### 9.65: November 28, 2001 Reasoning Handout

Outline:
Logical reasoning:

1. Syllogisms and problems with them:
-Atmosphere effect
-Conversion error
-Belief bias
2. Mental models in reasoning (Venn diagrams)
3. The Wason "Selection problem"
-modus ponens
-modus tollens
-meaningfulness?
-permission schemas/detect cheaters
4. Hypothesis testing:
-confirmation bias
5. Utility theory
-costs and benefits
-probability of outcomes
-choices between bets
-subjective utility
-risk aversion for gains, risk-taking for losses
6. Are we rational?

## Logical reasoning:

1. Syllogisms and problems with them:

All $X$ are $Y$
All $Y$ are $Z$
All $X$ are $Z$
-Atmosphere effect:
All A are B
All $C$ are $B$
All C are A?
-Conversion error:
Some P are not Q
All $P$ are $R$
Some $Q$ are not $R$ ?
-Belief bias
All robins are birds
Some birds eat worms
Some robins eat worms?
2. Mental models in reasoning (Venn diagrams)

## 3. The Wason "Selection problem"

If $X$ then $Y$
$X$ is true
$Y$ is true
-modus tollens
If $X$ then $Y$
Y is false
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$X$ is false

Difficulty with negative statements, in general
-meaningfulness? Two other Wason problems
-permission schemas/detect cheaters

## 4. Hypothesis testing:

The $2,4,6$ problem: What is the rule?
-confirmation bias

## 5. Utility theory: Rational decision-making

 -costs and benefits, probability of outcomes
-choices between bets (framing effects)
H: 8/9 chance to win \$4
L: $1 / 9$ chance to win $\$ 40$

Another choice:
A: Sure chance of gaining $\$ 100$
B: .50 of gaining $\$ 200, .50$ gain nothing

Versus:
You are given \$200:
A: Sure chance of losing $\$ 100$.
B. .50 chance of losing $\$ 200, .50$ of losing nothing.
-risk aversion for gains, risk-taking for losses
Subjective utility:
Loss aversion: gains considered less attractive than losses are considered aversive.

## 6. Are we rational?

Utility theory versus justification-seeking
E.g., sunk costs.

