

Electron Probe Micro-Analysis

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Uses of the EPMA

Spot mode operation for quantitative analysis:

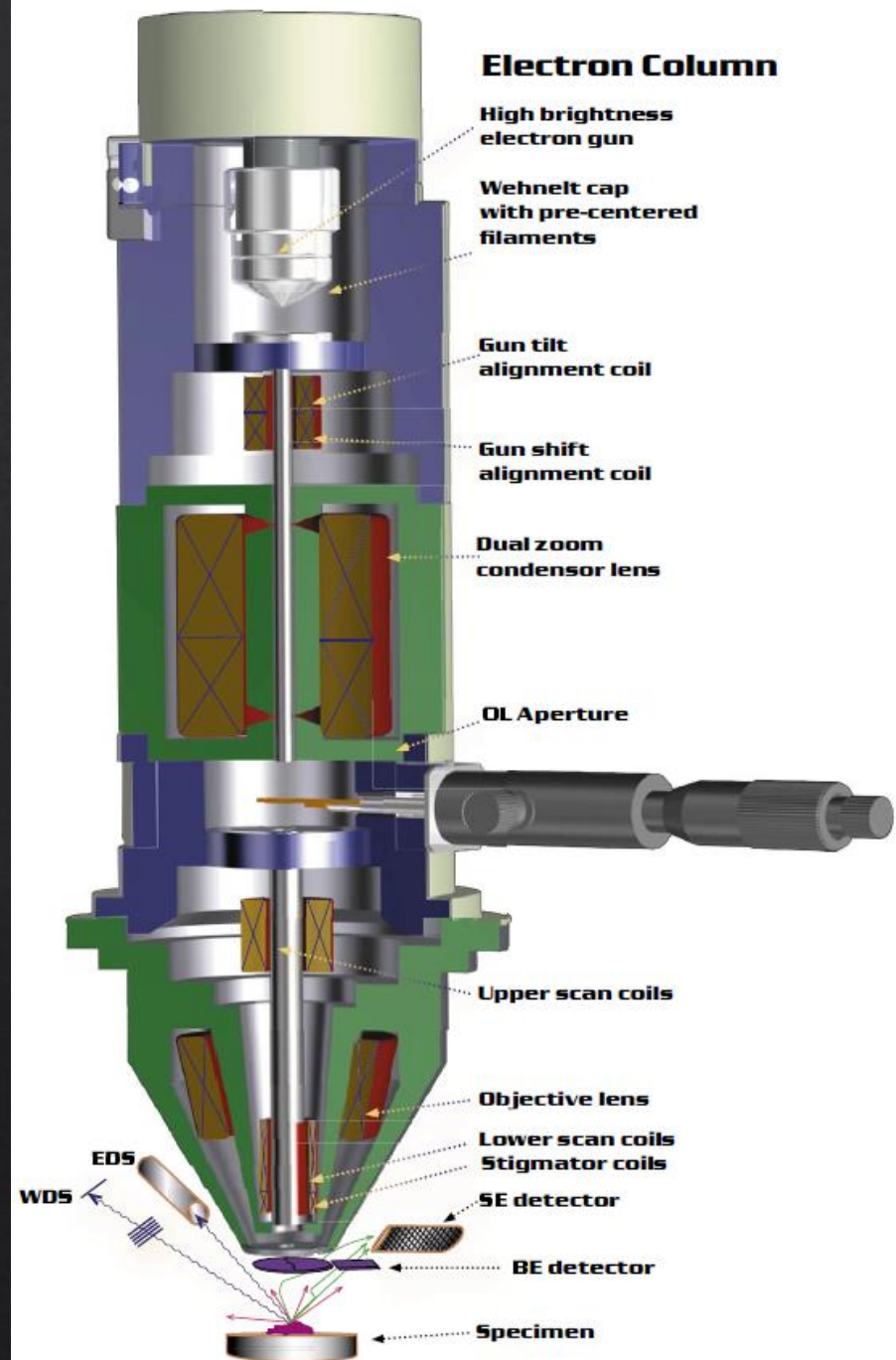
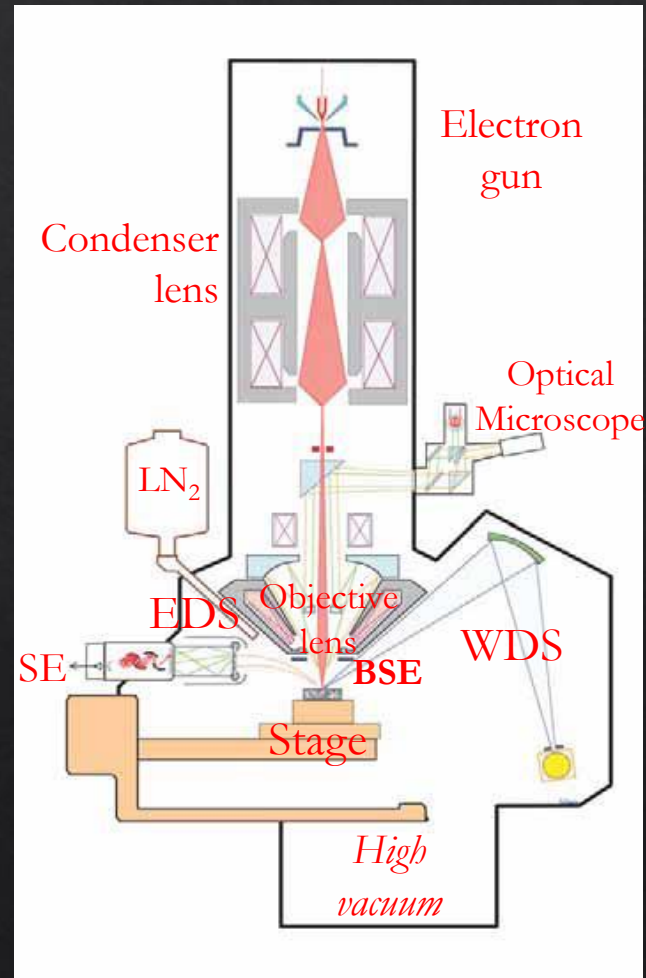
- Micron-scale, complete chemical analysis

Be to U (10-50 ppm under favorable conditions)

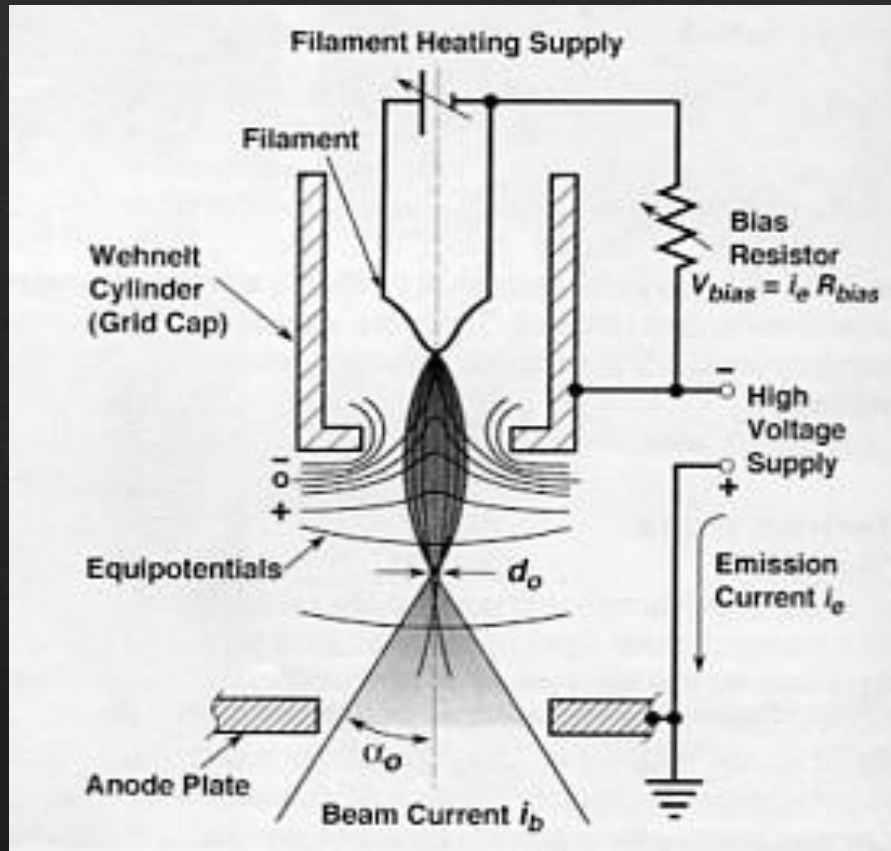
Raster mode operation for high resolution imaging:

- Back-scattered electron: *composition and topography*
- Secondary electron: *topography*
- X-ray map: *spatial distribution of elements*
- Cathodoluminescence: *trace elements, defects*

JXA-8200 scheme



Electron emitting source: Tungsten hairpin



Self-biased thermionic electron gun

- **Cathode: Filament** at negative potential

Tungsten has a high melting point and a low work-function energy barrier; heated by filament current, i_f , until electrons overcome the barrier

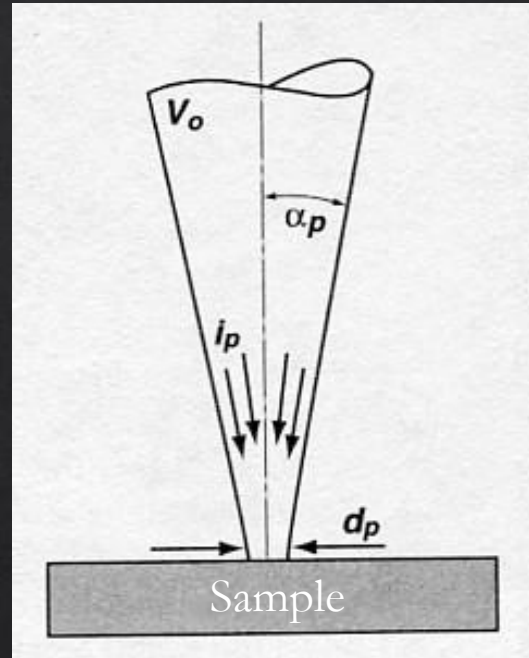
- **Wehnelt Cylinder** at a slightly higher negative potential than the filament because of the Bias Resistor

Bias voltage (V_{bias}) automatically adjusts with changes in i_e to stabilize emission; the grid cap also focuses the electron beam

- **Anode: Plate** at ground potential

Potential difference (accelerating voltage, V_0) causes electron emission (current, i_e)

Electron probe parameters



Accelerating voltage, V_o

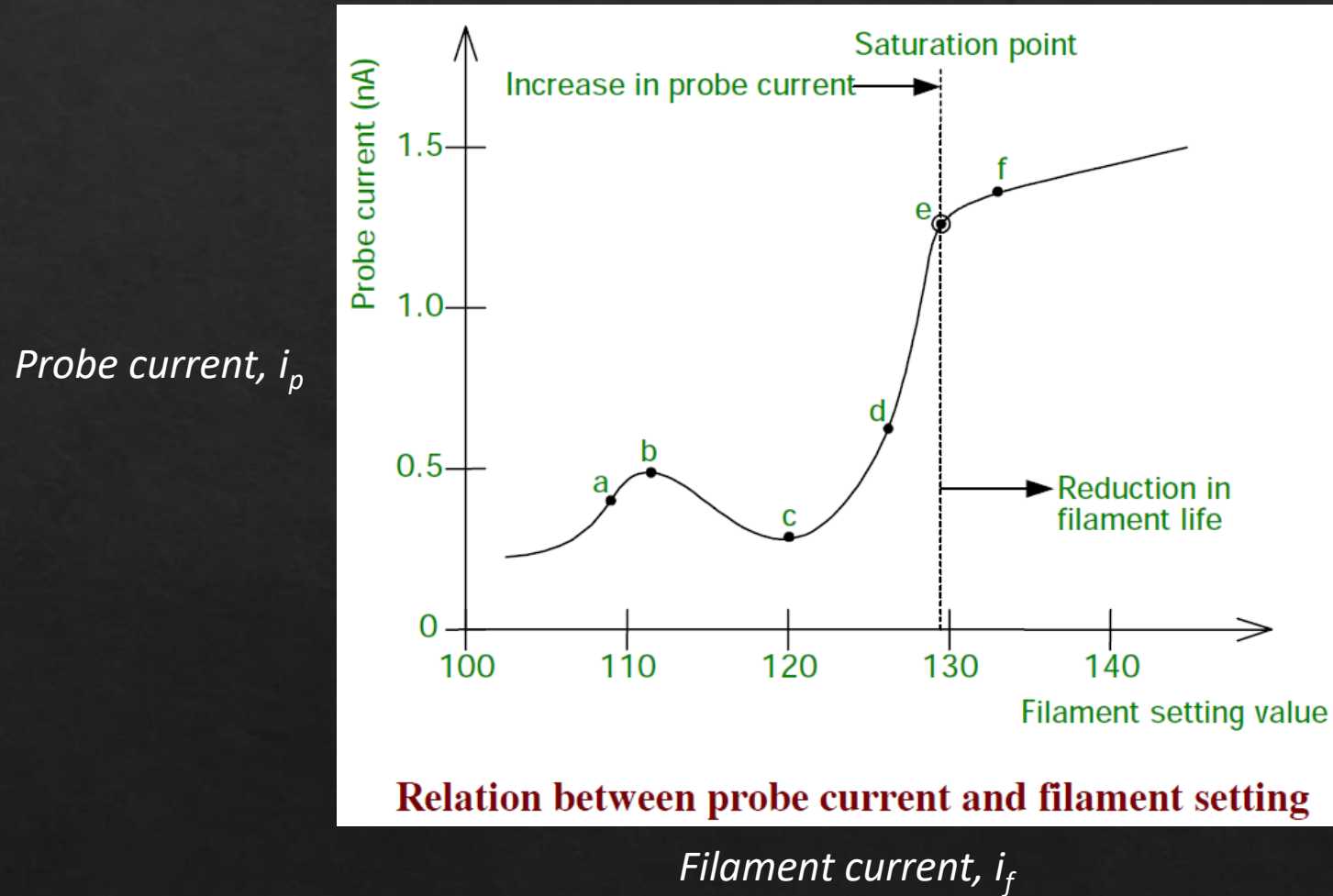
(V_o of 15 kV generates electron beam with 15 keV energy)

Final beam current, or **probe current**, i_p

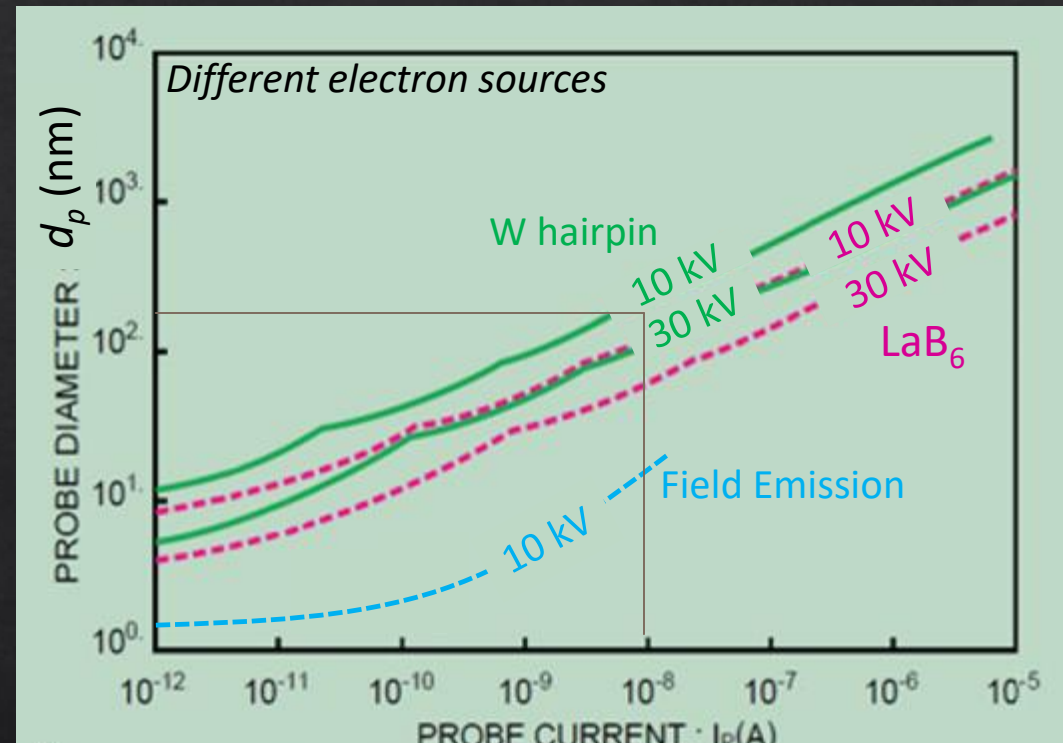
Final beam diameter, or **probe diameter**, d_p

Final beam convergence angle, or **probe convergence angle**, α_p

Filament saturation



Electron probe diameter



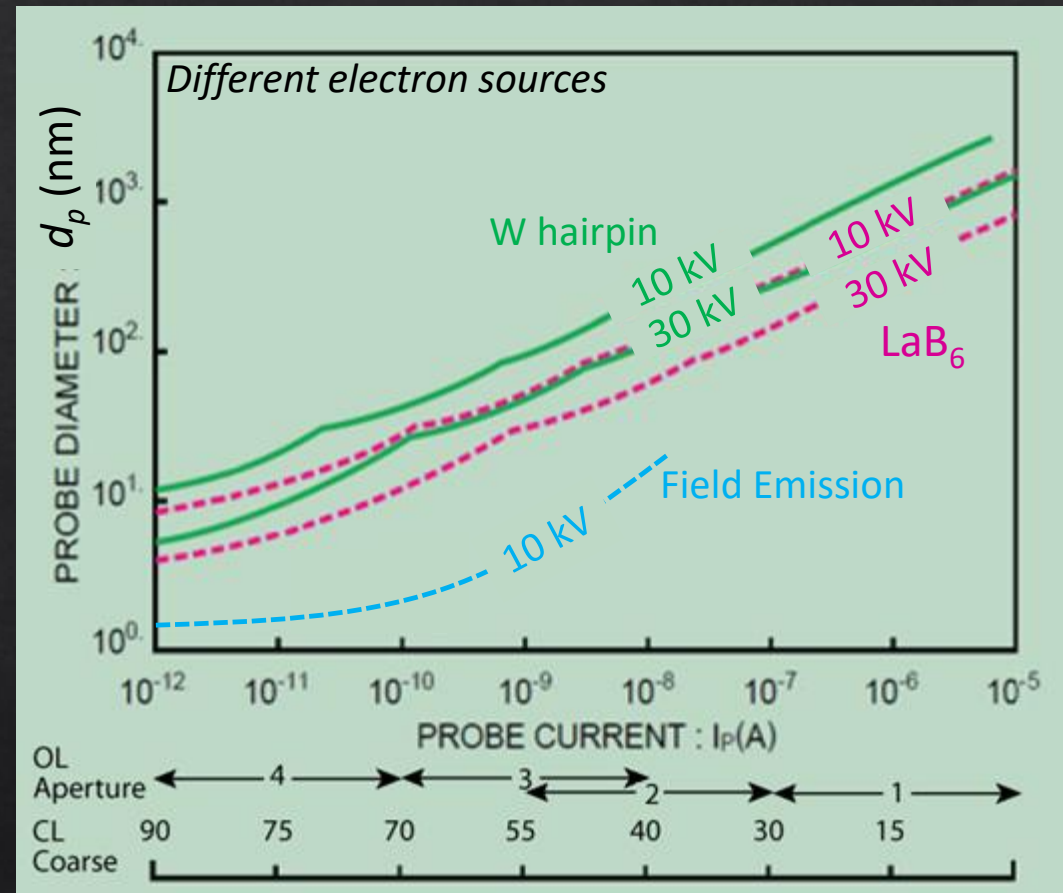
Probe diameter decreases with

- decrease in Probe current
- increase in Accelerating voltage
- $W > LaB_6 > \text{Field Emission source}$

Higher probe current improves signal but results in poorer image resolution

$d_p \approx 100$ nm at 10 nA and 15 kV with a Tungsten hairpin source

Electron probe diameter



*Probe current can be changed by adjusting the condenser lens (CL) current
and the objective lens (OL) aperture settings*

OL aperture control on probe diameter and current

Scale (OL aperture No.)	Aperture diameter (μm)	Indication coefficient	Probe current range (Acc. voltage: 25 kV)	Purpose of use
		Probe diameter*		
4	70	Approx. 0.3	10^{-10} A or less	High resolution SEM LDF mode; large depth of focus.
3	130	Approx. 0.5	10^{-10} to 10^{-8} A	
2	170	Approx. 0.7	10^{-8} to 10^{-7} A	
1	240	1	10^{-7} to 10^{-5} A	Higher current X-ray microanalysis.

* The value (other than 0) indicated in the Control window is an approximate probe diameter when OL aperture No. 1 is selected. When an aperture other than No. 1 is used, multiply the indicated probe diameter by the probe diameter indication coefficient to obtain the approximate value. The actual probe diameter can be determined from the diameter of a disk-shaped luminescent pattern of ZrO₂ displayed on the OM monitor of the workstation.

- *Actual diameter = diameter in control window X indication coefficient*
- *Use ZrO₂ and 25 kV to determine probe diameter, which depends on the material and increases sharply with accelerating voltage*

Electron gun brightness

$$\text{Brightness, } \beta = \frac{\text{current}}{(\text{area})(\text{solid angle})} = \frac{i_b}{\left(\pi\left(\frac{d}{2}\right)^2\right)(\pi\alpha^2)} \text{ A/cm}^2\text{sr}$$

i_b : beam current

d : beam diameter

α : beam convergence angle

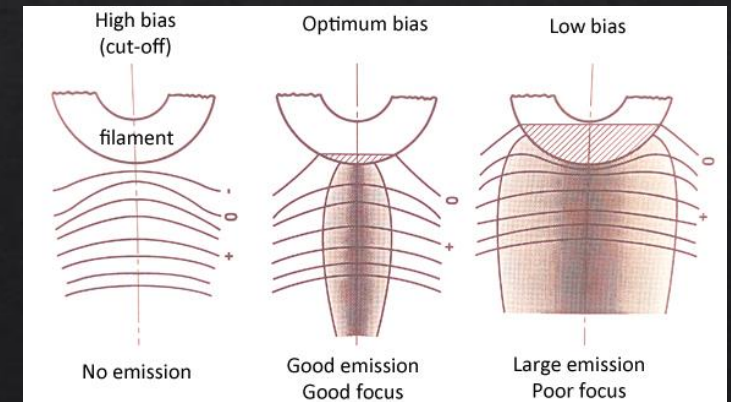
Higher beam current and smaller diameter results in greater brightness

Maximum brightness can be achieved by correctly setting the
gun bias voltage and **filament-to-grid cap distance**

Low bias: high emission but large d , hence low β

High bias (cut-off): no emission

Optimum bias and filament-grid cap distance: good emission and small d , hence high β



Comparison of electron emitting sources

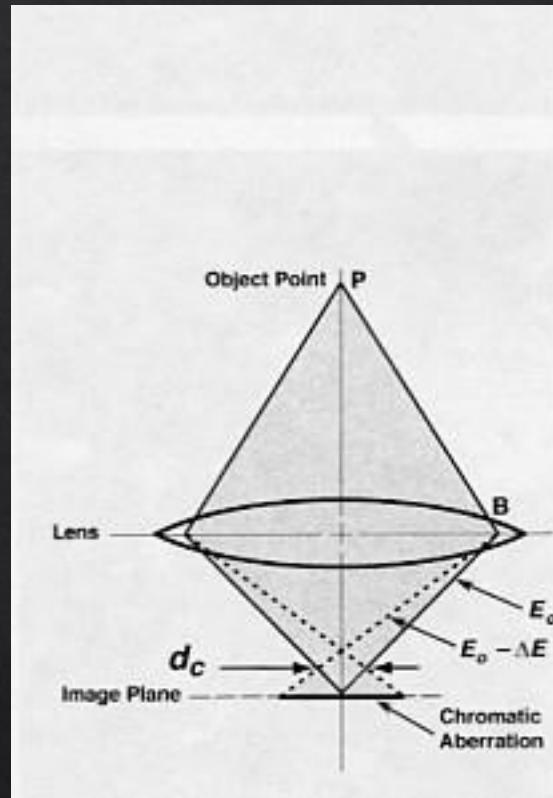
Source	Brightness, β at initial crossover (A/cm ² sr)	Initial beam diameter, d_0 (μ m)	Energy spread, ΔE (eV)	Beam current stability (% hour)
Thermionic emitter:				
Tungsten hairpin	10^5	30 - 100	1 - 3*	1
LaB ₆	10^6	5 - 50	1 - 2	1
Field emitter:				
Cold	10^8	<0.005	0.3	5
Thermal	10^8	<0.005	1	5
Schottky	10^8	0.015 - 0.030	0.3 - 1.0	~1

* E.g., a 15 keV electron beam actually has an energy of $15,000 \pm 3$ eV

Source: Goldstein et al. (2003) p. 35

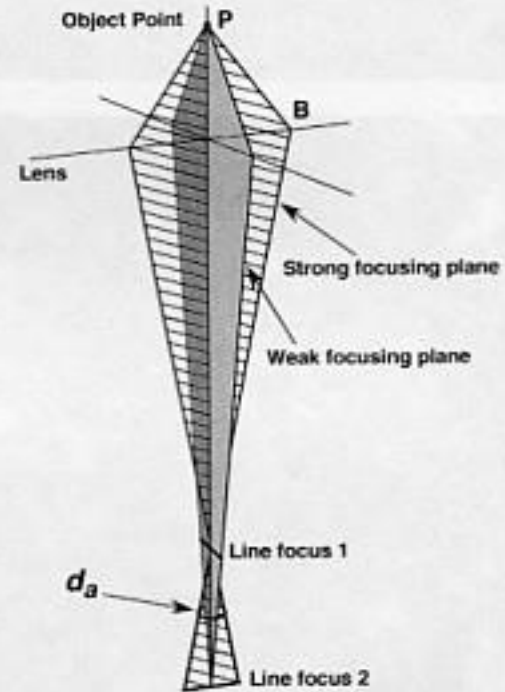
Lens aberration

Electrons with different energies are focused at different distances



Chromatic aberration

more at low voltage



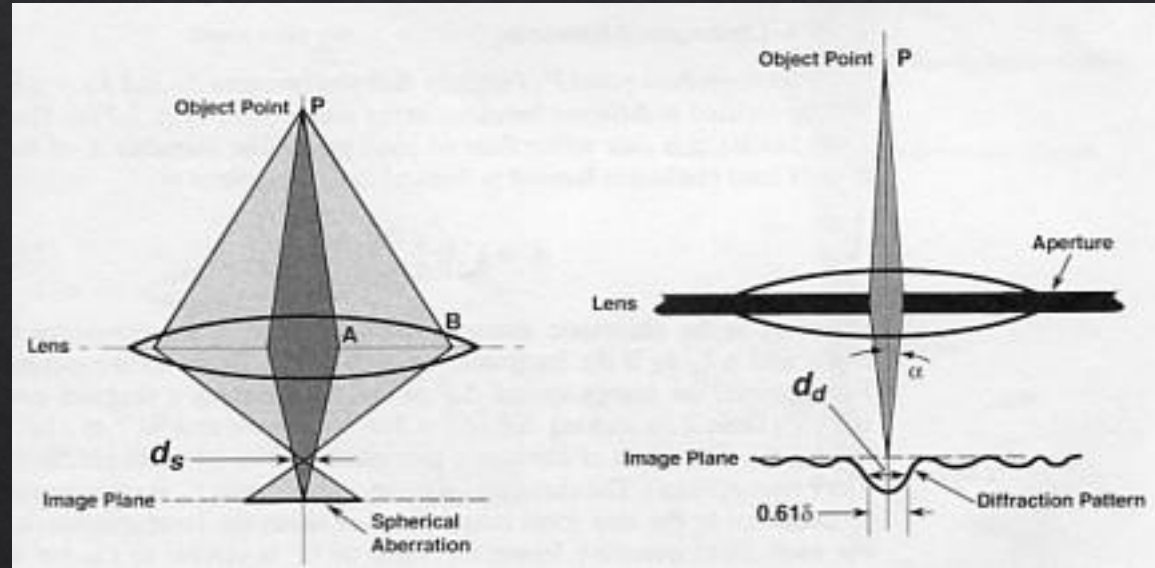
Astigmatism

corrected with stigmator controls

Electrons traveling on different planes are focused at different distances

Lens aberration

Electrons traveling through the center and edge of the lens are focused at different distances



Spherical aberration

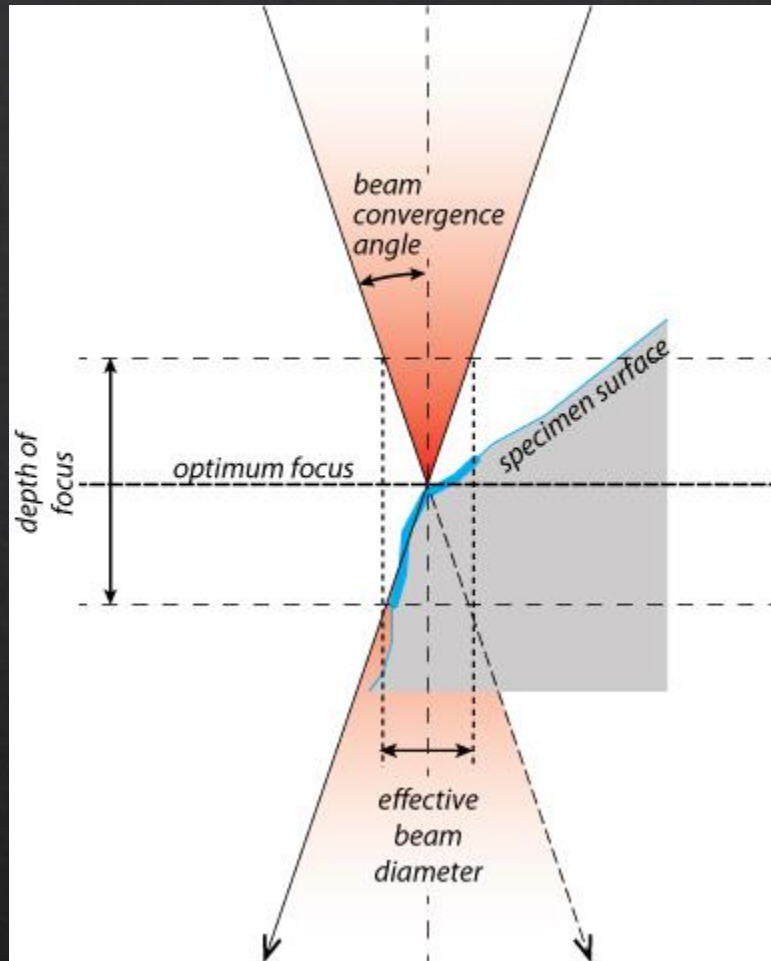
less with
smaller OL apertures

Aperture diffraction

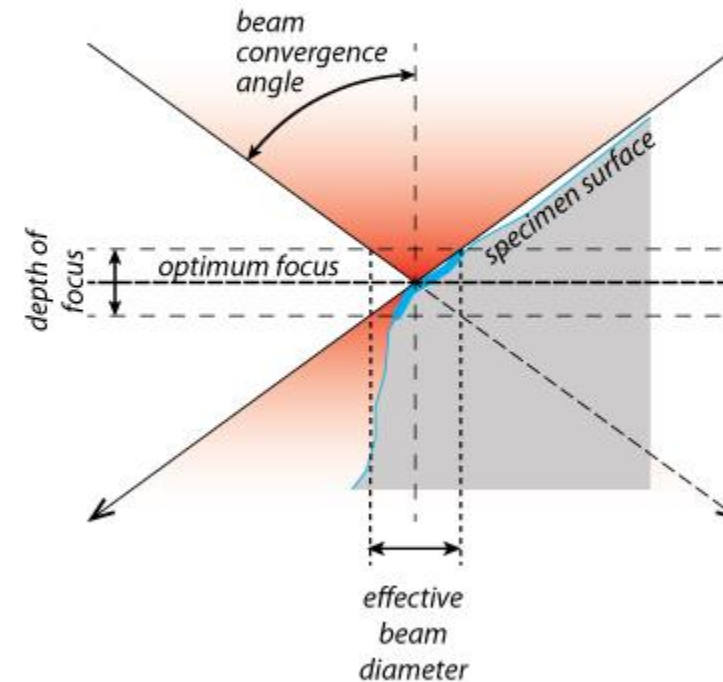
very small OL apertures
have this artifact

Very small apertures produce a concentric diffraction pattern instead of a spot

Depth of focus

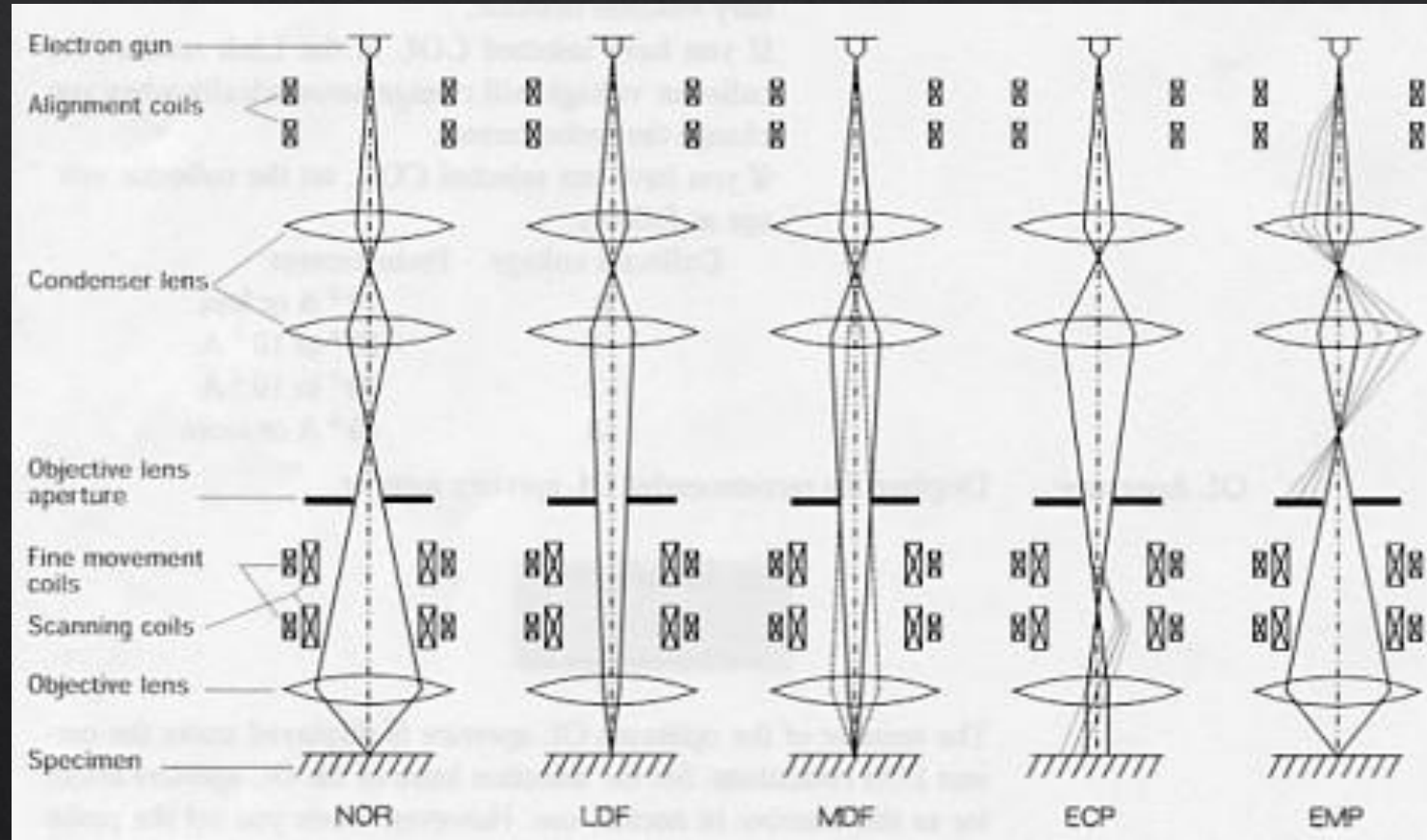


Large depth of focus



Small depth of focus

Column modes



Normal

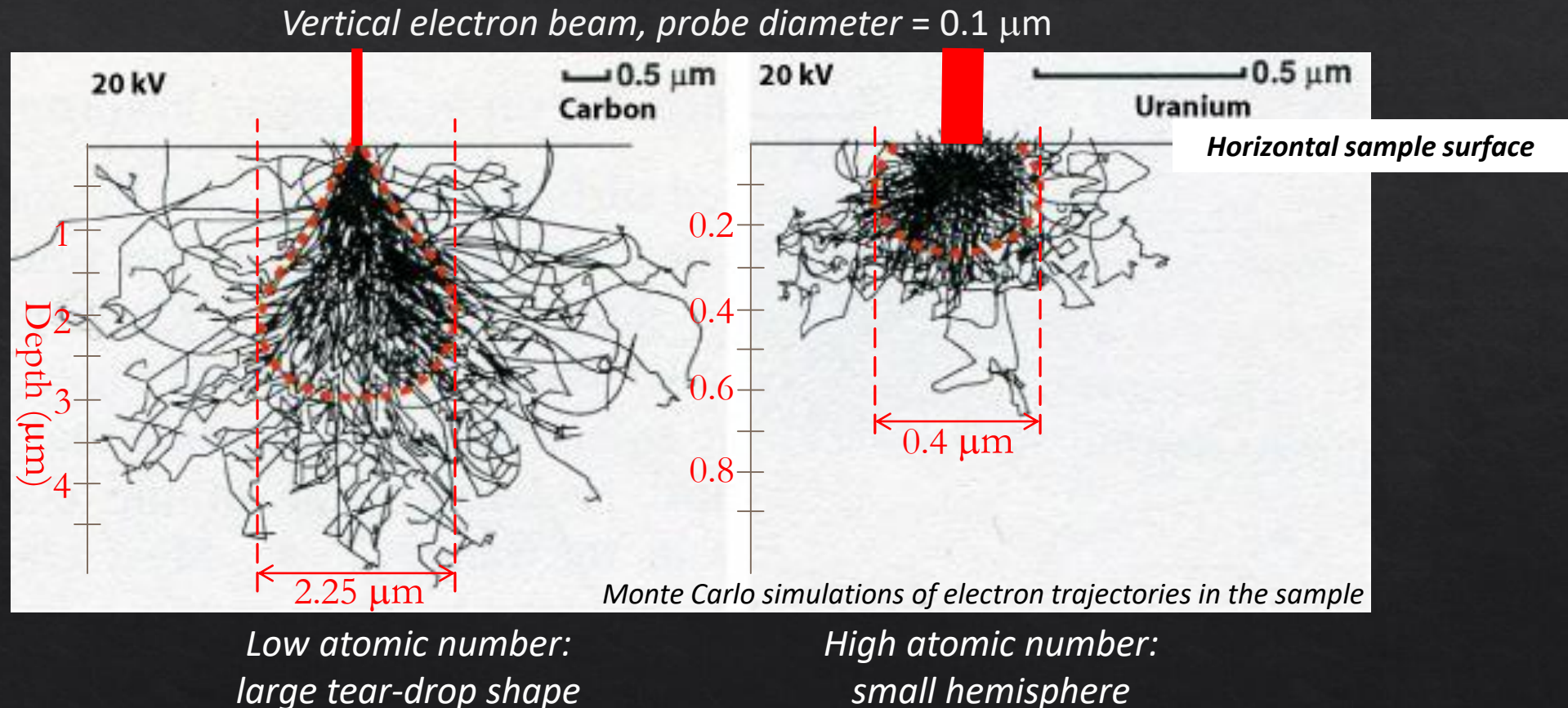
Large
depth of
focus

Maximum
depth of
focus

Electron
channeling
pattern

Emission
pattern

Spatial resolution: electron interaction volume



Width of interaction volume $\gg$ probe diameter
(interaction volume can be reduced by reducing the probe diameter using a lower accelerating voltage)

Electron interaction depth (range)

$$R = 0.0276 E^{1.67} \frac{A}{\rho Z^{0.889}}$$

*R : Kanaya-Okayama
electron range*

E : beam energy

A : atomic weight

ρ : density

Z : atomic number

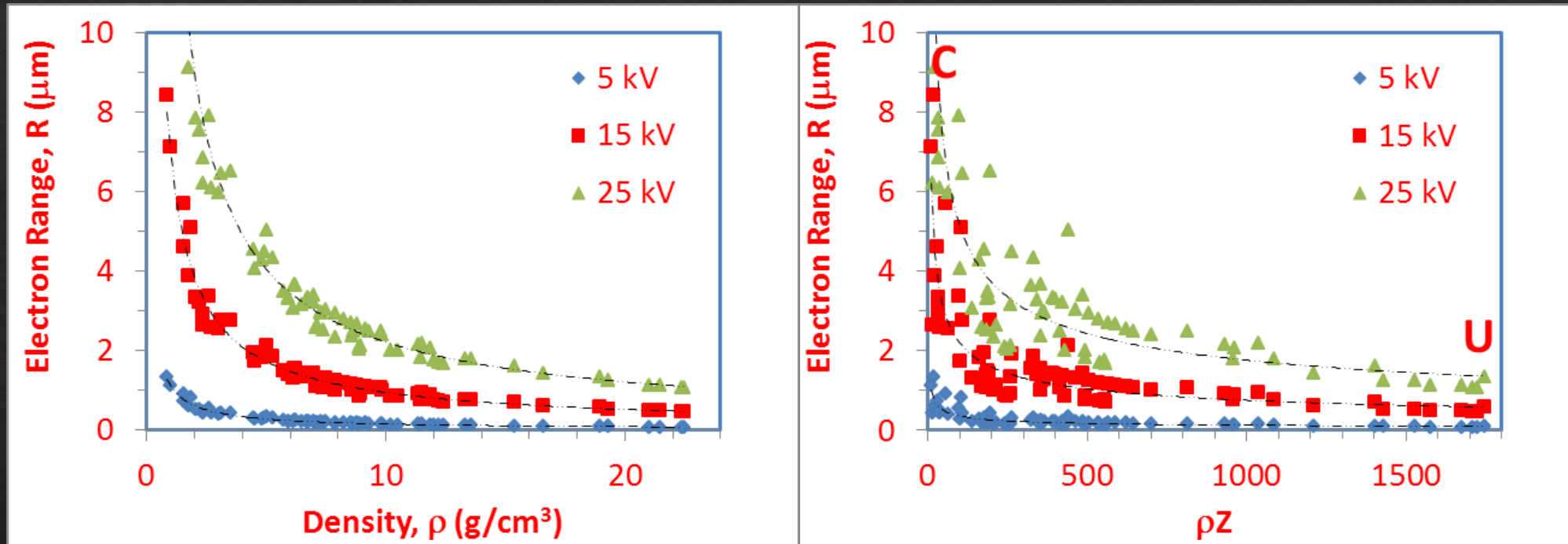
Electron range increases as E increases, and decreases as ρ and ρZ increase

E.g., at 20 kV,

$R = 4.29 \mu\text{m}$ in Carbon ($Z = 6$, $A = 12.01$, $\rho = 2.26 \text{ g/cc}$)

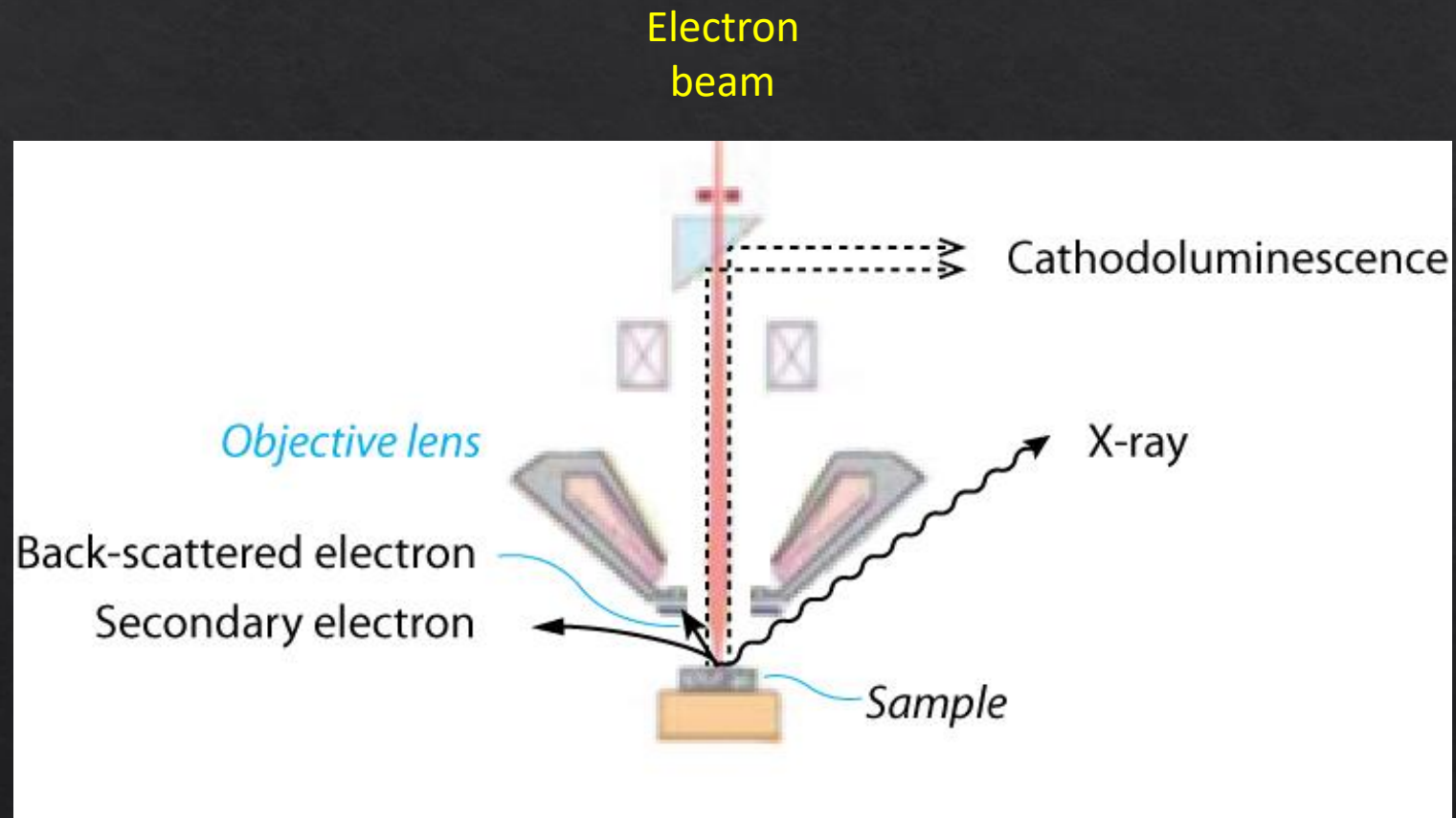
$R = 0.93 \mu\text{m}$ in Uranium ($Z = 92$, $A = 238.03$, $\rho = 19.07 \text{ g/cc}$)

Electron interaction depth (range)

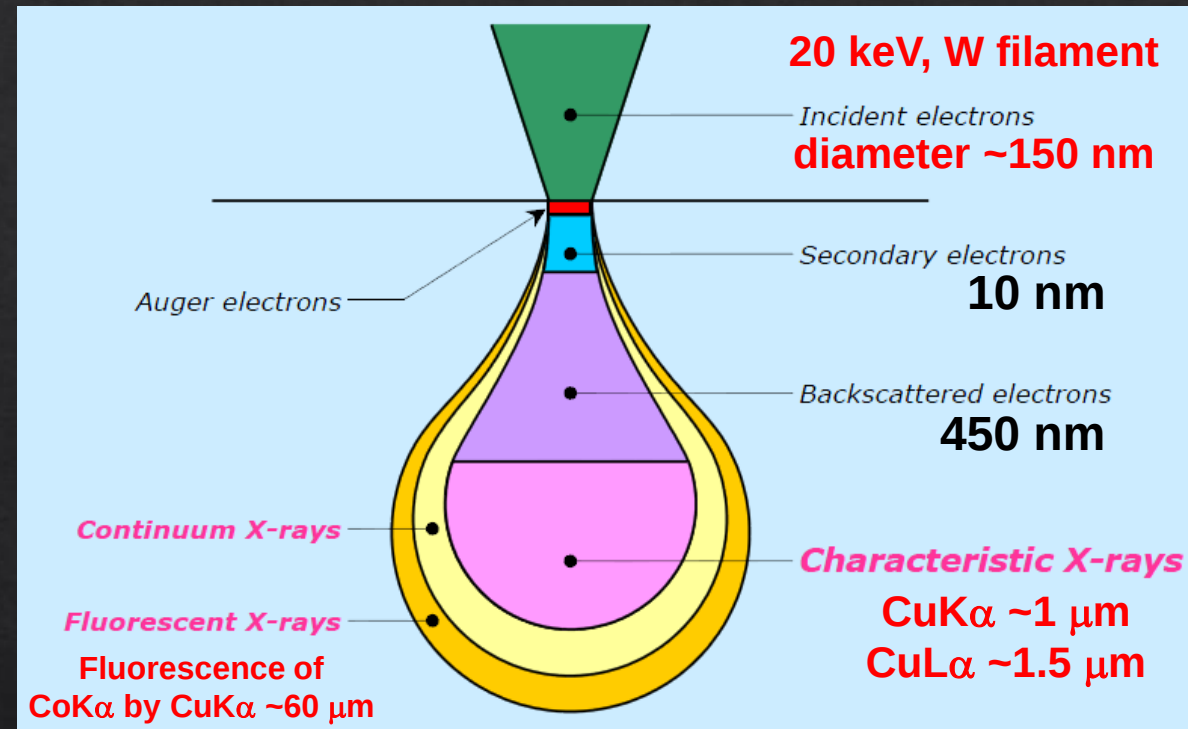


Electron range increases as E increases, and decreases as ρ and ρZ increase

Signal types



Spatial resolution for different signals (production volume)

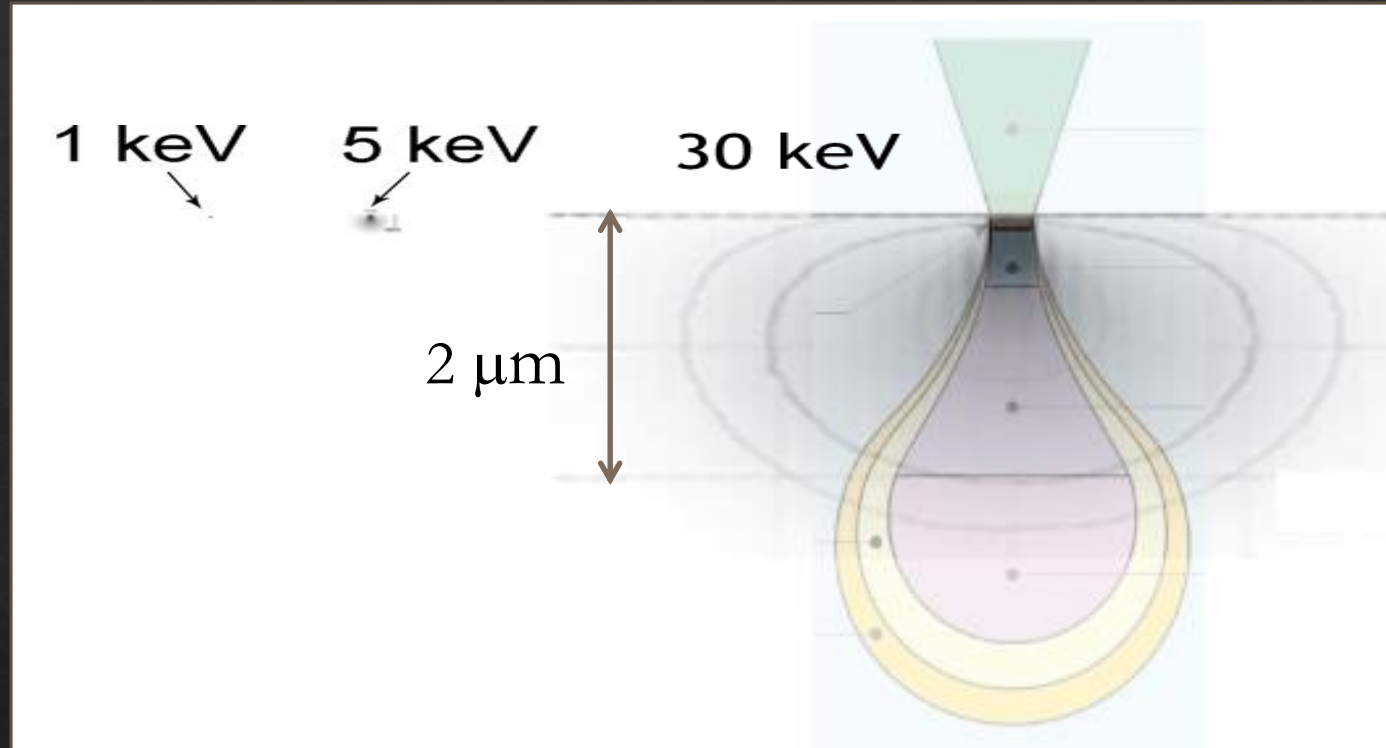


(not to scale)

Production volume for different signals is different

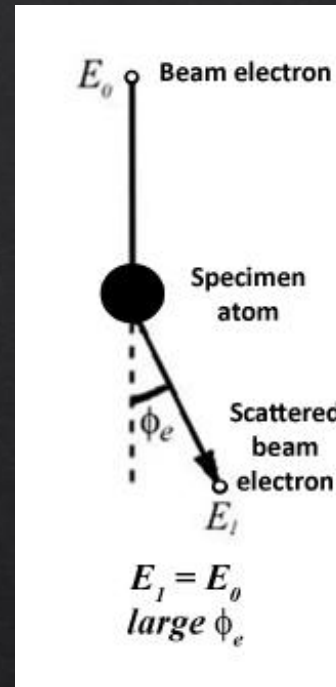
The “onion shell” model:
Cu-10%Co alloy

Spatial resolution for cathodoluminescence (production volume)



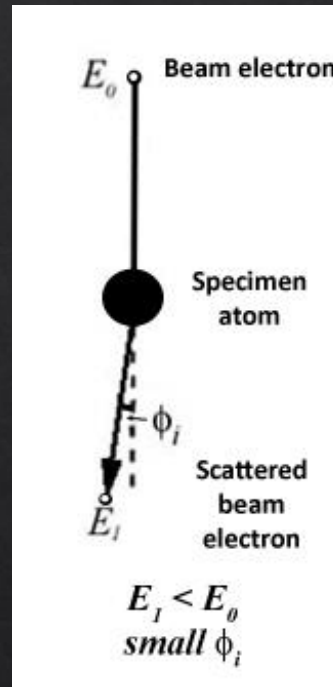
Gallium Nitride

Electron-specimen interactions: elastic scattering



E.g., Back-scattered electron (BSE)

Electron-specimen interactions: inelastic scattering



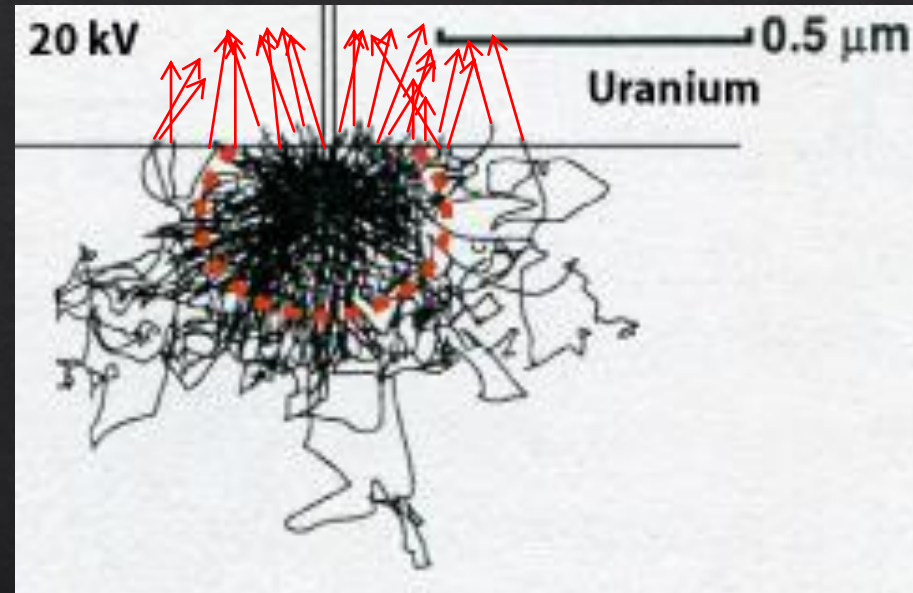
Inner shell interactions:

- Characteristic X-rays
- Secondary electron (SE)

Outer shell interactions:

- Continuum X-rays
- Secondary electron (SE)
- Cathodoluminescence (CL)

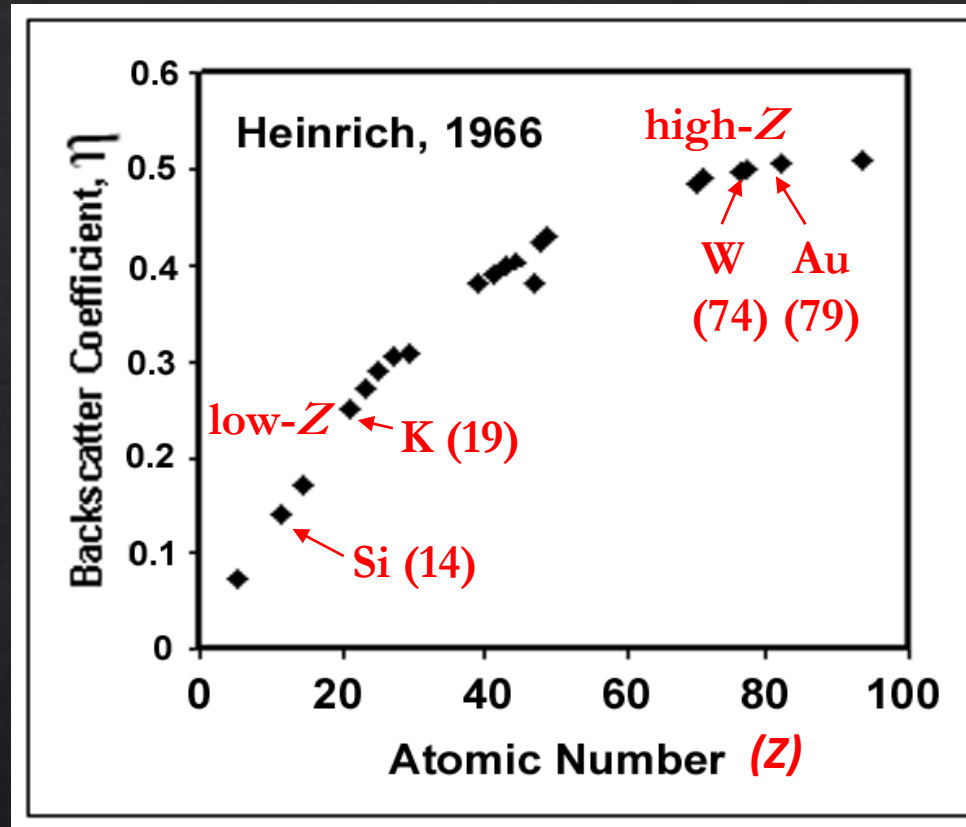
Back-scattered electron (BSE)



- *Beam electrons scattered elastically at high angles*
- *Commonly scattered multiple times, so energy of BSE $\leq$ beam energy*

Electron backscatter coefficient

Fraction of beam
electrons scattered
backward

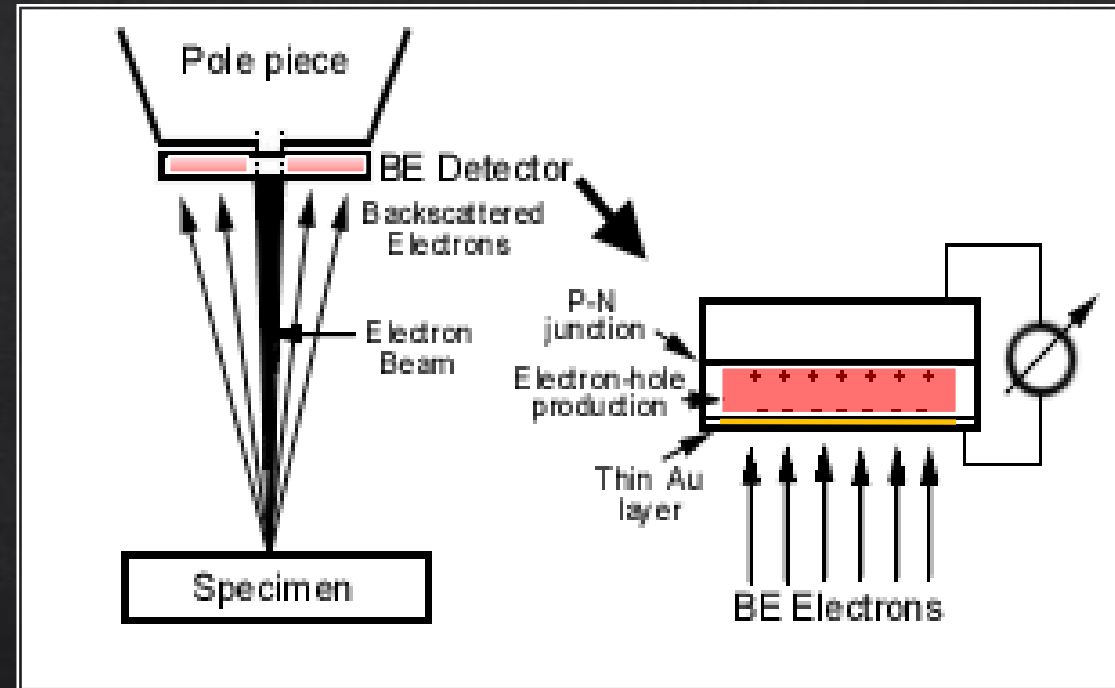


- Large differences between high- Z and low- Z elements
- Larger differences among low- Z elements than among high- Z elements

Back-scattered electron detector

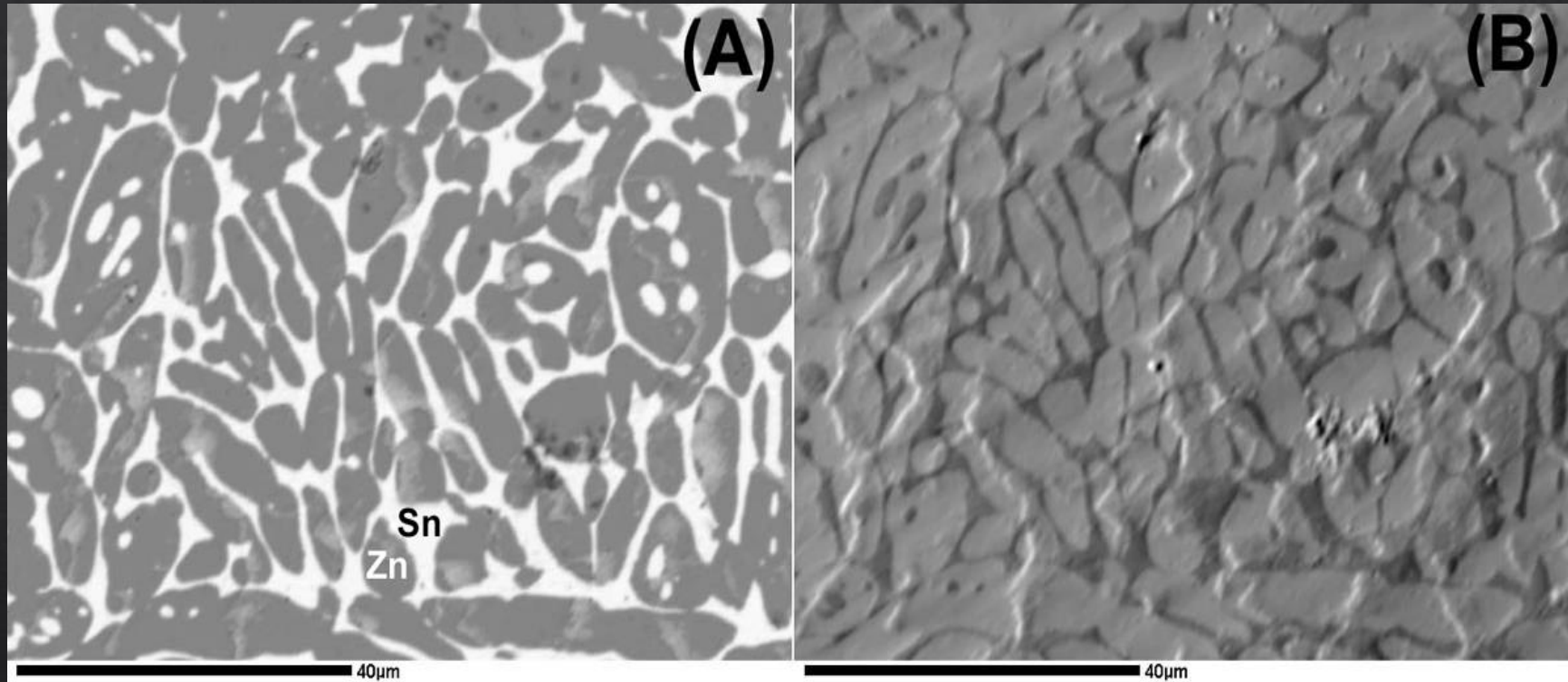


Back-scattered electron detector



Solid-state diode

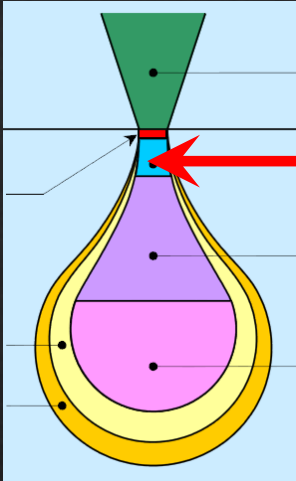
Compositional and topographic imaging with BSE



A+B
Compositional
mode

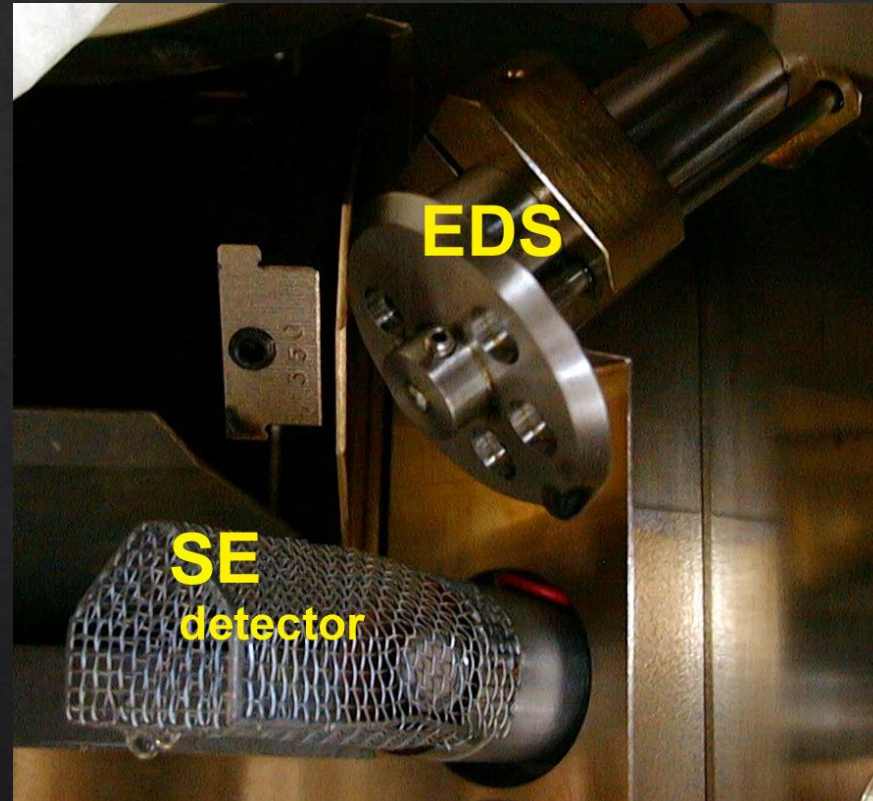
A-B
Topographic
mode

Secondary electron (SE)



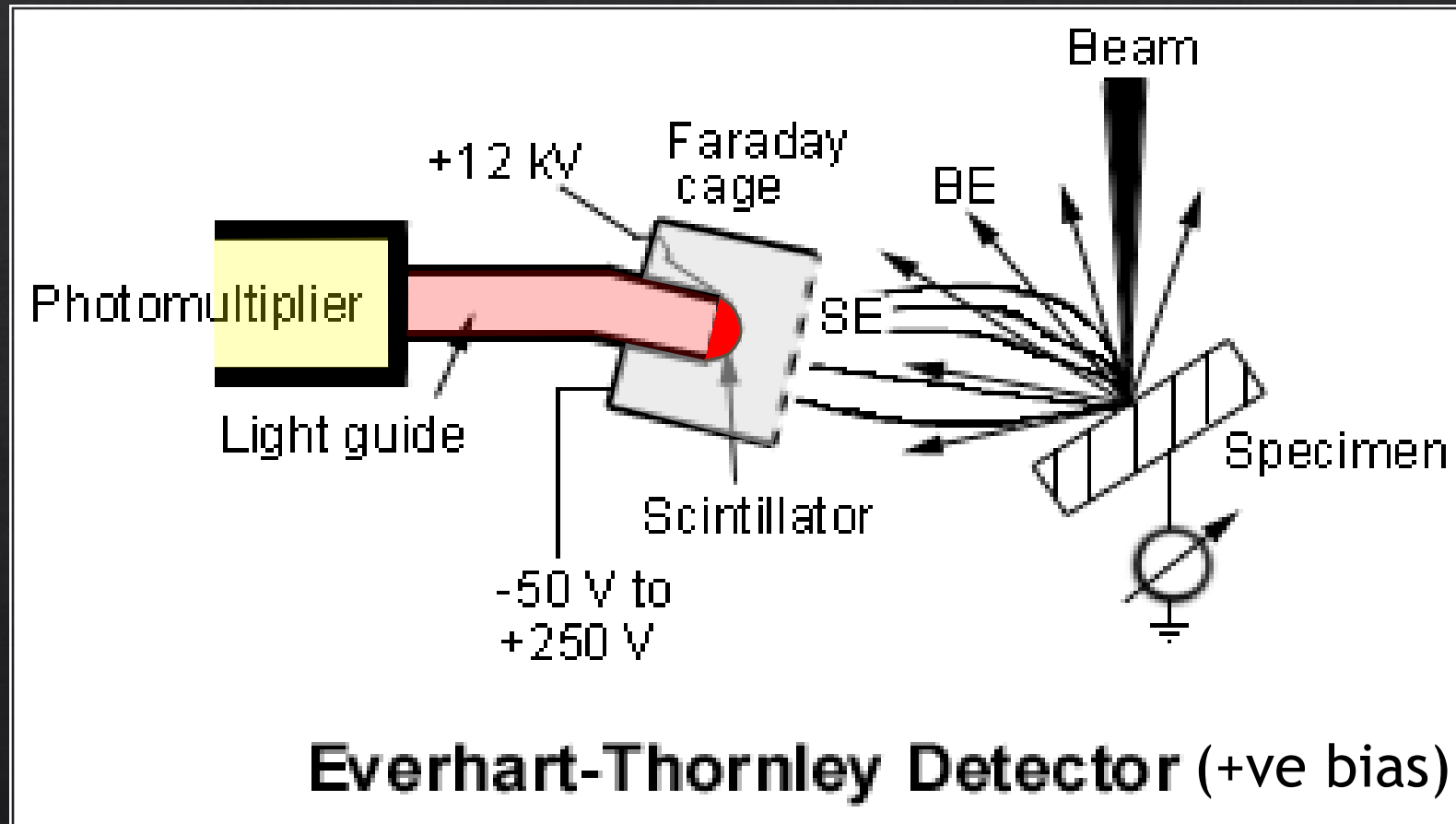
- *Specimen electrons mobilized by beam electrons through inelastic scattering (both outer and inner shell ionizations)*
- *Emitted at low energies (typical: <10 eV)*
(recall BSE have high energies up to that of the electron beam)

Secondary electron detector

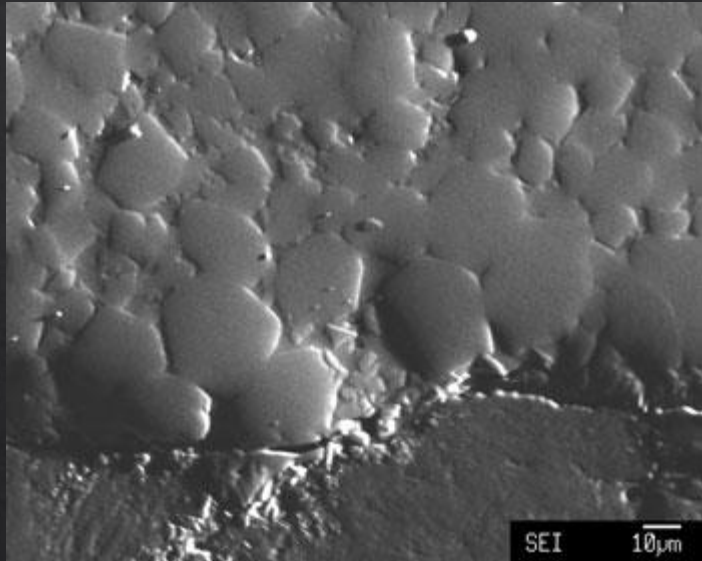


*Located on the side wall of
the sample chamber*

Secondary electron detector

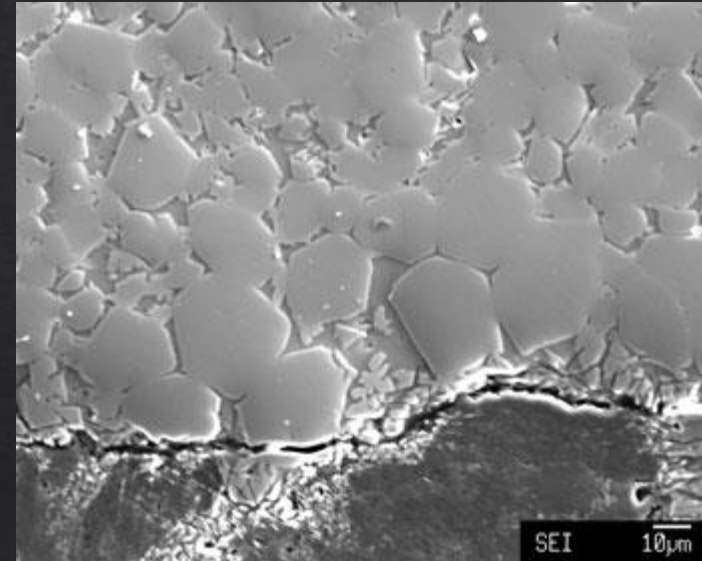


Imaging with the Everhart-Thornley detector



Negative Faraday cage bias
only BSE

*Surfaces in direct line of sight
are illuminated*

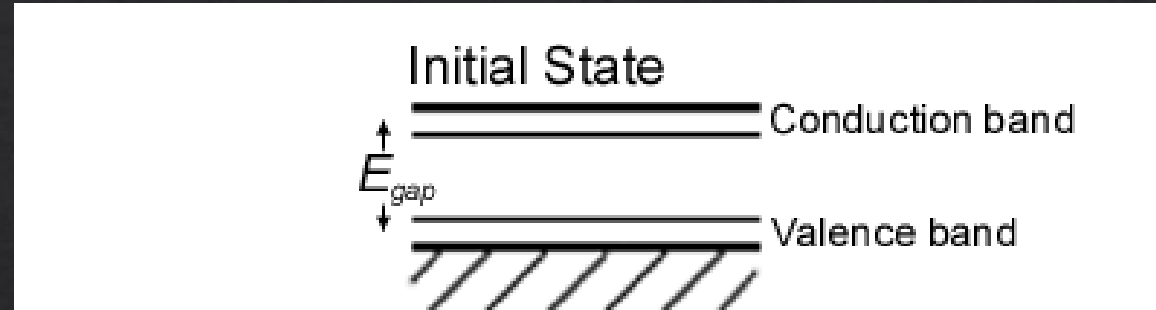


Positive Faraday cage bias
BSE + SE

All surfaces are illuminated

Cathodoluminescence (CL)

Caused by inelastic scattering of beam electrons in **semiconductors**



Filled valence band is separated from an empty conduction band by E_{gap} , characteristic of the compound

Electron recombines with the valence band to generate light with energy E_{gap}

Electron beam interacts:
Valence electron is promoted to the conduction band

Trace element impurities produce additional energy levels outside the conduction band and enable other electron transitions; emitted light has different colors with energies $E \neq E_{gap}$

Cathodoluminescence spectrometer

Optical microscope
camera (not used)

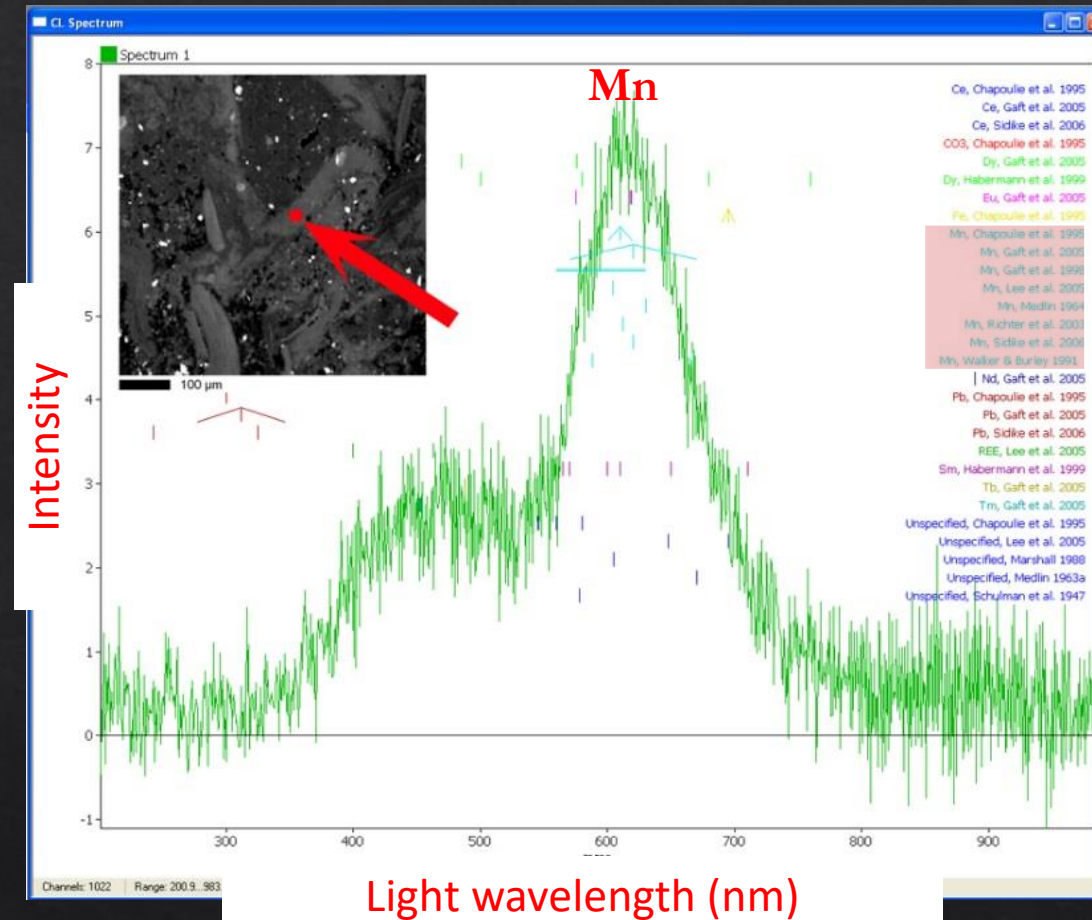


Optical microscope
light (turned off)



Optical spectrometer
(CCD array detector)

Cathodoluminescence spectrum

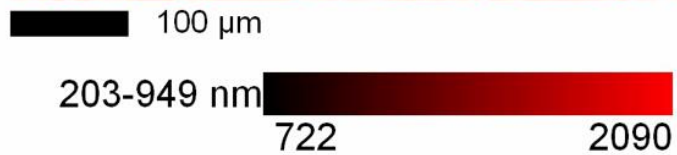
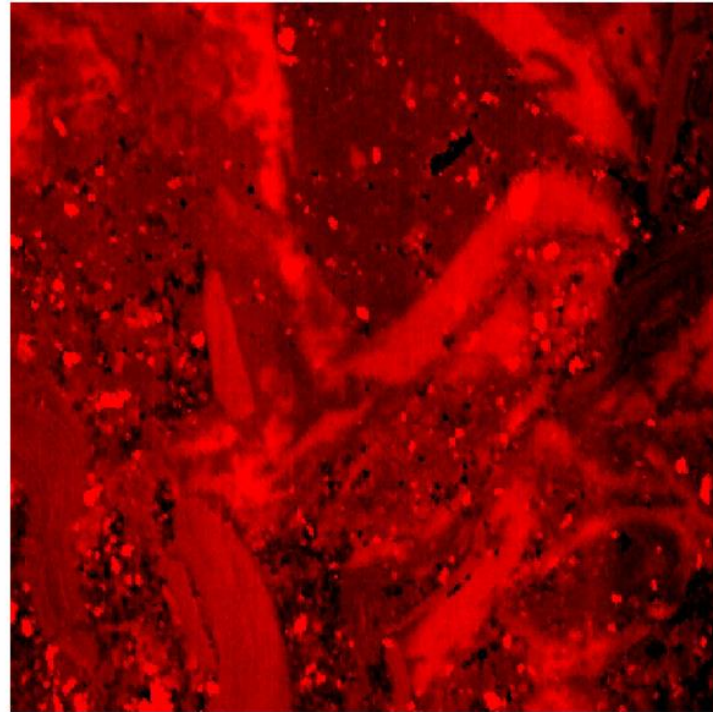


Dolomite with trace of Mn

Hyperspectral CL imaging

*A continuous ($\lambda = 200$
to 950 nm) light
spectrum is collected
at each point of the
image area*

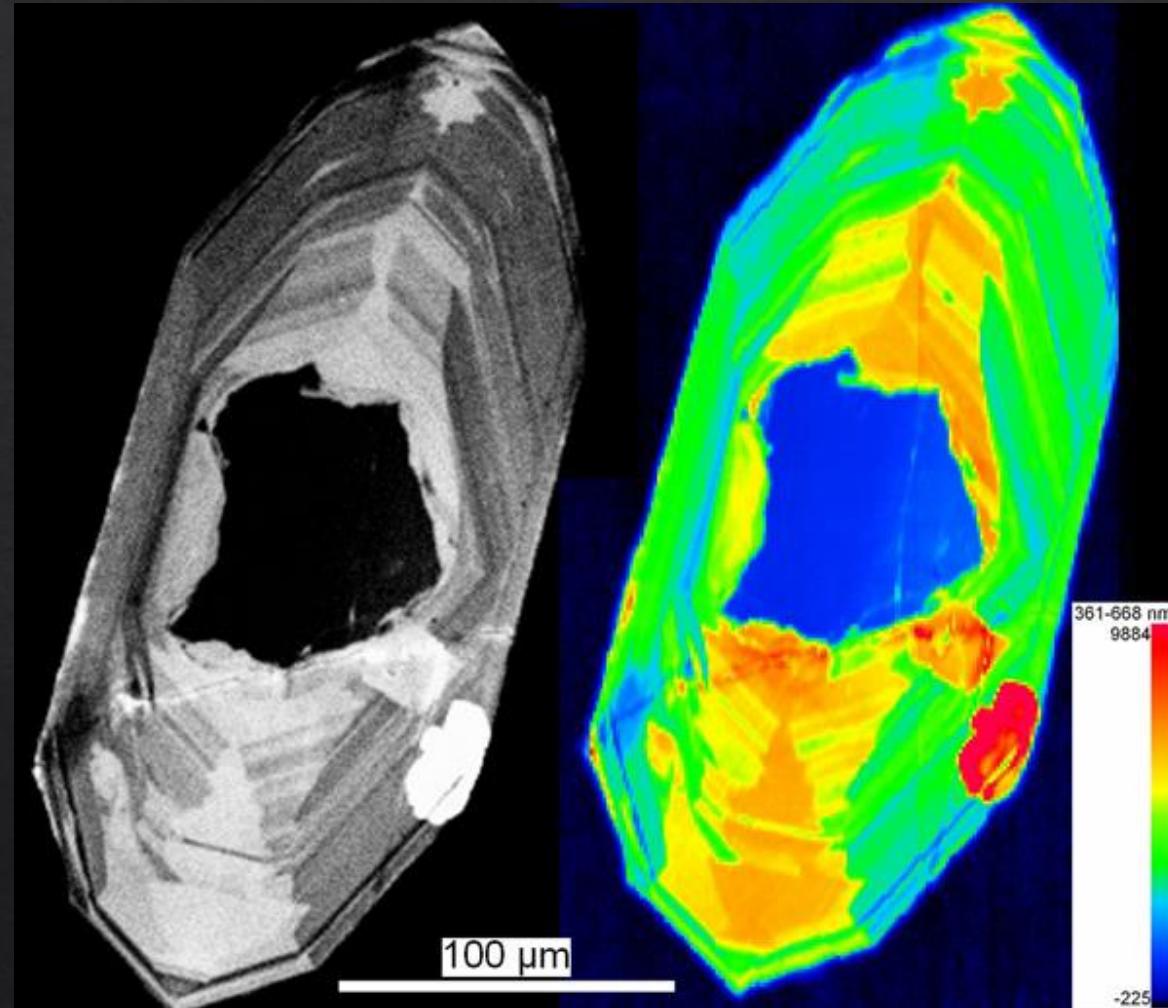
*Intensity range of
203-949 nm light:
722-2090 counts
(red shades)*



Hyperspectral CL imaging

Intensity range of
light (*all wavelengths*)
in *grey scale*:

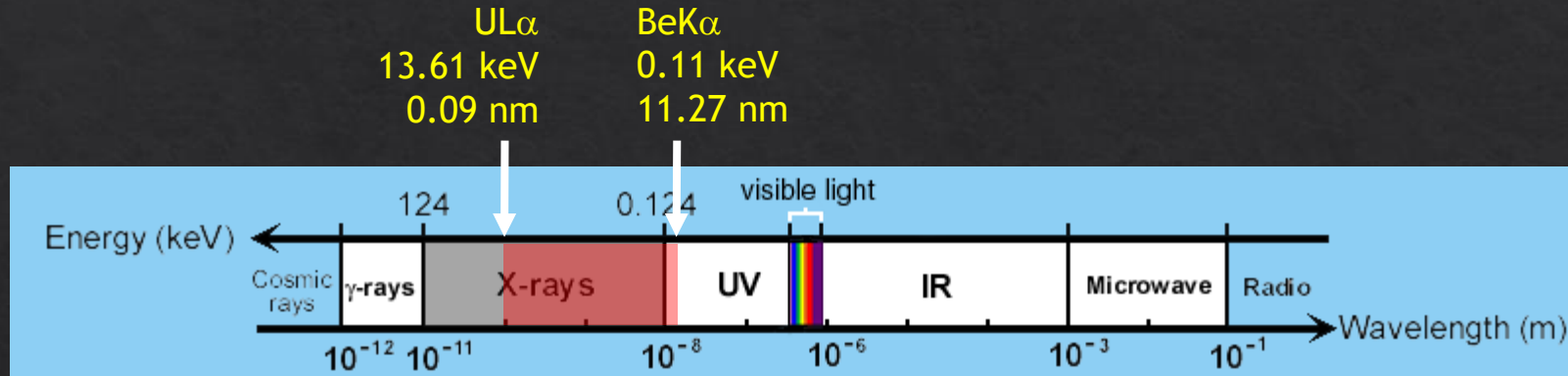
Black: no light
White: maximum intensity



Intensity range of
361-668 nm light
in *multicolor scale*:

Blue (≤ 0 counts):
no light
Red (9884 counts):
maximum intensity

Understanding X-rays: The electromagnetic spectrum



$$E = h\nu = h\frac{c}{\lambda}$$

where, E : energy, h : Planck's constant, ν : frequency
 c : speed of light in vacuum, λ : wavelength

$$E \text{ (keV)} = h\frac{c}{\lambda} = 1.2398/\lambda \text{ (nm)} \quad \text{or,} \quad \lambda \text{ (nm)} = h\frac{c}{E} = 1.2398/E \text{ (keV)}$$

Examples:

$$\lambda_{\text{BeK}\alpha} = 11.27 \text{ nm}; \text{ Hence, } E_{\text{BeK}\alpha} = 1.2398/11.27 = 0.11 \text{ keV}$$

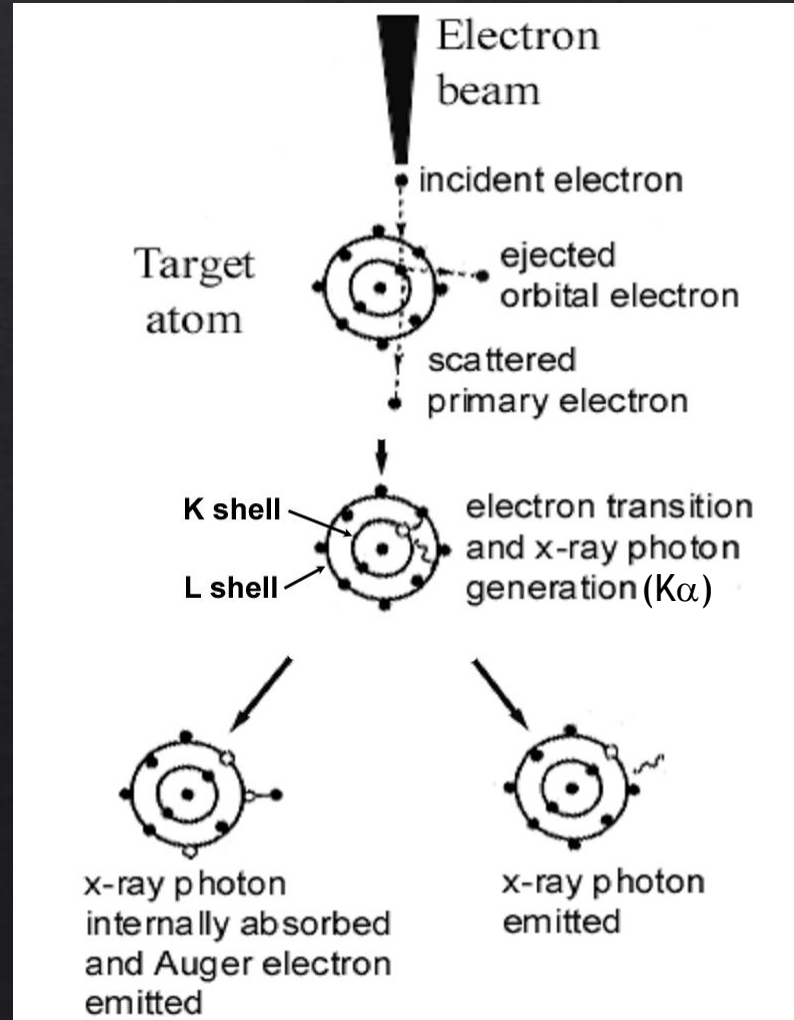
$$E_{\text{UL}\alpha} = 13.61 \text{ keV}; \text{ Hence, } \lambda_{\text{UL}\alpha} = 1.2398/13.61 = 0.09 \text{ nm}$$

Characteristic X-ray generation

Overvoltage, $U = E/E_c, > 1$

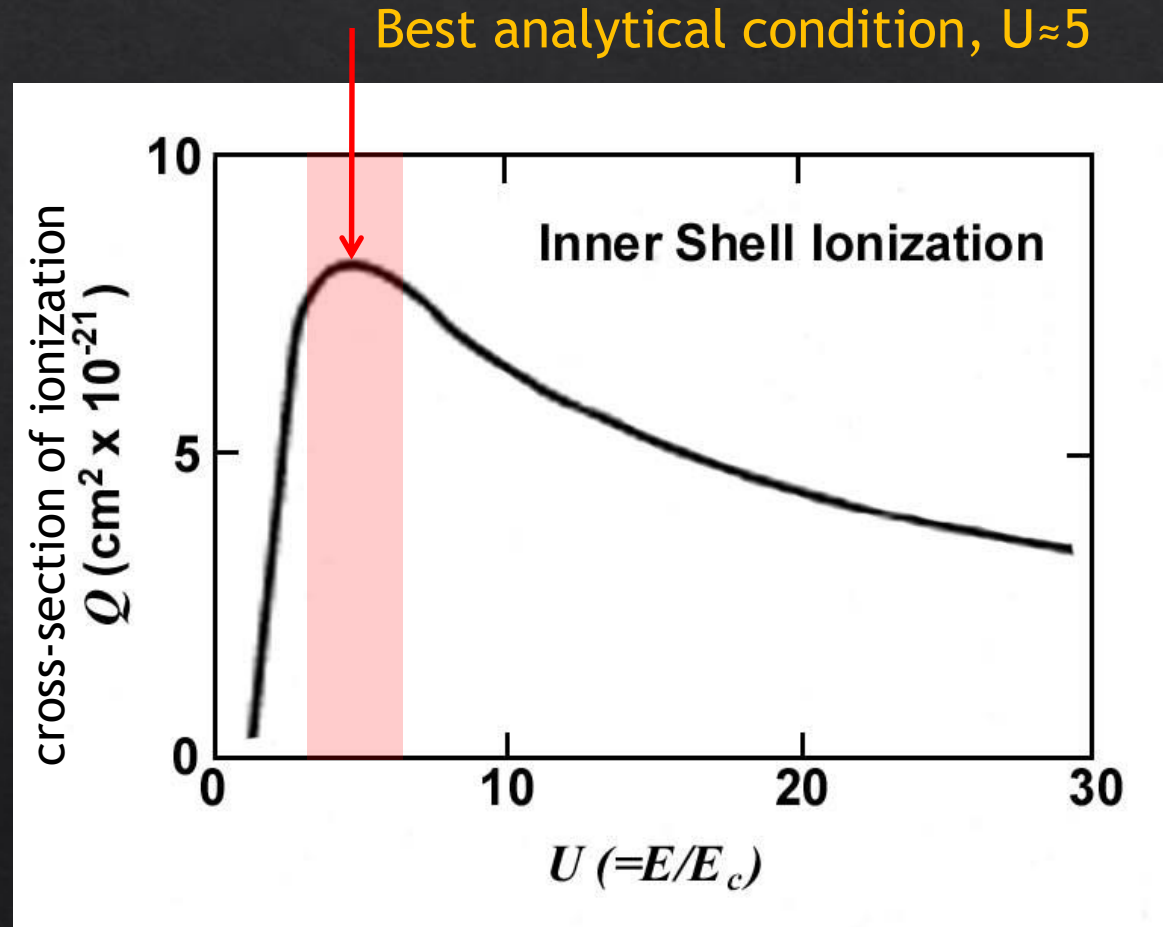
E : electron beam energy

E_c : critical excitation energy
(or, ionization energy)
of shell in target atom

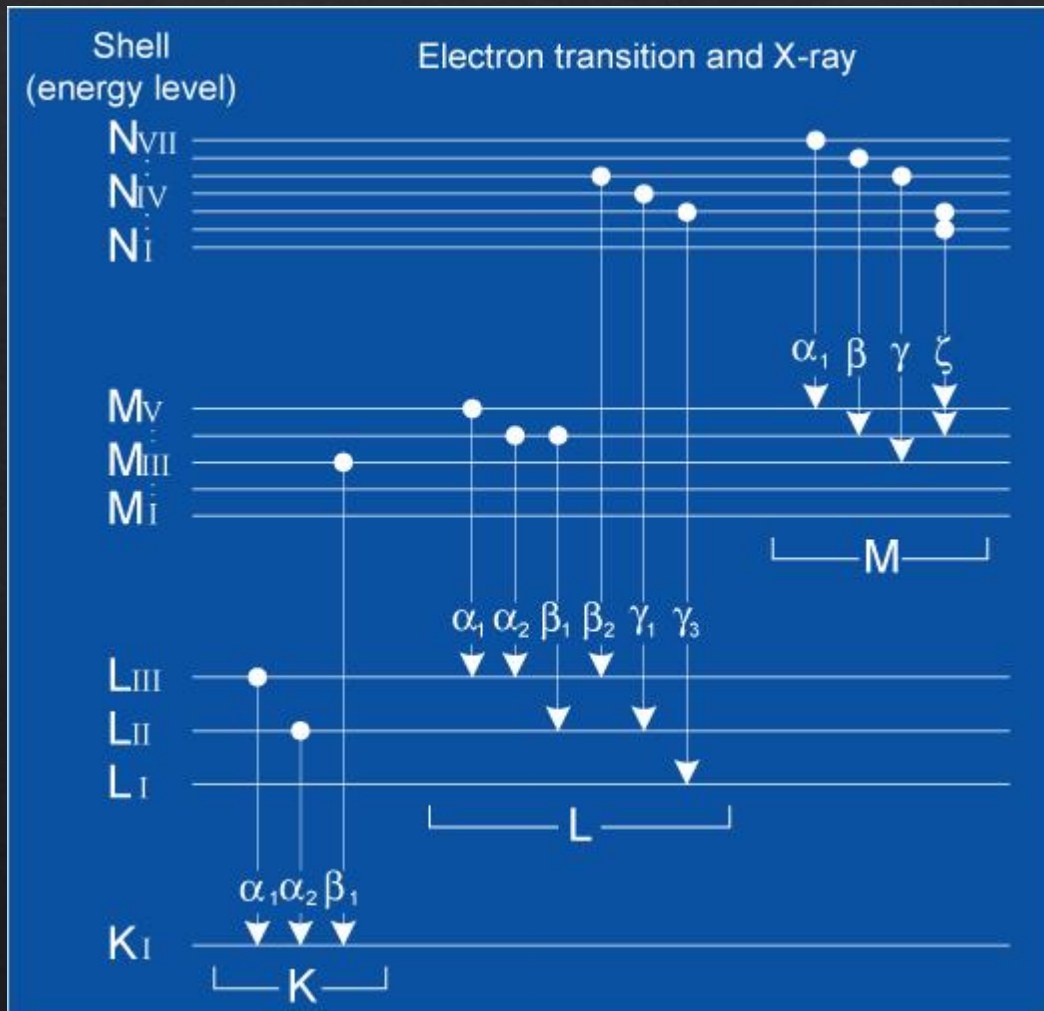


***Inner shell ionization
through inelastic scattering***

Condition for ionization: Overvoltage



Characteristic X-ray energies



<u>X-ray</u>	<u>Electron transition</u>	<u>Energy</u>
Kα	L _{II+III} to K _I	$E_{K\alpha} = E_{c(K_I)} - E_{c(L_{II+III})}$
Kβ	M _{III} to K _I	$E_{K\beta} = E_{c(K_I)} - E_{c(M_{III})}$
Lα	M _{IV+V} to L _{III}	$E_{L\alpha} = E_{c(L_{III})} - E_{c(M_{IV+V})}$
Mα	N _{VII} to M _V	$E_{M\alpha} = E_{c(M_V)} - E_{c(N_{VII})}$

Characteristic X-ray energy and critical excitation energy

The energy required to generate $UK\alpha$ must be higher than the critical excitation energy of the U K-shell, $E_{c(K)}$, i.e., overvoltage $E/E_{c(K)} > 1$

Number	92	Uranium	Name
Atomic mass	238.03	U	Symbol
Density (kg/m ³)	18.7		
	K α 98.434		Characteristic X-ray (keV)
	L α 13.612		
	M 3.164		

$$E_{c(K)} \approx 98.4 + 13.6 + 3.2$$

$$\approx 115.2 \text{ keV}$$

Required energy > 115.2 keV

To calculate $E_{c(K)}$:

Start

$$E_{K\alpha} = E_{c(K)} - E_{c(L)}$$

Rearrange

$$E_{c(K)} = E_{K\alpha} + E_{c(L)}$$

Substitute $E_{c(L)} = E_{L\alpha} + E_{c(M)}$

$$= E_{K\alpha} + (E_{L\alpha} + E_{c(M)})$$

Substitute $E_{c(M)} = E_{M\alpha} + E_{c(N)}$

$$= E_{K\alpha} + E_{L\alpha} + (E_{M\alpha} + E_{c(N)})$$

Therefore,

$$E_{c(K)} \approx E_{K\alpha} + E_{L\alpha} + E_{M\alpha}$$

Characteristic X-ray production depth (range)

Castaing's formula

$$R = 0.033 (E_0^{1.7} - E_c^{1.7}) \frac{A}{\rho Z}$$

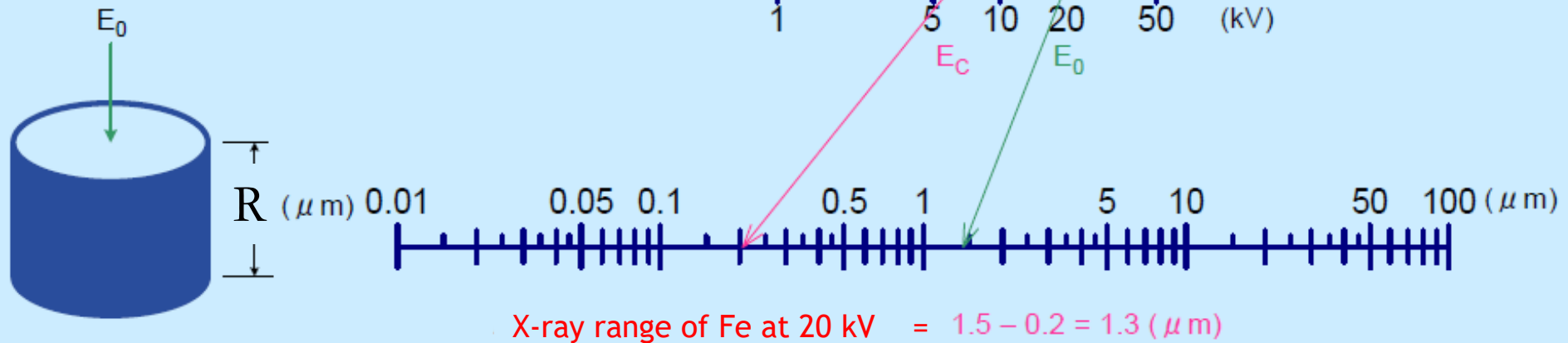
E_0 : Accelerating voltage (kV)

E_c : Critical excitation energy (keV)

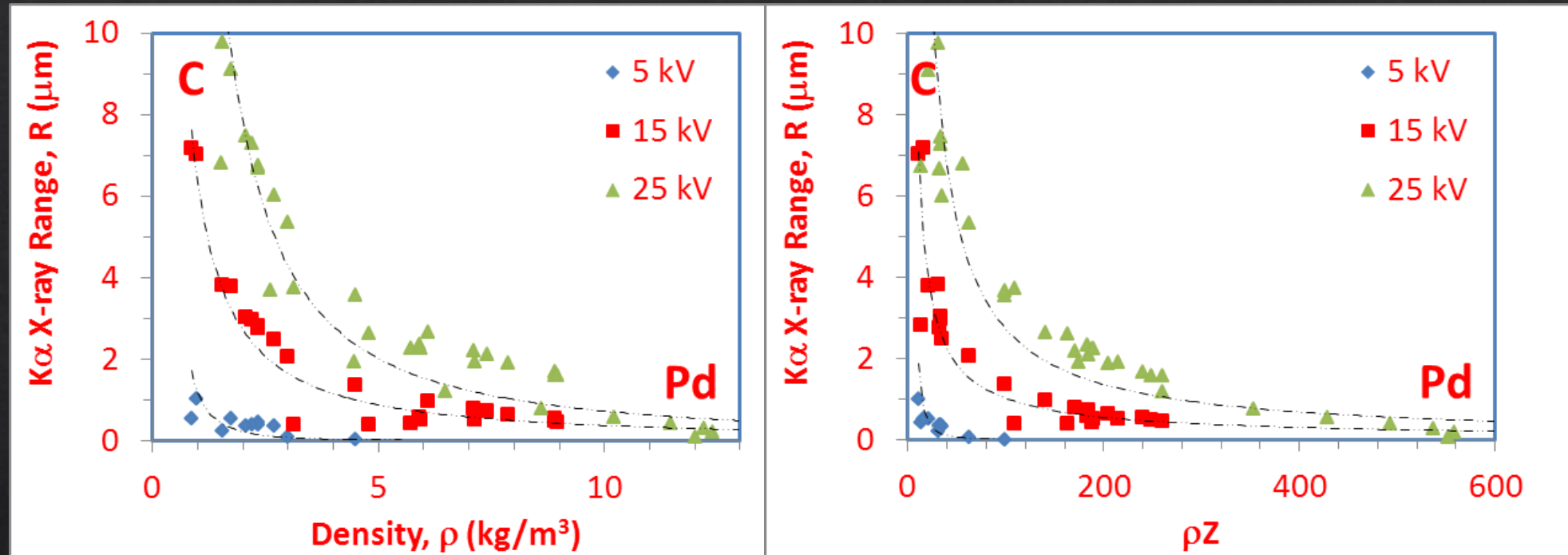
A : Atomic mass

ρ : Density (kg/m^3)

Z : Atomic number

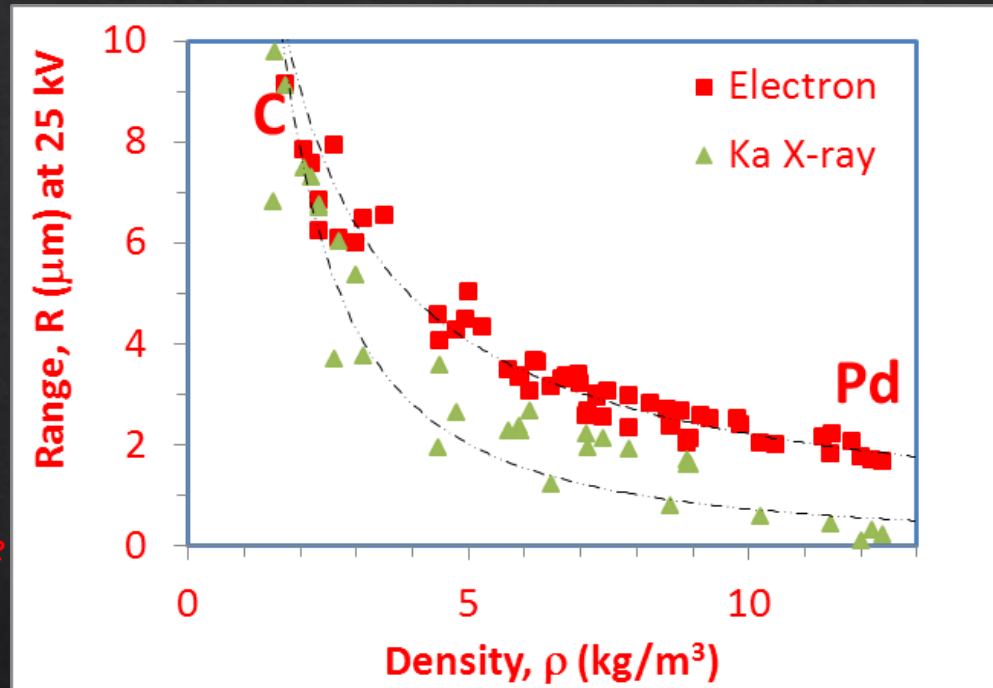
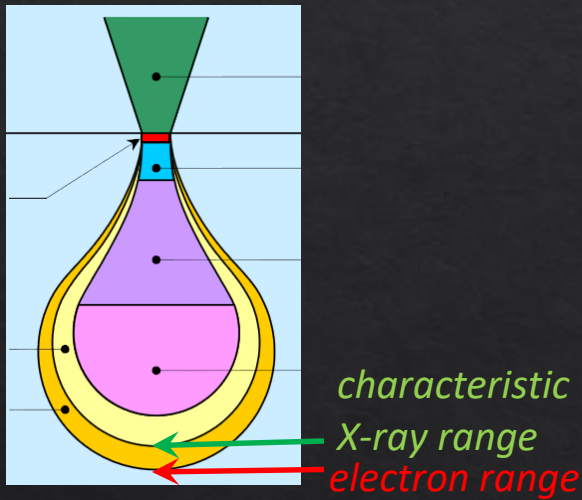


Characteristic X-ray production depth (range)



Characteristic X-ray range increases as E increases, and decreases as ρ and ρZ increase

Electron range versus Characteristic X-ray range



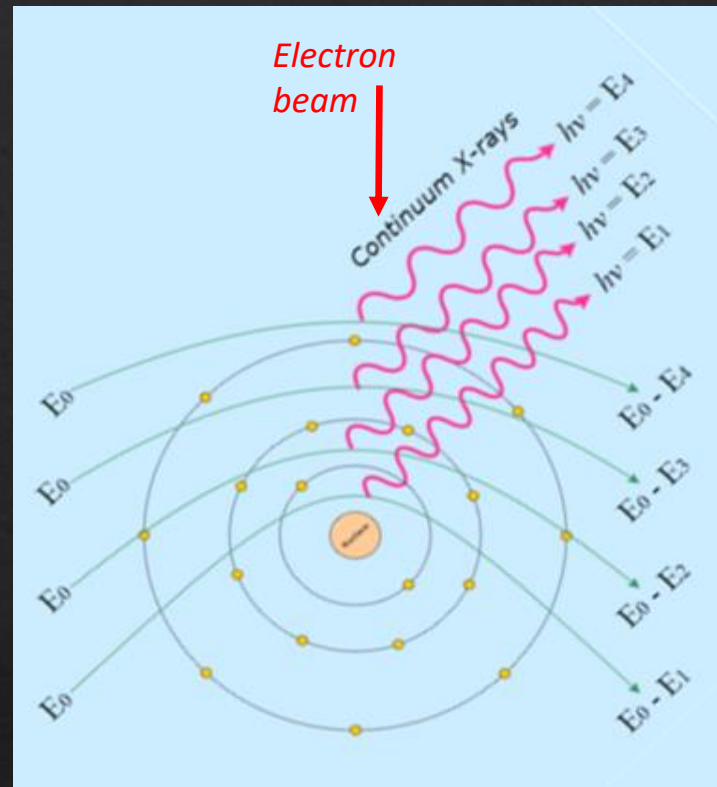
$$R_{electron} = 0.0276 E^{1.67} \frac{A}{\rho Z^{0.889}}$$

$$R_{X-ray} = 0.033 (E^{1.7} - E_c^{1.7}) \frac{A}{\rho Z}$$

E = beam energy
 E_c = critical excitation energy of the sample atomic shell
 Z = atomic number
 A = atomic weight
 ρ = density

The characteristic X-ray range is always smaller than the electron range

Continuum (Bremsstrahlung) X-ray generation

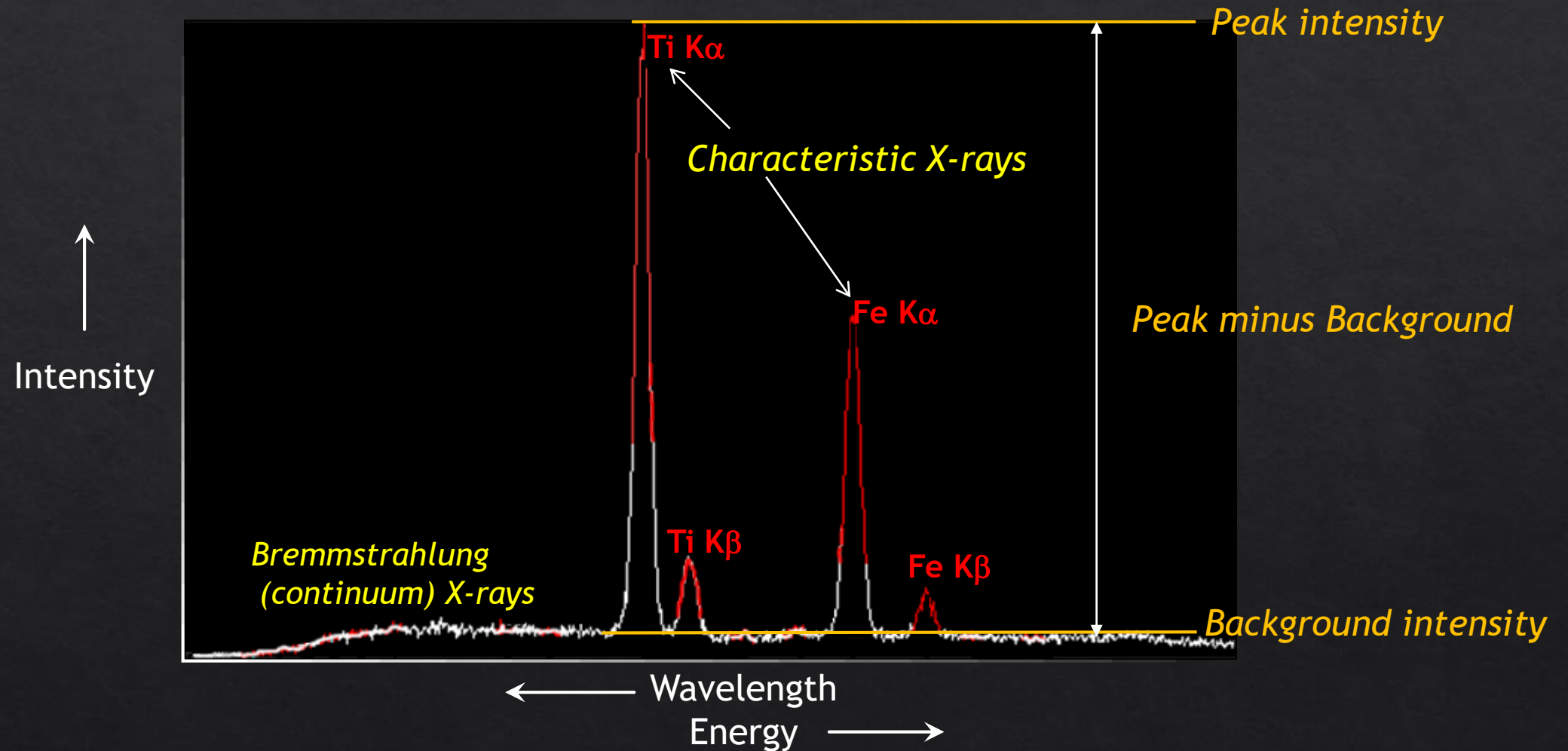


Produced by deceleration of beam electrons in the electrostatic field of target atoms

Energy lost by beam electrons is converted to x-ray

(Maximum energy of continuum X-rays = electron beam energy)

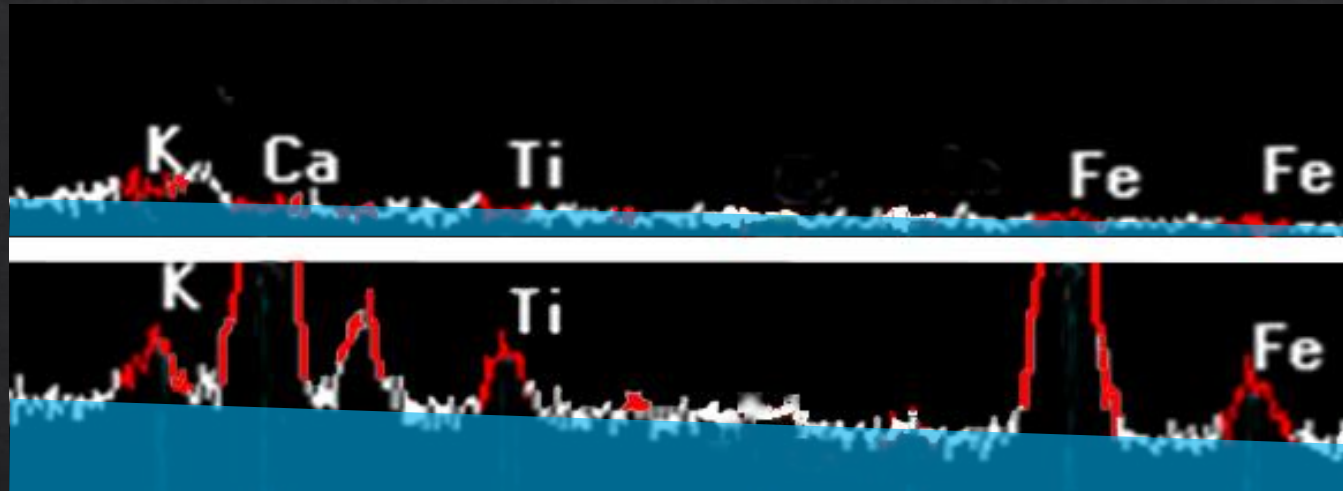
X-ray spectrum



X-ray background intensity

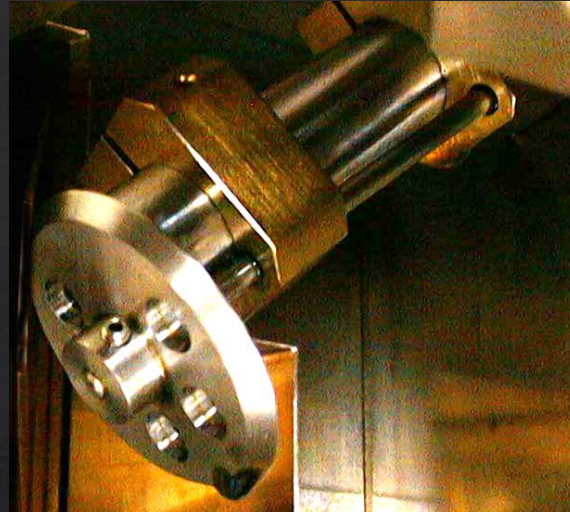
Low-Z sample
(Ca-Fe poor)
Low background

High-Z sample
(Ca-Fe rich)
High background



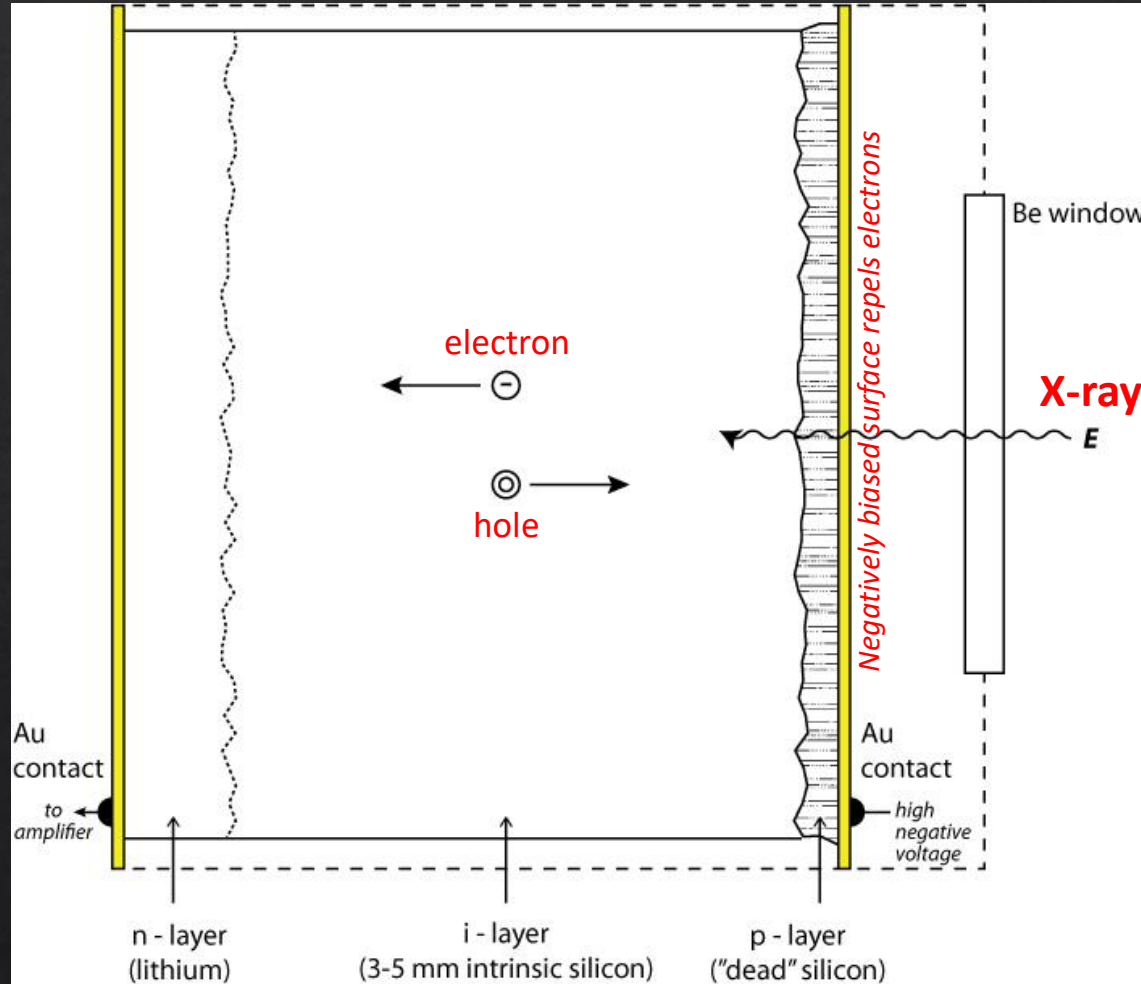
Increases with sample atomic number

Energy Dispersive Spectrometer (EDS)



- ◊ *EDS detector: solid-state semiconductor, window and aperture*
- ◊ *Multichannel analyzer (MCA) to process x-ray signal*

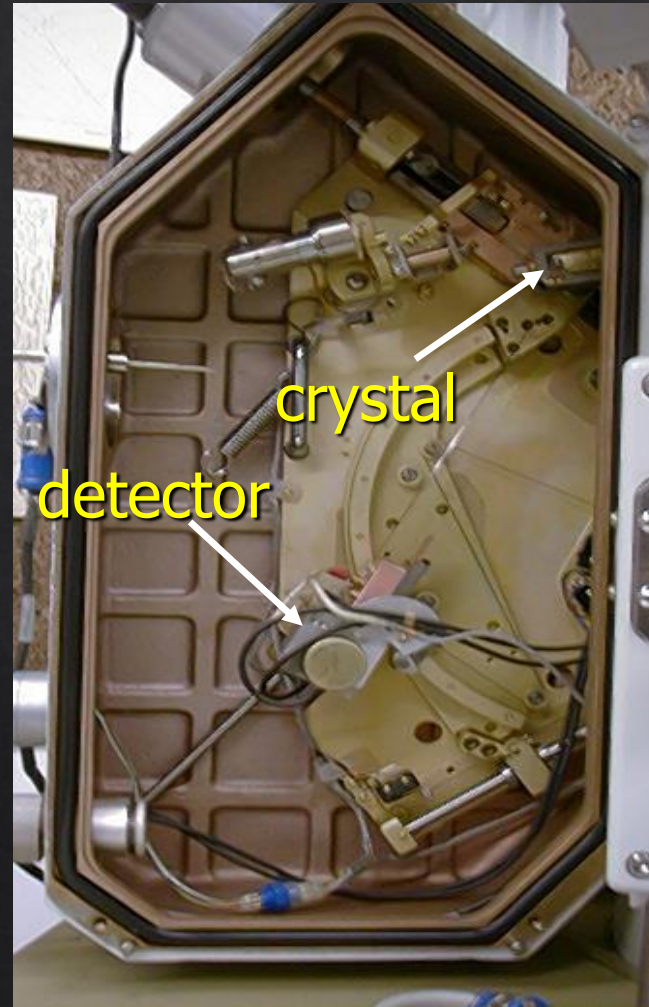
Energy Dispersive Spectrometer (EDS)



- A single crystal of silicon
- Pure Si is a semiconductor. But impurity of *boron*, a *p-type dopant*, makes it a conductor
- *Lithium*, an *n-type dopant*, counteracts the effect of boron and produces an *intrinsic semiconductor*

Lithium-drifted silicon, or Si(Li), “p-i-n” detector

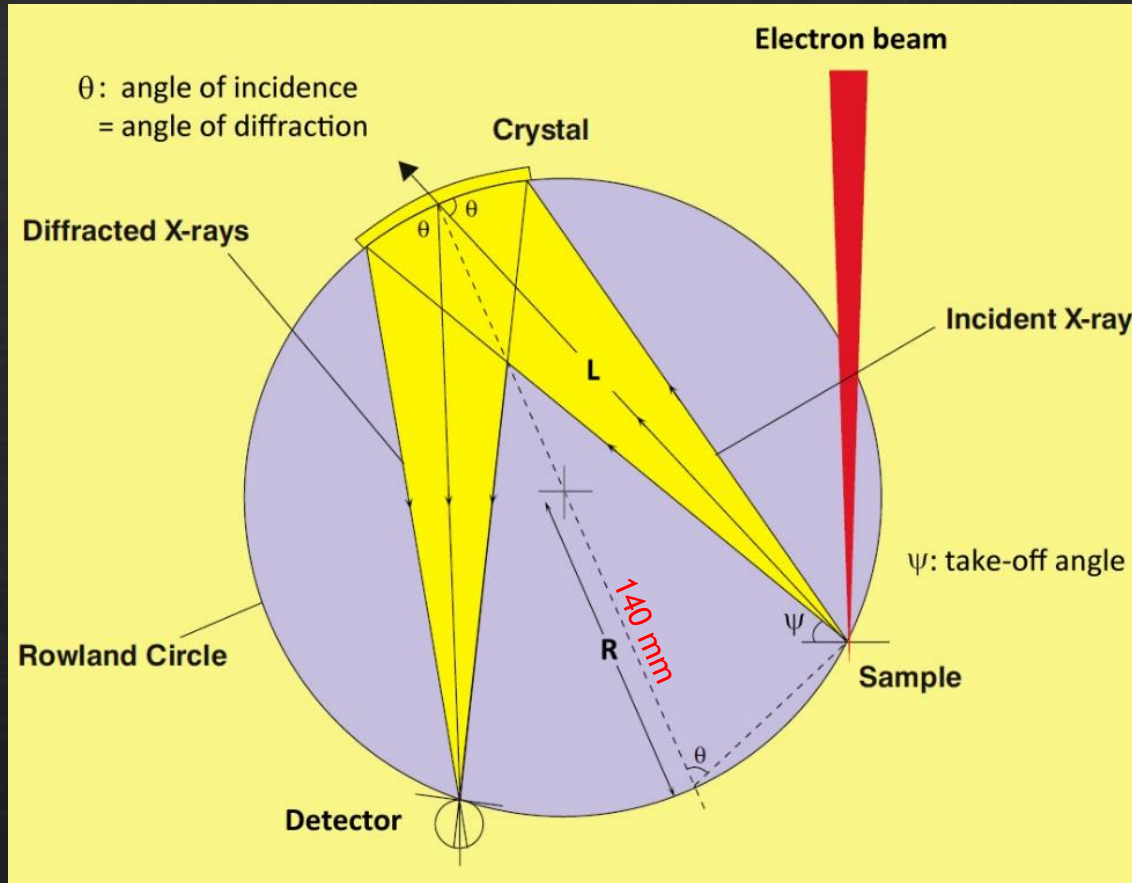
Wavelength Dispersive Spectrometer (WDS)



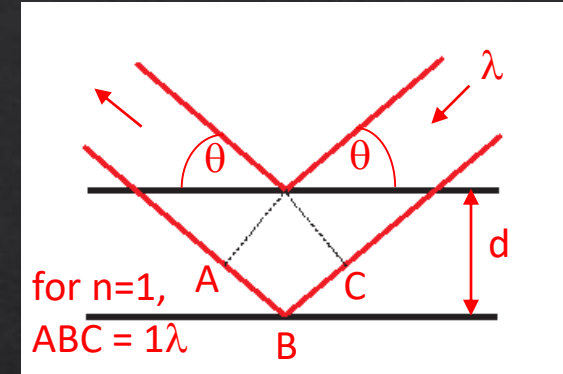
Wavelength Dispersive Spectrometer (WDS)

$$\sin \theta = \frac{L}{2R}$$

θ : angle of incidence
or diffraction
 L : distance between
sample and crystal
 R : radius of focusing
(Rowland) circle



“L-value”: $L = n\lambda \frac{R}{d}$



Bragg's Law:

$$n\lambda = 2d \sin \theta$$

n : order of diffraction
 λ : wavelength of X-ray
 d : lattice spacing in
diffracting crystal
 θ : angle of incidence or
diffraction

L-value

Example 1.

Si K α

Energy, E = 1.74 keV

$$\lambda \text{ (nm)} = \frac{1.2398}{E \text{ (keV)}}$$

$$\text{Wavelength, } \lambda = \frac{1.2398}{1.74} = 0.7125 \text{ nm}$$

$$L \text{ (mm)} = n \lambda \text{ (nm)} \frac{R \text{ (mm)}}{d \text{ (nm)}}$$

For n = 1, R = 140, and d_{TAP} = 1.2879,

$$L_{\text{TAP}} = 1 \times 0.7125 \times \frac{140}{1.2879} \\ = 77.45 \text{ mm}$$

Example 2.

U M α

Energy, E = 3.17 keV

$$\lambda \text{ (nm)} = \frac{1.2398}{E \text{ (keV)}}$$

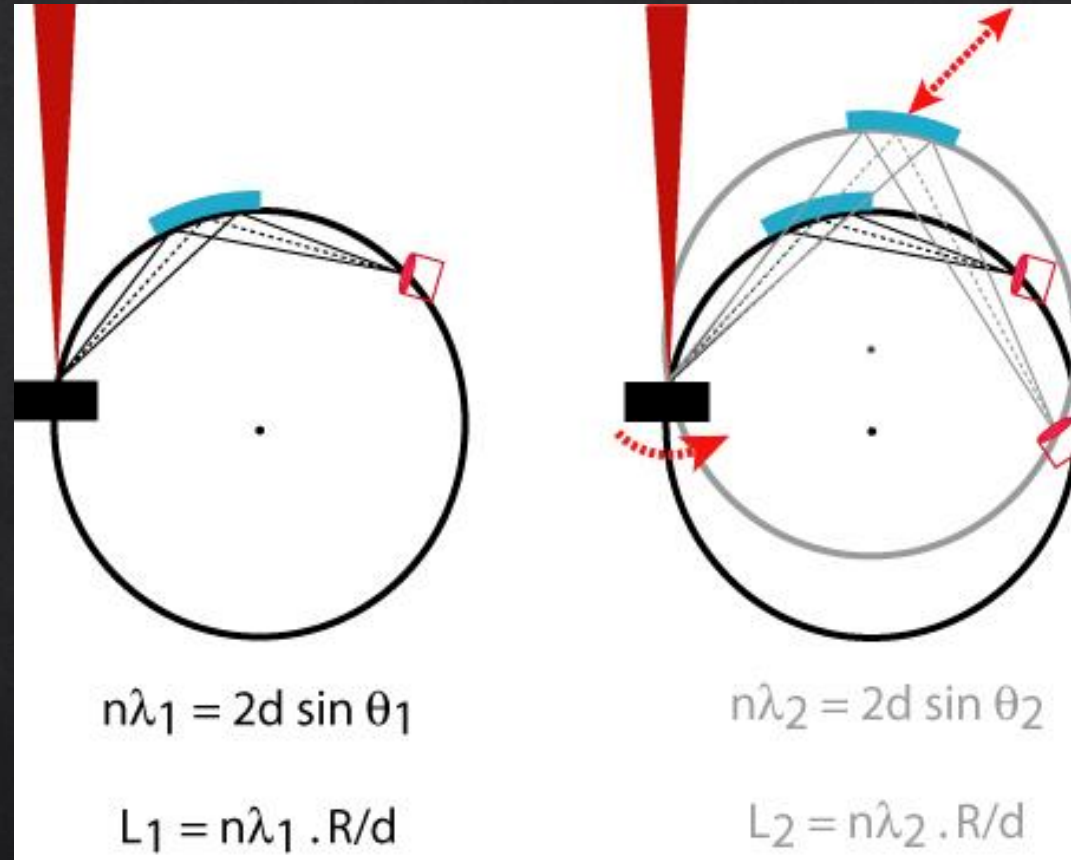
$$\text{Wavelength, } \lambda = \frac{1.2398}{3.17} = 0.3911 \text{ nm}$$

$$L \text{ (mm)} = n \lambda \text{ (nm)} \frac{R \text{ (mm)}}{d \text{ (nm)}}$$

For n = 1, R = 140, and d_{PET} = 0.4371,

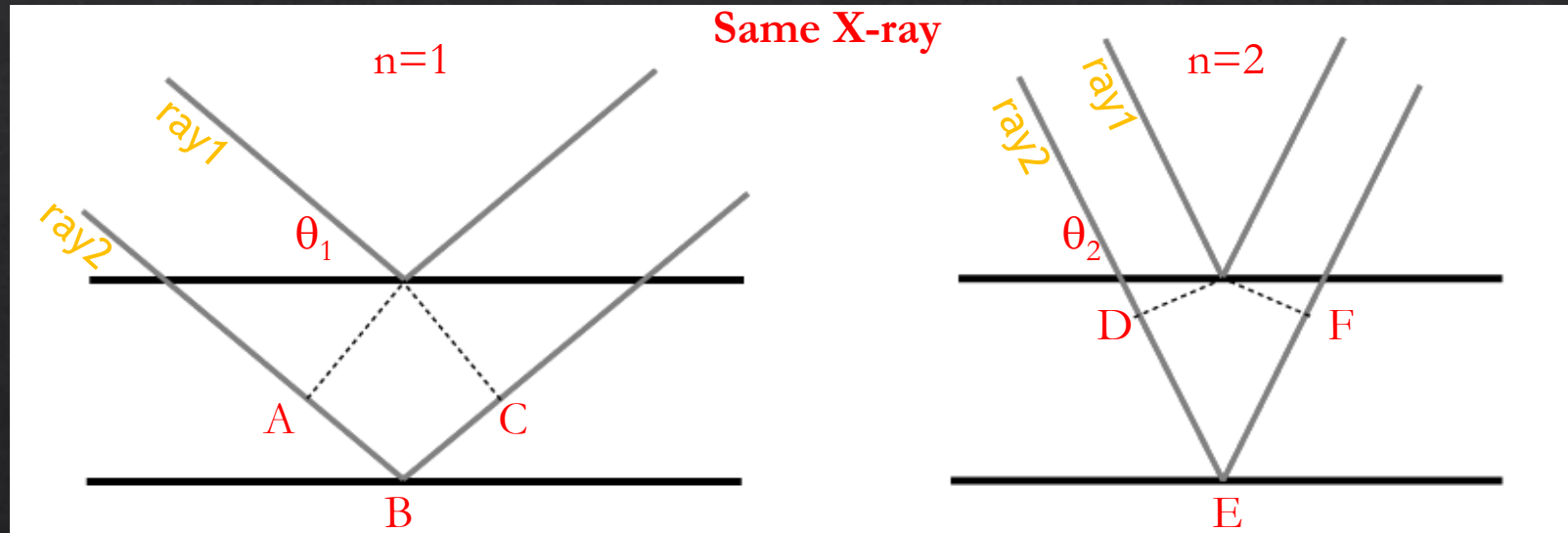
$$L_{\text{PET}} = 1 \times 0.3911 \times \frac{140}{0.4371} \\ = 125.27 \text{ mm}$$

WDS operation: detecting a specific λ



Different wavelengths (λ_1, λ_2) can be diffracted using appropriate incidence angles (θ_1, θ_2) by changing the L-value (L_1, L_2)

First and second order diffractions



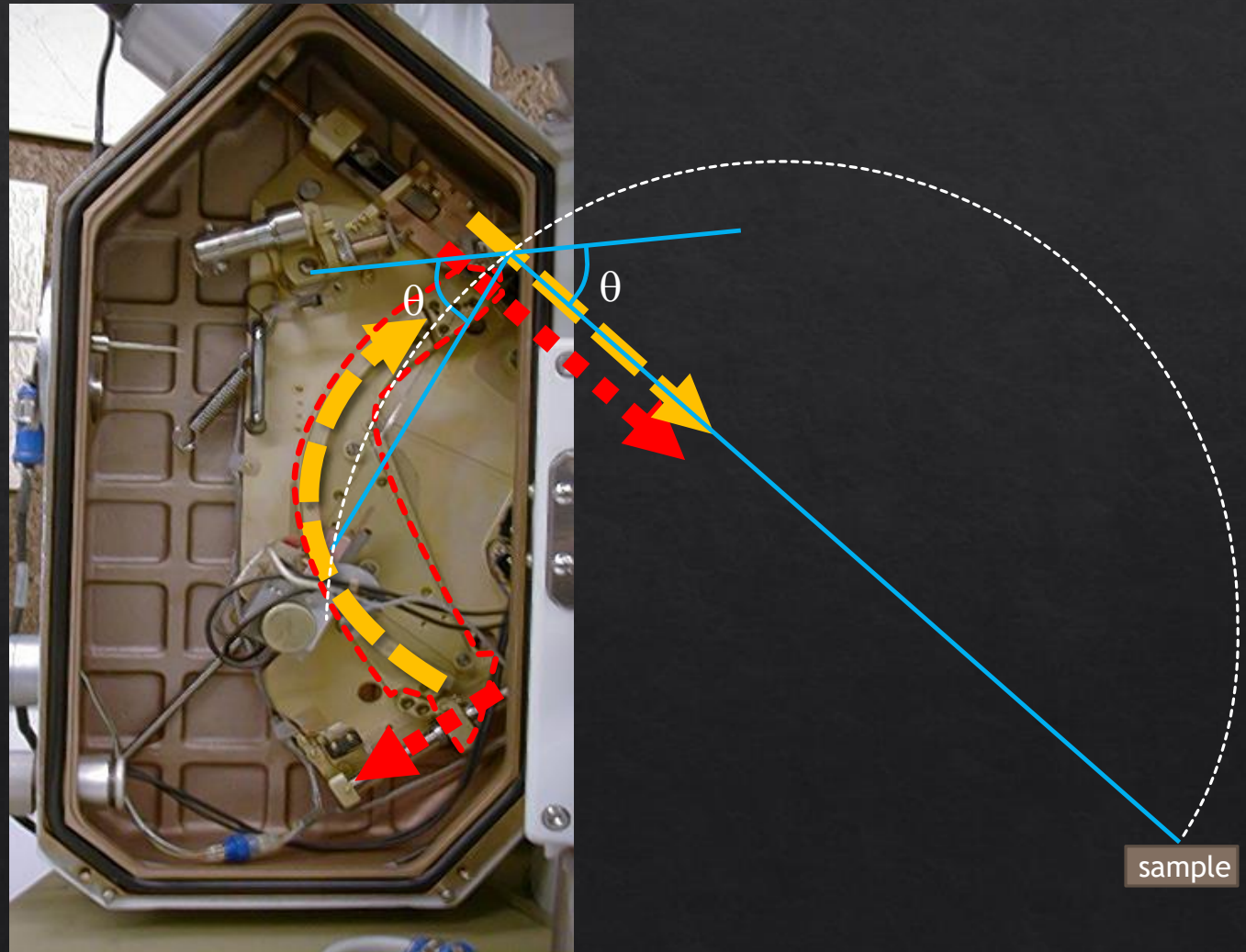
$$1\lambda = 2d \sin\theta_1 \\ = ABC$$

$$2\lambda = 2d \sin\theta_2 \\ = DEF$$

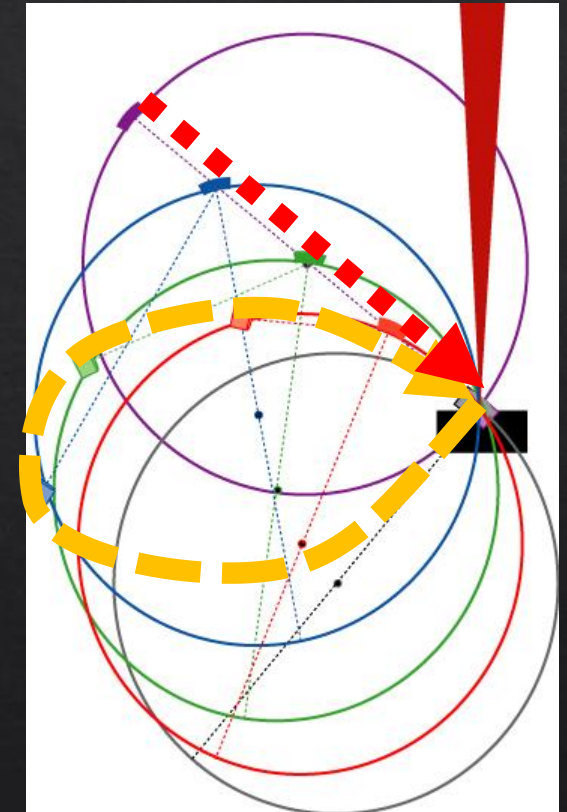
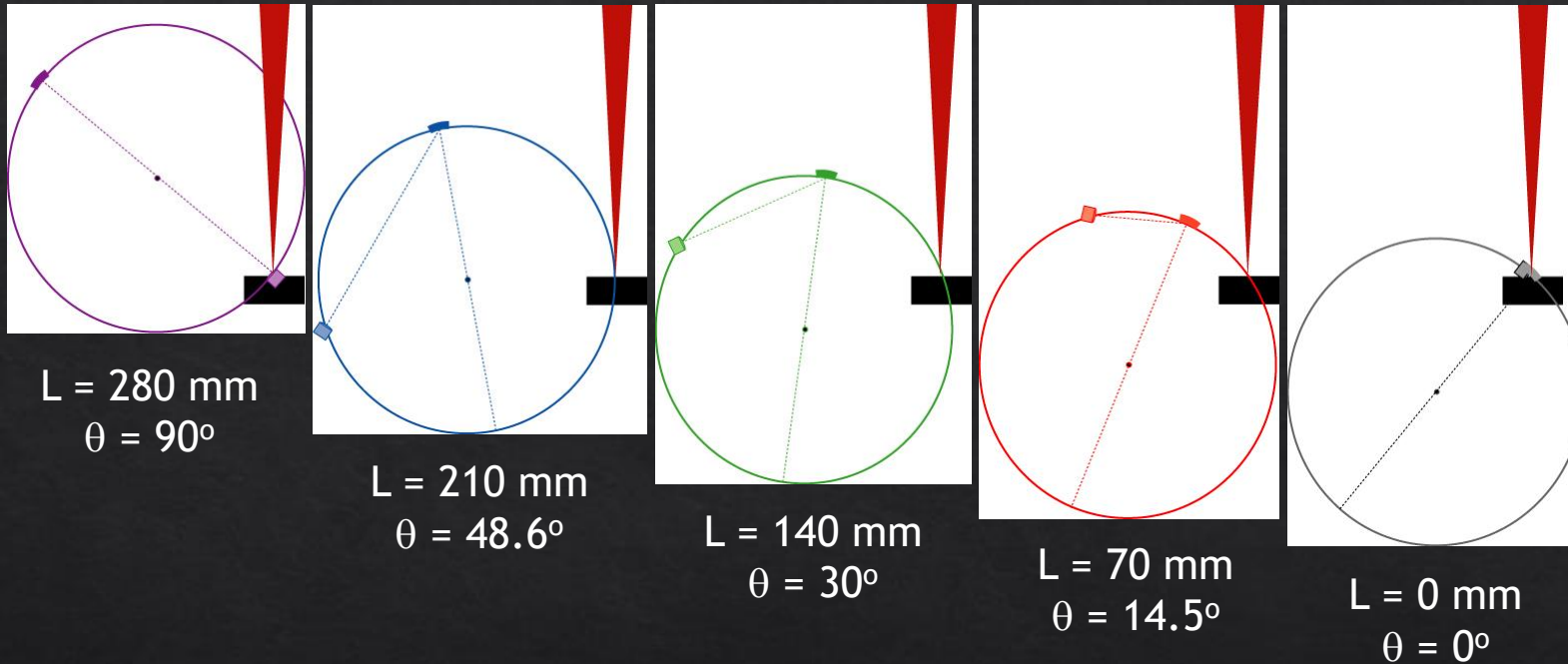
$$\text{path } DEF = 2 \times \text{path } ABC$$

Same wavelength is diffracted at different diffraction angles; $\sin\theta_2 = 2\sin\theta_1$

Spectrometer movement



Theoretical limits of spectrometer movement



Theoretical limits:

$$2R \geq L \geq 0$$

$$280 \text{ mm} \geq L \geq 0 \text{ mm}$$

$$90^\circ \geq \theta \geq 0^\circ$$

Actual limits of spectrometer movement

Actual limits:

$$60 \text{ mm} \leq L \leq 260 \text{ mm}$$

$$12.4^\circ \leq \theta \leq 68.2^\circ$$

Typically,

$$70 \text{ mm} \leq L \leq 230 \text{ mm}$$

$$14.5^\circ \leq \theta \leq 55.2^\circ$$

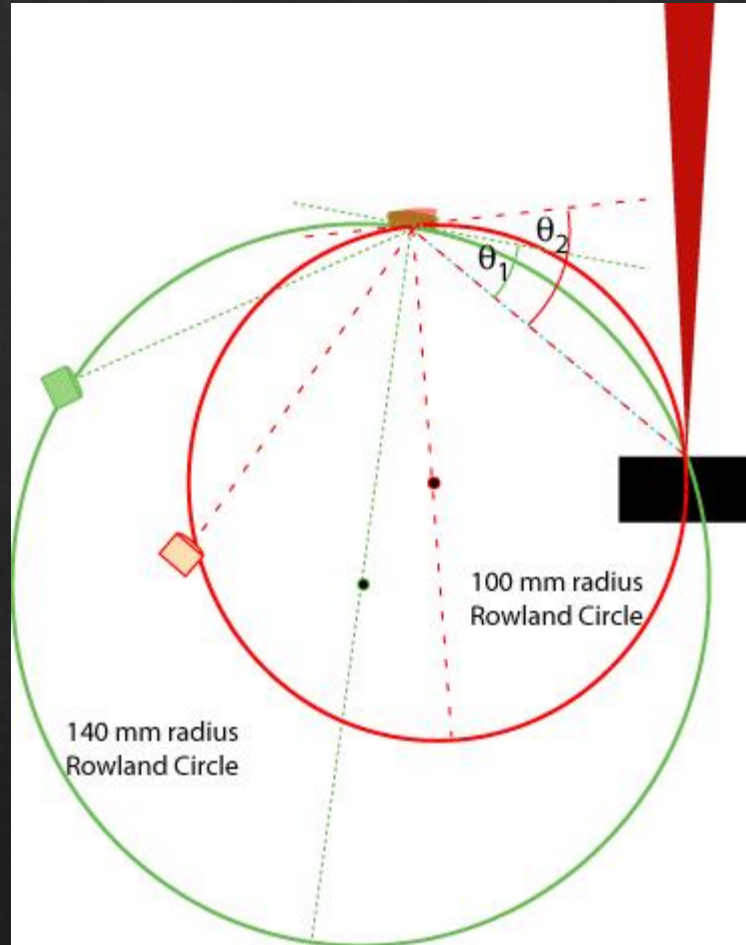
Recall $\sin\theta = \frac{L}{2R}$, so $L = 2R\sin\theta$ and $\theta = \sin^{-1}\left(\frac{L}{2R}\right)$

Hence,

for $L = 60 \text{ mm}$, $\theta = 12.4^\circ$ and $L = 260 \text{ mm}$, $\theta = 68.2^\circ$

for $\theta = 15^\circ$, $L = 72.47 \text{ mm}$ and $\theta = 55^\circ$, $L = 229.36 \text{ mm}$

Spectrometer with smaller focusing circle



140 mm focusing circle:

$$n\lambda_1 = 2d \sin \theta_1$$

$$L = n\lambda_1 \cdot 140/d$$

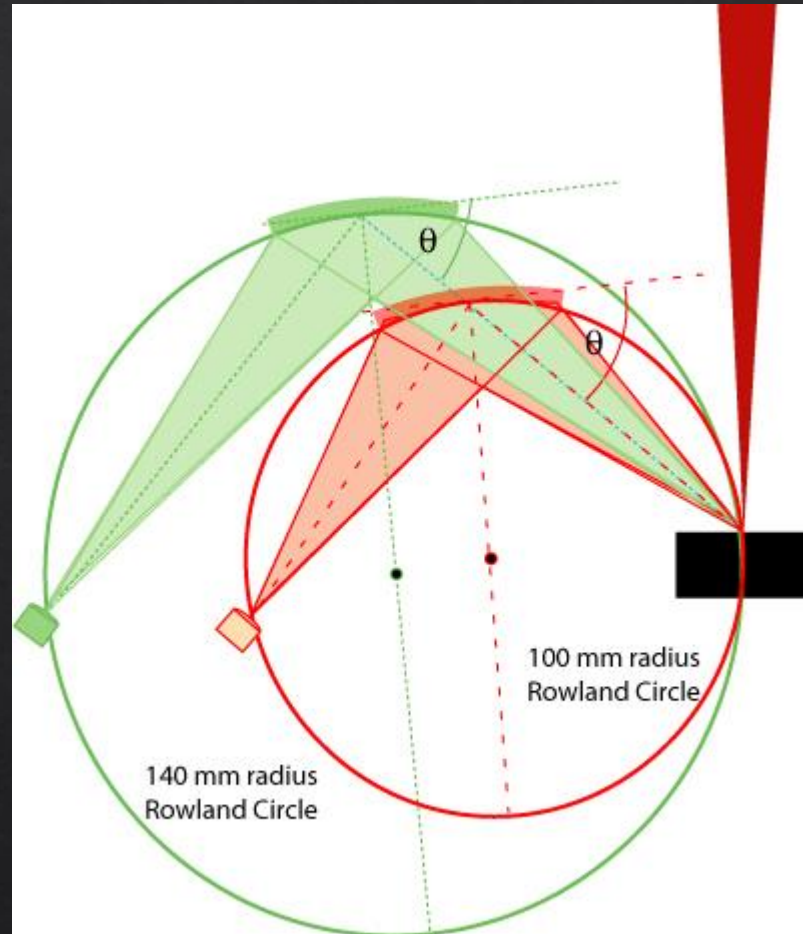
100 mm focusing circle:

$$n\lambda_2 = 2d \sin \theta_2$$

$$L = n\lambda_2 \cdot 100/d$$

*With the crystal at the same position (**same L**), different X-rays (λ_1, λ_2) are diffracted by the two spectrometers*

Spectrometer with smaller focusing circle



140 mm focusing circle:

$$n\lambda = 2d \sin \theta$$

$$L_{140} = n\lambda \cdot 140/d$$

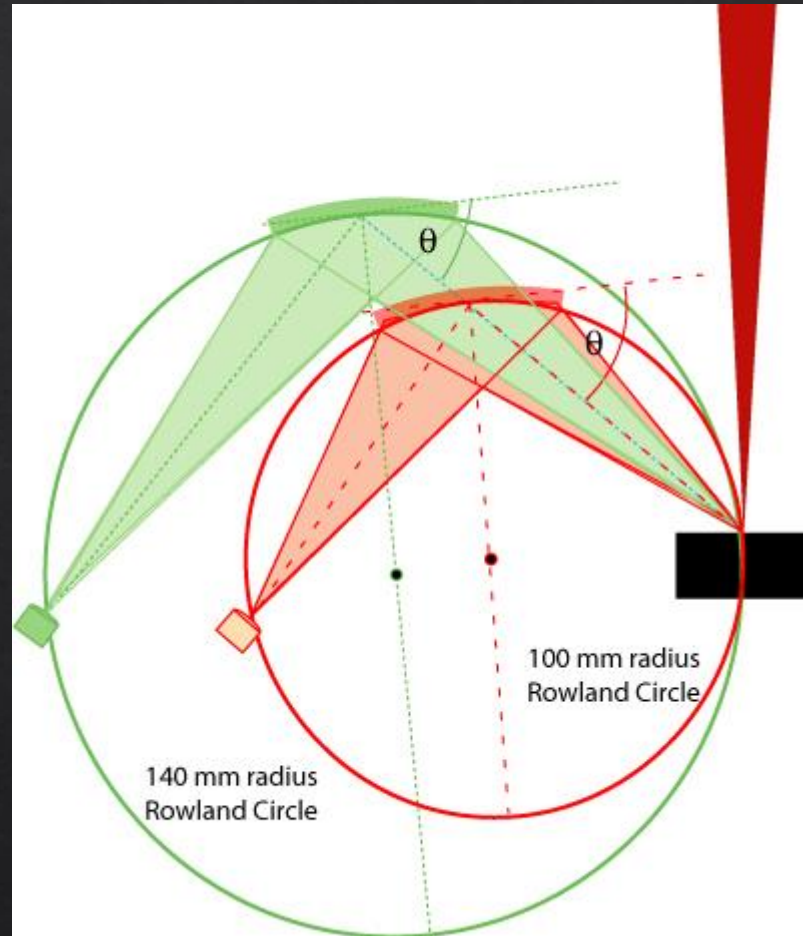
100 mm focusing circle:

$$n\lambda = 2d \sin \theta$$

$$L_{100} = n\lambda \cdot 100/d$$

With the crystal at different positions (L_{140} , L_{100}), the same X-ray (same λ) is diffracted by the two spectrometers

L values for H-type WD spectrometer



$$L_{100} = n\lambda \cdot 100/d$$

L in “L-Value Chart” is L_{140}

L_{100} is converted to L as follows:

$$\begin{aligned} L &= GR \cdot L_{100} \\ &= GR \cdot n\lambda \cdot 100/d \end{aligned}$$

where

$$\text{Gear Ratio, } GR = L_{140}/L_{100}$$

Larger Johansson-type crystal closer to sample yields a higher count rate

2d of x-ray diffractors

Crystal lattices

	2d (nm)	6 C	14 Si	22 Ti	30 Zn	38 Sr	46 Pd	54 Xe	62 Sm	70 Yb	78 Pt	86 Rn
		2.36	0.62	2.16	0.57	2.33					0.58	λ (nm)
TAP	2.576	8O	15P	24Cr	41Nb	46Pd					79Au	
TAPH	2.576	9F	13Al	24Cr	35Br	47Ag				70Yb		
PET	0.8742	13Al	25Mn	36Kr	65Tb	70Yb						
PETH	0.8742	14Si	22Ti	37Rb	56Ba	72Hf						
LIF	0.4027	19K	37Rb	48Cd								
LIFH	0.4027	20Ca	31Ga	50Sn							79Au	

$K_{\alpha,\beta}$
 $L_{\alpha,\beta}$
 $M_{\alpha,\beta,\gamma}$

For $n=1$, $\sim 0.5d < \lambda < 1.6d$ (L 73-230 mm or θ 15-55°)

Layered structures

	2d (nm)	Be	B	C	N	O	F
NSTE	Approx.10		○	○	○	○	
LDE1	Approx.6			△	◎	◎	◎
LDE2	Approx.10		◎	◎	◎	○	
LDEB	Approx.14.5	◎	○				
LDE1H	Approx.6			△	◎	◎	
LDE2H	Approx.10		◎	◎			
LDENH	Approx.8			○	◎		
LDE3H	Approx.20	◎	○				
LDE5H	Approx.8			◎	◎		
LDEBH	Approx.14.5	◎	◎				

λ of $\text{BeK}\alpha = 11.27$ nm

$\text{BeK}\alpha$ can be diffracted only by $2d > 11.27$ nm diffractors,

e.g., LDE3H with L= 157.8 mm, and LDEB or LDEBH with L=217.6 mm

X-ray diffractors

Analyzing crystals
and
layered structures

Table 4.6 Analyzing crystals and element analysis ranges for X-ray spectrometer

Analyzing crystals	2d (nm)	Type of spectrometer	¹⁰ Ne ¹⁰ Ca ¹⁰ Zn ¹⁰ Zr ¹⁰ Sn ¹⁰ Nd ¹⁰ Yb ¹⁰ Hg ¹⁰ Th
NEWSTE	10.04	TXE	¹⁰ B ¹⁰ O ¹⁰ S ¹⁰ V
TAPJ	2.5757	XCE	¹⁰ O ¹⁰ P ¹⁰ Cr ¹⁰ Nb ¹⁰ Pd ¹⁰ Au
		TXE	¹⁰ O ¹⁰ P ¹⁰ Cr ¹⁰ Nb ¹⁰ Pd ¹⁰ Hg
PETJ	0.8742	XCE	¹⁰ Al ¹⁰ Mn ¹⁰ Kr ¹⁰ Tb ¹⁰ Yb ¹⁰ U
		TXE	¹⁰ Al ¹⁰ Fe ¹⁰ Kr ¹⁰ Dy ¹⁰ Yb ¹⁰ U
LIF	0.40267	XCE, TXE	¹⁰ K ¹⁰ Rb ¹⁰ Cd ¹⁰ U
LDE1	About 6	XCE, TXE	¹⁰ C ¹⁰ Ne
LDE2	About 10	XCE, TXE	¹⁰ B ¹⁰ O
LDEB	About 14.5	XCE, TXE	¹⁰ Be ¹⁰ B
TAPH	2.5757	H	¹⁰ F ¹⁰ Al ¹⁰ Cr ¹⁰ Br ¹⁰ Ag ¹⁰ Yb
PETHS	0.8742	H	¹⁰ Si ¹⁰ Ti ¹⁰ Rb ¹⁰ Ba ¹⁰ Hf ¹⁰ U
LIFHS	0.40267	H	¹⁰ Ca ¹⁰ Ga ¹⁰ Sn ¹⁰ Au
LDE1H	About 6	H	¹⁰ C ¹⁰ O
LDE2H	About 10	H	¹⁰ B ¹⁰ C
LDE3H	About 20	H	¹⁰ Be ¹⁰ B
LDE4H	About 12	H	¹⁰ B ¹⁰ C
LDE5H	About 8	H	¹⁰ C ¹⁰ N
LDENH	About 8	H	¹⁰ C ¹⁰ N
LDEBH	About 14.5	H	¹⁰ Be ¹⁰ B

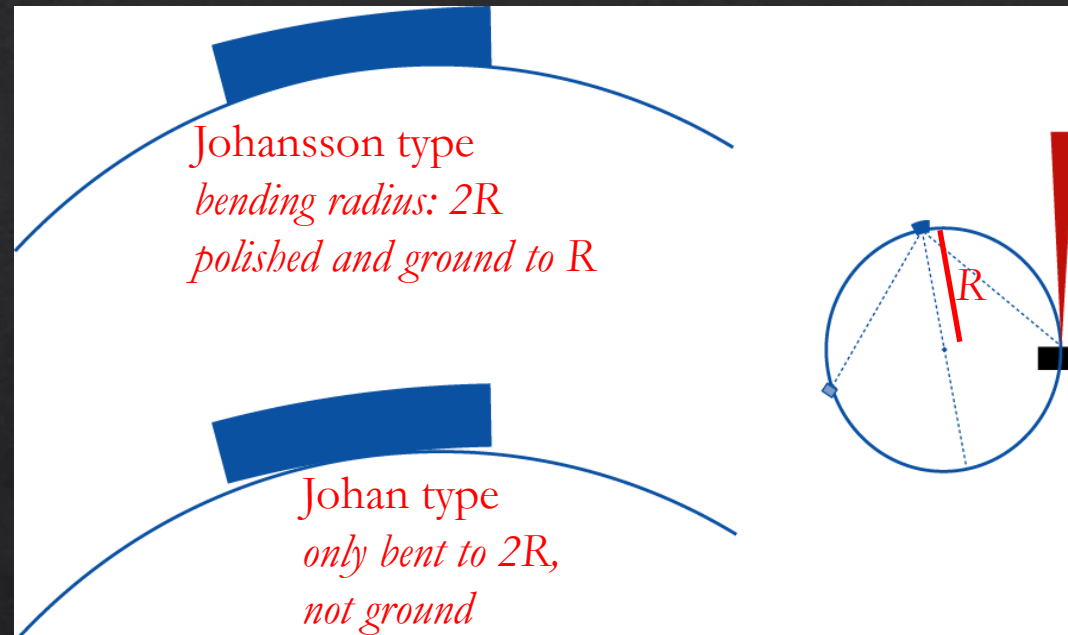
R line (K α or K β)

L line (L α or L β)

M line (M α , M β or M γ)

XCE: XCE type X-ray spectrometer (XM-86010)
TXE: TXE type X-ray spectrometer (XM-86020)
H: H type X-ray spectrometer (XM-86030)

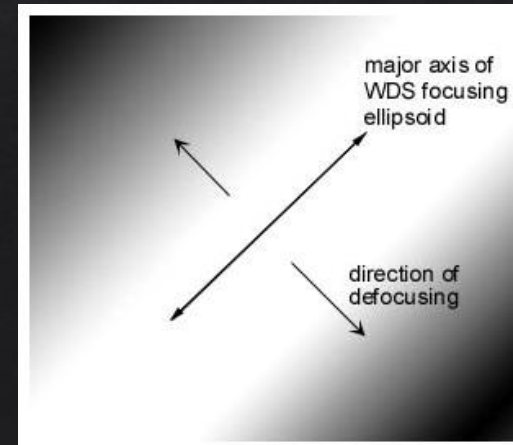
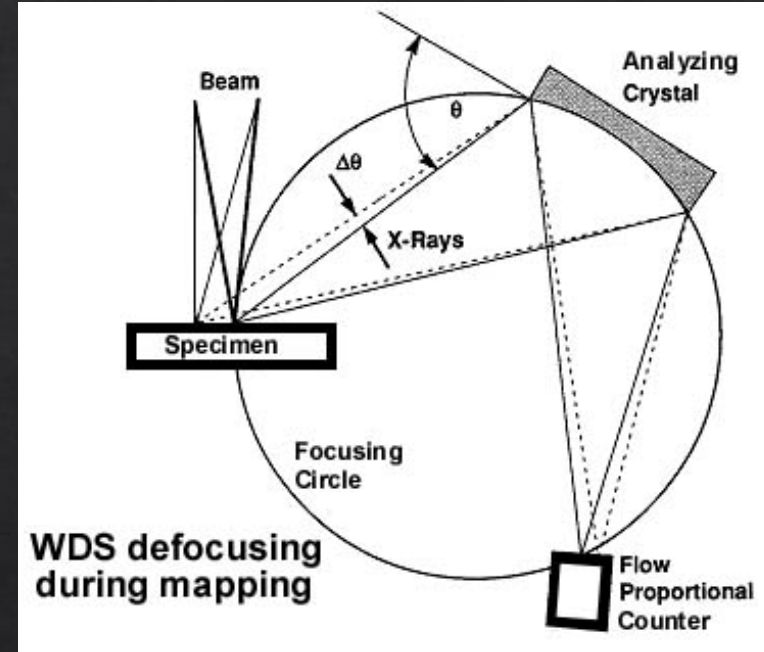
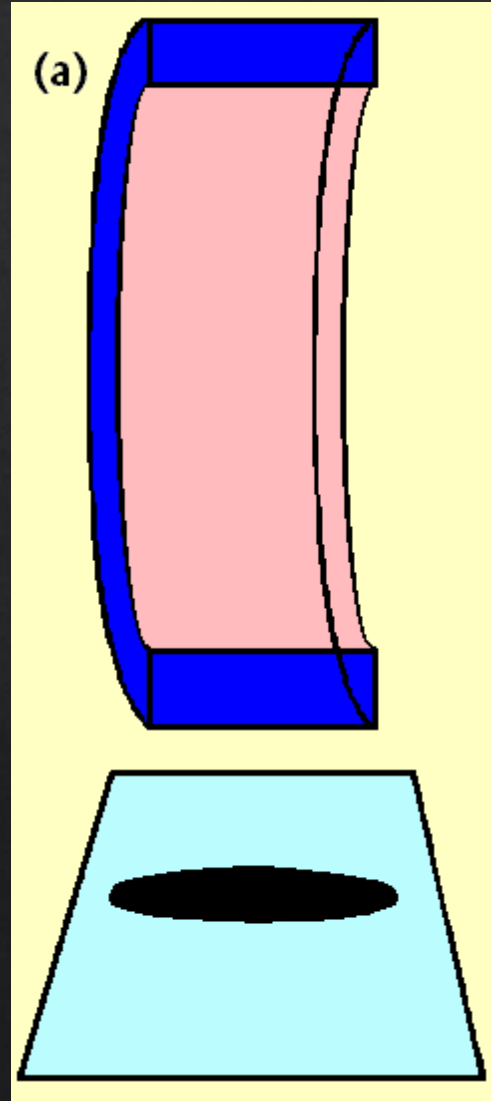
Curved diffracting crystals



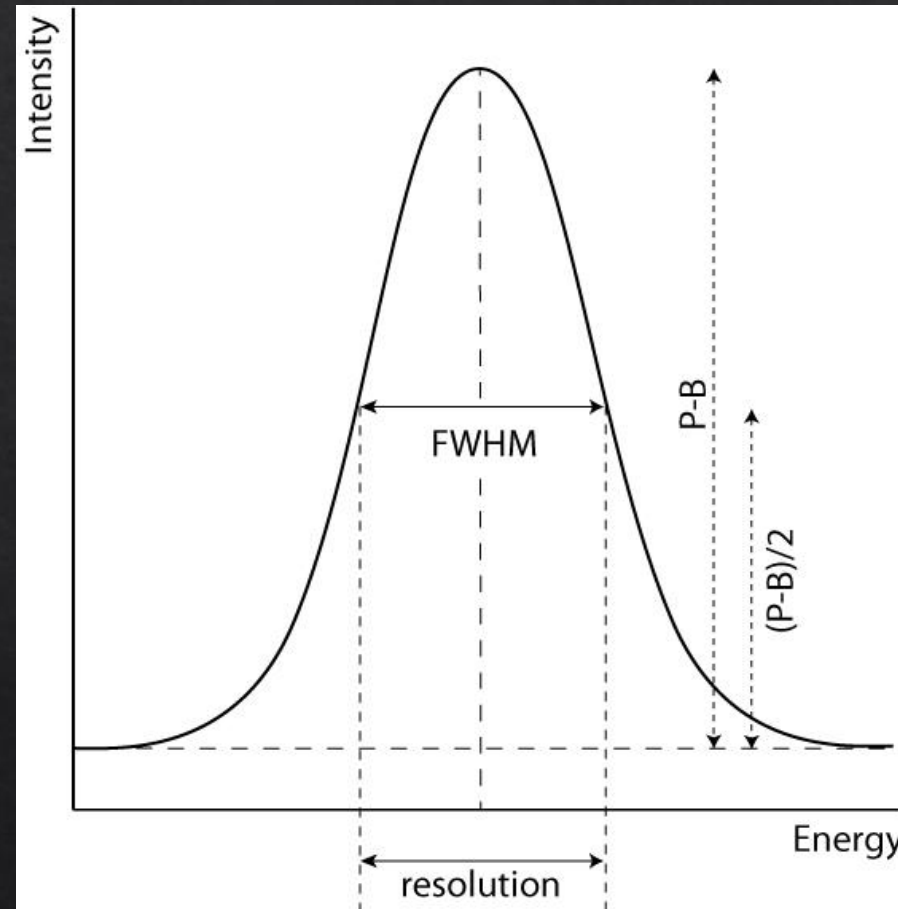
Peak resolution with fully focusing **Johansson-type** crystal: FWHM ~ 10 eV

Some defocusing in **Johan-type**, but resolution is not compromised

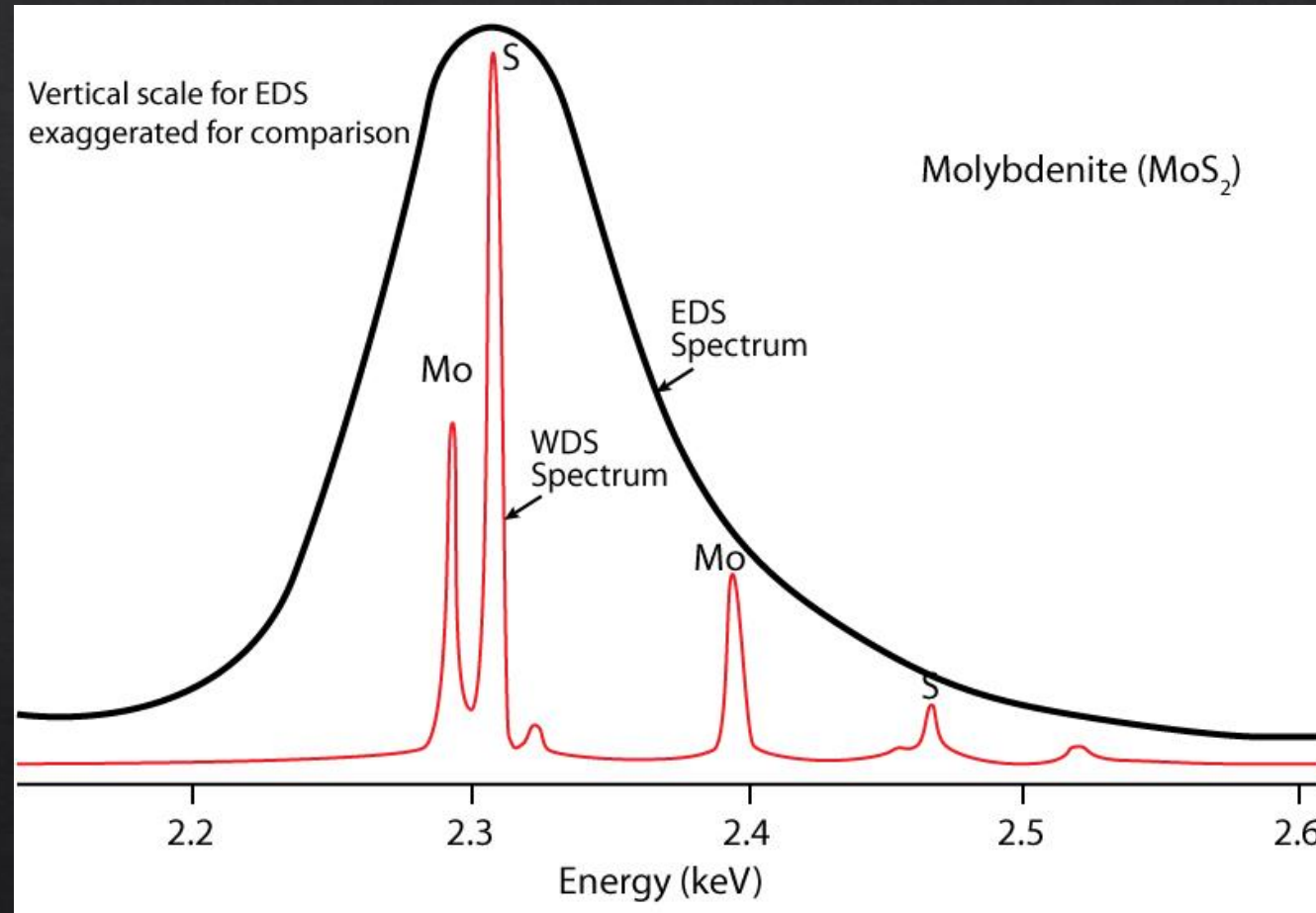
X-ray focusing ellipsoid



Spectral resolution: Full-Width Half-Maximum (FWHM)



WDS vs. EDS spectral resolution

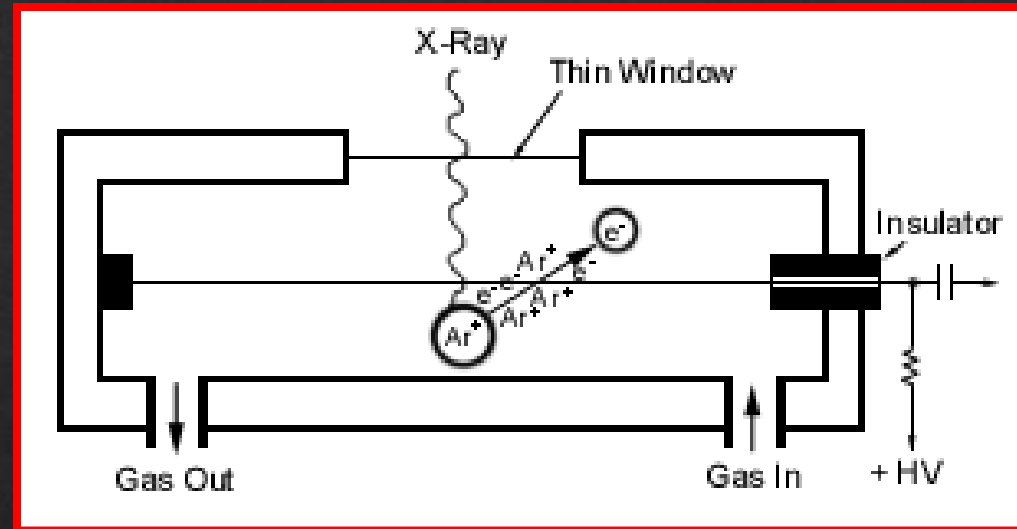


*Peak overlaps
in EDS
spectrum*

*Peak resolution of **WDS spectrum (FWHM ~10 eV)**
EDS spectrum (FWHM ~150 eV)*

WDS detector: Proportional counter

*Tungsten collection wire
at 1-3 kV voltage*



- *Pulse voltage generated is proportional to the voltage in the collection wire*
- *Signal is amplified through a chain of outer-shell ionizations in the gas by the incoming X-ray*

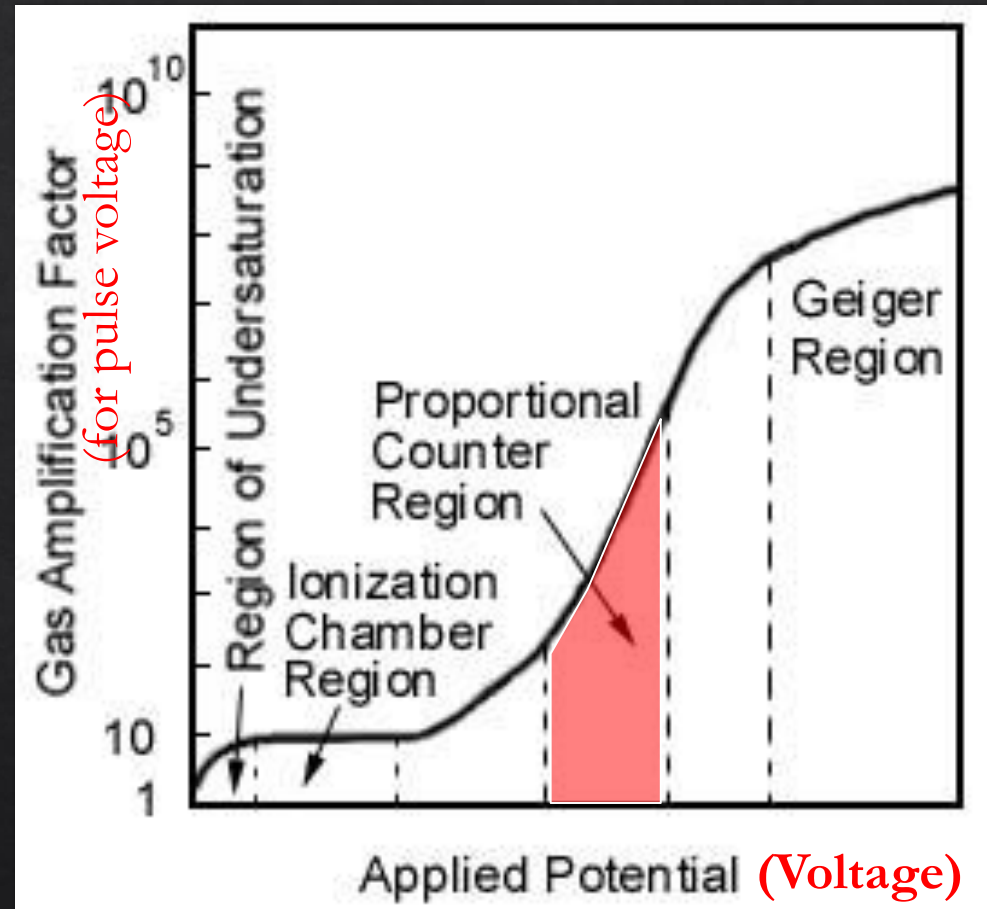
◇ Flow counter:

- ◇ *P-10 gas (90% Argon + 10% methane quenching agent)*
- ◇ *Polypropylene window*

◇ Sealed counter:

- ◇ *Xenon gas*
- ◇ *Beryllium window*

Signal amplification



The amplification factor is *proportional to the voltage in the collection wire* in the proportional counter region

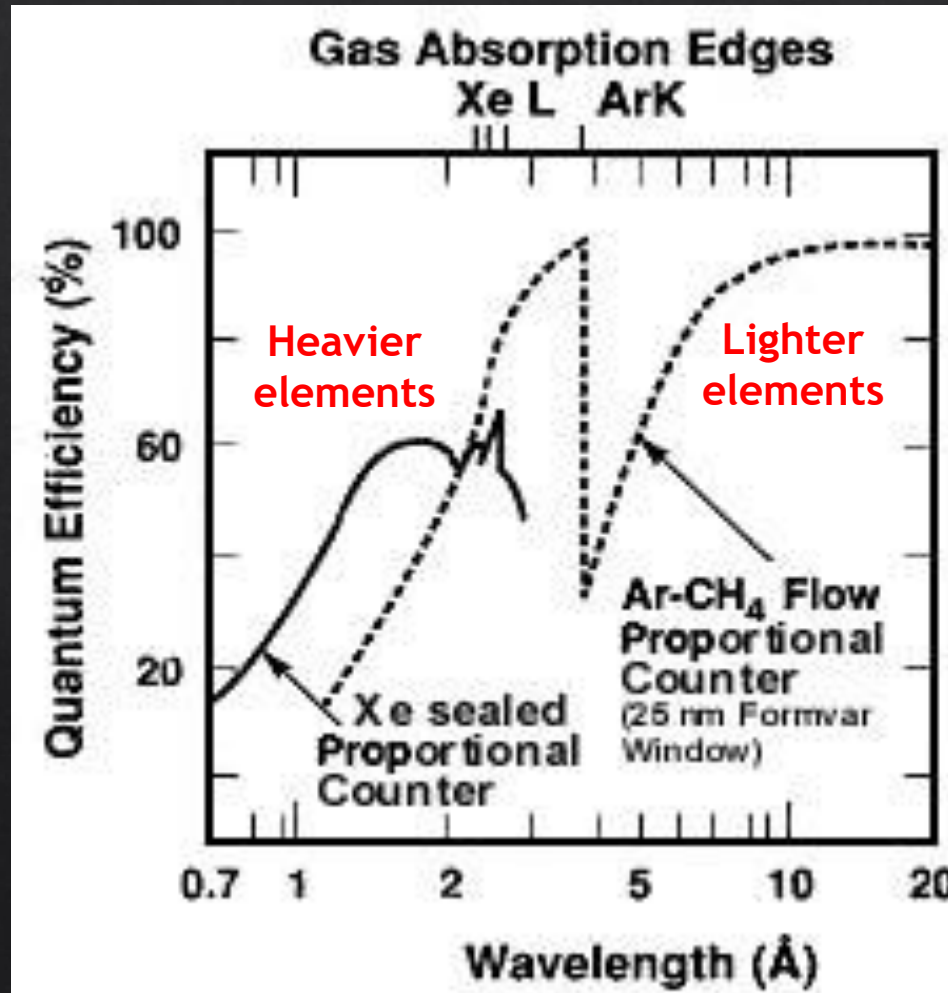
Typical voltage range in the proportional counter region for a W wire: 1600-1850 V

Quantum efficiency of counter gas

Highest when the incoming X-ray is least absorbed by the gas

Decreases when the X-ray is absorbed by ionizing an inner shell of the gas atom, generating $\text{ArK}\alpha$ or $\text{XeL}\alpha$

Lowest when $E_{\text{X-ray}}$ is slightly higher than the $E_{c(\text{Ar K-shell})}$ or $E_{c(\text{Xe L-shell})}$ absorption edges



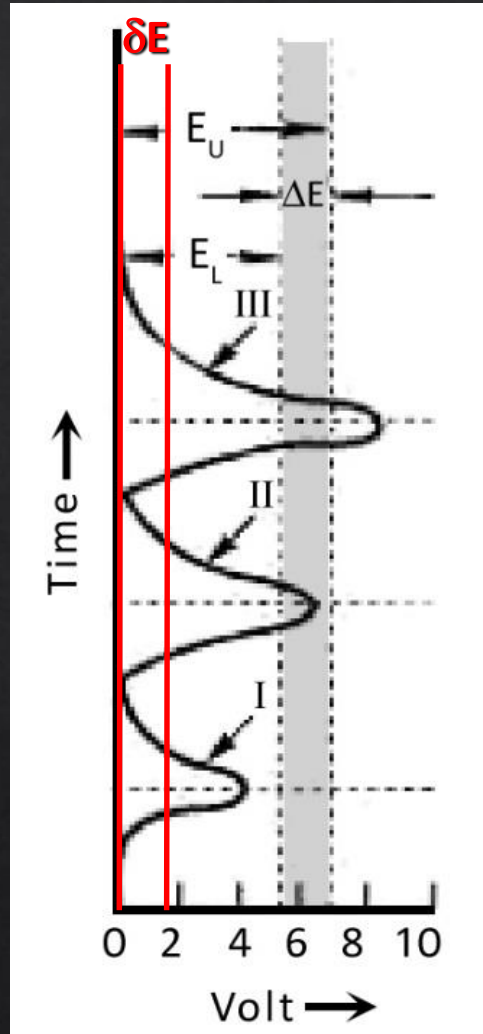
- Argon: **long wavelength** (low energy) detection
- Xenon: **short wavelength** (high energy) detection

Proportional counter setup

Proportional counter output:
Voltage pulses
including noise
and X-ray signal

*Voltage pulses
including noise
and X-ray signal*

A *Single Channel Analyzer (SCA)* allows only X-ray pulses to pass through ΔE and enter the detector

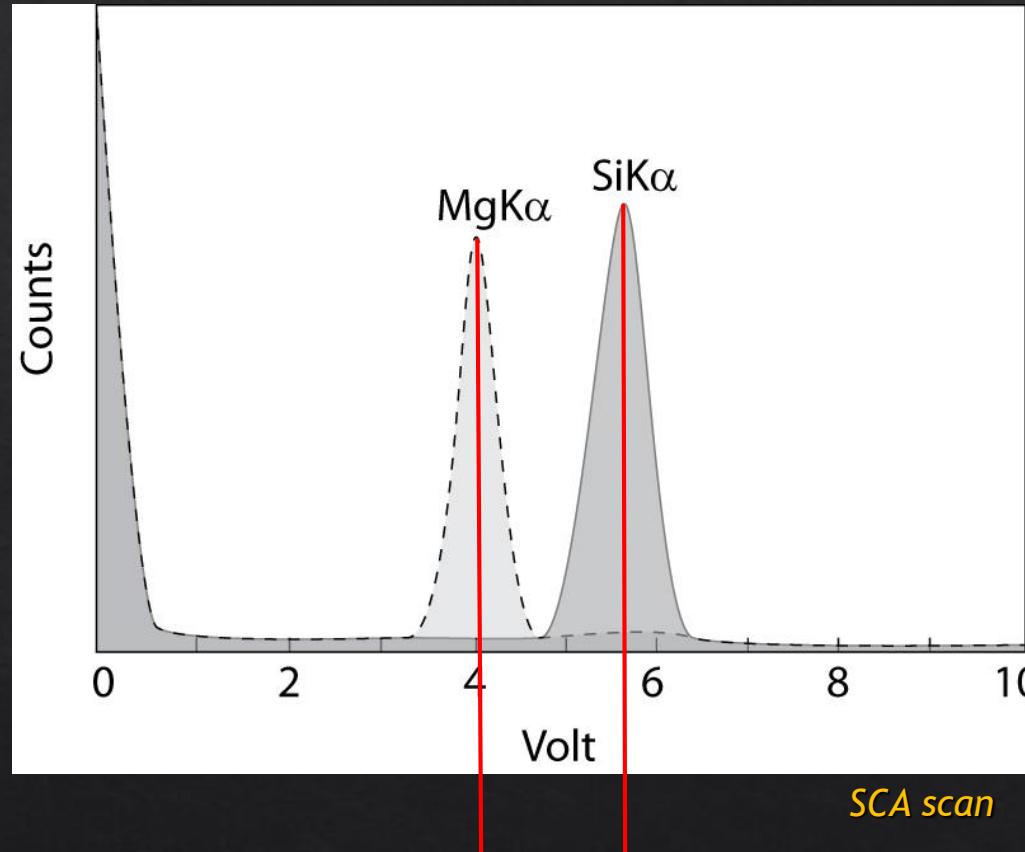


An SCA scan shows the variation in count rate as a small voltage window (δE) is moved across the voltage range

Baseline and window voltages (ΔE) are set to filter out noise

ΔE is determined through *Pulse Height Analysis (PHA)* using an SCA scan

Pulse voltage in SCA scan

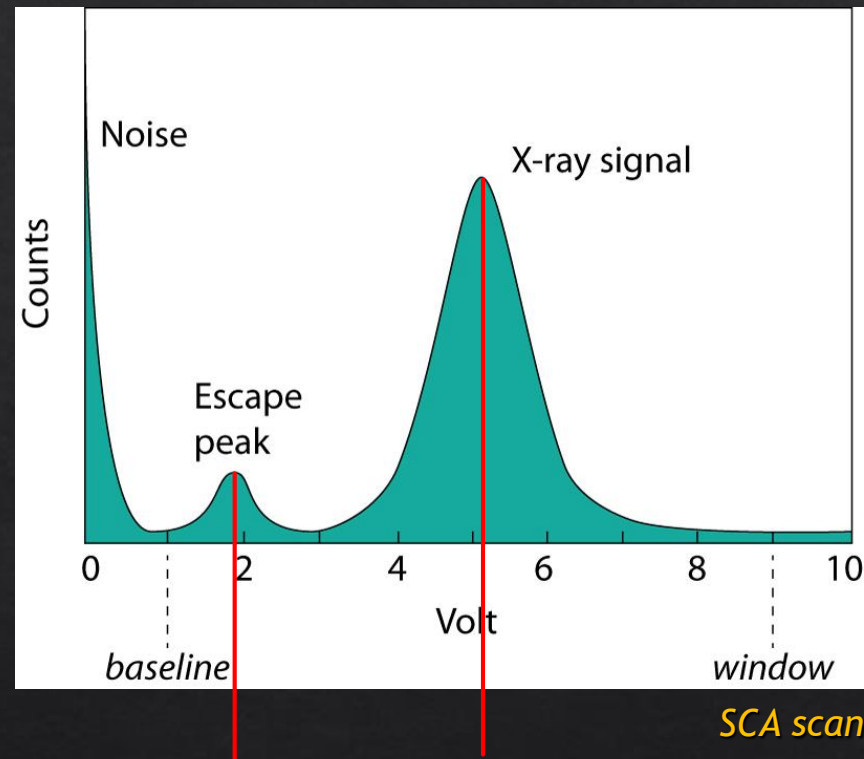


Pulse voltage is proportional to energy of the X-ray being detected

Energy of **SiKα** (1.739 keV) is ~1.39 times the energy of **MgKα** (1.253 keV)

If the pulse for **MgKα** is at 4 V, the pulse for **SiKα** will be at $4 \times 1.39 = 5.56$ V

Escape peak in SCA scan



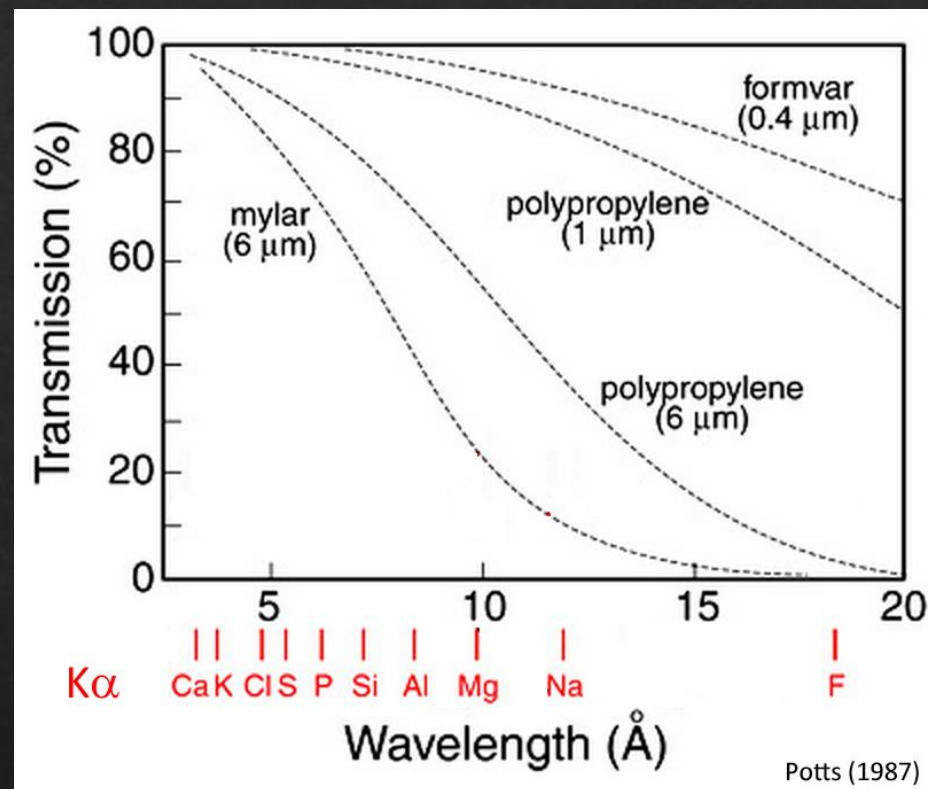
Energy difference
between incoming X-ray
and $\text{ArK}\alpha$ or $\text{XeL}\alpha$

Escape peaks fluoresced by
incoming X-ray:

- P-10 counter: $\text{ArK}\alpha$
- Xenon counter: $\text{XeL}\alpha$

If the pulse for $\text{NiK}\alpha$ (7.47 keV) is at 5.20 V, the $\text{XeL}\alpha$ (4.11 keV) escape peak will be at $5.2 - (7.47 - 4.11) = 1.84$ V

Proportional counter window



- Mylar has lower transmittance than polypropylene, especially for light element X-rays
- Thin windows are better for light elements

1 μm thick polypropylene window transmits ~60% of the F Kα

6 μm thick polypropylene window transmits only ~5% of the F Kα

SCA configurations

Analyzing crystal	X-ray detector	Standard pulse height of a specified X-ray		SCA Configuration setting				
		X-ray	Pulse height (V)	Mode	Base (V)	Window (V)	Gain	HV (V)
NEWSTE, STE, LDE2	GPC	CK α	2.5	Diff	0.7	9.3	64	Set the HV so that the specified X-ray has the standard pulse height.
TAPJ, TAPH	GPC/GPCH	MgK α	4.1	Diff	0.7	9.3	32	
PETJ, PETHS	XPC/XPCH	TiK α	5.8	Int	0.7	9.3	64	
LIF, LIFHS	XPC/XPCH	CuK α	5.0	Int	0.7	9.3	32	
PETJ, LIF, PETHS, LIFHS	GPC/GPCH	TiK α	7.0	Int	0.7	9.3	16	
LDE1	GPC	OK α	3.0	Diff	0.7	9.3	64	
LDEB, LDEBH	GPC/GPCH	BK α	3.5	Diff	0.7	9.3	128	
LDE1H	GPCH	CK α	2.0	Diff	0.7	9.3	64	
LDE2H, LDE4H	GPCH	CK α	3.0	Diff	0.7	9.3	64	
LDE3H	GPCH	BK α	3.5	Diff	0.7	9.3	128	
LDENH, LDE5H	GPCH	CK α	2.5	Diff	1.0	8.0	64	

Detector slit

Table 4.5 Relationship of analyzing crystals' lattice planes and spacings to standard detector slit settings

Analyzing crystals	STE NEWSTE	TAPJ TAPH	PETJ PETHS	LIF LIFHS	LDE1 LDE1H	LDE2 LDE2H	LDEB LDEBH	LDE3H	LDE5H LDENH	LDE4H
Lattice planes	STE Film	TAP (100)	PET (002)	LIF (200)	Super- lattice	Super- lattice	Super- lattice	Super- lattice	Super- lattice	Super- lattice
2d (nm)*	10.04	2.5757	0.8742	0.40267	About 5.8 – 6.2	About 9.5 – 10.5	About 14.5 – 15	About 19 – 21	About 7.6 – 8.4	About 11.5 – 12.5
Standard slit settings	Open	300 – 550 μm			Open					

* LDE series of analyzing elements having artificial superlattice structures differ from 2d, lattice spacing, each other, even if they are the same kind.

Table 4.8 X-ray spectrometer detector slit settings

X-ray spectrometers	Position that allows slit exchange (mm)	Slit settings		
		Pushed-in position	Midway position	Pulled-out position
XCE	L ≐ 110	300 μm	Open	550 μm
TXE				
H	L ≐ 140			500 μm
FCS	L ≐ 110	300 μm with Mylar film		300 μm

*Positioned at convergence point of diffracted X-rays (on the Rowland circle)
Cuts off stray X-rays and electrons*

Crystal, counter and slit combinations

Table 4.4 Standard combination of analyzing crystals, detector slits and detectors

X-ray spec-trometers	TXE type X-ray spectrometer		XCE type X-ray spectrometer		H type X-ray spectrometer		FCS type four-crystal X-ray spectrometer			
Radius of Rowland circle (mm)	140		140		100		140			
Spectromete r installation ports	2nd or 1st ^{*1}		All		Other than 3rd		1st or 2nd			
Analyzing crystals	NEWSTE	TAPJ	PETJ	LIF	LIFHS ^{*1}	PETHS ^{*1}	STE	TAPJ	PETJ	LIF
Detector slits	Open	300 μm or 550 μm	300 μm or 550 μm		500 μm ^{*2}		Open	300 μm	300 μm with Mylar film	
Detectors	Gas flow proportional counter		Xe-filled proportional counter		Xe-filled proportional counter ^{*3}		Gas flow proportional counter			
Remarks	The 733-NEW STE, a new large stearate crystal, is provided for analysis of light elements.		Analyzing crystals can be exchanged at any desired analysis position.		A stronger X-ray intensity is available than with another X-ray spectrometer. The dedicated analyzing crystals and detector are used. The analyzing crystals can be exchanged at any desired position within 90% of the analysis range.		Four crystals (STE, TAPJ, PETJ, LIF) are provided, allowing a wide range of analysis (a combination of these crystals allows analysis from B to U). The analyzing crystals can be exchanged at any desired position within 90% of the analysis range.			

*1: An LDE1H/LDE2H combination is available for analyzing light elements.

*2: Select "Open" for the light element analysis combination.

*3: Use a gas flow proportional counter (GPCH) for the light element analysis combination.

*4: When the front-type EDS detector is installed, the TXE X-ray spectrometer cannot be installed to the 1st port.

Mylar is used when light elements are not being analyzed

Electron Probe Microanalysis

Wavelength Dispersive Spectrometry (WDS)

Goals:

- ◆ High resolution elemental mapping
- ◆ Measurement of concentration of all elements in a microscopic volume

EPMA: Analytical procedure

- Sample preparation (mounting, polishing, carbon coating)

Carbon coating is essential for electrically insulating material

- Setting up the Electron Microprobe

Voltage, beam conditions, spectrometers, etc.

- Qualitative analysis with EDS and WDS

Important if nothing is known about the chemical composition

- Measurement of X-ray intensities in standards (calibration)

A different standard can be used for each element

- Measurement of X-ray intensities in the specimen and matrix corrections

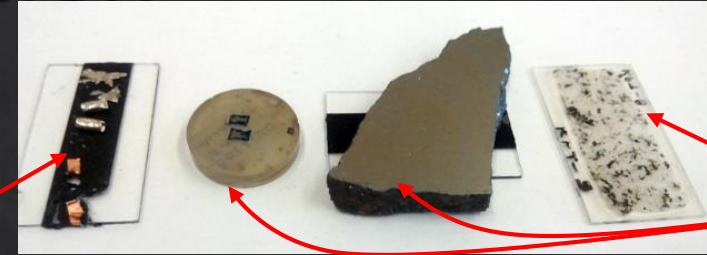
Different components of matrix corrections

Sample preparation

- Sample **cut and mounted** in epoxy, if necessary
- **Coarse polished** with 240-600 SiC paper (53-16 μm)
- **Fine polished** with alumina slurry or diamond paste on cloth (grit size 1.00-0.25 μm)
- **Washed** with water in ultrasonic cleaner after each polishing step, **dried** after final step, **wiped** with ethanol
- **Carbon coated** (25 nm thick) in vacuum

Qualitative analysis

Quantitative analysis



brass monitor

Setting up the Electron Microprobe

Voltage, filament saturation and beam alignment

- Accelerating voltage
 - Depends on *overvoltage* requirement,
e.g., *FeK α is not emitted with a 5 keV beam because $E_{c(K-shell)}=7.111$ keV, and $U < 1$.*
 - For a particular accelerating voltage, *overvoltage will be different for different elements*. U should be about 2-10.
- Filament saturation and beam alignment
 - *Saturation*: filament current is adjusted to ensure saturation
 - *Gun bias* should be properly set to ensure optimum emission
 - *Shift and tilt alignment*: beam current is maximized
 - *Wobble adjustment*: image defocusing should be symmetrical above and below the optimum beam focusing plane. If not, position of the objective lens aperture is adjusted
 - *Astigmatism correction*: image is distorted if the spot is elliptical. Stigmator controls are used to remove distortion

Setting up the Electron Microprobe

Spectrometer choice

- Crystal/diffractor

E.g., $\text{FeK}\alpha$ ($\lambda_{\text{K}\alpha} = 0.1937 \text{ nm}$, $E_{\text{FeK}\alpha} = 6.4 \text{ keV}$) can be diffracted by TAP ($2d = 2.5757 \text{ nm}$), PET ($2d = 0.8742 \text{ nm}$) and LIF ($2d = 0.4027 \text{ nm}$).

For $n = 1$, equation $\lambda = 2d \sin \theta$, i.e., $\theta = \sin^{-1}\left(\frac{\lambda}{2d}\right)$, and for $R = 140 \text{ mm}$, equation $L = n\lambda \frac{140}{d}$ indicate:

$\theta = 4.3^\circ$ and $L = 191.2 \text{ mm}$ for TAP

$\theta = 12.8^\circ$ and $L = 62.0 \text{ mm}$ for PET

$\theta = 28.8^\circ$ and $L = 134.6 \text{ mm}$ for LIF

Acceptable ranges for θ and L are $15\text{-}55^\circ$ and $70\text{-}230 \text{ mm}$. Therefore, **LIF** is the correct choice.

- Counter and window

Xe has a better quantum efficiency for $\text{FeK}\alpha$. So, a **Xe counter** with a **Be window** is the right choice.

- SCA settings

Using **LIF/Xe counter** and an appropriate collection wire voltage, the $\text{CuK}\alpha$ ($E_{\text{CuK}\alpha} = 8.04 \text{ keV}$) pulse should be set at 5 V by performing PHA. Since $E_{\text{FeK}\alpha} = 0.8 \times E_{\text{CuK}\alpha}$ the $\text{FeK}\alpha$ pulse should be at $0.8 \times 5 = 4 \text{ V}$.

- Detector slit

For higher energy X-rays, smaller slits are recommended. The **300-550 μm** slit should be selected.

Setting up the Electron Microprobe

Beam current, counting time and probe diameter

- Beam current and counting time depend on concentration of the element of interest

Higher beam current increases count rate and longer counting time increases total counts (improves precision)

For *N counts*, the counting uncertainty is $\frac{1}{\sqrt{N}} \times 100 \%$. Counting is more precise as N increases. E.g.,

For *25 counts*, the uncertainty is *20 %*

For *100 counts*, the uncertainty is *10 %*

For *10,000 counts*, the uncertainty is *1 %*

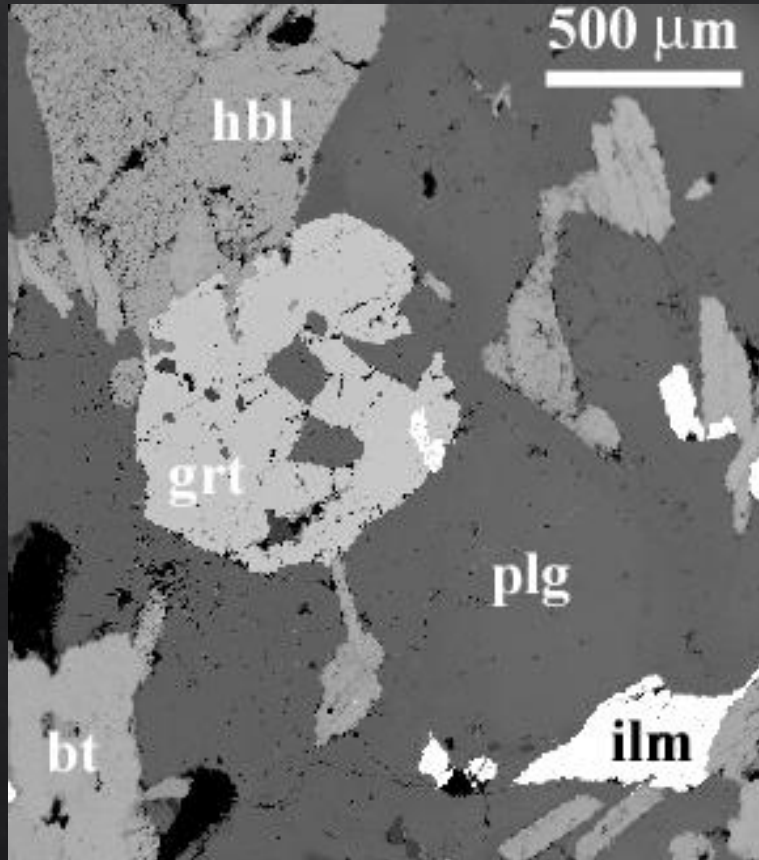
- Probe diameter

Sometimes necessary to use a defocused beam (large spot size). E.g.,

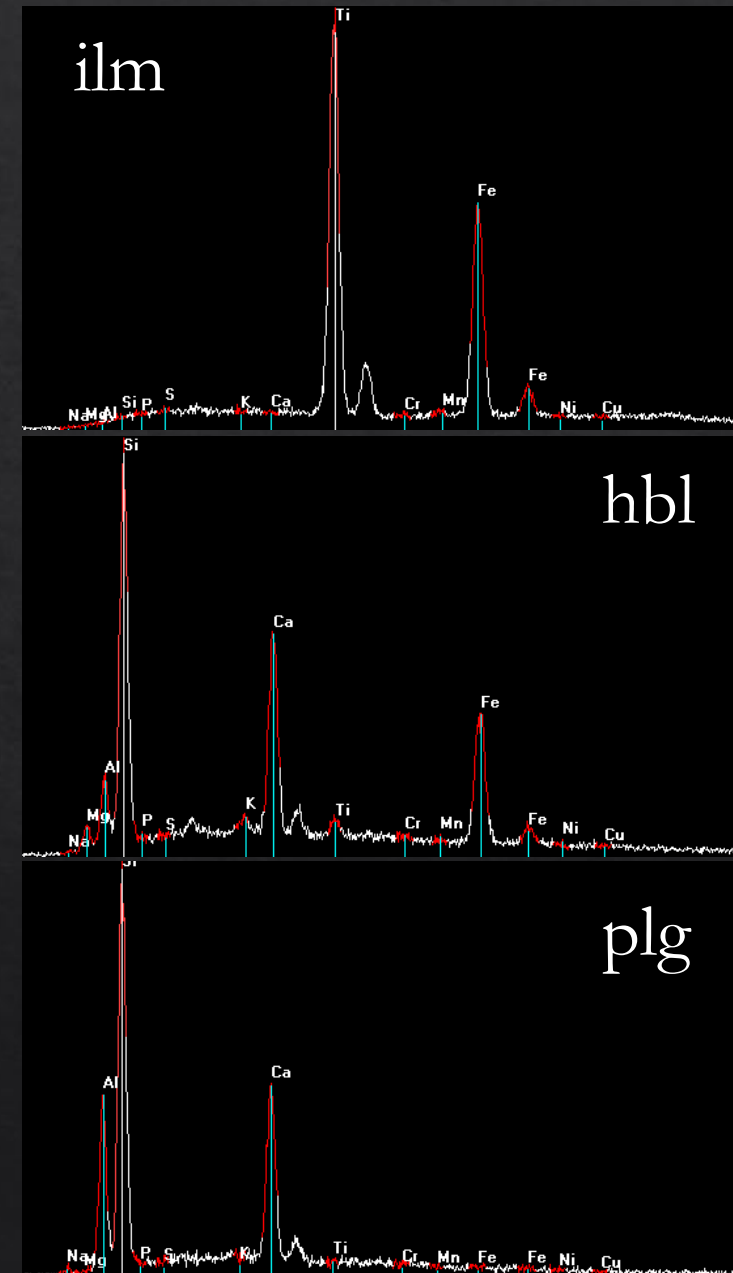
Average composition of fine-grained material (spot size > grain size)

Hydrous, and Na or F containing glass: Na migrates away, F migrates toward the spot (spot size ~ 10 μm)

Qualitative analysis with BSE and EDS

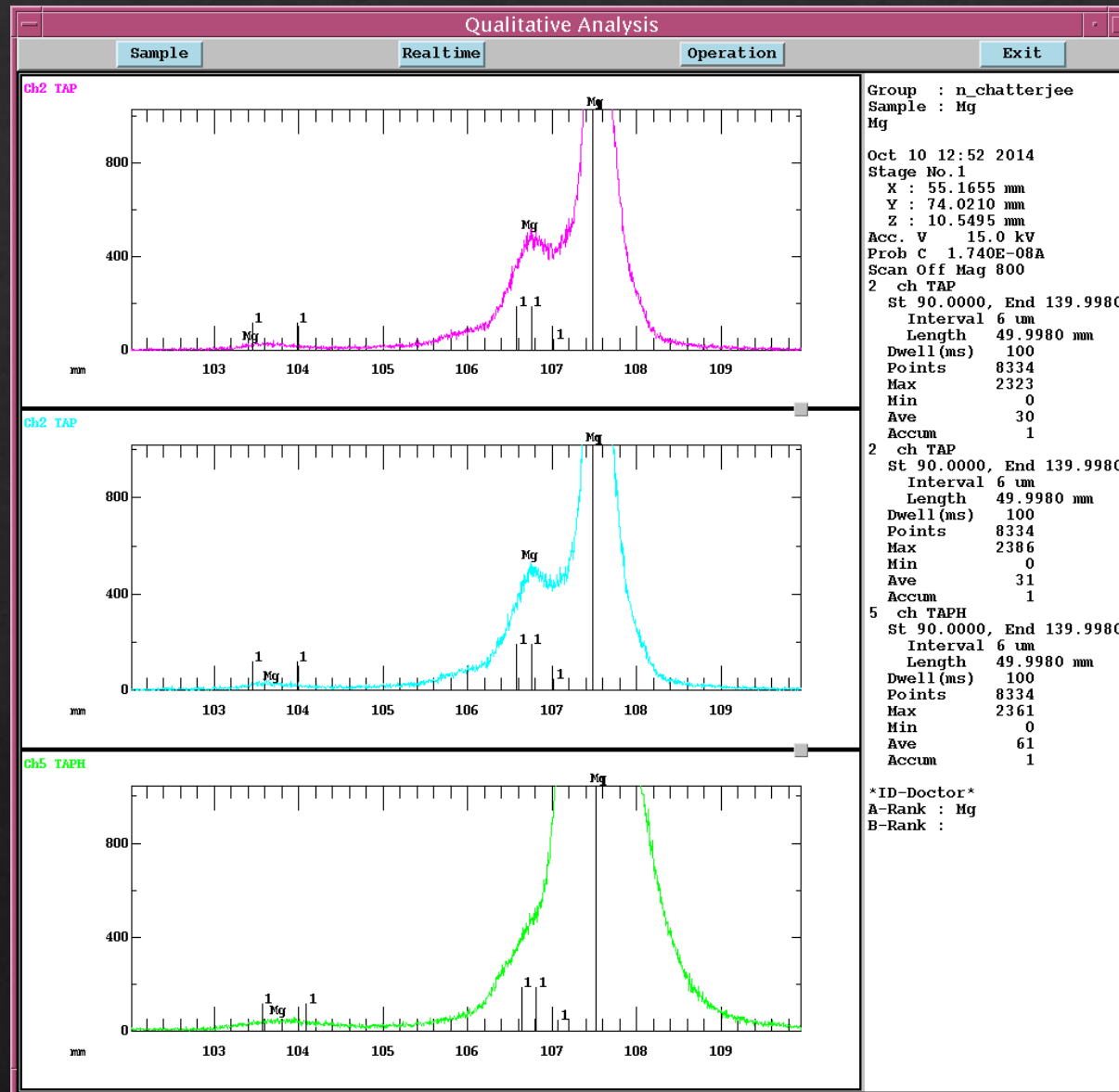


Mean atomic number: $\text{plg} < \text{hbl} < \text{bt} < \text{grt} < \text{ilm}$



EDS spectra

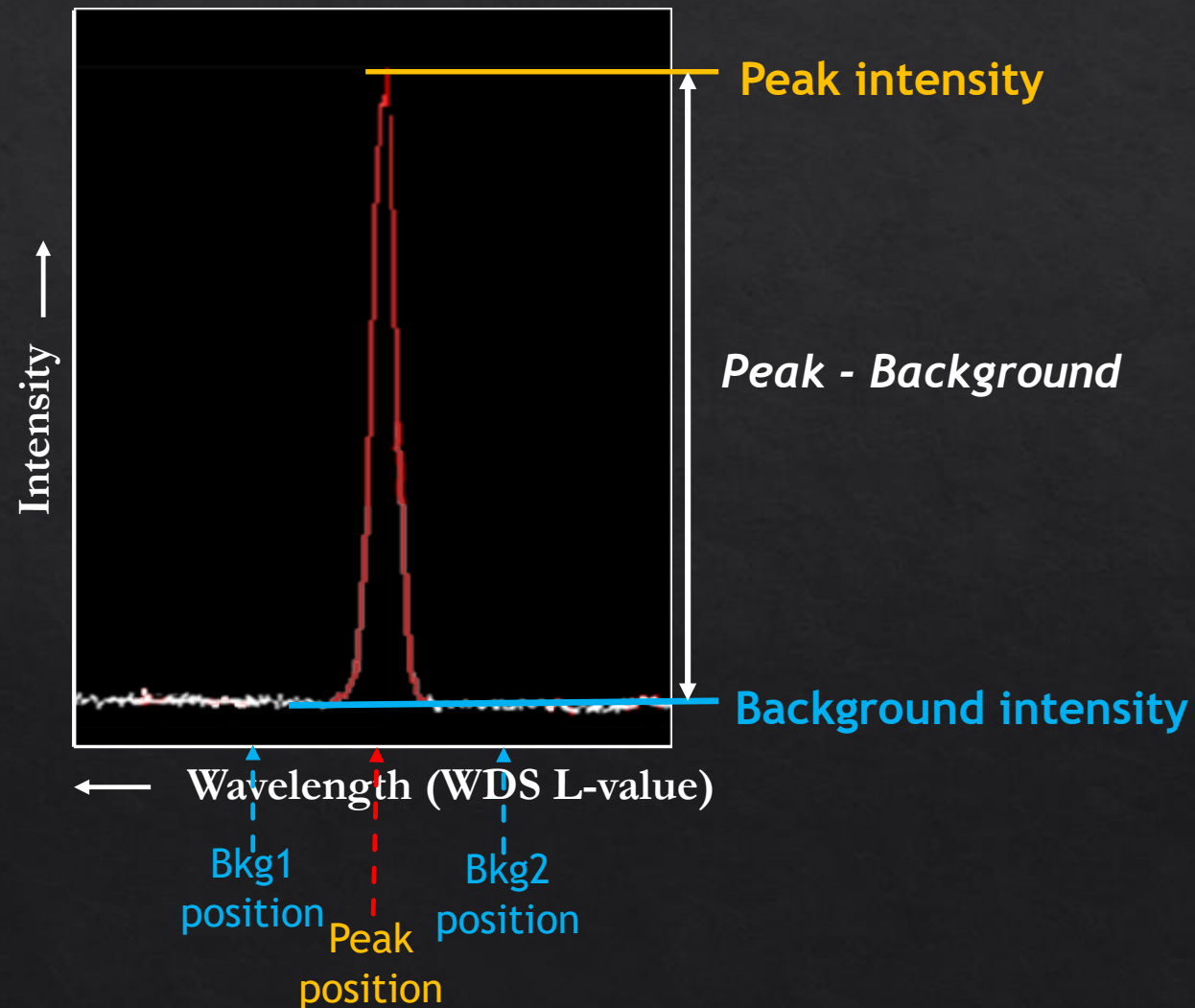
Qualitative and semi-quantitative analysis with WDS



Standard X-ray intensity measurement (calibration)

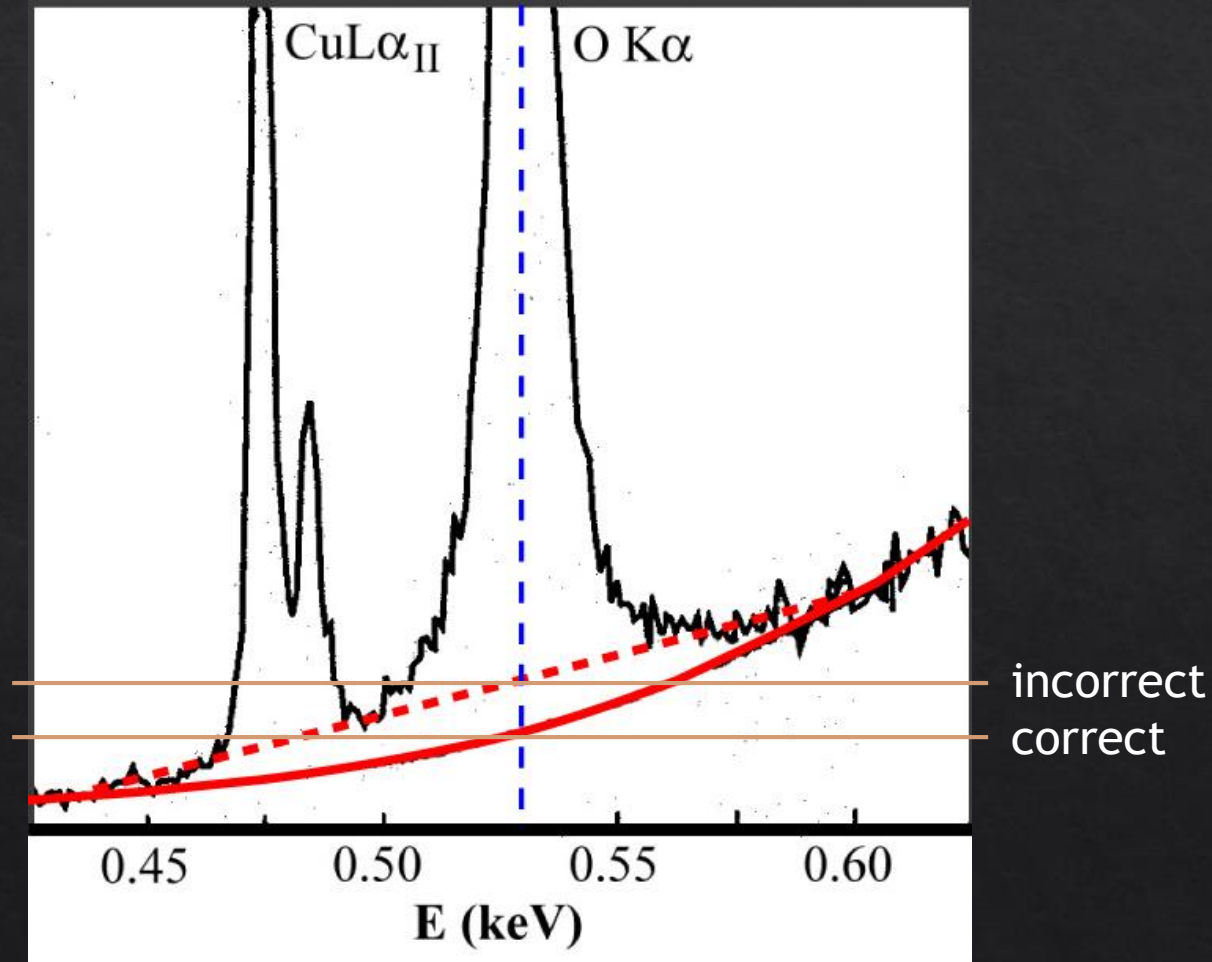
- Calibration is performed on standards, a set of **homogenous**, natural or synthetic **compounds** with well **known composition**
- A good calibration is essential for **accurate** analysis.
It eliminates **systematic errors** (fixed but unknown offsets from the actual values in all measurements)
- After primary calibration, **secondary standards** (working standards) are analyzed to make sure the results are as expected

X-ray intensity measurement: peak minus background

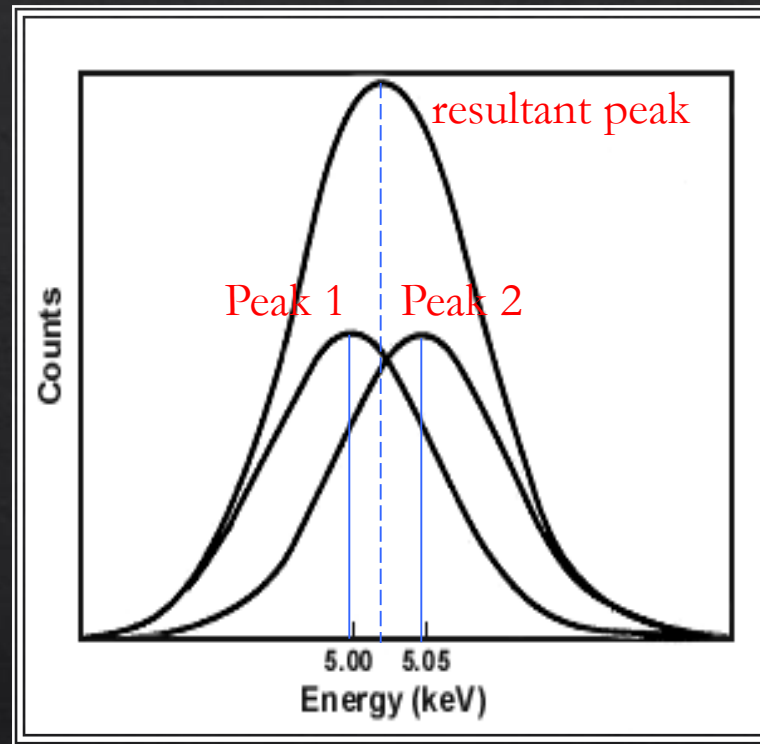


Long counting times are used to achieve statistical precision

X-ray background measurement: special case

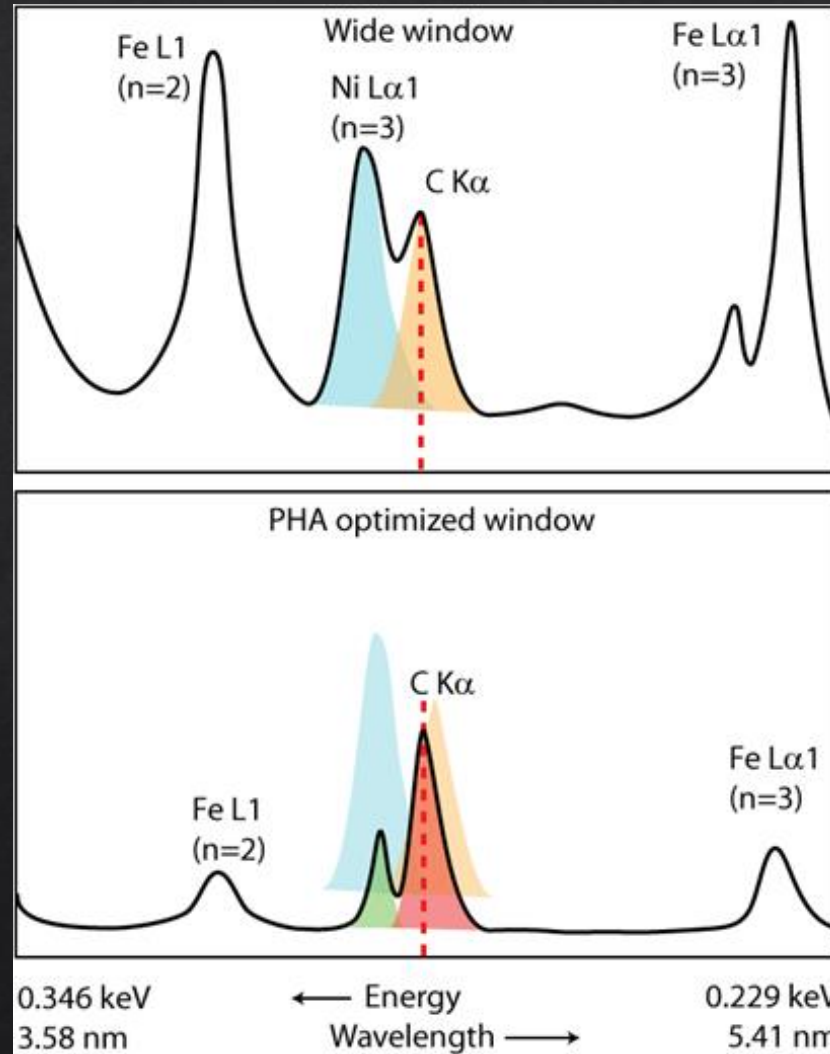


Peak overlap in X-ray spectra



Overlap between Peak 1 and Peak 2 results in a broad single peak

PHA reduces peak and background overlaps

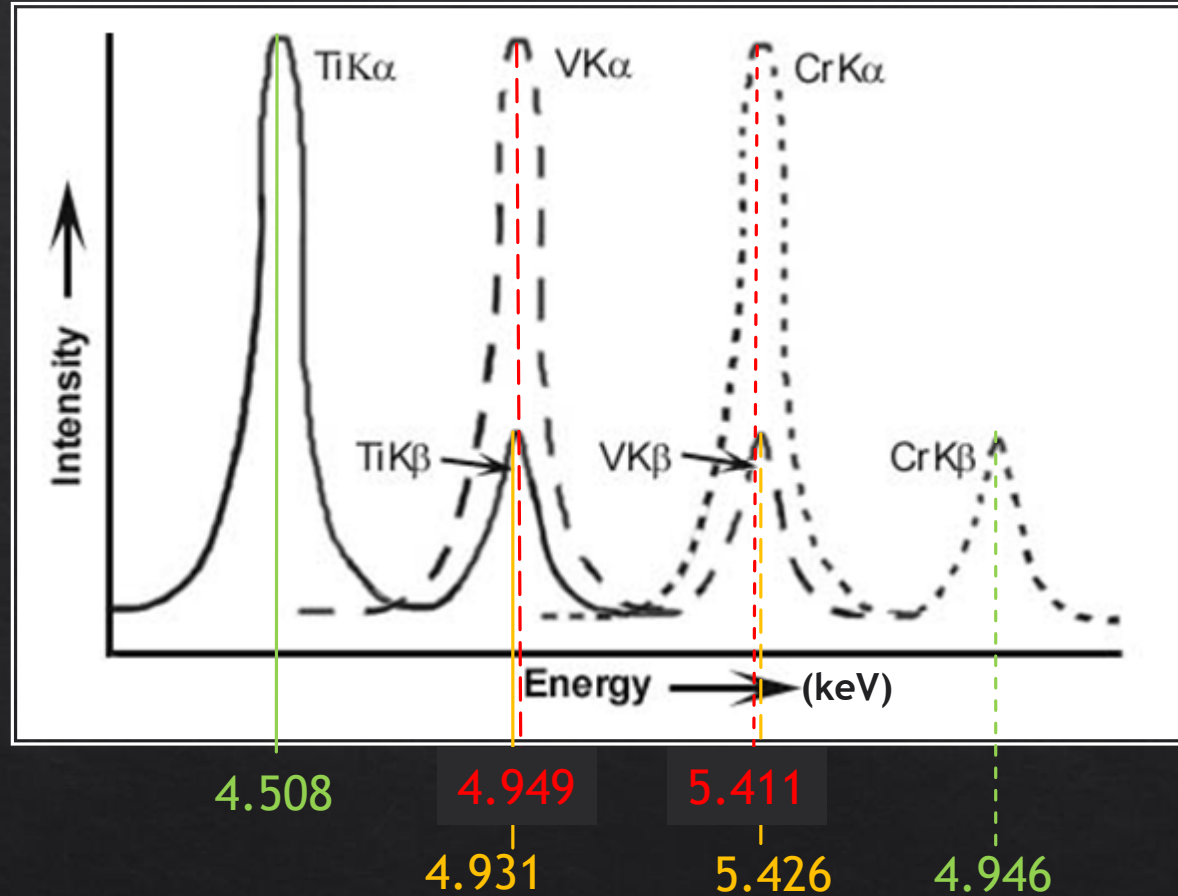


Wide open SCA voltage window

PHA optimized SCA voltage window

Spectrum of carbon steel

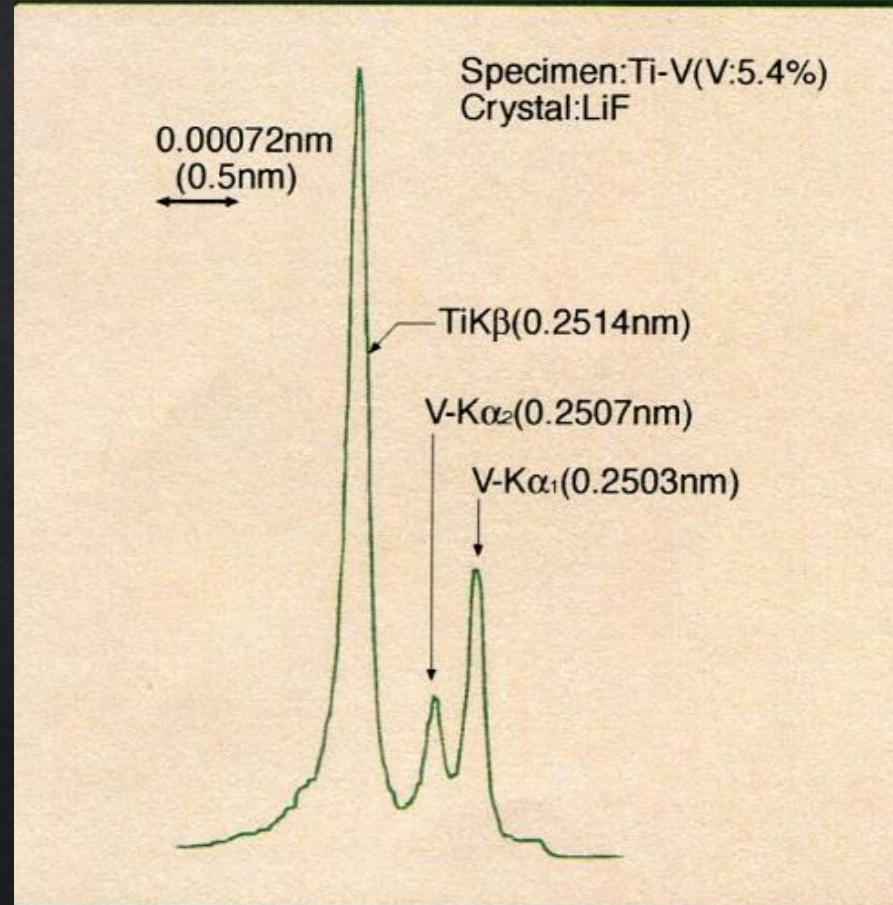
Peak overlap corrections for Ti-V-Cr



$$I_{VK\alpha}^{corr} = I_{VK\alpha}^{meas} - \frac{I_{TiK\alpha}^{meas}}{I_{TiK\alpha}^{std}} I_{VK\alpha}^{std}$$

$$I_{CrK\alpha}^{corr} = I_{CrK\alpha}^{meas} - \frac{I_{VK\alpha}^{corr}}{I_{VK\alpha}^{std}} I_{CrK\alpha}^{std}$$

Peak resolution with LIF



LIF is able to resolve the TiK β , VK α_1 and VK α_2 peaks

XCE type spectrometer with Xe counter

EPMA Quantitative analysis

X-ray intensity is proportional to the concentration, $C \propto I$

$$\frac{C_i}{C_{(i)}} \propto \frac{I_i}{I_{(i)}}$$

C_i , I_i : concentration and intensity in sample

$C_{(i)}$, $I_{(i)}$: concentration and intensity in standard

$$\frac{I_i}{I_{(i)}} = k_i \text{ (k - ratio)}$$

$$\frac{C_i}{C_{(i)}} = k_i \cdot [\text{ZAF}]_i$$

Matrix (ZAF) corrections

Z : atomic number correction

*electron back-scattering difference
between standard and sample*

A : absorption correction

absorption of x-ray inside the sample

F : fluorescence correction

*fluorescence of x-ray due to absorption of
a higher energy x-ray inside the sample*

X-ray absorption

$$\begin{aligned} I &= I_0 \exp^{-\left(\frac{\mu}{\rho}\right)(\rho x)} \\ &= I_0 \exp^{-\left(\frac{\mu}{\rho}\right)(\rho z \operatorname{cosec} \psi)} \end{aligned}$$

$$\begin{aligned} I &= I_0 \exp^{-\left(\frac{\mu}{\rho}\right)(\rho x)} \\ &= I_0 \exp^{-\left(\frac{\mu}{\rho}\right)(\rho z \operatorname{cosec} \psi)} \end{aligned}$$

I : Intensity emitted

I₀ : Intensity generated

μ/ρ : mass absorption coefficient

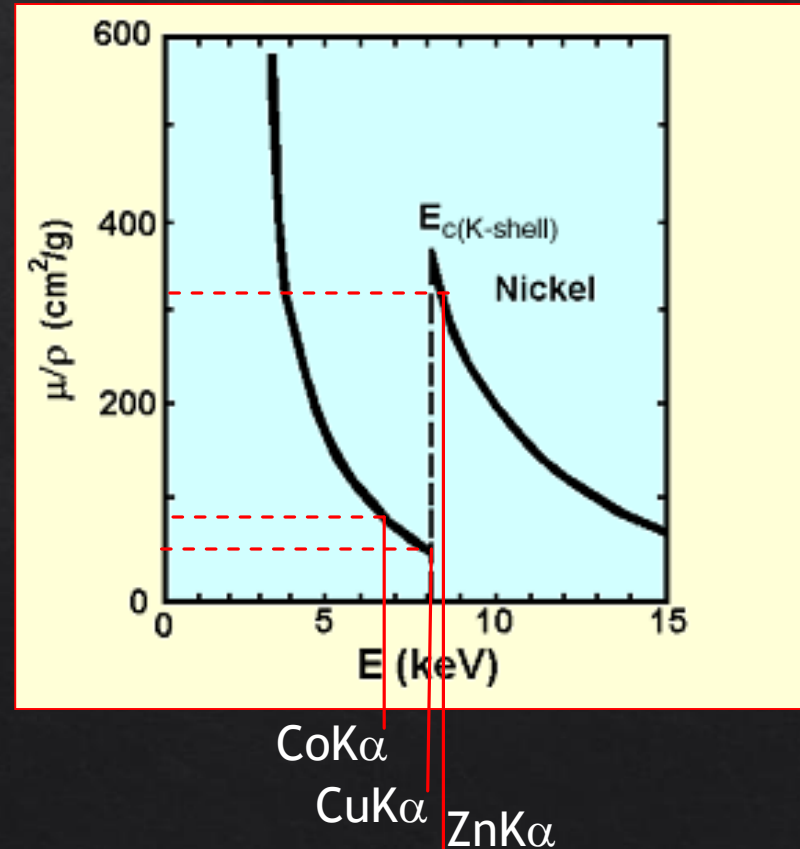
ρ : density

z : depth

ψ : take-off angle

Mass absorption coefficient, $(\mu/\rho)_{\text{absorber}}^{x\text{-ray}}$

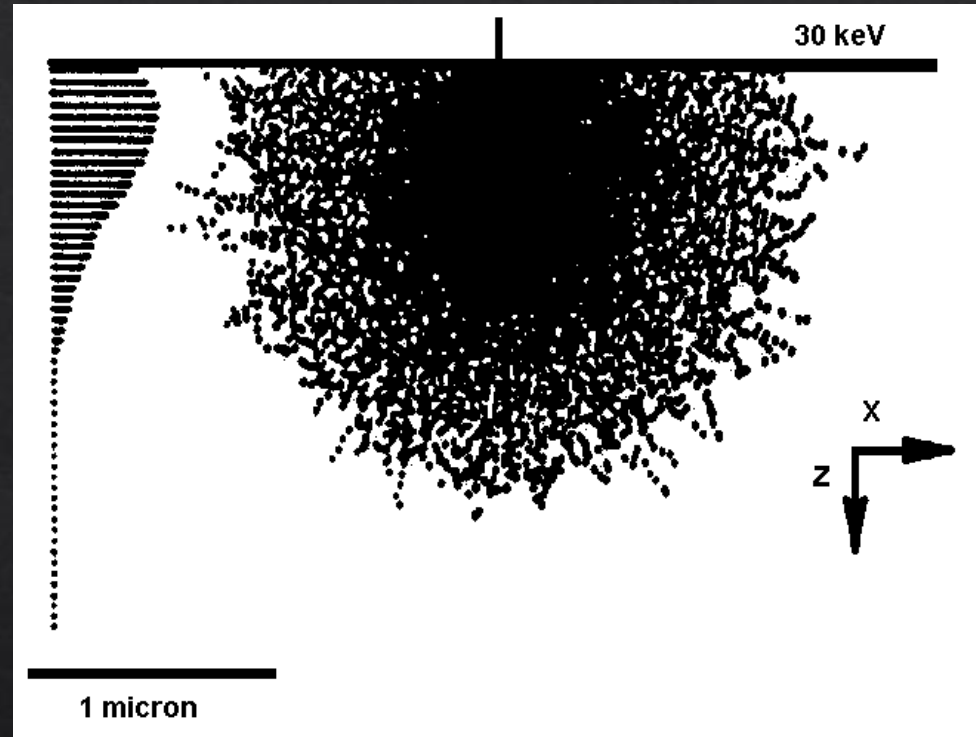
Variation of $(\mu/\rho)_{\text{Ni}}^{x\text{-ray}}$
as a function of incident
X-ray energies



Sharply increases at the **critical excitation energy of Ni K-shell**, $E_{c(\text{Ni K-shell})}$

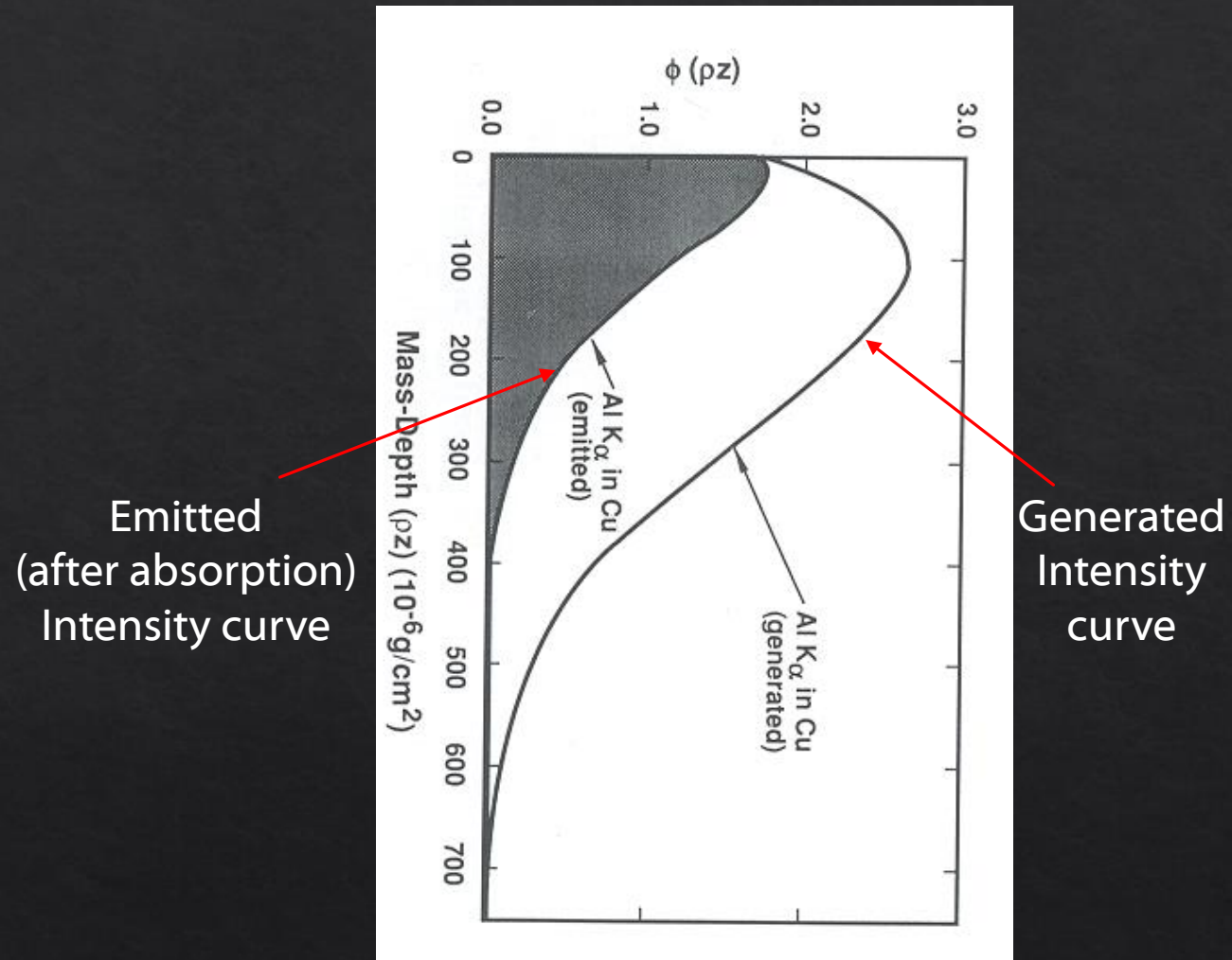
Any X-ray with a **slightly higher energy than $E_{c(\text{Ni K-shell})}$** (e.g., ZnK α) is efficiently **absorbed** as it ionizes the Ni K-shell and **generates (fluoresces) NiK α**

Depth-distribution of x-rays: $\phi(\rho z)$ function



Intensity from each layer normalized by intensity from a free-standing layer of the same material

$\phi(\rho z)$ correction

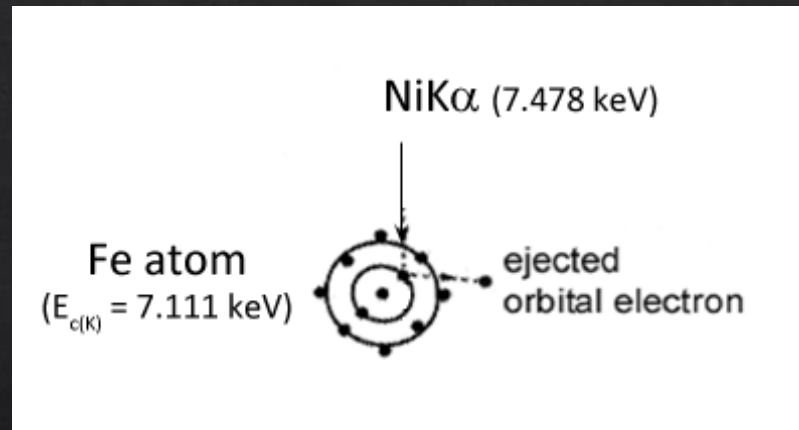


Al K_{α} is efficiently absorbed by Cu in Al-Cu alloy

X-ray fluorescence

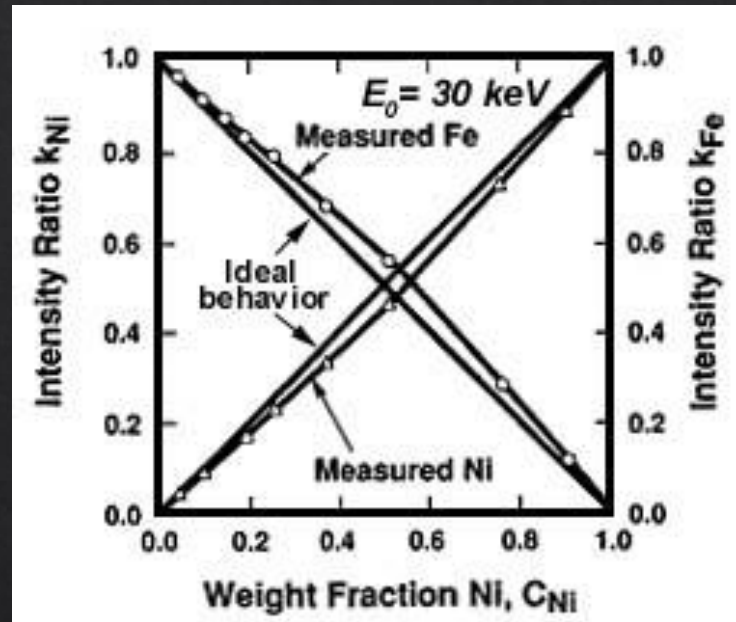
*A consequence of X-ray absorption
when*

$$E_{\text{incident X-ray}} > E_{\text{c(absorber shell)}}$$



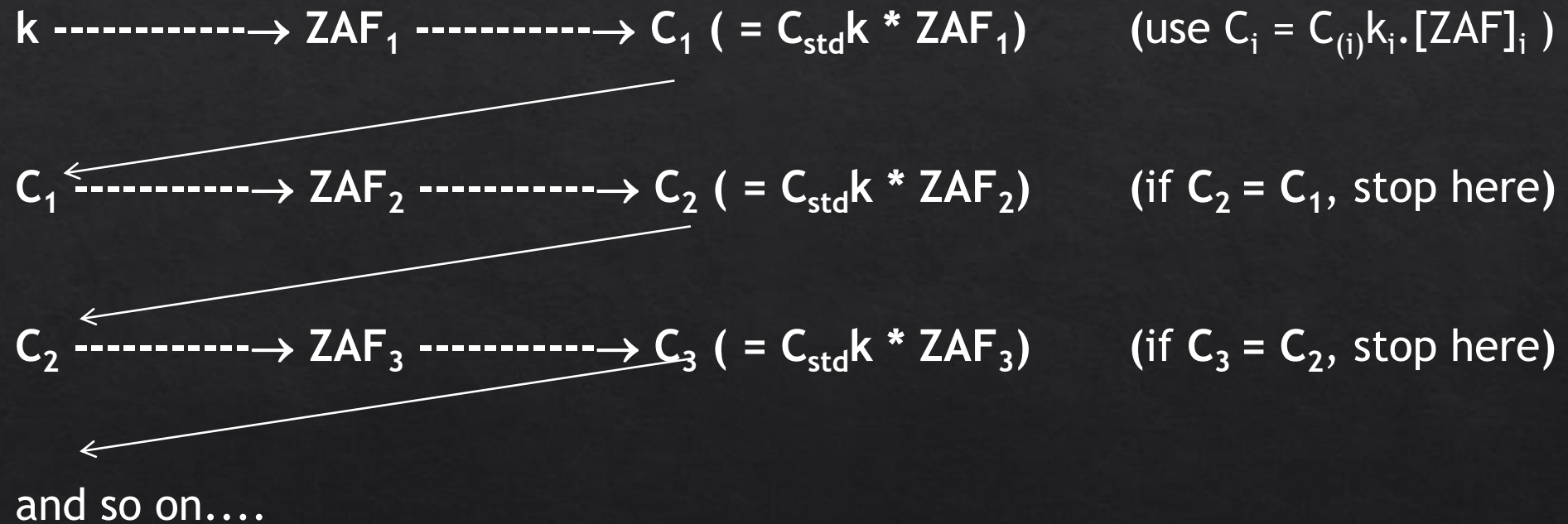
- NiK α is absorbed by Fe atom
- FeK α is fluoresced

X-ray absorption and fluorescence



- $\text{NiK}\alpha$ is absorbed by Fe atom
- $\text{FeK}\alpha$ is fluoresced

Matrix correction flowchart



Compositional imaging with X-rays: elemental mapping

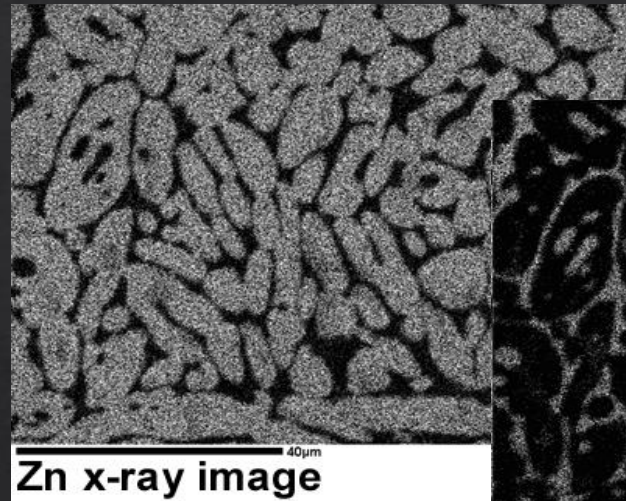
- ◆ **Beam-rastered image:**

electron beam rasters over the area to be imaged

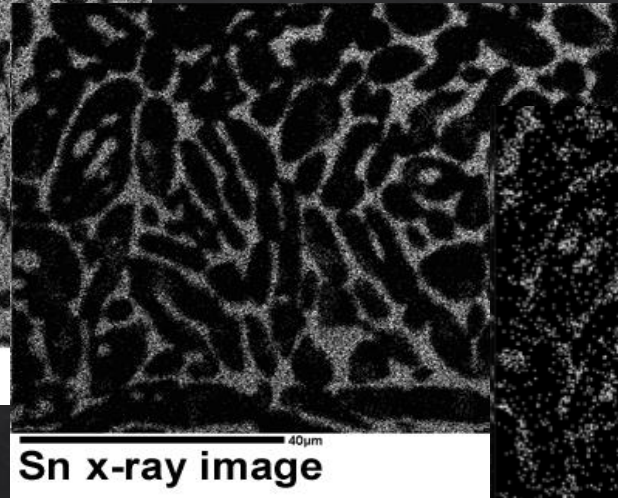
- ◆ **Stage-rastered image:**

electron beam is stationary, stage moves

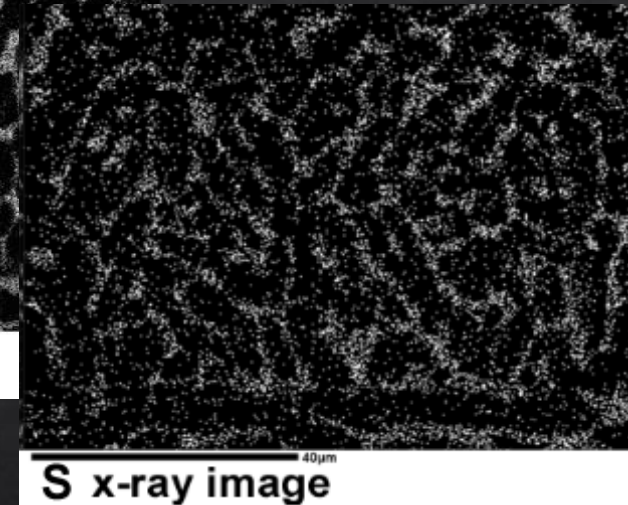
Background in x-ray image



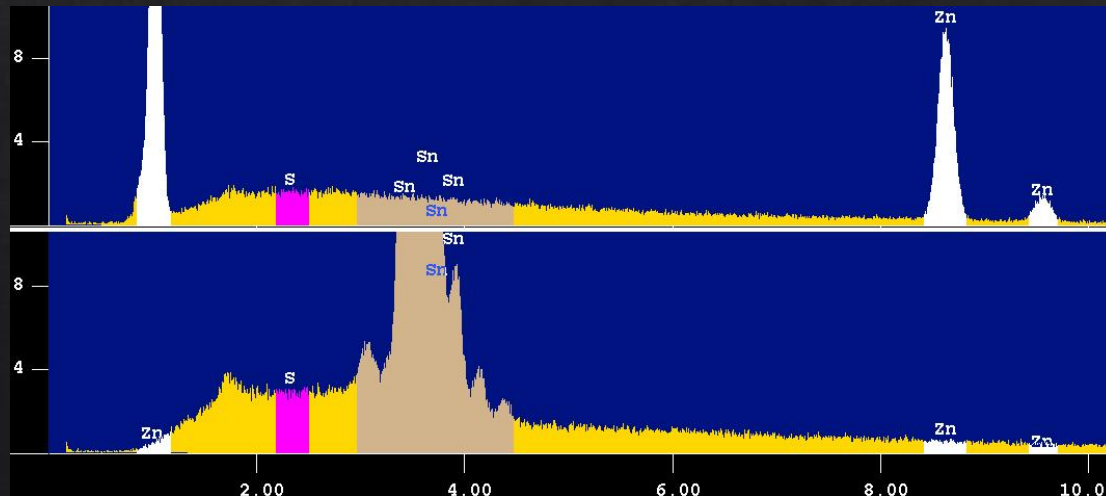
Zn-Sn composite



Background image



Zn-rich phase
(low Z)



Sn-rich phase
(low Z)

X-ray defocusing in beam-rastered image

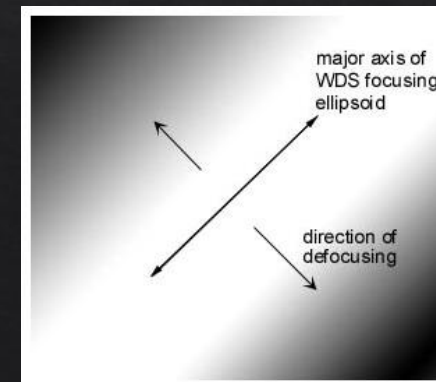
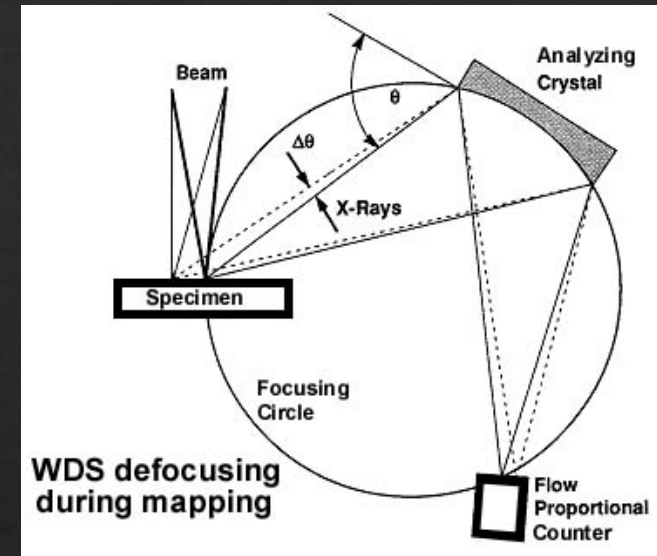
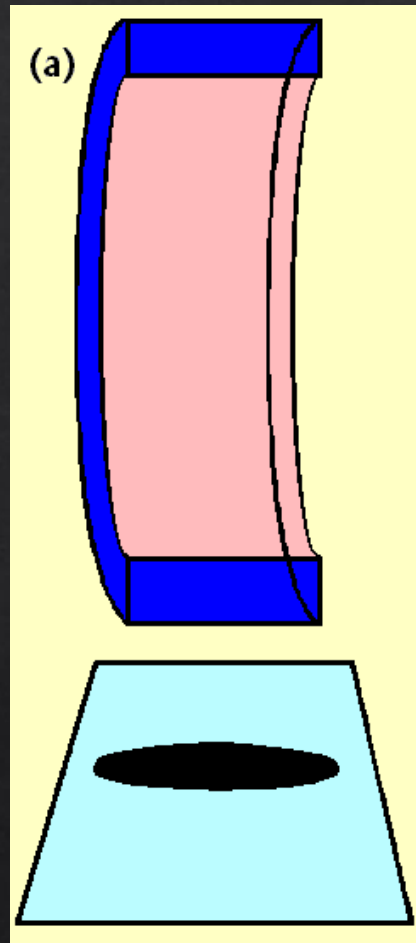
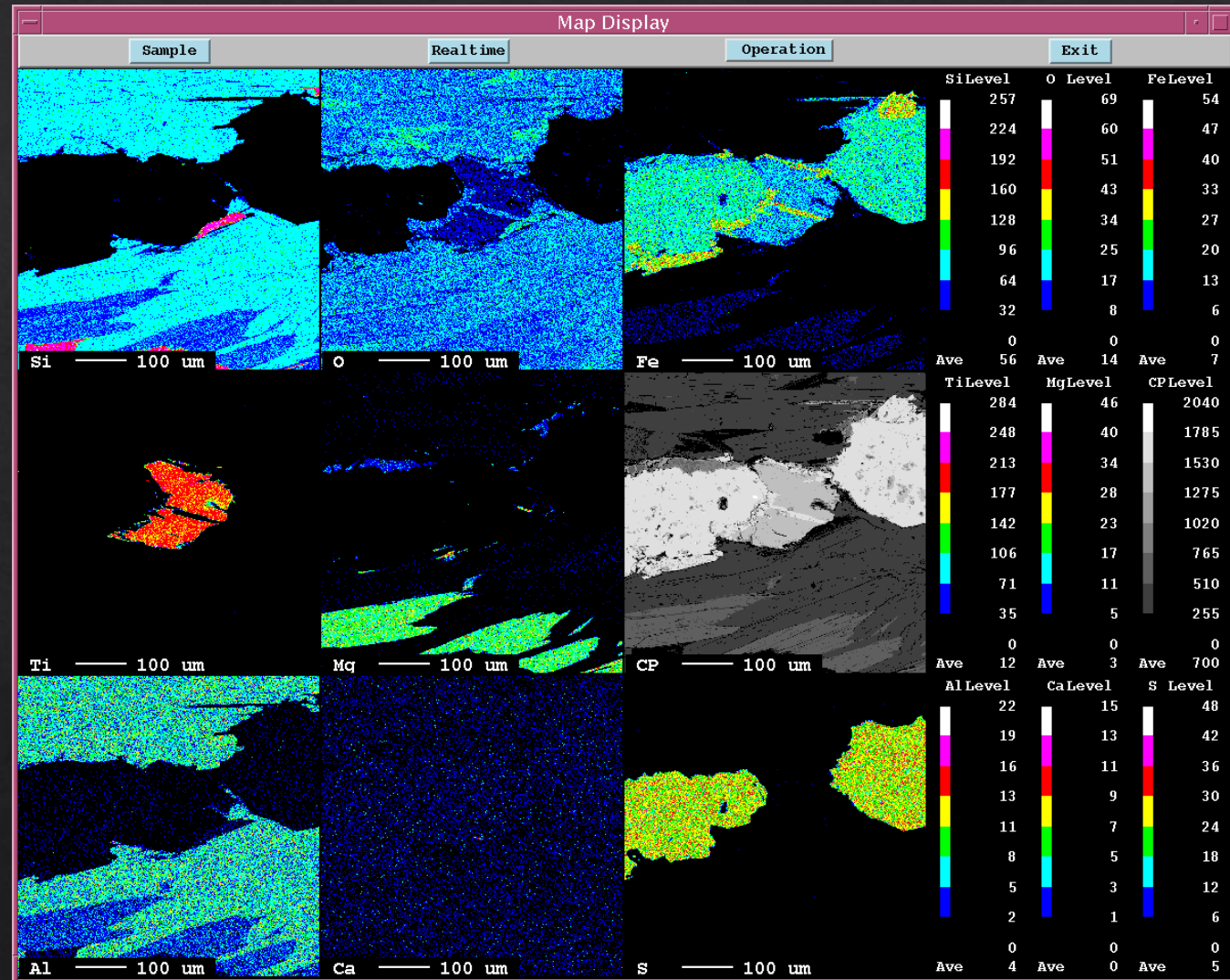


Image quality of X-ray maps

Two factors:

- ❑ Image resolution:
number of points measured within the imaged area
- ❑ X-ray Signal:
beam current and counting (dwell) time per point

Combined WDS and EDS X-ray mapping



Combined BSE, CL and X-ray mapping

