### 8.02X Electricity and Magnetism

## Quiz \#1

## Tuesday, Feb 22 10:05-10:55am Room 26-100

The quiz has four questions. It is a closed book quiz. No calculators are allowed. A letter-size formula sheet can be used, but has to be signed and submitted together with the quiz.

LAST NAME

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## FIRST NAME

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RECITATION SECTION

|  |  |  | MARK YOURS |
| :--- | :--- | :---: | :---: |
| $\operatorname{Rec} 01$ | MW11 | B. Zeng |  |
| $\operatorname{Rec} 02$ | MW12 | B. Zeng |  |
| Rec03 | MW1 | D. Nagaj |  |
| $\operatorname{Rec} 04$ | TR11 | G. Benedek |  |
| Rec05 | TR1 | G. Benedek |  |
| $\operatorname{Rec} 06$ | TR2 | G. Benedek |  |
| $\operatorname{Rec} 07$ | TR3 | Daniel Nagaj |  |


| Problem \#1 |  |
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| Problem \#2 |  |
| Problem \#3 |  |
| Problem \#4 |  |
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| TOTAL |  |

## Problem 1 (25 points)

Consider the configuration of point charges shown below, with two negative charges $-Q_{0}$ and a positive charge $+Q_{0}$ forming a equilateral triangle (all sides have length $d$ ) in the $x-y$ plane.
(a) What is the direction and magnitude of the force on the positive charge $+Q_{0}$ in terms of the given quantities?
(b) What is the direction and magnitude of the electric field at point $x_{0}$ halfway in between the two negative charges?
(c) Now, assume that the two negative charges are fixed in space and that $+Q_{0}$ is freely movable. Describe the motion $+Q_{0}$ would undergo if released from rest from the original position shown below ( $2-3$ sentences)


## Problem 2 (25 points)

In lecture, you saw that an electrically charged plexiglass rod could be used to attract electrically neutral objects like a balloon made out of conducting foil.
(a) In a few sentences, explain the origin of the force between a charged object like the rod and an electrically neutral conducting object.
(b) Attraction can also be seen between a charged object and electrically neutral insulators. For example, the rod can be used to pick up pieces of confetti. How does this differ from the process described in (a)?

## Problem 3 (25 points)

Shown below is the cross-section of a conducting sphere of radius $R / 2$, surrounded by a very thin conducting spherical shell of radius $R$. The inner sphere carries a charge $+Q_{0}$ and the outer shell carries a charge $-Q_{0}$.
(a) On the figure, indicate the distribution of charge on the inner sphere.
(b) Using Gauss's Law, find the strength of the electric field $E(r)$ as a function of $r$ from $r=0$ to $r>R$, where $r$ is the distance from the center of the sphere. Results without work will not receive credit.
(c) On the figure, show your solution to (b) using field lines


## Problem 4 (25 points)

Shown below is the cross-section of two large parallel plates carrying charges $+Q$ (top) and $-Q$ (bottom). Each plate has area A. Vertically between the plates, a small charged particle with charge $q$ and mass $m$ is suspended at $y=d / 2$, i.e. the force of gravity $F_{G}=-m^{*} g$ and the electrostatic force on the particle cancel.
(a) What is the sign of the small particles charge $q$ ?
(b) Determine $q$ in terms of the other quantities given. Neglect fringe effects for the electric field created by the two plates.
(c) Sketch the electric potential energy $U_{E}$ of the charged particle as a function of $y$ from $y=0$ to $y=d$, assuming $U_{E}=$ 0 at $\mathrm{y}=0$.
(d) Sketch the total potential energy $U_{T}$ of the particle as a function of $y$ from $y=0$ to $y=d$.
(e) Sketch the electric potential V between the plates (ignore the charge $q$ ) from $y=0$ to $y=d$.


