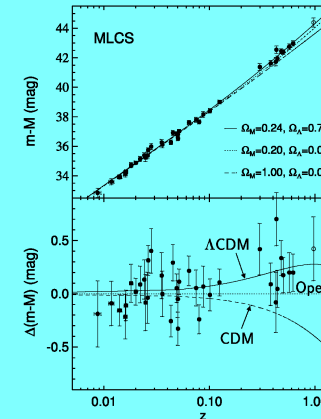


8.286 Lecture 21  
November 26, 2013

PROBLEMS OF THE  
(NON-INFLATIONARY)  
HOT BIG BANG MODEL

Summary of Lecture 20:  
Supernovae Ia as Standard Candles



Supernova Data of Hi-Z Supernova Search Team, 1998

-1-

Summary of Lecture 20

Evidence for the Accelerating Universe

- 1) Supernova Data: distant SN Ia are dimmer than expected by about 20–30%.
  - 2) Cosmic Microwave Background (CMB) anisotropies: gives  $\Omega_{\text{vac}}$  close to SN value. Also gives  $\Omega_{\text{tot}} = 1$  to 1/2% accuracy, which cannot be accounted for without dark energy.
  - 3) Inclusion of  $\Omega_{\text{vac}} \approx 0.70$  makes the age of the universe consistent with the age of the oldest stars.
- ★ With the 3 arguments together, the case for the accelerating universe and  $\Omega_{\text{dark energy}} \approx 0.70$  has persuaded almost everyone.
  - ★ The simplest explanation for dark energy is vacuum energy, but “quintessence” is also possible.

-2-

Summary of Lecture 20:  
Particle Physics of a Cosmological Constant

$$\star u_{\text{vac}} = \rho_{\text{vac}} c^2 = \frac{\Lambda c^4}{8\pi G}$$

- ★ Contributions to vacuum energy density:
  - 1) Quantum fluctuations of the photon and other bosonic fields: positive and divergent.
  - 2) Quantum fluctuations of the electron and other fermionic fields: negative and divergent.
  - 3) Fields with nonzero values in the vacuum, like the Higgs field.

-3-

Summary of Lecture 20

★ If infinities are cut off at the Planck scale (quantum gravity scale), then infinities become finite, but

**> 120 orders of magnitude too large!**

★ For lack of a better explanation, many cosmologists (including Steve Weinberg and yours truly) seriously discuss the possibility that the vacuum energy density is determined by “anthropic” selection effects: that is, maybe there are many types of vacuum, with different vacuum energy densities, with most  $\sim 120$  orders of magnitude larger than ours. Maybe we live in a very low energy density vacuum because it is conducive to life.

Summary of Lecture 20:  
**Einstein and Friedmann**

June 29, 1922: Alexander Friedmann’s paper received at *Zeitschrift für Physik*.

September 18, 1922: Einstein’s refutation received at *Zeitschrift für Physik*: claimed that Friedmann failed to notice that  $\dot{\rho} = 0$ .

May, 1923: Einstein met Friedmann’s friend, Yuri A. Krutkov, at retirement lecture by Lorentz in Leiden, and Krutkov convinced Einstein of his error.

May 31, 1923: Einstein’s retraction of his refutation is received at *Zeitschrift für Physik*.

The handwritten draft of Einstein’s retraction included the phrase “a physical significance can hardly be ascribed to them,” referring to Friedmann’s solutions, but Einstein crossed it out before submitting.

**The Standard Model of Particle Physics**

Three Generations of Matter (Fermions)			
	I	II	III
mass	2.4 MeV	1.27 GeV	171.2 GeV
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
name	u	c	t
	up	charm	top
	d	s	b
	down	strange	bottom
	$\nu_e$	$\nu_\mu$	$\nu_\tau$
	electron neutrino	muon neutrino	tau neutrino
	e	$\mu$	$\tau$
	electron	muon	tau
			W <sup>±</sup>
			W boson
			Z <sup>0</sup>
			Z boson

From the Wikimedia Commons. Source: PBS NOVA, Fermilab, Office of Science, United States Department of Energy, Particle Data Group.

**Gauge Theories**

$$\vec{E} = -\vec{\nabla}\phi - \frac{1}{c} \frac{\partial \vec{A}}{\partial t},$$

$$\vec{B} = \vec{\nabla} \times \vec{A}.$$

$$A_\mu = (-\phi, A_i).$$

$$\phi'(t, \vec{x}) = \phi - \frac{\partial \Lambda}{\partial t},$$

$$\vec{A}'(t, \vec{x}) = \vec{A} + \vec{\nabla} \Lambda,$$

$$A'_\mu(x) = A_\mu(x) + \frac{\partial \Lambda}{\partial x^\mu}.$$

Combining gauge transformations:  $\Lambda_3 = \Lambda_1 + \Lambda_2$ .