
 the $z$-axis of the coordinate system:
 II! construct a model of a cylindrical universe, one which is expanding in the $x$ and $y$


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 What is $V(a)$ ? Will this universe expand forever, or will it collapse? Find an expression for a conserved quantity of the form

$$
E=\frac{1}{2} \dot{a}^{2}+V(a) .
$$

What is $V(a)$ ? Will this universe expand forever, or will $a, \rho$, and any relevant constants. scale factor $a(t)$. Use this expression to obtain an expression for $\ddot{a}$ in terms of d) Express the mass density $\rho(t)$ in terms of the initial mass density $\rho_{i}$ and the
 will undergo uniform expansion, just as the sphere did in the case discussed in show that $u\left(r_{i}, t\right)$ is in fact independent of $r_{i}$. This implies that the cylinder $\frac{?^{l} l}{\left(7^{6 ?} \cdot l\right) \cdot l} \equiv\left(7^{6!} \cdot\right) n$ (әл!̣ұел!мәр әш!̣ е sәұоиәр ұорләло

|  <br>  <br>  $\cdot \frac{l}{n^{\prime}} \frac{l}{n_{V}}-\underline{b}$ <br>  <br>  <br> Кq шәл!̣̊ s!̣ ұи!̣od Кие ұе шо!̣ұеләәәәэе <br>  |
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|  |  | - $l^{l} H=?$


 8.286 PROBLEM SET 3, FALL 2009

Kq (e) 7еч7 мочS explained below.


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Total points for Problem Set 3: 25.

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(c) Show that the total potential energy of the sphere can similarly be written as is the initial radius of the sphere. Evaluate the numerical constant $c_{K}$. where $c_{K}$ is a numerical constant, $M$ is the total mass of the sphere, and $R_{\text {max }, i}$

## 

## $\iota p_{z^{\prime}} \quad \nu \overline{ }=\Lambda p$

has a volume



















