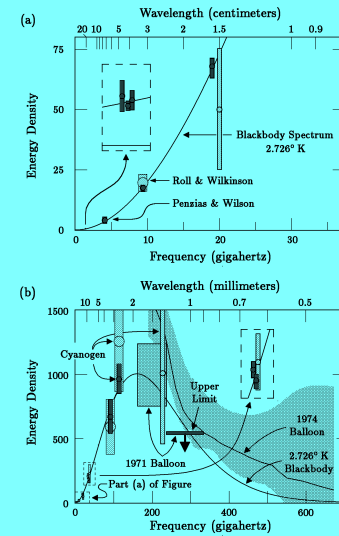


8.286 Lecture 19  
November 19, 2013

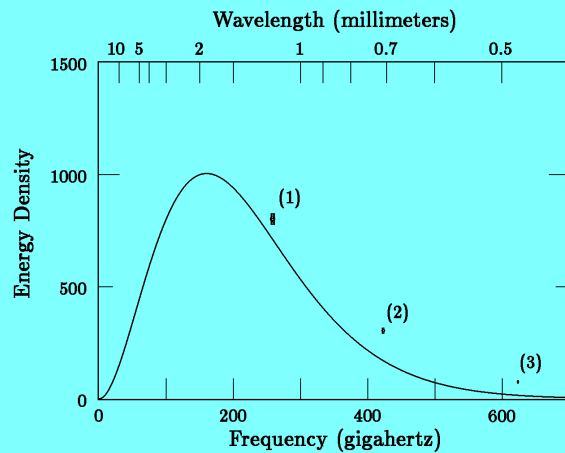
THE  
COSMOLOGICAL CONSTANT

Summary of Lecture 18



CMB Data in 1975

Summary of Lecture 18



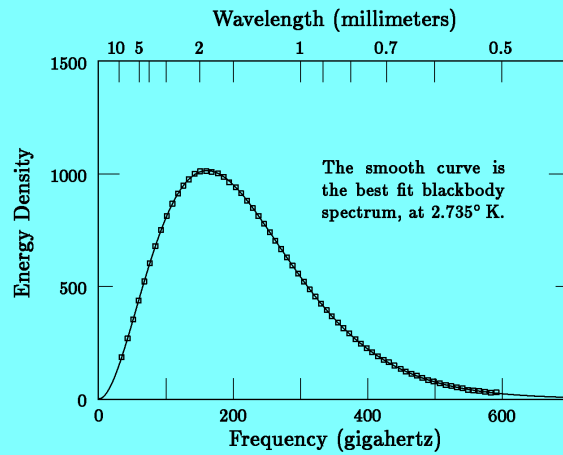
Data from Berkeley-Nagoya Rocket Flight, 1987

Summary of Lecture 18



Cover Page of Original Preprint of the COBE Measurement of the CMB Spectrum, 1990

Summary of Lecture 18



Original COBE Measurement of the CMB Spectrum, Jan 1990. Energy density is in units of electron volts per cubic meter per gigahertz.

Summary of Lecture 18:  
Gravitational Effect of Pressure

$$\frac{d^2a}{dt^2} = -\frac{4\pi}{3}G \left( \rho + \frac{3p}{c^2} \right) a .$$

Vacuum Energy and the Cosmological Constant:

$$u_{\text{vac}} = \rho_{\text{vac}}c^2 = \frac{\Lambda c^4}{8\pi G} .$$

$$\dot{\rho}_{\text{vac}} = 0 \implies p_{\text{vac}} = -\rho_{\text{vac}}c^2 = -\frac{\Lambda c^4}{8\pi G} .$$

Summary of Lecture 18

Defining  $\rho = \rho_n + \rho_{\text{vac}}$  and  $p = p_n + p_{\text{vac}}$ ,

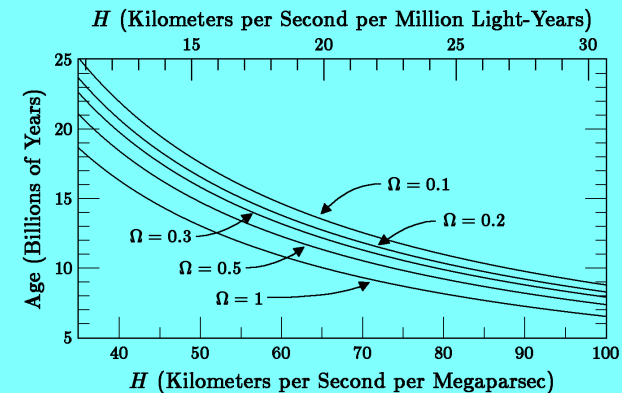
$$\frac{d^2a}{dt^2} = -\frac{4\pi}{3}G \left( \rho_n + \frac{3p_n}{c^2} - 2\rho_{\text{vac}} \right) a .$$

$$\left( \frac{\dot{a}}{a} \right)^2 = \frac{8\pi}{3}G(\rho_n + \rho_{\text{vac}}) - \frac{kc^2}{a^2} .$$

Dominance of vacuum energy at late time implies

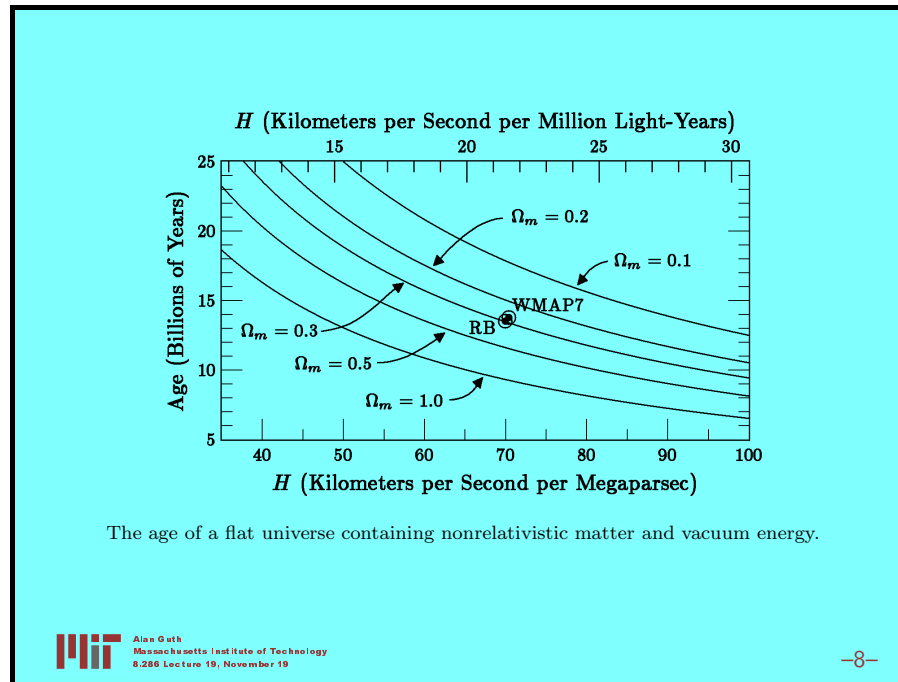
$$H \rightarrow H_{\text{vac}} = \sqrt{\frac{8\pi}{3}G\rho_{\text{vac}}} ,$$

$$a(t) \propto e^{H_{\text{vac}}t} .$$



The age of an open ( $\Omega < 1$ ), closed ( $\Omega > 1$ ), or flat ( $\Omega = 1$ ) universe containing only nonrelativistic matter.

Alan Guth, *The Cosmological Constant*, 8.286 Lecture 19, November 19, 2013, p. 3.



The age of a flat universe containing nonrelativistic matter and vacuum energy.