Physics 8.286: The Early Universe Prof. Alan Guth

September 9, 2011

PROBLEM SET 1

DUE DATE: Thursday, September 15, 2011

READING ASSIGNMENT: The First Three Minutes, Chapters 1 and 2.

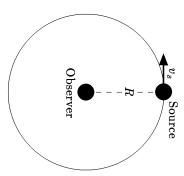
PROBLEM 1: NONRELATIVISTIC DOPPLER SHIFT, SOURCE AND OBSERVER IN MOTION (5 points)

direction with speed v_o relative to the air. Calculate the Doppler shift z. and the observer are moving. Suppose the source is moving with a speed v_s relative to the air, while the observer is receding from the source, moving in the opposite Consider the Doppler shift of sound waves, for a case in which both the source



PROBLEM 2: THE TRANSVERSE DOPPLER SHIFT (5 points)

source be v_s . that travels in a circular orbit of radius R about the observer. Let the speed of the Consider the Doppler shift observed by a stationary observer, from a source



(a) If the wave in question is sound, and both the source speed v_s and the wave shift z? speed u are very small compared to the speed of light c, what is the Doppler

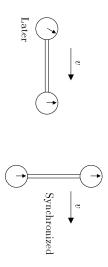
- (b) If the wave is light, traveling with speed c, and v_s is not necessarily small compared to c, what is the Doppler shift z? In answering this part of the question, you will want to keep in mind the following facts from special relativity:
- (1) TIME DILATION: Any clock which is moving at speed v relative to a given and given by reference frame will appear (to an observer using that reference frame) to run slower than normal by a factor denoted by the Greek letter γ (gamma),

$$\gamma \equiv \frac{1}{\sqrt{1-\beta^2}} \ , \qquad \beta \equiv v/c \ .$$

(2) LORENTZ-FITZGERALD CONTRACTION: Any rod which is moving length does not undergo a change in apparent length length by the same factor γ . A rod which is moving perpendicular to its at a speed v along its length relative to a given reference frame will appear (to an observer using that reference frame) to be shorter than its normal

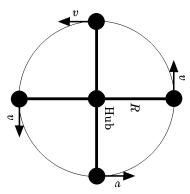


(3) RELATIVITY OF SIMULTANEITY: Suppose a rod which has rest length the clocks is not disturbed. the system moves perpendicular to its length, then the synchronization of is later than the leading clock by an amount $\beta \ell_0/c$. If, on the other hand along its length, then the trailing clock will appear to read a time which be started when they receive the pulses.) If the system moves at speed vpulse can be sent out from the center, and the clocks at both ends can in the rest frame of the system by using light pulses. (That is, a light ℓ_0 is equipped with a clock at each end. The clocks can be synchronized



PROBLEM 3: A HIGH-SPEED MERRY-GO-ROUND (5 points)

Now consider the Doppler shift as it would be observed in a high-speed "merry-go-round." Four evenly-spaced cars travel around a central hub at speed v, all at a distance R from a central hub. Each car is sending waves to all three of the other cars.



- (a) If the wave in question is sound, and both the source speed v and the wave speed u are very small compared to the speed of light c, with what Doppler shift z does a given car receive the sound from (i) the car in front of it; (ii) the car behind it; and (iii) the car opposite it?
- (b) In the relativistic situation, where the wave is light and the speed v may be comparable to c, what is the answer to the same three parts (i)-(iii) above?

Total points for Problem Set 1: 15.