Quiz #4 preparations

- Quiz 4: Wed, 5/4, 10AM, 26-100
 - 1 sheet with formulae etc
 - No books, calculators
- Evening review: Tue, 5/3, 7PM, 26-100
- Tutoring:
 - Angel Solis, Mon + Tue, 5/2, 5-7PM, Room 4-3XX

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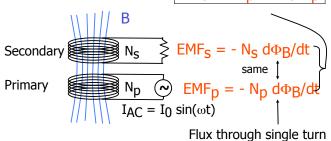
Review for Quiz #4

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Transformer Action

• Transformer action $EMF_S / EMF_D = N_S/N_D$



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Transformer Action

- Transformer action $| EMF_S / EMF_D = N_S/N_D$
- Transformers allow change of amplitude for AC voltage
 - ratio of secondary to primary windings
- primary and secondary

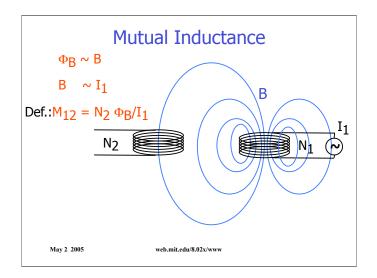
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What you need to know

- Transformers
 - Basic principle
 - Transformer in HVPS
 - Relationship between I,V,P on primary/ secondary side
 - Demos
 - Jacobs Ladder
 - Melting nail

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Mutal Inductance

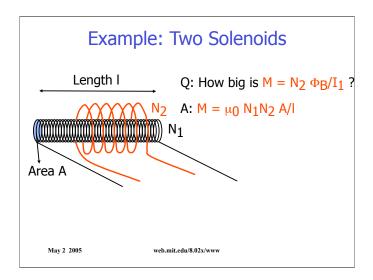
- Coupling is symmetric: M₁₂ = M₂₁ = M
- M depends only on Geometry and Material
- Mutual inductance gives strength of coupling between two coils (conductors):

$$EMF_2 = - N_2 d\Phi_B/dt = - M dI_1/dt$$

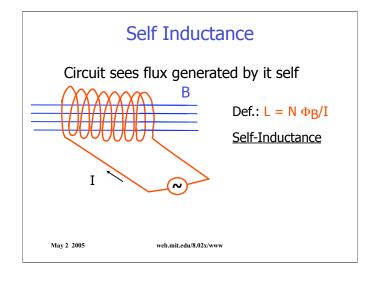
- M relates EMF2 and I1 (or EMF1 and I2)
- Units: [M] = V/(A/s) = V s /A = H ('Henry')

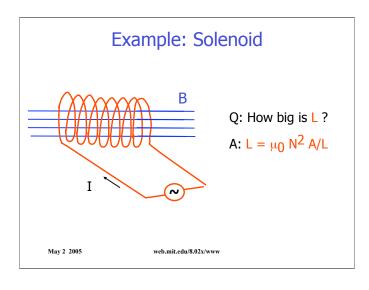
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Padio Radio Speaker Signal transmitted by varying B-Field Coupling depends on Geometry (angle, distance) May 2 2005 web.mit.edu/8.02x/www





Self Inductance

- L is also measured in [H]
- L connects induced EMF and variation in current:

$$EMF = - L dI/dt$$

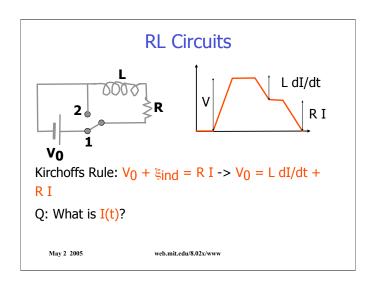
- Remember Lenz' Rule:
 - Induced EMF will 'act against' change in current -> effective 'inertia'
- Delay between current and voltage

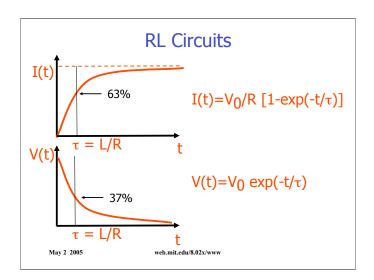
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What you need to know Inductance Mutual Inductance Definition Calculation for simple geometry Self Inductance Definition Calculation for simple geometry Definition Calculation for simple geometry Direction of induced EMF (depends only on dI/dt)

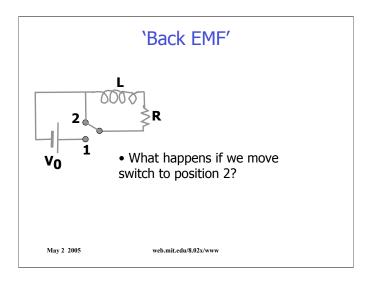
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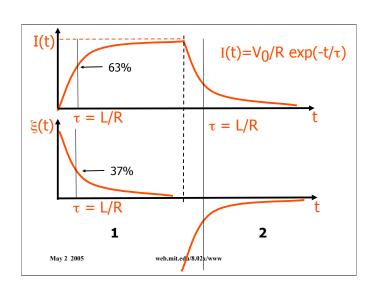
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RL Circuits Inductance leads to 'delay' in reaction of current to change of voltage V₀ All practical circuits have some L and R change in I never instantaneous





RL circuit

- L counteracts change in current both ways
 - Resists increase in I when connecting voltage
 - Resists decrease in I when disconnecting voltage source
 - 'Back EMF'
- That's what causes spark when switching off e.g. appliance, light

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Energy Storage in Inductor

- Energy in Inductor
 - Start with Power $P = V*I = L \frac{dI}{dt} I = \frac{dU}{dt}$

$$\rightarrow$$
 dU = L dI I

$$-> U = 1/2 L I^2$$

- Where is the Energy stored?
 - Example: Solenoid (but true in general)

U/Volume =
$$1/2 B^2/\mu_0$$

What you need to know

- Inductors
 - I(t) in DC RL circuits
 - Energy storage in inductors
 - Practical use

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RLC circuits

- Combine everything we know...
- Resonance Phenomena in RLC circuits
 - Resonance Phenomena known from mechanics (and engineering)
 - Great practical importance

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Summary of Circuit Components

$$V V(t) = V_0 \cos(\omega t)$$

$$\neg \lor \lor$$

$$\neg \lor \lor \land R \qquad V_R = -IR$$

$$V_L = -L dI/dt$$

$$-\parallel$$

$$C \qquad V_C = -Q/C = -1/C \int Idt$$

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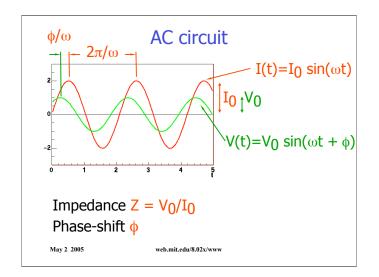
R,L,C in AC circuit

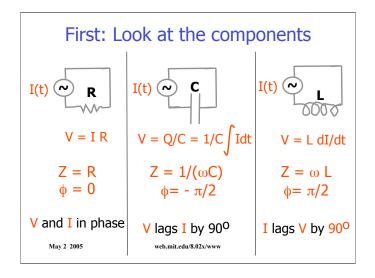
- AC circuit
 - $I(t) = I_0 \sin(\omega t)$
 - $V(t) = V_0 \sin(\omega t + \phi)$

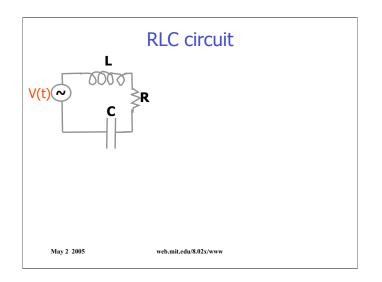
same $\omega!$

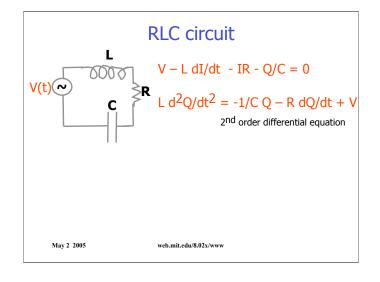
- Relationship between V and I can be characterized by two quantities
 - Impedance $Z = V_0/I_0$
 - Phase-shift φ

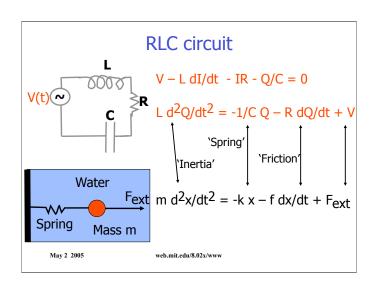
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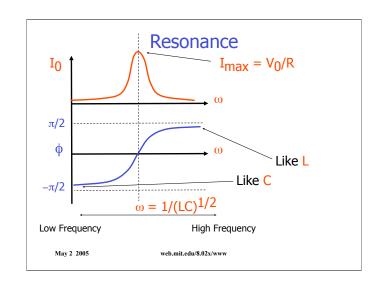












RLC circuit

 $V_0 \sin(\omega t) = I_0\{[\omega L - 1/(\omega C)] \cos(\omega t - \phi) + R \sin(\omega t - \phi)\}$

Solution (requires two tricks):

$$I_0 = V_0/([\omega L - 1/(\omega C)]^2 + R^2)^{1/2} = V_0/Z$$

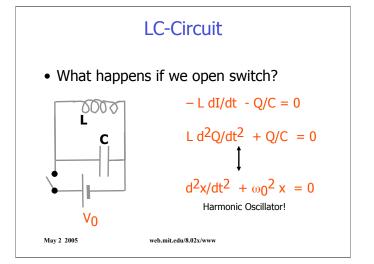
 $tan(\phi) = [\omega L - 1/(\omega C)]/R$

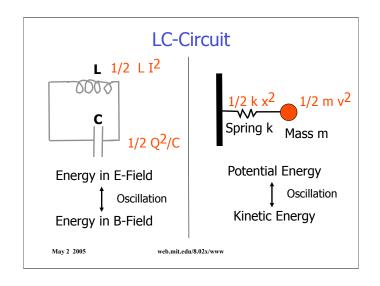
-> For $\omega L = 1/(\omega C)$, Z is minimal and $\phi = 0$ i.e. $\omega 0 = 1/(LC)^{1/2}$ Resonance Frequency

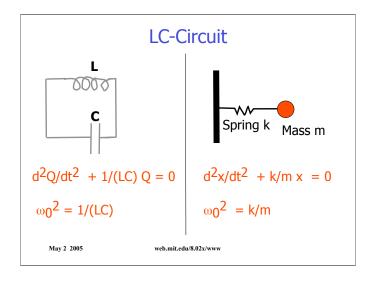
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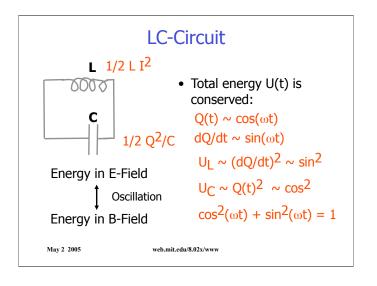
Resonance

- Practical importance
 - 'Tuning' a radio or TV means adjusting the resonance frequency of a circuit to match the frequency of the carrier signal









Electromagnetic Oscillations

• In an LC circuit, we see oscillations:

Energy in E-Field Energy in B-Field

- Q: Can we get oscillations without circuit?
- A: Yes!
 - Electromagnetic Waves

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What you need to know

- RLC Circuits
 - How to obtain diff. equ (but not solve it)
 - Definition of impedance, phase shift
 - Phaseshift for C,R,L AC circuits
 - Impedance, phase shift at resonance
 - Limiting behavior of RLC circuit with frequency
 - LC, RLC analogy with mechanical systems
 - LC oscillations: Frequency, role of E,B energy

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Displacement Current

• Ampere's Law broken – How can we fix it?

Displacement Current $I_D = \epsilon_0 d\Phi_E/dt$

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Displacement Current

• Extension of Ampere's Law:



Displacement Current $I_D = \epsilon_0 d\Phi_F/dt$

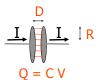
Changing field inside C also produces B-Field!

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Displacement Current

• Example calculation: B(r) for r > R



 $-> B(r) = R^2/(2rc^2) dV/dt$

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Maxwell's Equations

$$\begin{split} \oint_{A_{closed}} \vec{E} \cdot d\vec{A} &= \frac{Q_{encl}}{\epsilon_0} \\ \oint_{L_{closed}} \vec{E} \cdot d\vec{l} &= -\frac{d\Phi_B}{dt} \\ \oint_{A_{closed}} \vec{B} \cdot d\vec{A} &= 0 \\ \oint_{L_{closed}} \vec{B} \cdot d\vec{l} &= \mu_0 I_{encl} + \mu_0 \ \epsilon_0 \frac{d\Phi_E}{dt} \end{split}$$

- Symmetry between E and B
 - although there are no magnetic monopoles
- Basis for radio, TV, electric motors, generators, electric power transmission, electric circuits etc

Maxwell's Equations

$$\oint_{A_{closed}} \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0}$$

$$\oint_{L_{closed}} \vec{E} \cdot d\vec{l} = -\frac{d\Phi_B}{dt}$$

$$\oint_{A_{closed}} \vec{B} \cdot d\vec{A} = 0$$

$$\oint_{L_{closed}} \vec{B} \cdot d\vec{l} = \mu_0 I_{encl} + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$$

- M.E.'s **predict** electromagnetic waves, moving with speed of light
- Major triumph of science

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What you need to know

- Displacement current
 - Definition
 - Calculation for simple geometry
 - It's not a current
- Maxwells equations
 - Meaning in words

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Reminder on waves

- Types of waves
 - Transverse
 - Longitudinal
 - compression/decompression

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Reminder on waves

- For a travelling wave (sound, water)Q: What is actually moving?
- -> **Energy!**
- Speed of propagation: $v = \lambda f$
- Wave equation:

$$\frac{\partial^2 D(x,t)}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 D(x,t)}{\partial t^2}$$

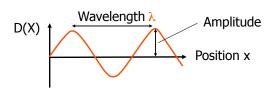
Couples variation in time and space

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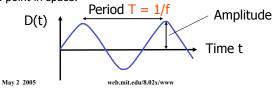
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Reminder on waves

At a moment in time:



At a point in space:



Wave Equation

• Wave equation:

$$\frac{\partial^2 D(x,t)}{\partial x^2} \;\; = \;\; \frac{1}{v^2} \frac{\partial^2 D(x,t)}{\partial t^2} \qquad \begin{array}{c} \text{Couples variation in} \\ \text{time and space} \end{array}$$

- Speed of propagation: $v = \lambda f$
- We can derive a wave equation from Maxwells equations (NOT IN QUIZ)

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Plane waves

• Example solution: Plane waves

$$E_y = E_0 \cos(kz - \omega t)$$

$$B_x = B_0 \cos(kz - \omega t)$$
 with $k = \frac{2\pi}{\lambda}, \omega = 2\pi f$ and $f\lambda = c$.

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E.M. Wave Summary

- E _ B and perpendicular to direction of propagation
- Transverse waves
- Speed of propagation $v = c = \lambda f$
- |E|/|B| = c
- E.M. waves travel without medium

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What you need to know

- Waves
 - What is a wave?
 - Types of waves
 - Relationships between wavelength, frequency wave speed
- E.M. waves
 - Properties
 - Connection to demos (speed, polarisation)
 - Relative direction of E,B,v

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AMP Experiment

- Understand general idea/purpose
- Understand voltage dividers
- Undertand need for negative feedback loop

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