MASSACHUSETTS INSTITUTE OF TECHNOLOGY

DEPARTMENT OF PHYSICS

8.01X FALL 2001

Practice Exam 3 Solutions

Med. Energy is conserved some T is always perpendicular to the displacement 1 m(v,2-v2) + mg(al) = 3 solvens for v= v= 2g (al) $-v_{f} = \left((7.0 \text{ m/s})^{2} - (2)(7.8 \text{m})(2)(.5 \text{m}) \right)^{1/2} = 5.4 \frac{\text{m}}{\text{s}}$ b) $T = m v_1^2 - m g = m(v_0^2 - 2g(2l)) - m g$ $T = m v_0^2 - 5 m g = (1/kg)(7.0m)^2 - (5)(.1kg)(9.5m)$ (.5m)Troblem 3:

the pen should have zero

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so on served 0+ 1k(x2-x2) - 6m, m2 (1-1) + 0 $-\frac{1}{2}KX_{0}^{2} + 6\frac{m_{1}m_{2}}{R_{p}} = 0 \implies X_{0}^{2} = \frac{26m_{1}m_{2}}{R_{0}k}$

 $X_0 = \left(\frac{(2)(6.67 \times (0^{-11} N - m^2)(.01 \text{ kg})(2.6 \times (0^{15} \text{ kg}))}{\frac{1}{2}}\right)^{1/2} = .042 \text{ m} = 4.2 \text{ cm}$ $(5.0 \times 10^3 \text{ m}) (400 \text{ N/m})$

$$F_{grav} \mid \Gamma_{s}$$

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$$G_{rs} = G_{rs}$$

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$$\frac{Frad}{G m_s m_p} = m_s r \left(\frac{2T}{T}\right)^2$$

$$Solve for$$

$$I_{S} = \left(\frac{(6.67 \times 10^{-11} N - m^{2})(2.6 \times 10^{15} kg)(2)(3.6 \times 10^{3} sc)^{2}}{4 \pi z} \right)^{1/3}$$

$$V_s = \frac{2\pi r_s}{T^2} = \frac{(2\pi)(6.1\times10^3 \text{m})}{(7.2\times10^3 \text{sec})} = 5.3 \text{ m/s}$$

d) At the redius is, the conservation of mechanical energy can be used to columbte the velocity of the pen

So eg (1) be comes
$$I m_z v^2 - G m_z m_z = 0$$

 $v' = \left(\frac{2Gm_1}{r_s}\right)^{V_2} = \left(\frac{2}{2}\right)\left(6.67x\left(c^{-11}N - m^2\right)\left(2.6x\left(0^{15}kg\right)\right)^{1/2}$
 $v' = 7.54 m/s$

Y

Problem 4

$$v_0 = 0$$
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$$\frac{Problem 5}{= (.25 \text{ kg})(4190 \text{ F})(28 \text{ K})} = 2.9 \times 10^4 \text{ J}$$

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momentum is conserved because there are no external forces. energy is not conserved due to the explosion.

$$\Delta P_{x} = 0$$
 $m_{z}v_{z} - m_{1}v_{1} = mv = 0$
 $v_{z} = m v + m_{1}v_{1} = (2.0 kg)(2.0 m) + (0.5 kg)(1.0 x 10 m)$
 $m_{z} = 6 m/c$
 $(1.5 kg)$

DKf = Wn.c 1 m2 2 - 1 m, v 2 - 1 m v2 - Wn.c. (1)(15kg)(6m)2+(1)(.5kg)(10m)2-1(2.0kg)(2.0m)2=48J 15 the uncross on kinetic energy due to 460 explosion. Problem 7:

+ i'

m, 0 7 2,0 2,0 m, 0 5, f = +4. m2 Gr.f=+450 $\Delta P_{x} = 0 \Rightarrow P_{x,o} = P_{x,c}$ m, v,, - m2 v2, = m2 v2, f cos 62, f (1) Doy = c => Py.o= Py.f 0 = m, v,f - m2 22,f sm 62,f (2) DK = 0 =7 Ko= Kf $\frac{1}{2}m_{1}v_{10}^{2} + \frac{1}{2}m_{2}v_{2,0}^{2} = \frac{1}{2}m_{1}v_{10}^{2} + \frac{1}{2}m_{2}v_{2,p}^{2}$ (3) Additionally we are told that Vif = Vio eglz) can be rewritten using this fact as m2 22, 5 5 5 5 2, f = m, Vic eg (1) mz vz,f (05 6z,f = m, v,o-mz vz,o 50 dividing those equations yulds tan Bz,f = m, v,o /2
m, v,o m2 v2,0

Problem 8: m - Jy Jy = arbitrary strotch from aquilibrium positon is already a The regulation position sino at equilibrium slightly stratiled position $m_i g - k y_{eg} = 0$ => $y_{eg} = \frac{m_g}{k}$ Then when the system is stretched an additional distance y $\frac{F_y = m_1 \ell_y}{m_1 - k(y - y_{21}) = m_1 \frac{d^2y}{dt^2}} \quad \text{here } y = 15$ an arbitrary stretch from ag. pos we get simple harmonic motion about yes positem $y = A \cos \int_{m_1}^{k} t + B \sin \int_{m_1}^{k} t$ $A = y_0$, $B = \frac{v_0}{\sqrt{y_{m_1}}} = 0$ released from rest V = dy = - \[\frac{k}{m} A sun \[\frac{k}{m} \tau + \sqrt{\frac{k}{m}} B cos \[\frac{k}{m} \tau \tau \] period T: [T = 211 = 7 TT = 211 [m.

we can find the velouty using $y = y_0 \cos \sqrt{\frac{k}{m}} t$, $v_y = -\sqrt{\frac{k}{m}} y_0 \sin \sqrt{\frac{k}{m}} t$ moting that when $\sqrt{\frac{k}{m}} t = \frac{\pi}{2} (\cos(\sqrt{\frac{k}{m}} t) = 0)$ so y = 0, mass is back at $\log p_0 \cos \frac{\pi}{2}$.

Also, $\sin(\sqrt{\frac{\pi}{2}}) = 1$ so $v_y = -\sqrt{\frac{k}{m}} y_0$ at $\log p_0 \cos \frac{\pi}{2} = \frac{\pi}{2} \sqrt{\frac{m}{k}} \sin \frac{\pi}{2}$ since a new mass $m = \pi m$

c) since a new mass $m_2 = zm_1$ $m + otal = 3m_1$ and $T = 2\pi \sqrt{\frac{3m_1}{K}}$

d) since the collision occurred when
the mass was completely compressed,
the velocity was zero, hence for
the collision DK = 0, no energy
was lost. Therefore, the new system
of mass 3 m, will satisfy
a new equilibrium condition
3 m, g = Kyeq! = 7 yeq! = 3 m, g/k
and the esullations are about these position,

 $\int_{\mathbb{R}^{3}} y = 0$ $\int_{\mathbb{R}^{3}} y = \frac{3m_{1}g}{k}$ $\int_{\mathbb{R}^{3}} y = \frac{3m_{1}g}{k}$

So the new equilibrium position is lowered by $2m_i g$

When the rubber bands were fully compressed by yo, the collision occured. The

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