

FOR A TWO-LEVEL SYSTEM:

$$\text{Hamiltonian: } \hat{H} = \begin{bmatrix} H_1 & V_{12} \\ V_{21} & H_2 \end{bmatrix}$$

Eigenvalues:

$$E_- = \frac{H_1 + H_2}{2} - \frac{1}{2} \sqrt{(H_2 - H_1)^2 + 4|V_{12}|^2}$$
$$E_+ = \frac{H_1 + H_2}{2} + \frac{1}{2} \sqrt{(H_2 - H_1)^2 + 4|V_{12}|^2}$$

Eigenfunctions:

$$\psi_-(x, t) = [\cos \theta \phi_1(x) + \sin \theta \phi_2(x)] e^{-iE_- t / \hbar}$$
$$\psi_+(x, t) = [-\sin \theta \phi_1(x) + \cos \theta \phi_2(x)] e^{-iE_+ t / \hbar}$$

where $\phi_1(x)$, $\phi_2(x)$ are the wavefunctions of the unperturbed system and

$$\cos(\theta) = \frac{1}{\sqrt{1 + |V_{12}|^2 / (E_- - H_2)^2}}, \quad \sin(\theta) = \frac{V_{12} / (E_- - H_2)}{\sqrt{1 + |V_{12}|^2 / (E_- - H_2)^2}}$$

If you start your perturbed system in $\phi_1(x)$ the probability as a function of time of being in $\phi_2(x)$ is given by Rabi's Formula:

$$p_2(t) = \sin^2(2\theta) \sin^2 \frac{(E_+ - E_-)t}{2\hbar} = \frac{4|V_{12}|^2}{(H_2 - H_1)^2 + 4|V_{12}|^2} \sin^2 \frac{(E_+ - E_-)t}{2\hbar}$$