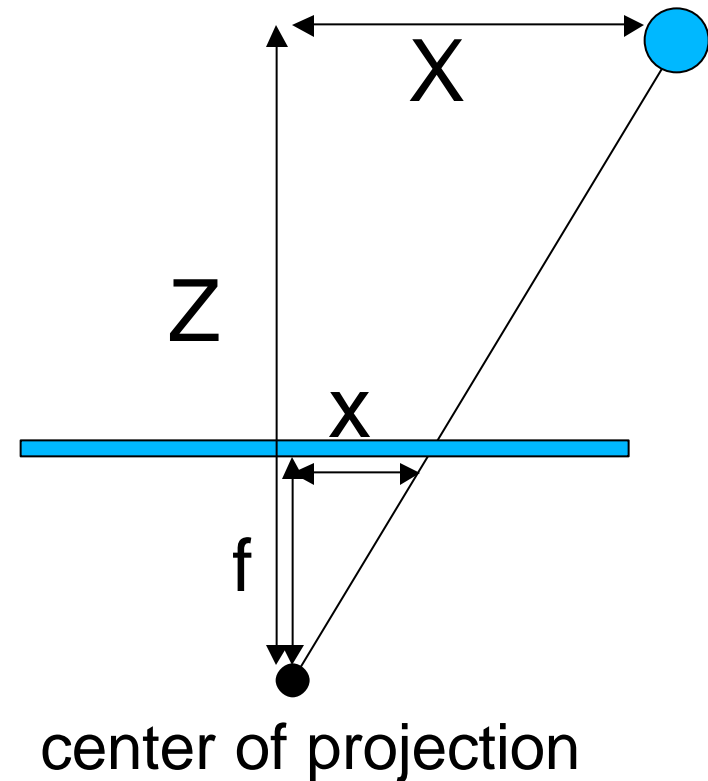
Right Image



angle-side-angle gives you a unique triangle

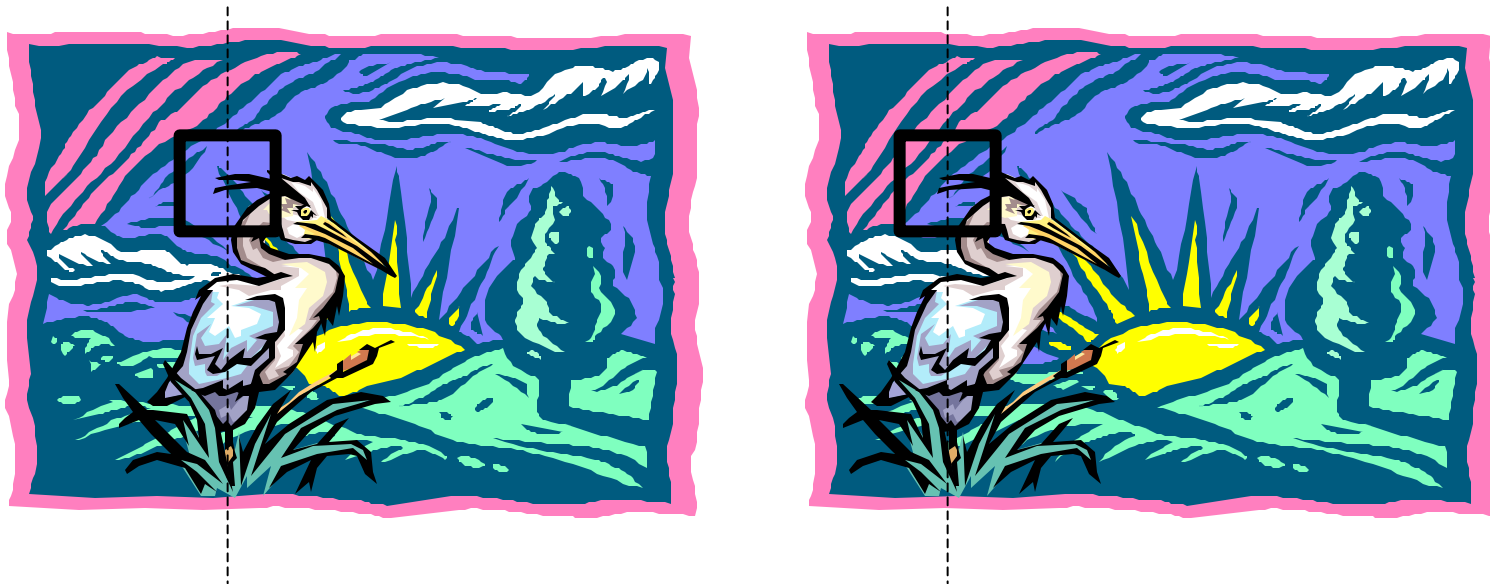
# Stereo Vision

- ✍ What's the angle?
- ✍ Perspective projection equation tells us
$$x/f = X/Z$$
- ✍  $f$  is focal length,  $x$  is pixel location
- ✍  $\tan(\theta) = X/Z = x/f$



# Stereo Vision

- ✍ But in a complex image, objects may be hard to identify...
- ✍ Try to match regions instead (block correlation)

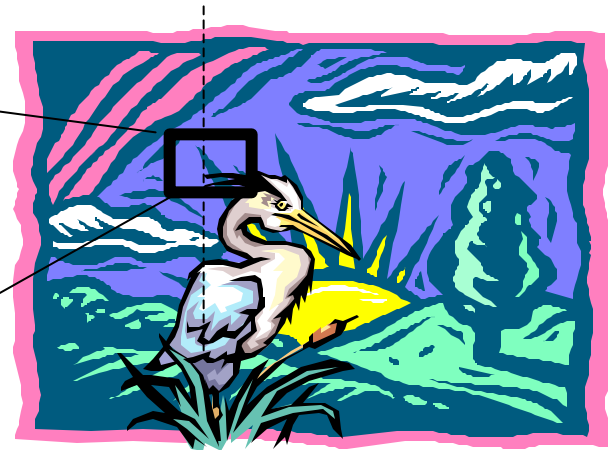


# Stereo Vision

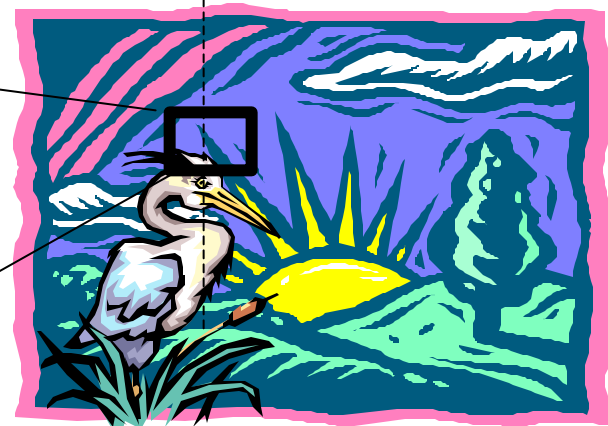
✍ Difference metric = Sum of  $(L_i - R_i)^2$

✍ Search horizontally for best match (least difference)

6	5	5
5	6	5
5	5	7

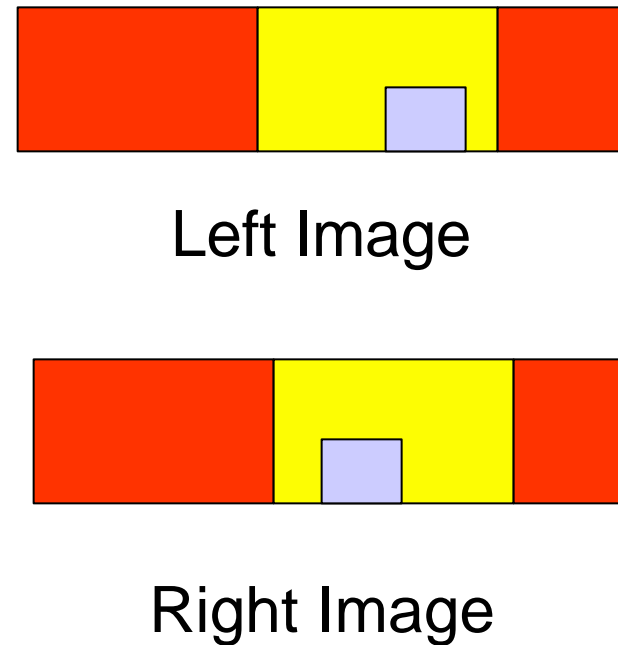
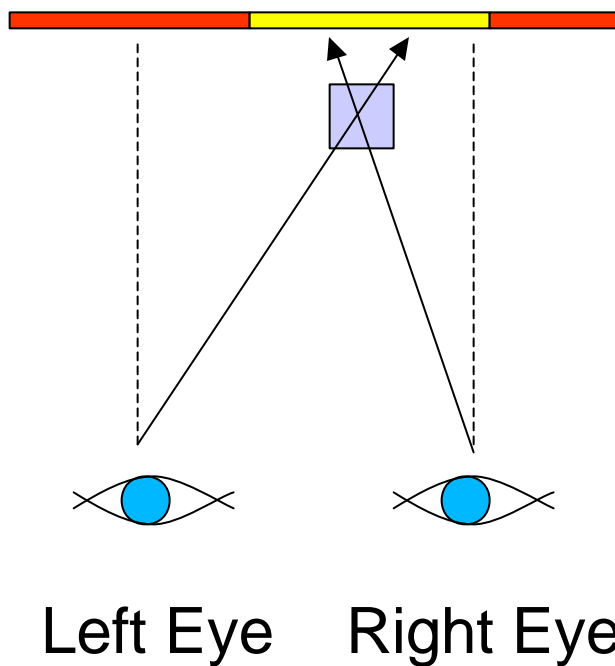


6	5	5
5	6	5
1	1	6



# Stereo Vision

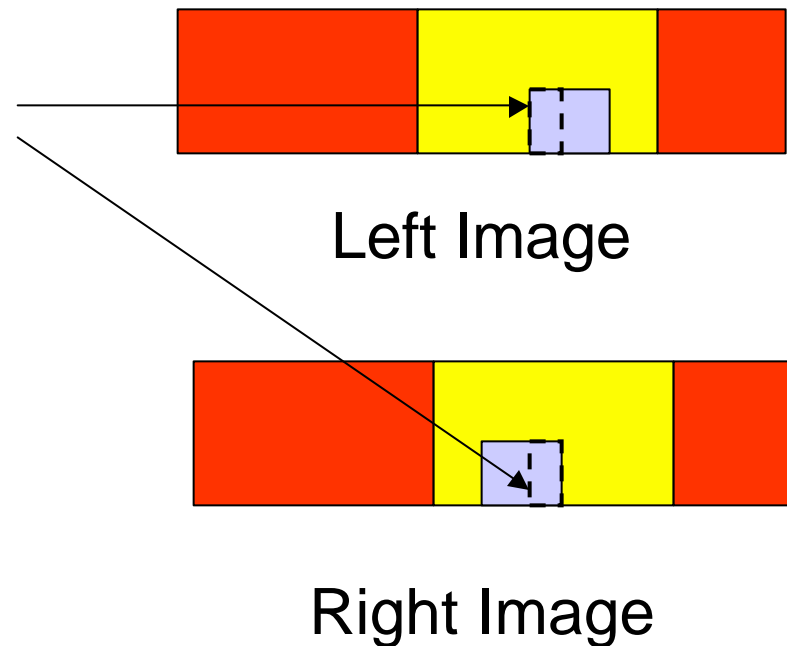
- ✍ Still have a problem: unless the object is really close, the change might be small...





# Stereo Vision

- ✎ And many regions will be the same in both pictures, even if the object has moved.
- ✎ We need to apply stereo only to “interesting” regions.



# Stereo Vision

- ✍ Uniform regions are not interesting
- ✍ Patterned regions are interesting
- ✍ Let the “interest” operator be the lowest eigenvalue of a matrix passed over the region.

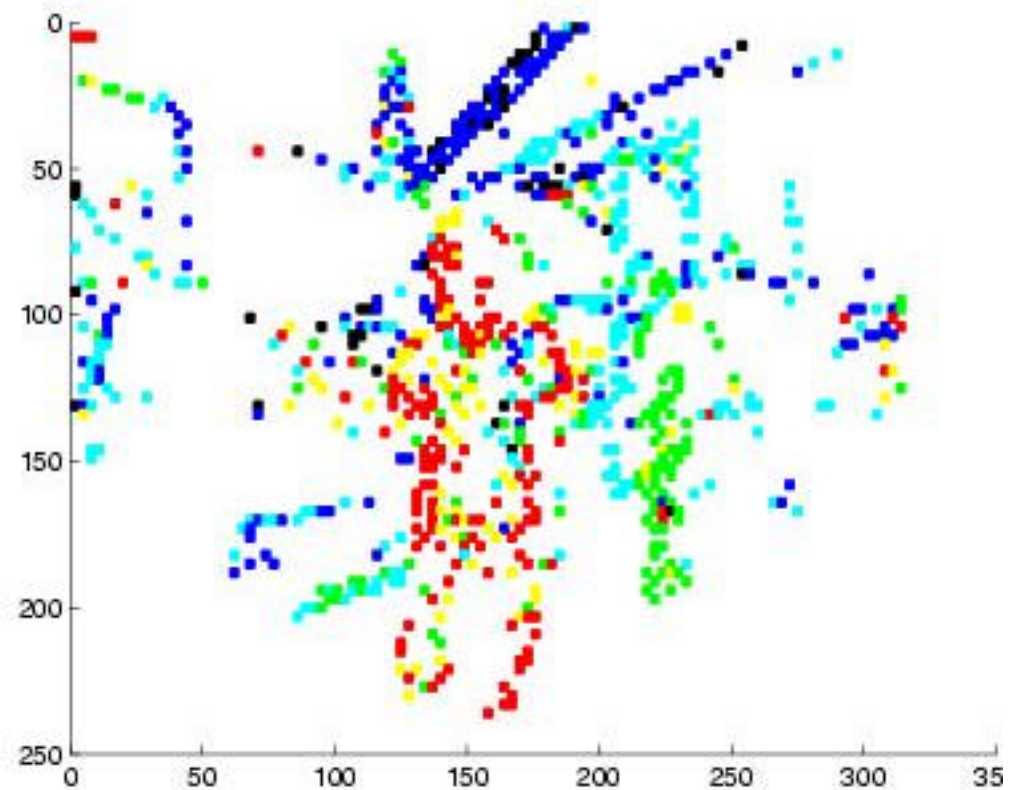
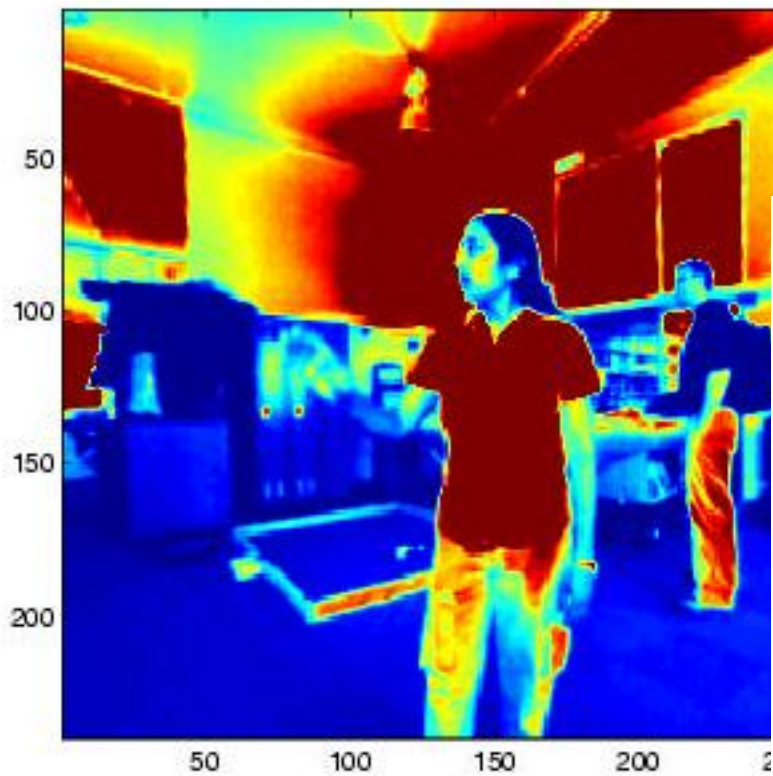
5	5	5
5	5	5
5	5	4

lowest eigenvalue = 0

8	5	2
5	1	5
5	5	4

lowest eigenvalue = 2.5

# Stereo Vision





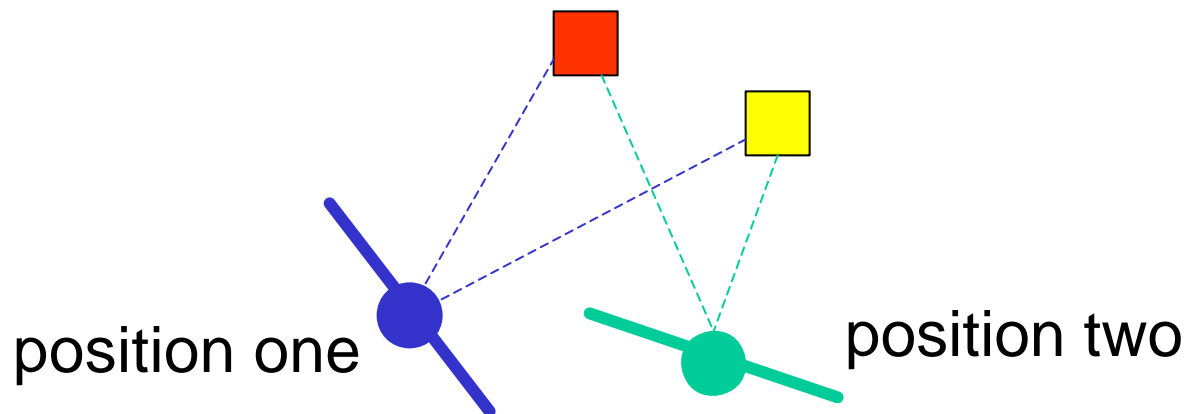
# Stereo Vision

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- ✍ For Maslab, the problem is simpler... can easily identify objects and compute horizontal disparity.
- ✍ To convert disparity to distance, calibrate the trig.
- ✍ Use two cameras... or mount a camera on a movable platform... or move your robot

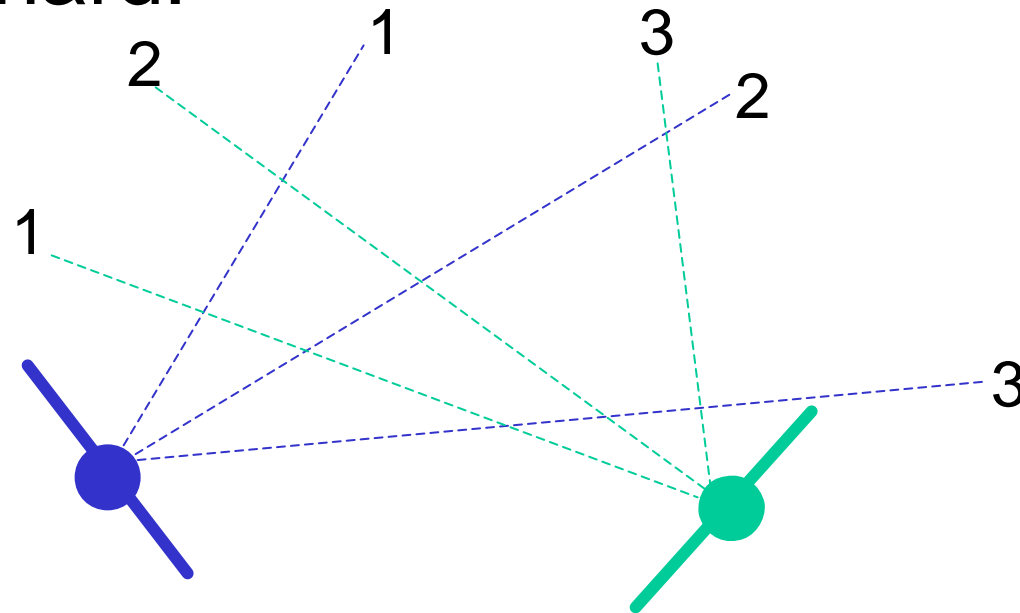
# Rigid Body Motion

- ✍ Going from data association to motion
- ✍ Given
  - ✍ a starting  $x_1, y_1, ?_1$
  - ✍ a set of objects visible in both images
- ✍ What is  $x_2, y_2, \text{ and } ?_2$ ?



# Rigid Body Motion

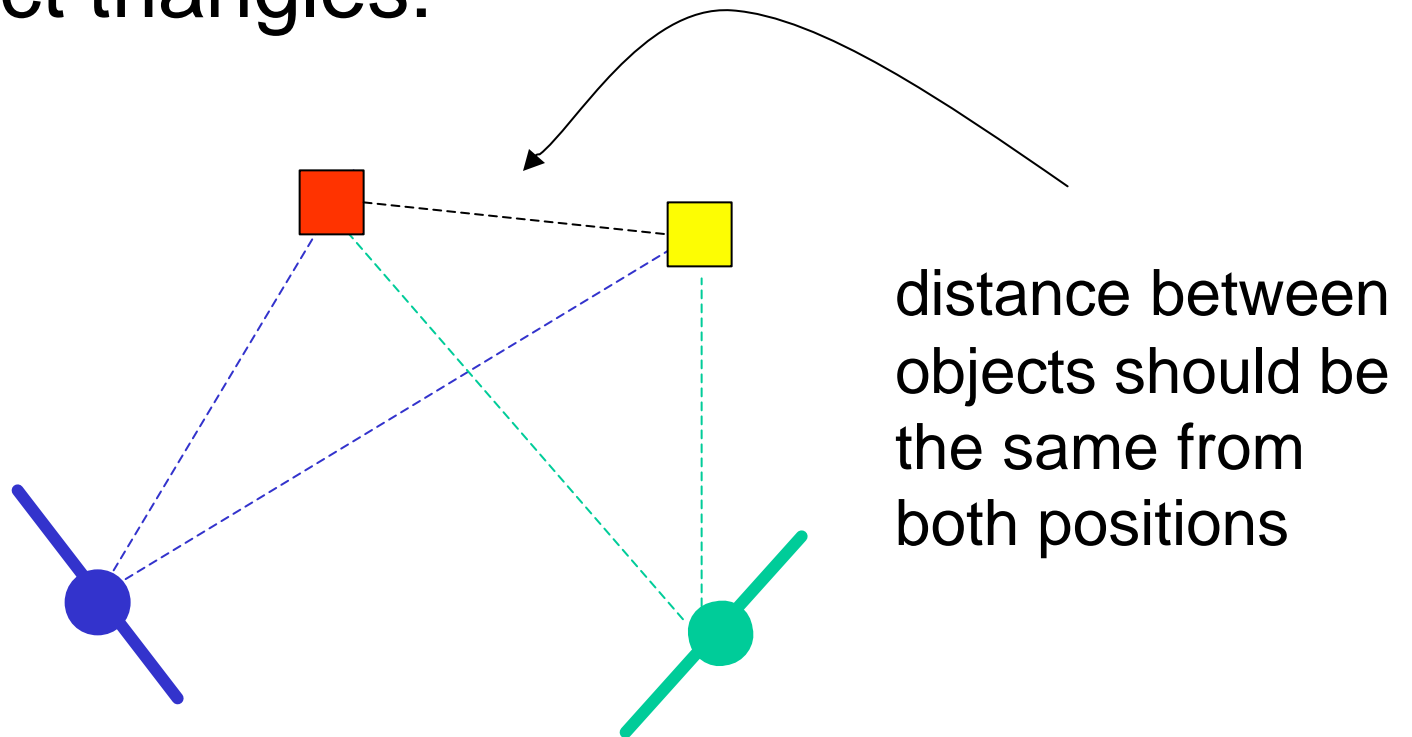
- ✍ If we only know angles, the problem is quite hard:



- ✍ Assume distances to objects are known.

# Rigid Body Motion

- ✍ If angles and distances are known, we can construct triangles:





# Rigid Body Motion

✍ Apply the math for a rotation:

$$x_{1i} = \cos(?) * x_{2i} + \sin(?) * y_{2i} + x_0$$

$$y_{1i} = \cos(?) * y_{2i} - \sin(?) * x_{2i} + y_0$$

✍ Solve for  $x_0$ ,  $y_0$ , and  $?$  with least squares:

$$S (x_{1i} - \cos(?) * x_{2i} - \sin(?) * y_{2i} - x_0)^2 + \\ (y_{1i} - \cos(?) * y_{2i} + \sin(?) * x_{2i} - y_0)^2$$

✍ Need at least two objects to solve







# Rigid Body Motion

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## Advantages

-  Relies on the world, not on odometry
-  Can use many or few associations

## Disadvantage

-  Can take time to compute

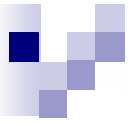


# Edge Detection

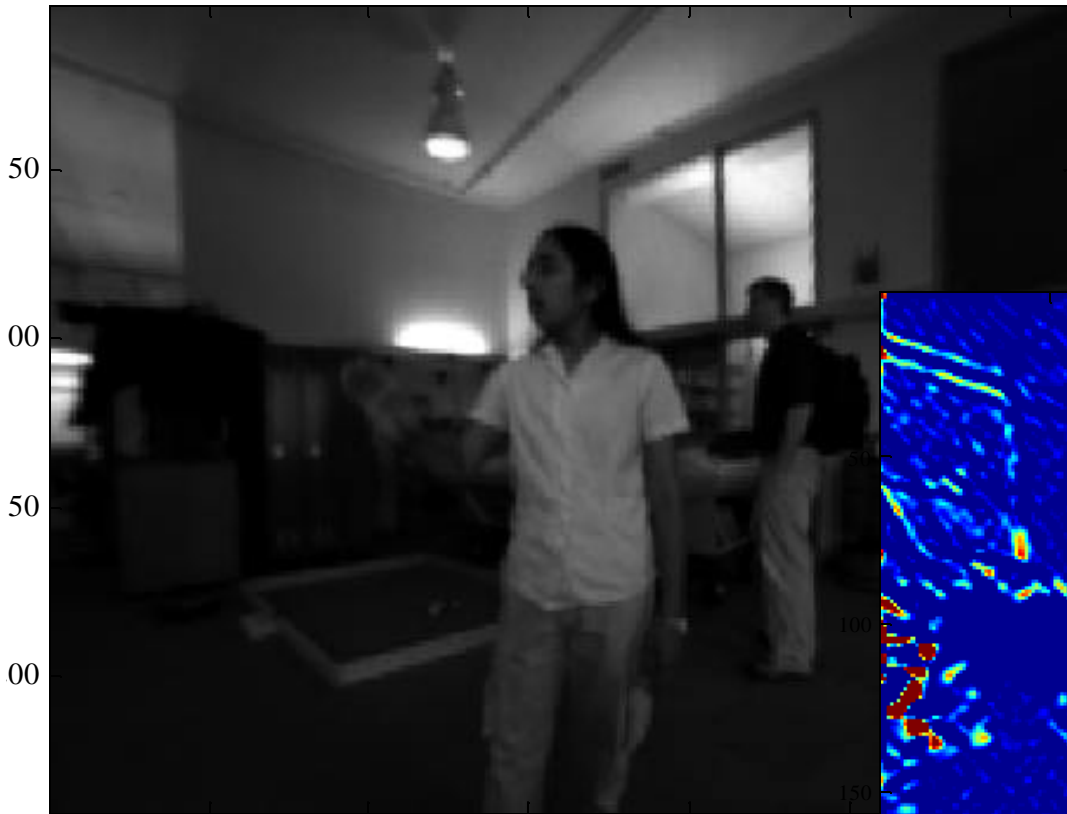
- ✍ Edges are places of large change
- ✍ Scan the image with little computational molecules or a 'kernel'

1
0
-1

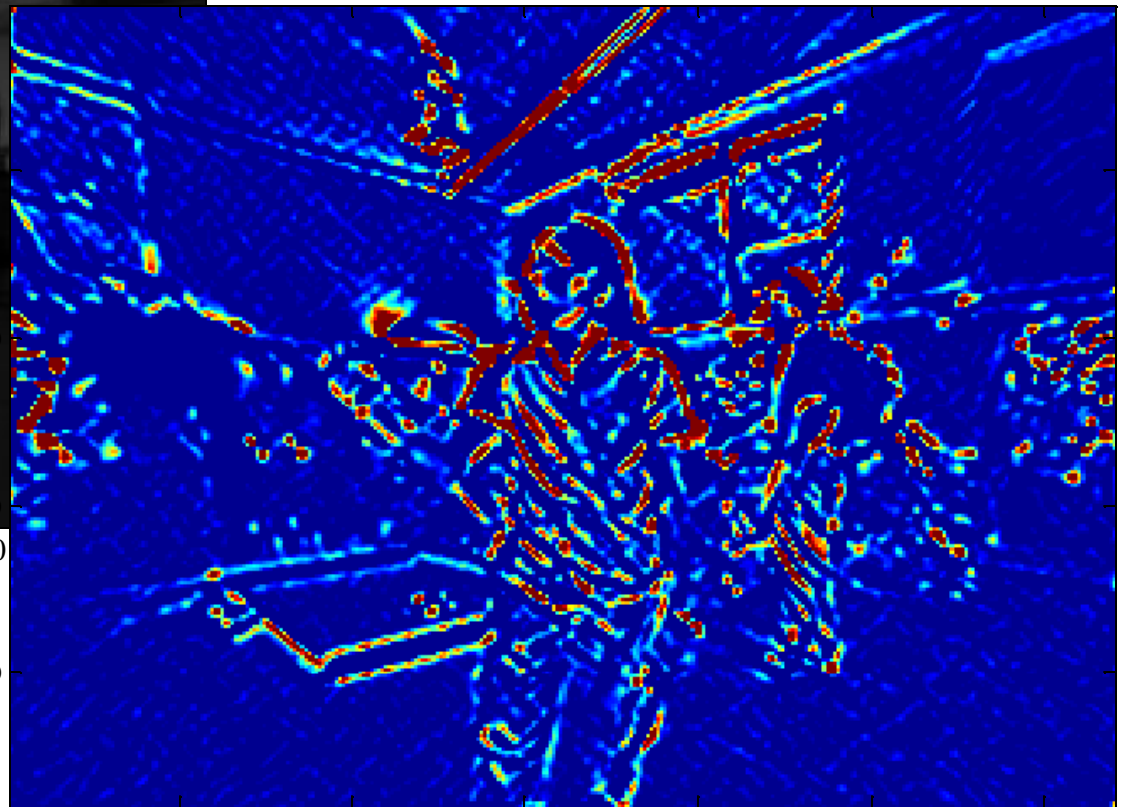
1	0	-1
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# Edge Detection



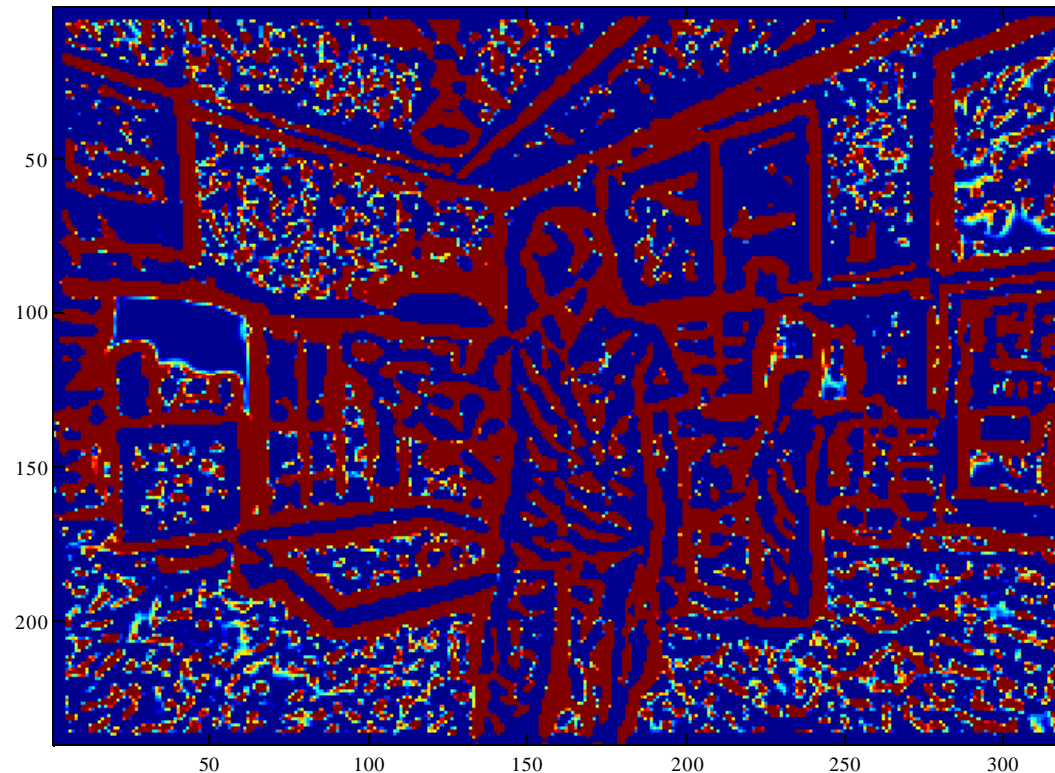
50 100 150 200 250



50 100 150 200 250 300

# Edge Detection

- ✍ More sophisticated filters work better (Laplacian of Gaussian, for example)





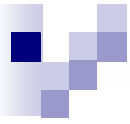
# Edge Detection

- ✍ Need to choose a good value for threshold
  - ✍ Too small—gets lots of noise, fat edges
  - ✍ Too big—lose sections of edge
- ✍ What do you do with an edge?
  - ✍ Extract lines for a map?
  - ✍ Use to separate regions?

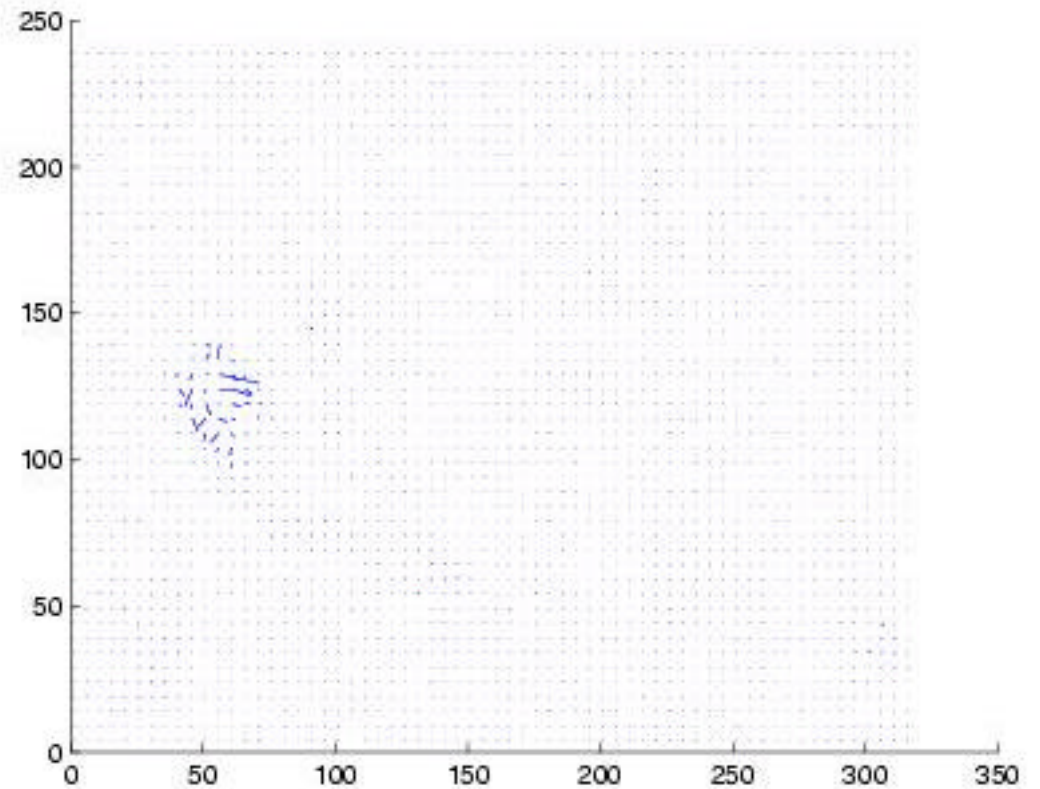
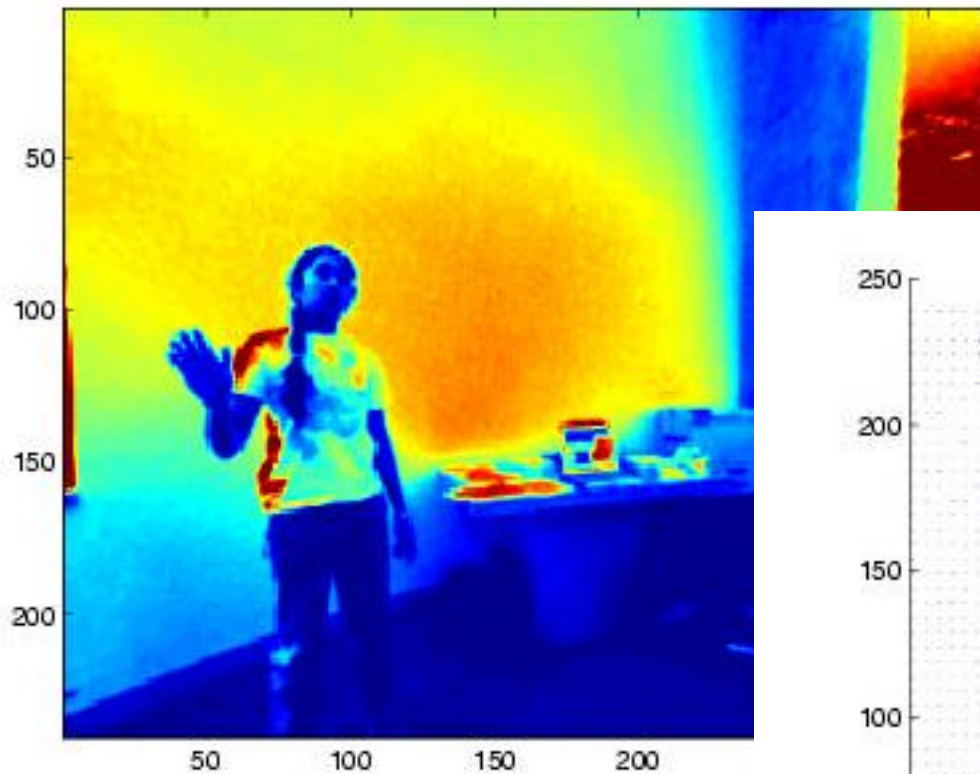


# Optical Flow

- ✍ Look at changes between successive images
  - ✍ identify moving objects
  - ✍ identify robot motion (flow will radiate out from direction of motion)
- ✍ For each point on image, set total derivative of brightness change to zero:
  - ✍  $0 = u * E_x + v * E_y + E_t$



# Optical flow





# Optical Flow

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- ✍ Computationally expensive and requires very fast frame rates... or very slow robots
- ✍ Idea from optical flow: looking at change between frames can help segment an image (only edges will move).





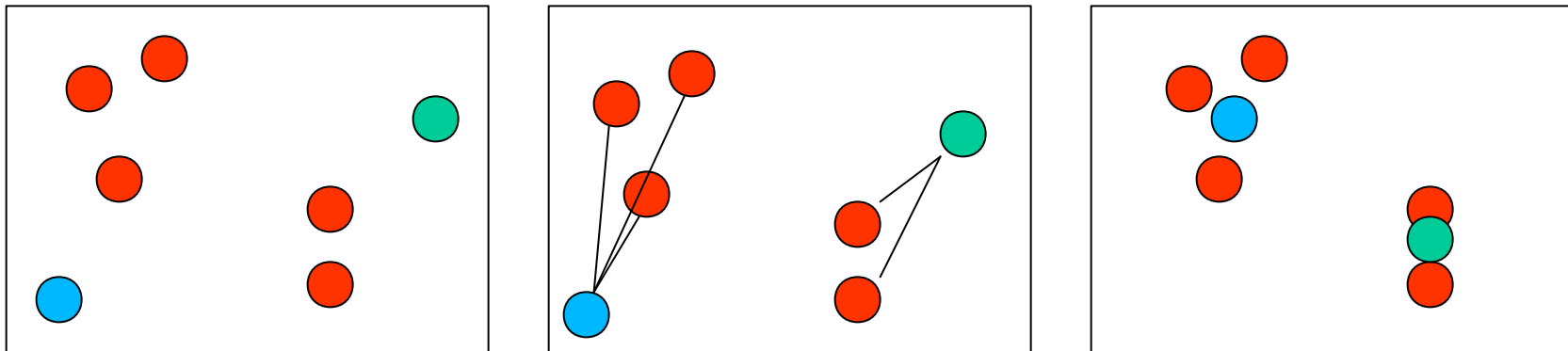
# EM Algorithm

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- ✍ Given an image with  $k$  objects
- ✍ How can we find their locations?

# EM Algorithm

- ✍ Assume there are  $k$  red objects
- ✍ Randomly choose object locations  $x_k, y_k$
- ✍ Loop:
  - ✍ Assign each pixel to nearest  $x_k, y_k$
  - ✍ Recenter  $x_k, y_k$  at center of all pixels associated with it





# EM Algorithm




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- ✍ Key question: what is  $k$ ?
  - ✍ Need to know how many objects
- ✍ Convergence criteria for random values?
  - ✍ Pick good guesses for centers







# Performance Note

## Faster access:

-  bufferedImage =  
ImageUtil.convertImage(bufferedImage,  
BufferedImage.INT\_RGB);
-  DataBufferInt intBuffer = (DataBufferInt)  
bufferedImage.getRaster().getDataBuffer();
-  int[] b = dataBufferInt.getData();

## Need to keep track of where pixels are:

-  offset = (y\*width + x)
-  (b[offset] >> 16) & 0xFF = red or hue
-  (b[offset] >> 8) & 0xFF = green or saturation
-  b[offset] & 0xFF = blue or value



# Reminders

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- ✍ No lecture tomorrow
- ✍ Design Review Wednesday
- ✍ Check Point Two: Friday
  
- ✍ If you haven't completed check point one, you finish it today!