
initial velocity of a particle at position $\vec{r}$ is given by the Hubble relation l

## $\tau / \varepsilon^{q 9}=(7) \mathcal{Y}$

that the Robertson-Walker scale factor behaves as
Consider a flat universe which is filled with some peculiar form of matter, so

## - $Л T O \Lambda$ H GINIL TV

What is $V(R)$ ? Will this universe expand forever, or will it collapse?

## $(\mathcal{U}) ~ \Lambda+{ }_{z} \Psi \frac{\sigma}{I}=G$

e) Find an expression for a conserved quantity of the form $R, \rho$, and any relevant constants. scale factor $R(t)$. Use this expression to obtain an expression for $R$ in terms of
d) Express the mass density $\rho(t)$ in terms of the initial mass density $\rho_{i}$ and the
the lecture notes. As before, we define the scale factor $R(t) \equiv u\left(r_{i}, t\right)$.

show that $u\left(r_{i}, t\right)$ is in fact independent of $r_{i}$. This implies that the cylinder
$\frac{\cdot!}{\left(7^{6} \cdot \iota\right) \cdot l} \equiv\left(7^{6} \cdot l\right) n$
c) Defining


b) As in the lecture notes, we let $r\left(r_{i}, t\right)$ denote the trajectory of a particle that


$\stackrel{\iota}{r_{V}}-=\underline{\square}$
acceleration at any point is given by

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 әq II! series expansion to express $\theta$ as a function of $t$, and then $R$ as a function of $t$.
e) For very small values of $t$, it is possible to use the first nonzero term of a powerand $\theta$.

 b) Find the mass density $\rho$ as a function of $\alpha$ and $\theta$.

$\frac{i \varepsilon}{{ }_{\varepsilon} \theta}+\frac{i z}{z^{\theta}}+\frac{\mathrm{iL}}{\theta}+\mathrm{I}={ }_{\theta^{2}}$
$\frac{7}{\theta^{-\partial}-\theta^{\partial}}=\theta$ पuIs
which you should know, may also prove useful on parts (e) and ( f ):


pue
were given in Lecture Notes 5 as

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 (b) Find $\rho$, the mass density, as a function of $\alpha$ and $\theta$.

$$
\cosh \theta=\frac{e^{\theta}+e^{-\theta}}{2}
$$


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