



$$g \bar{\Psi} (\phi_1 + i \gamma_5 \phi_2) \Psi$$

Induced Current Calculation

expand around
 $\phi_1 = v$ point
 $m = gv$

$$g \int \frac{d^2 k}{(2\pi)^2} \frac{\text{tr} \gamma_\mu (k+m) \gamma_5 (\not{k} + m)}{(k^2 - m^2) ((k+p)^2 - m^2)}$$

$p \rightarrow 0$, leading term, Euclideanize

$$g \int \frac{d^2 k}{(2\pi)^2} \frac{m \text{tr} \gamma_\mu \gamma_5 \not{k}}{(k^2 + m^2)^2}$$

$$\gamma_0 = \sigma_2, \quad \gamma_1 = i\sigma_1, \quad \gamma_5 = \sigma_3$$

from trace
 \downarrow

$$2 \frac{g}{4\pi^2} \pi \int_0^\infty \frac{dk^2}{(k^2 + m^2)^2}$$

$$\epsilon_{uv} p_\nu$$

$$\frac{1}{m^2}$$

$$\rightarrow \frac{g}{m} = \frac{1}{f} \phi_1$$

$$\frac{1}{2\pi} \epsilon_{uv} \partial_\nu \phi_2$$

invariant form:

$$\frac{1}{2\pi} \frac{\epsilon^{ab} \epsilon_{uv} \phi^a \partial_\nu \phi^b}{|\phi|^2}$$

$$= \frac{1}{2\pi} \epsilon_{uv} \partial_\nu \Theta$$

$$\Theta = \tan^{-1} \phi_1 / \phi_2$$



for $\phi_1 \rightarrow \pm v$ at $\pm \infty$, $\Delta\phi = \pi$

$$Q = \frac{1}{2}$$