

The Franck-Hertz Experiment and the Ramsauer-Townsend Effect: Elastic and Inelastic Scattering of Electrons by Atoms

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These experiments measure two phenomena encountered in collisions between electrons and atoms: quantized excitation due to inelastic scattering, and ionization. The experiments also provide an opportunity to explore the thermionic emission of electrons and space charge limited current in a vacuum tube.

I. PREPARATORY QUESTIONS

Please visit the Franck-Hertz chapter on the 8.13x website at mitx.mit.edu to review the background material for this experiment. Answer all questions found in the chapter. Work out the solutions in your laboratory notebook; submit your answers on the web site.

II. INTRODUCTION

Franck and Hertz described the first observation of quantized excitation in 1914, one year after Bohr published his theory of the hydrogen atom with its concept of quantized energy states. They discovered that electrons moving through mercury vapor with an energy greater than or equal to a critical value near 4.9 eV can excite the 2536 Å line of the mercury spectrum. Electrons with less than the critical energy bounce elastically when they collide with mercury atoms and fail to excite any electromagnetic emission. The experiment provided crucial evidence in favor of the Bohr theory.

A version of the Franck-Hertz experiment, employing a mercury-filled vacuum tube with four electrodes made by the Leybold Company, is described in References [1, 2] to which the reader is referred for a discussion of the physical principles and the measurement objectives of the Franck-Hertz experiment.

Experiments on the related Ramsauer-Townsend effect are described in Section VII.

III. APPARATUS

The present Junior Lab version of the experiment uses a different version of the equipment which consists of a mercury-filled triode and an oven with glass windows through which one can view the action. A power supply and control circuit built in the Junior Lab shop provides adjustable filament voltage for heating the cathode, adjustable accelerating grid voltage, and an adjustable retarding voltage. The same triode tube and power supply are used in the measurement of the ionization potential.

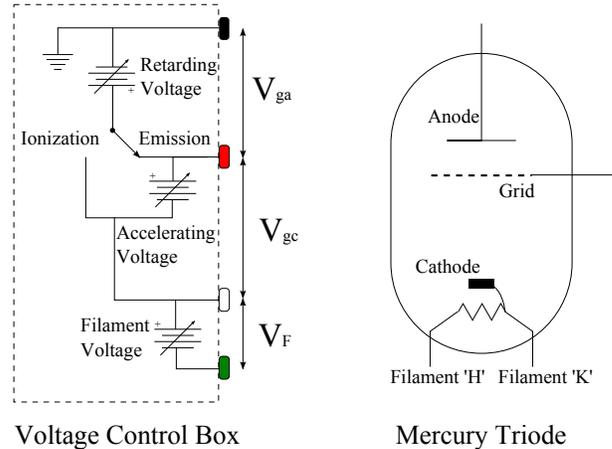


FIG. 1. Schematic illustrations of the mercury-filled triode and the voltage control box.

III.1. Mercury Filled Triode

The experiments on the excitation and ionization of mercury atoms are carried out with a mercury-filled triode which is a sealed glass envelope containing three electrodes and a drop of mercury.¹ The experiments will be performed with the three configurations of the tube and associated circuits illustrated in Figure 1 and, in more detail, Figures 3, 4, and 7. The three electrodes are:

- a cathode which emits electrons when raised to a temperature of several hundred degrees by application of a voltage V_F to a heater filament,
- a perforated grid which is set at a positive potential V_{gc} relative to the cathode so that electrons emitted by the cathode are drawn toward it,
- an anode (counter electrode plate) which is connected to an ultra-sensitive Keithley electrometer for the measurement of the anode current I_a .

¹ Mercury is an ideal element for a study of excitation phenomena because its vapor is monatomic and its vapor pressure can be readily controlled over the range useful for this experiment by adjusting the temperature in the range from room temperature to 200°C.

In the Junior Lab apparatus, the distance from the cathode to the perforated grid is 8mm while the distance between the grid and the anode is small (of order 1mm).

All of the measurements in these experiments can be made with total tube currents (*i.e.* cathode current = anode + grid current) of 1000 nA or less. To prolong the useful life of the tube care should be taken not to exceed 1000 nA.

III.2. Voltage Control Box

The voltage control box, built by Junior Lab staff, is used to supply the desired voltages to the mercury-filled triode. The control box functions as three variable voltage supplies, shown in Figure 1:

- the filament voltage V_F , which controls the temperature of the cathode
- the accelerating voltage V_{gc} , between the grid and the cathode
- the retarding voltage V_{ga} , between the grid and the anode.

The values for the voltage supplies can be measured using the “Isolated D.C. Voltmeter” outputs. These outputs are designed for use with a voltmeter that does not have any connection to the wall or ground, *i.e.* a multimeter. See Section III.4 for how to connect any of the circuit outputs to an oscilloscope.

It is wise to start each session by disassembling whatever wired-up circuit the previous users may have left. The only way to know for sure how a circuit is connected is to wire it yourself.

The control box has four circuit outputs which are color coded:

- Black is the common ground. It should be connected to the banana jack with the ground symbol near the anode connection on the oven chassis. This will establish a common ground.
- Red is connected to different points for different measurements during the experiment.
- White goes to the ‘K’ side of the filament, which determines the potential at the cathode. In our boxes, this is the banana jack on the right side.
- Green goes to the ‘H’ side of the filament, which determines the electrical power going through the filament (which has a fairly low resistance).

III.3. Electrometer

An ultra-sensitive Keithley Model 6485 picometer is used to measure the current from the anode to the laboratory ground. Similar to the Keithley 614 that is used in

Photoelectric Effect, it is essential that the input cable be kept stationary during measurements. Zero check should also be engaged before connecting and disconnecting cables, and for optimal accuracy it is recommended you zero correct the picometer before use. All of this can be found in the Keithley 6485 instruction manual. To zero correct

1. Enable zero check (ZC message displayed).
2. Select the range that will be used for measurement.
3. Press ZCOR to enable zero correct (ZZ message displayed).
4. Press ZCHK to disable zero check.
5. Readings can now be taken from the display. The CZ message indicates that the reading is zero corrected.

III.4. Oscilloscope Setup

In this experiment you may wish to use an oscilloscope to measure a voltage difference where neither of the measurement points are at the ground potential (most notably, the accelerating voltage). This *cannot* be done using a banana-to-BNC connector from the voltage control box isolated voltmeter output, because the oscilloscope will make a connection between the negative output and ground. As neither of the outputs are supposed to be at the ground potential, this will have adverse effects on the circuit.

Instead, a floating voltage measurement may be set up using two oscilloscope probes:

1. Check that the oscilloscope probes are 10× probes or that the probes are set to 10×. This is needed to increase the impedance of the probe-oscilloscope-ground connection and prevent the measurement from affecting the control box outputs.
2. On the oscilloscope, go to the Channel 1 menu and change the probe setting to 10× or 10:1. Do the same for Channel 2. This tells the oscilloscope you are using 10× probes.
3. Connect the probes to the voltage difference on the control box as shown in Figure 2. The probes can be connected to the actual circuit outputs or the isolated voltmeter outputs.
4. Use the math function built into the oscilloscope to subtract channel 1 from channel 2.

The math function displayed is the voltage difference. When saving data from the oscilloscope, the math function will not be saved. Make sure both channel 1 and 2 are saved so the math function can be reconstructed during analysis.

III.5. Oven

Several sections of this experiment require the mercury filled triode be heated above room temperature to increase the mercury vapor pressure. A ceramic heating element is situated below the triode and is used to heat the apparatus. Plug the oven electrical cord into the variable AC source (variac) and the variac into the wall outlet. The variac can then be used to set the oven temperature. **WARNING:** The heater should never receive more the 75 volts AC.

III.6. Grounding

The electrometer and oscilloscope make connections between the negative input from the BNC cable and the ground of the electrical outlet. To prevent ground loops from affecting the experiment, **the voltage control box, electrometer, and oscilloscope must all share the same ground.** This is done by plugging all three boxes into the same wall circuit. The electrical outlets in lab are labeled with numbers indicating which circuit each outlet is on.

IV. THERMIONIC EMISSION OF ELECTRONS AND SPACE CHARGE LIMITED CURRENT

Consider first the situation in the tube connected as shown in Figure 3. At room temperature the vapor pressure of the mercury is so low that the mean free path of electrons emitted by the cathode is large compared to the dimensions of the tube (~ 8 mm). When the cathode is heated by the filament, it emits electrons in a process called thermionic emission. In thermionic emission, electrons near the top of the Fermi distribution in the metal penetrate the potential barrier at the surface and escape. The kinetic energies of the emitted electrons roughly follow a Maxwell-Boltzmann distribution with a mean energy E_0 near kT , where T is the cathode temperature.

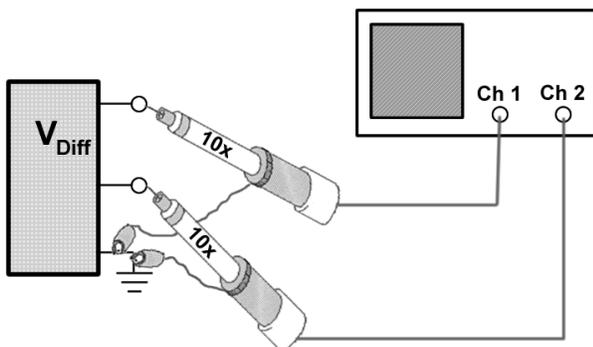


FIG. 2. The setup necessary to measure a floating voltage from the voltage control box with an oscilloscope.

In the steady state, with the grid at a positive potential relative to the cathode, the emitted electrons form a cloud of negative charge over the surface of the cathode. This cloud changes the local electric field, suppressing electron emission by forcing lower energy electrons back to the cathode. This condition is known as space charge limited current. The physics of thermionic emission and space charge limited current is discussed in [1] for a tube with ideal cylindrical geometry. Our tube, designed for other purposes, has a different geometry that does not lend itself to a “clean” experiment in thermionic emission. Nevertheless the qualitative characteristics of space-charge limited current can be observed with it.

The first part of the experiment is an exploration of the dependence of the total tube current on two quantities: (1) the filament voltage which controls the temperature of the cathode and thus the emitted current density and (2) the accelerating potential between the electron emitting cathode and the grid. You will find a filament voltage which will be used throughout the rest of the experiment. The measurements are made at room temperature ($20 - 25^\circ\text{C}$).

IV.1. Procedure for Exploring Thermionic Emission

1. Connect the tube as shown in Figure 3. Set the toggle switch to ‘emission’. Set the filament voltage V_F and the retarding voltage V_{ga} to their lowest values (~ 1.2 V and 0 V, respectively).
2. In order to measure the TOTAL tube current, the grid and anode currents should be summed at the electrometer input with coaxial cables and a BNC ‘T’ connector. Use a two-prong banana plug-to-BNC adapter at the grid terminal on the triode tube, taking care as to which side of the banana plug adapter is connected to the grid’s banana jack.
3. Set the accelerating voltage V_{gc} to its highest voltage, about 60V. The retarding voltage control should still be at $V_{ga} = 0$. Increase V_F in small steps until the total current is between 100 and 1000 nA. Tabulate and plot the total current (grid + anode) I_{ag} versus V_F as you proceed.
4. Set V_F at a value for which I_{ag} is in the range 100 – 1000 nA when $V_{gc} \approx 60$ V. Allow several minutes for the current to stabilize to ensure the current will remain in the desired range. Do not allow the current to remain above 1000nA, as that will shorten the life of the apparatus.
5. Now, tabulate and plot I_{ag} as a function of V_{gc} , shifting scales on the electrometer as needed. You may find that the current drifts substantially at any given setting of V_F and V_{gc} . Don’t panic. **The purpose of this section is to obtain a rough idea of how the cathode current, *i.e.* the**

total tube current, is affected by the cathode temperature and the accelerating voltage. Don't spend a lot of time trying to perfect these particular data. Since the tube characteristics change significantly with usage, you should start each session with a similar rough check of I_{ag} versus V_F with V_{gc} set to ~ 60 V and the oven at room temperature.

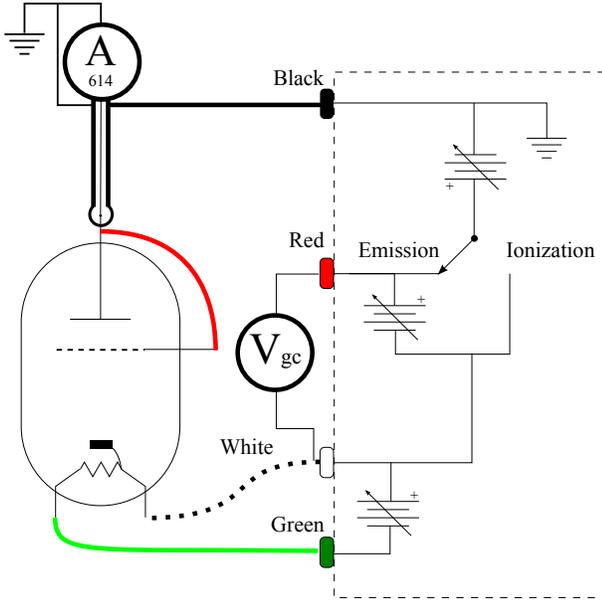


FIG. 3. Schematic diagram of the tube and circuit for measurements of space charge limited current from thermionic emission. The voltmeter labeled V_{gc} is the 'Isolated D.C. Voltmeter' outputs connected to a floating (non-grounded) voltmeter.

V. IONIZATION POTENTIAL OF MERCURY

In this next experiment the tube is connected as shown in Figure 4 so that the anode is maintained at a negative potential of a couple of volts with respect to the cathode. In this condition it is energetically impossible for any electrons to reach the anode. When the grid potential is made positive with respect to the cathode, electrons are accelerated to the grid. Some pass through the grid into the space between the grid and anode, but all are eventually pulled back and collected by the grid. However, if the electrons that enter the space between the grid and anode have sufficient energy to ionize the mercury atoms, then the resulting positive mercury ions are drawn to the anode and a *positive* current is registered by the electrometer. The experiment consists of measuring the anode current as a function of the grid-to-cathode potential difference. Analysis of the current-voltage relation yields a measure of the ionization potential.

The first task is to determine the optimum oven temperature for measurement of the ionization effect. If the

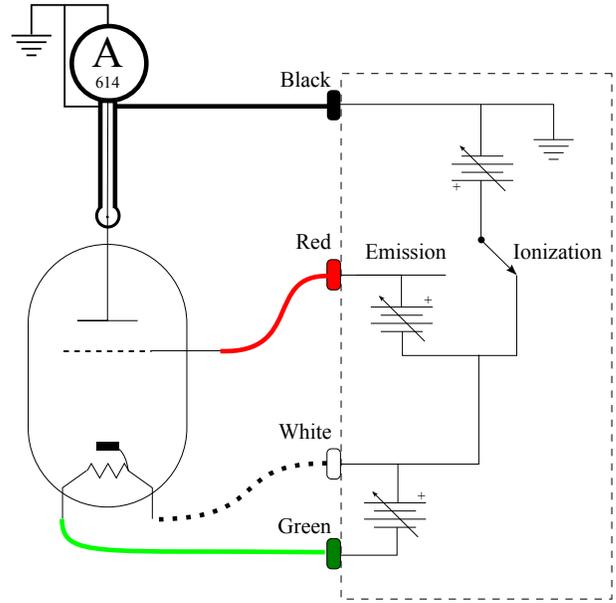


FIG. 4. Schematic diagram of the mercury-filled triode in the configuration for measurement of the ionization potential of mercury. After you complete the connections check all the potential differences in your setup with the floating Fluke voltmeter and verify that they are consistent with the instructions. Note that the mode-selecting toggle switch should be in the 'Ionization' position.

vapor pressure of the mercury is too low, then electrons entering the grid-to-anode region with sufficient energy to cause ionization will have a small probability of collision (long mean free path) and the ion current collected by the anode will be too small for accurate measurement. If the vapor pressure is too high, then electrons will suffer inelastic collisions in the space between the cathode and grid as soon as their energies slightly exceed the energy required to raise mercury atoms to their first excited (not ionized) state and will therefore never attain sufficient energies to cause ionization.

V.1. Ionization Potential: Procedure

1. Connect the tube as shown in Figure 4. Make sure that you switch the toggle switch to 'ionization'.
2. Set the filament voltage at the value which gives a total tube current in the range 100–1000 nA when $V_{gc} \approx 60$ V, as determined in Section IV.
3. Set the accelerating voltage V_{gc} to 25 V (measure with the floating voltmeter connected between cathode and grid), which is a few volts above the ionization potential. You should see a blue glow from the cathode. This is lower-energy photon emission of the ionizing mercury in the visible spectrum. If you do not see this glow, raise V_{gc} or V_F

path is short compared with all dimensions, including the wire diameter, the electron orbits jitter along the field lines. Regardless of their energy, they are mostly intercepted by the grid since most of the field lines end there.

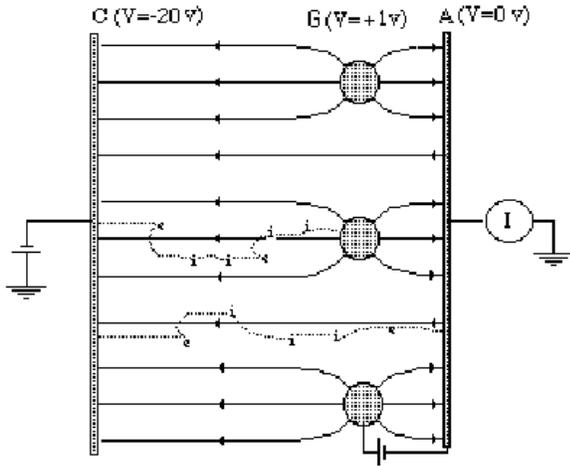


FIG. 6. Schematic illustration of the electric field lines in the measurement of the excitation potential. Two electron trajectories are illustrated. Elastic and inelastic scatterings are indicated by “e” and “i”, respectively. One electron is caught by the grid G. The other makes it to the anode A.

Note that the lowest excited state of mercury is the 6^3P_0 state, which is metastable: a dipole transition to the ground state is forbidden. Its lifetime is $\sim 10^5$ times that of ordinary allowed transitions. As the electrons accelerate toward the grid they acquire sufficient energies to excite a mercury atom in the ground state to the 6^3P_0 state. Because the excited atoms decay slowly, their number builds up to the point where most of the electron-mercury atom interactions become elastic collisions off of excited atoms. The 6^3P_1 state is not metastable and decays immediately by emission of a 2536 Å photon. Franck and Hertz detected these photons through a window in their tube. Having measured the threshold voltage V at which the photons appeared, they could derive a value for $h = Ve\lambda/c$. The agreement with the values obtained previously by Planck, Einstein, and Bohr from their theories of the blackbody spectrum, the photoelectric effect, and the hydrogen spectrum, respectively, was a striking and historic confirmation of the new quantum theory.

VI.1. Excitation Potential of Mercury: Procedure

1. For the excitation potential measurement connect the tube as shown in Figure 7. Check all the potentials with the floating voltmeter.
2. Set the oven temperature at so that the mean free path of the electrons is short compared to the cathode-grid distance.

3. Set the filament voltage to a value that would give a *total* tube saturation current (anode + grid) in the range 100–1000 nA *at room temperature*, as measured in Section IV.
4. Set the retarding voltage at a value between 0.1 and 2 volts. Electrons that pass through the grid with less than enough energy to overcome the retarding potential are turned back to be collected by the grid. Higher energy electrons reach the anode and are registered as a negative current by the Keithley electrometer.
5. By hand or by using the ramp function, sweep the accelerating voltage, V_{gc} , from 0 to 60 volts and note the occurrence of maxima and minima in the anode current I_a (probably best done on the picoampere scale). Measure and tabulate the values of V_{gc} at the maximum and minimum values of the current, and the corresponding maximum and minimum anode currents. In the measurement of the excitation potential, the accelerating voltage is between the cathode and grid. Neither of these electrodes is at ground potential. Therefore, if V_{gc} is measured on the oscilloscope, the measurement must be set up following Section III.4.

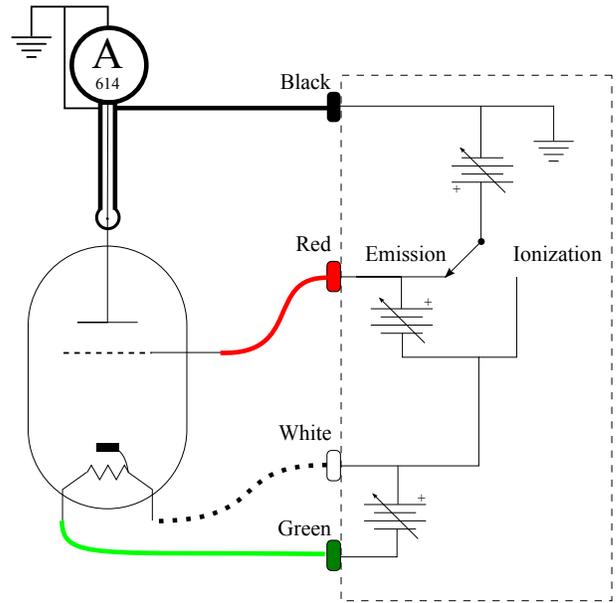


FIG. 7. Circuit arrangement for measurement of the critical excitation potential.

VI.2. Excitation Potential: Analysis

Derive from your data the value and error of the excitation potential. Referring to the plot of I_a vs. V_{gc} , at what point between each successive pair of minima do

you think the next set of excitation events begins? Derive an estimate of the value and error of the contact potential (see [1, 2] for a discussion of the physics of contact potential) between the cathode and grid. You will need to correct the measurement of the ionization potential in section V by this quantity.

VII. THE RAMSAUER-TOWNSEND EFFECT

“The Ramsauer-Townsend effect may be thought of as a diffraction of the electron around the rare-gas atom, in which the wave function inside the atom is distorted in just such a way that it fits on smoothly to an undistorted wave function outside” [3].

The result is a near extinction of the scattered $\ell = 0$ partial wave (s-wave) and a consequent suppression of the scattering cross section. The effect can be observed only when it occurs at an energy below that of the first excited state of the scattering atom. Otherwise it is masked by inelastic scattering. Noble gases provide especially suitable targets because they are monatomic, their outer electrons are in a closed shell, excitation of their lowest excited state requires a comparatively large amount of energy, and they do not attach electrons to form negative ions.

The Ramsauer-Townsend effect was discovered in 1921, before the invention of wave mechanics in 1926 and the discovery of the electron diffraction by Davisson and Germer in 1927. Its explanation in terms of the scattering of matter waves — first suggested by Bohr and worked out in detail by Mott and Massey[4] and others on the basis of the Schrödinger equation — was one of the early successes of the new wave mechanics.

The theoretical treatment of the elastic scattering of an electron by a noble gas atom requires the solution of the three dimensional Schrödinger equation for a free electron incident on a spherically symmetric attractive potential. This can be done by the method of partial waves as explained in various intermediate texts on quantum mechanics (*e.g.* [3, 5–7]).

The well-known model of a 1-dimensional scattering problem, solved in many elementary quantum mechanics texts, is often put forward as exhibiting the essential features of wave mechanical behavior that one observes in the Ramsauer-Townsend effect. The 1-D model bears a relation to the real 3-D scattering problem that is similar to the relation which the problem of the energy levels of a particle in a 1-D box bears to the 3-D problem of the hydrogen atom, *i.e.* suggestive, but fairly distant as far as numerical agreement is concerned. In the 1-D scattering problem, one finds the transmission coefficient has maxima at a series of discrete energies for both positive and negative potential wells, whereas in the 3-D case there is only one maximum, and that only for an attractive potential.

The present experiment is described in Reference [8]. A xenon-filled tube is commercially available in the form of a thyratron switch tube (2D21). The depression of the scattering cross section at the critical energy is indicated by the reduction in the intensity of an electron beam directed from the cathode to the anode.

VII.1. Ramsauer-Townsend: Apparatus

The apparatus and circuitry are illustrated schematically in Figure ?? . Electrons emitted from the heated cathode are accelerated through a small potential difference toward the “grid” which is actually a metal box inside of which there is no electric field. The electrons that enter the box “drift” through it, and those that emerge from the far end are collected by the anode and measured as a current by the Keithley electrometer. At high vacuum, when the xenon gas is condensed on the glass walls of the thyratron by cooling in liquid nitrogen, the fraction of atoms emitted by the cathode that reaches the anode depends only on the geometry of the electrodes. When the xenon is vaporized, the fraction reaching the anode is reduced by elastic scatterings which deflect electrons from the trajectories that would otherwise bring them to the anode. The amount of the reduction is a measure of the elastic scattering cross section of the xenon atoms. One obtains the required data by measuring the anode current as a function of the accelerating voltage both with and without the xenon vapor.

VII.2. Ramsauer-Townsend: Procedure

1. With all voltages set to their minimum values, connect the circuit as shown in Figure ??, using the Keithley electrometer to measure the anode current and an isolated multimeter to measure the accelerating voltage. Again, the Keithley electrometer should be zero checked (ZC) before attaching cables. The thyratron needs around five minutes to warm up before being put into liquid nitrogen.
2. Dip the tip of the thyratron in liquid nitrogen to freeze out the xenon. **To reduce the likelihood of cracking the tube by thermal shock, the filament voltage should always be zero as the tube is dipped into the liquid nitrogen.**
3. With an accelerating voltage of 5 V, increase the filament heater voltage until the anode current is 10 μA .
4. Leaving the filament voltage at the value just found, tabulate and plot the anode current (shifting to the nanoampere or picoampere scales where necessary) as a function of the accelerating voltage from 5 V down to zero both with and without the xenon vapor frozen out, taking special care in

the region between 0 and 2 V where the interesting phenomenon occurs. It is wise to make your two sets of measurements at the same sequence of voltage values so that you can easily calculate the ratio of currents with and without the xenon frozen out. *Compute and plot in your lab book the ratio against the accelerating voltage as you go along to monitor the trend of the data.*

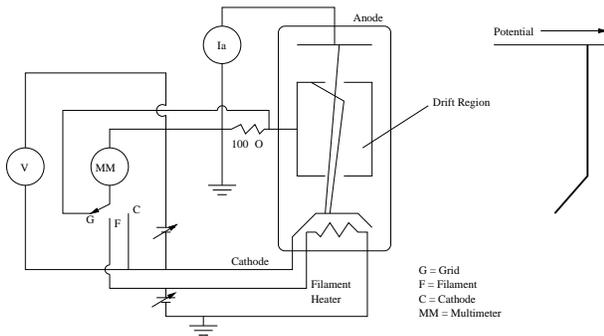


FIG. 8. Schematic diagram of the 2D21 thyratron and circuit used in the measurement of the xenon elastic scattering cross section using low energy electrons. The trajectories of two electrons are shown, one scattered by a Xenon atom and the other reaching the anode undeflected. Adjust the filament voltage so that the anode current measures $\approx 10 \mu\text{A}$ with an accelerating voltage of 5.0 V. The vapor pressure in the tube is approximately 0.05 torr at room temperature (≈ 0.001 torr at 77 K) and the length of the scattering volume is 0.7 cm.

The liquid nitrogen needed to freeze out the xenon is available in a 240 L dewar in the lab. **Handle it carefully and wear goggles!** Do not fill the Dewar flask to the brim. The tube need only be partially immersed to bring the xenon below its boiling point.

VII.3. Ramsauer-Townsend: Analysis

The discussion of the experiment's interpretation by Kukolich [8] may be a little obscure. The following remarks may help. Call $I_0(V)$ the measured current with the xenon frozen out when the accelerating potential is V , and $I(V)$ the measured current at the same accelerating voltage with the xenon gas free in the tube. If

every electron scattered by a xenon atom were effectively removed from the beam, then these two measurements would be related by the equation

$$I(V) = I_0(V)e^{[-n\sigma(V)l]}, \quad (1)$$

where n is the number of xenon atoms cm^{-3} , $\sigma(V)$ is the cross section of the xenon atoms for inelastic scattering the electrons of energy eV, and l is the path length from cathode to anode. The desired measure of the cross section would then be

$$\sigma(V) = \frac{1}{nl} \ln \left[\frac{I_0(V)}{I(V)} \right] \quad (2)$$

Actually, not every scattered electron is removed from the beam due to the poor geometry of the thyratron tube in this particular application. Therefore the value of the cross section derived from the simple analysis of the present experiment, assuming the quantity nl were accurately known, is somewhat less than the true value of the total inelastic scattering cross section.

Plot $\ln \left[\frac{I_0(V)}{I(V)} \right]$ against V . Discuss the sources and magnitudes of the errors and indicate your error estimates on the plot. Comment on the position of the minimum and its relation to the size of the xenon atom.

VIII. POSSIBLE THEORETICAL TOPICS FOR ORAL EXAM

- Richardson's law
- Child's law
- Distribution in energy of electrons emitted by a hot metal
- Propagation of electrons through Hg vapor
- Transmission of electrons through a rectangular potential well
- Partial-wave scattering theory of the Ramsauer-Townsend effect

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- [2] A. Melissinos, *Experiments in Modern Physics*, 2nd ed. (Academic Press Inc., 2003) pp. 10–19.
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