Task and Motion Planning (TAMP)

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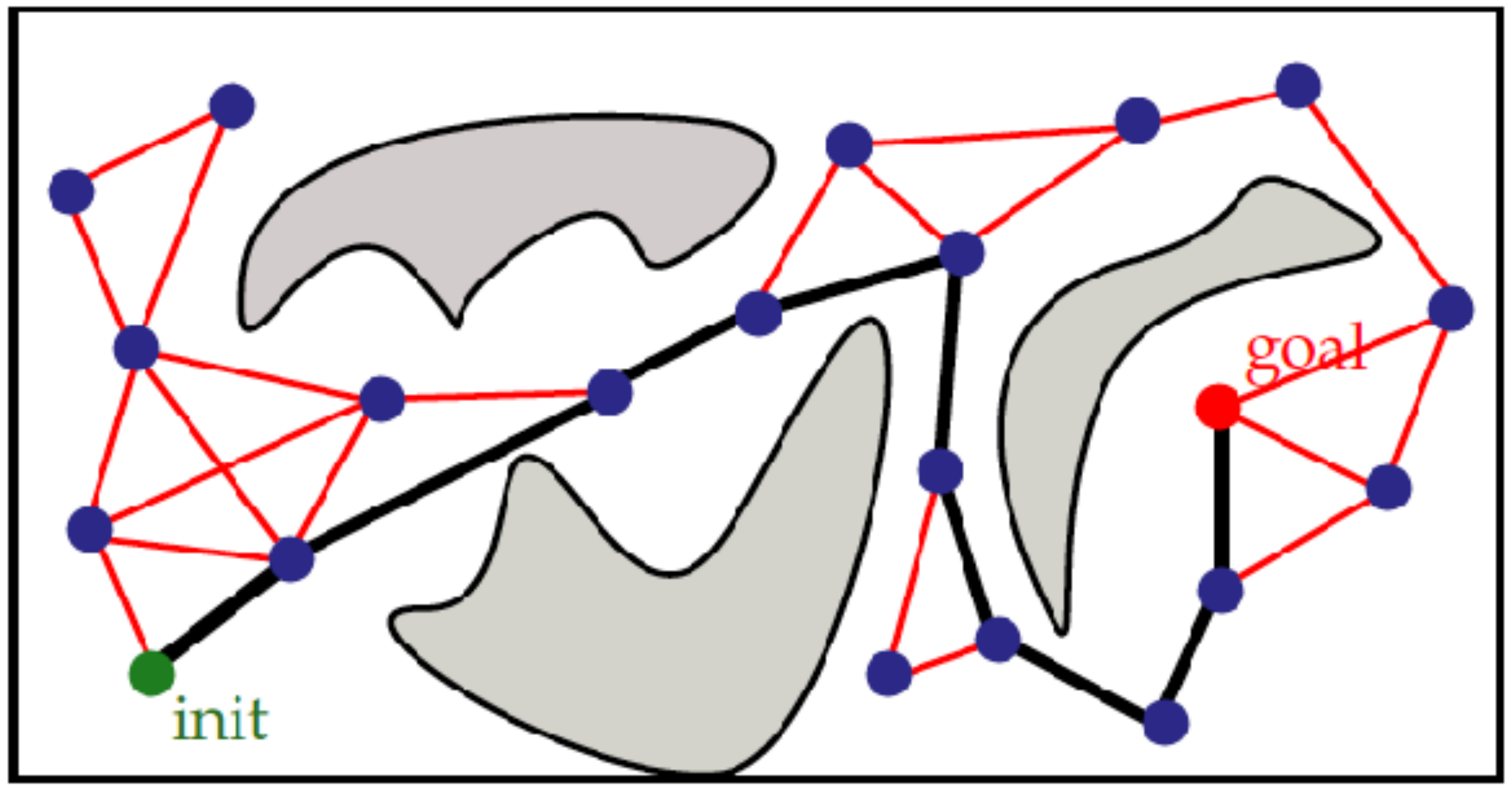
6.881 - Intelligent Robot Manipulation

11/12/2019

manipulation.csail.mit.edu/

github.com/caelan/pddlstream

(Probable) Roadmap

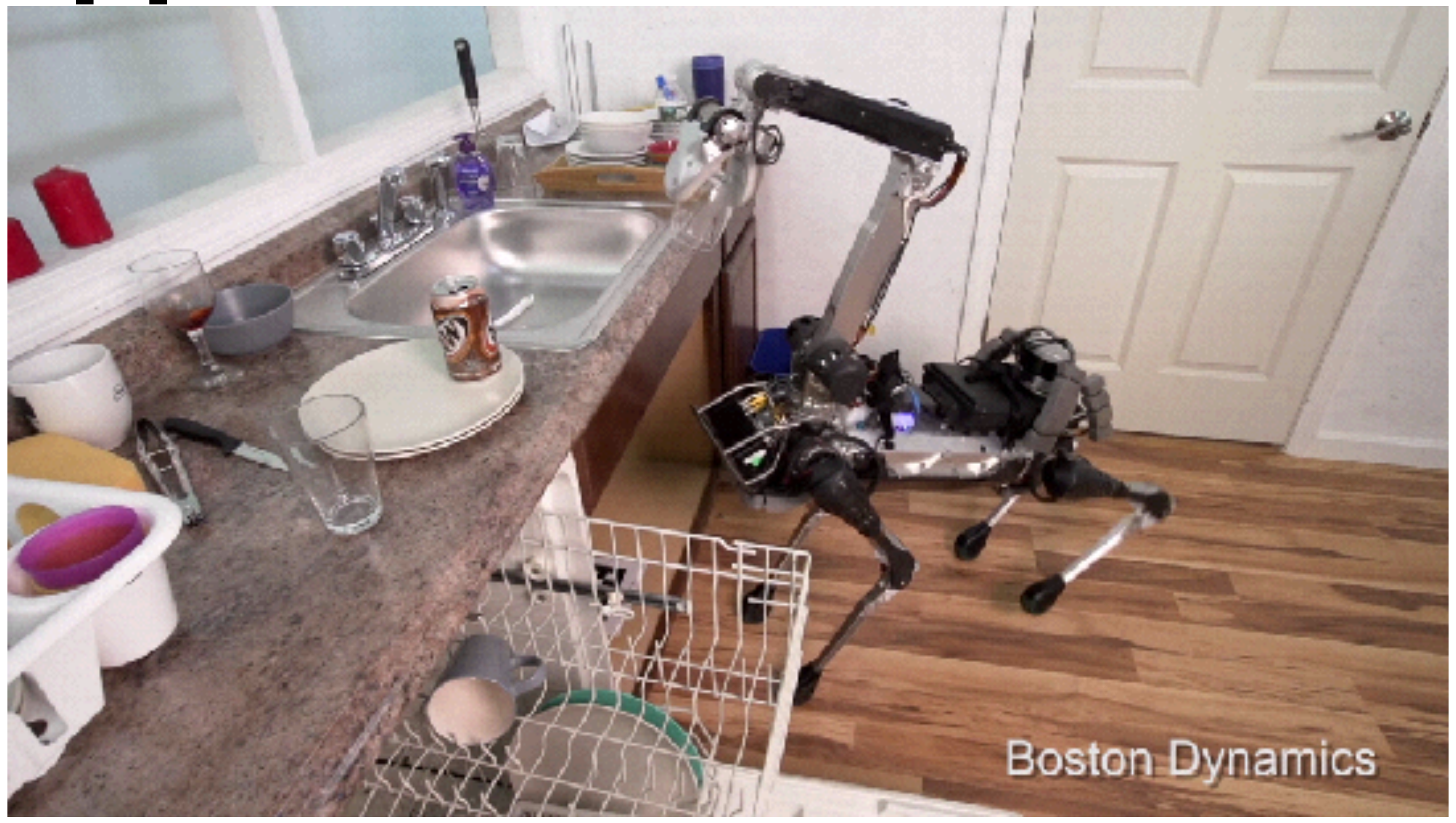


[Fig from Erion Plaku]

1. **Background**
   1. Task Planning
   2. Motion Planning
2. **Hybrid Planning**
   1. Prediscretized & Numeric Planning
   2. Multi-Modal Motion Planning
   3. Integrated TAMP
3. **STRIPStream**
4. Temporal TAMP
5. TAMP under Uncertainty

Planning for Autonomous Robots

- Robot must select both **high-level** actions & **low-level** controls
- **Application areas**: semi-structured and human environments



Household

Warehouse fulfilment

Food service

Construction

Task and Motion Planning (TAMP)

- Plan in a **factored, hybrid** space
  - **Discrete** and **continuous** variables & actions

- **Variables**
  - **Continuous**: robot configuration, object poses, door joint positions,
  - **Discrete**: is-on, is-in-hand, is-holding-water, is-cooked, …

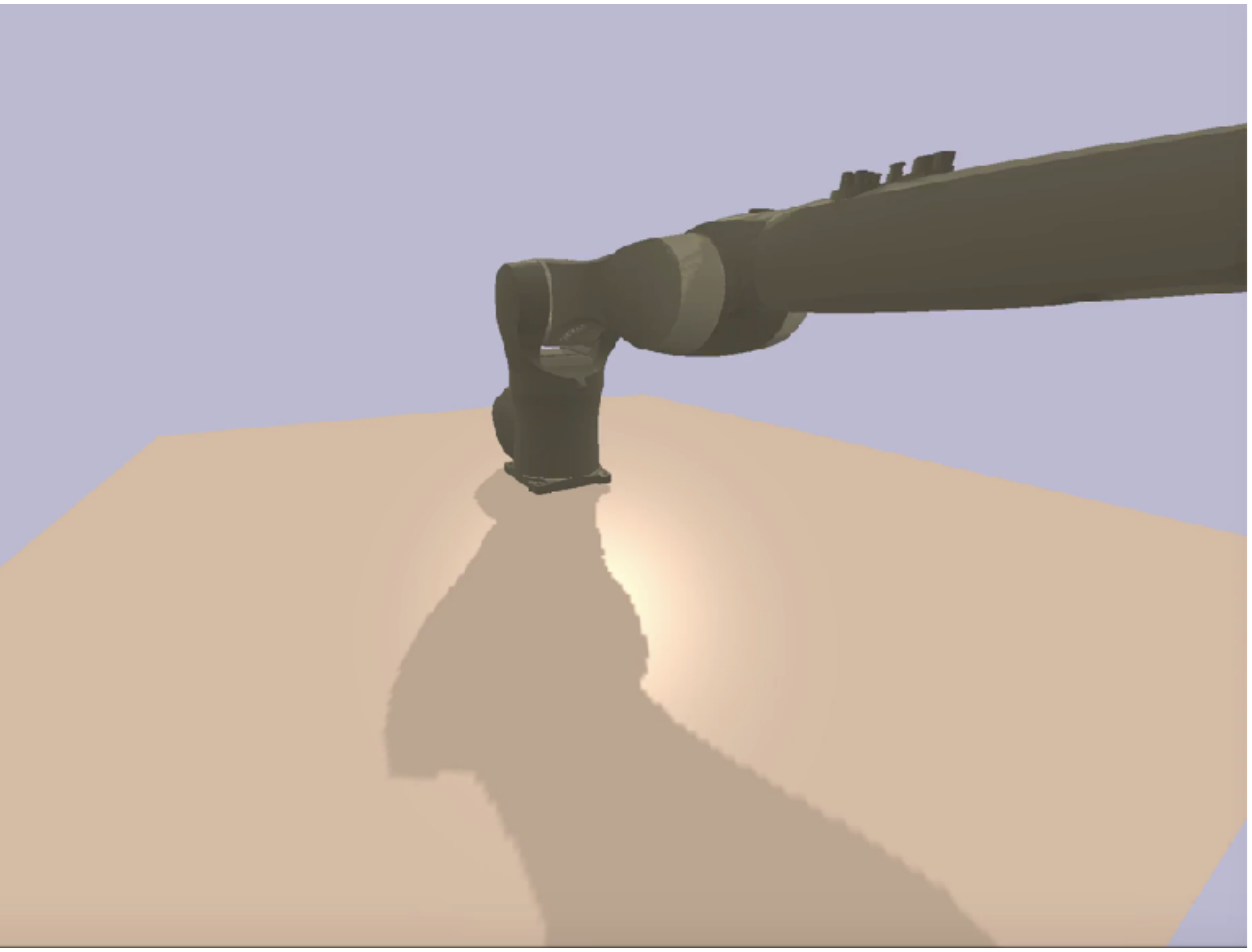
- **Actions:** move, pick, place, push, pull, pour, detect, cook, …

Cooking and Stacking

Preparing Coffee

Automated Fabrication

- Plan sequence of **306** 3D printing extrusions (actions)
- Collision, kinematic, **stability** and **stiffness** constraints



[Huang, Garrett, & Mueller 2018]

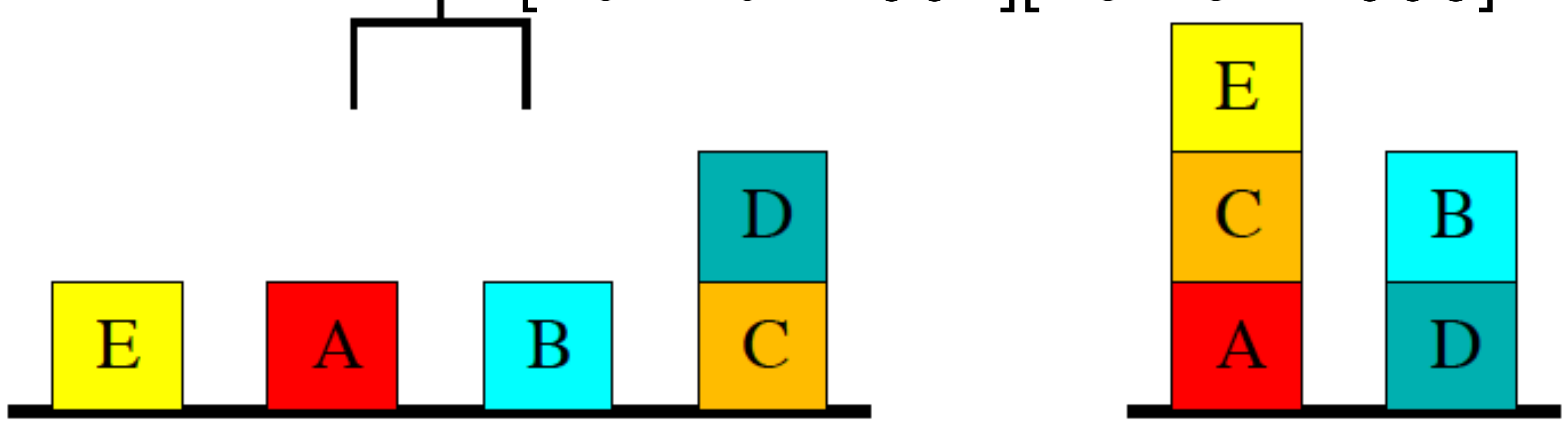
Problem Class

- **Discrete-time**
  - Plans are finite sequences of controls
- **Deterministic** (for now)
  - Actions always produce the intended effect
  - Solutions are **plans** (instead of policies)
- **Observable** (for now)
  - Access to the full world state
- **Hybrid**
  - States & controls composed of **mixed discrete-continuous variables**

Review: Task Planning (10/31/19)

- Plan in a large **discrete** space with **many variables**
- **Planning languages:** STRIPS/PDDL [Fikes 1971] [Aeronautiques 1998]
  - **Facts:** boolean state variables
  - **Parameterized** actions
    - **Preconditions** test validity
    - **Effects** change the state
- **Heuristic search** algorithms [Hoffman 2001][Helmert 2006]

```
(:action stack
  :parameters (?b1 ?b2)
  :precondition (and
    (Holding ?b1)
    (Clear ?b2))
  :effect (and
    (HandEmpty)
    (On ?b1 ?b2)
    (not (Holding ?b1))
    (not (Clear ?b2))))
```



Initial State Goal State

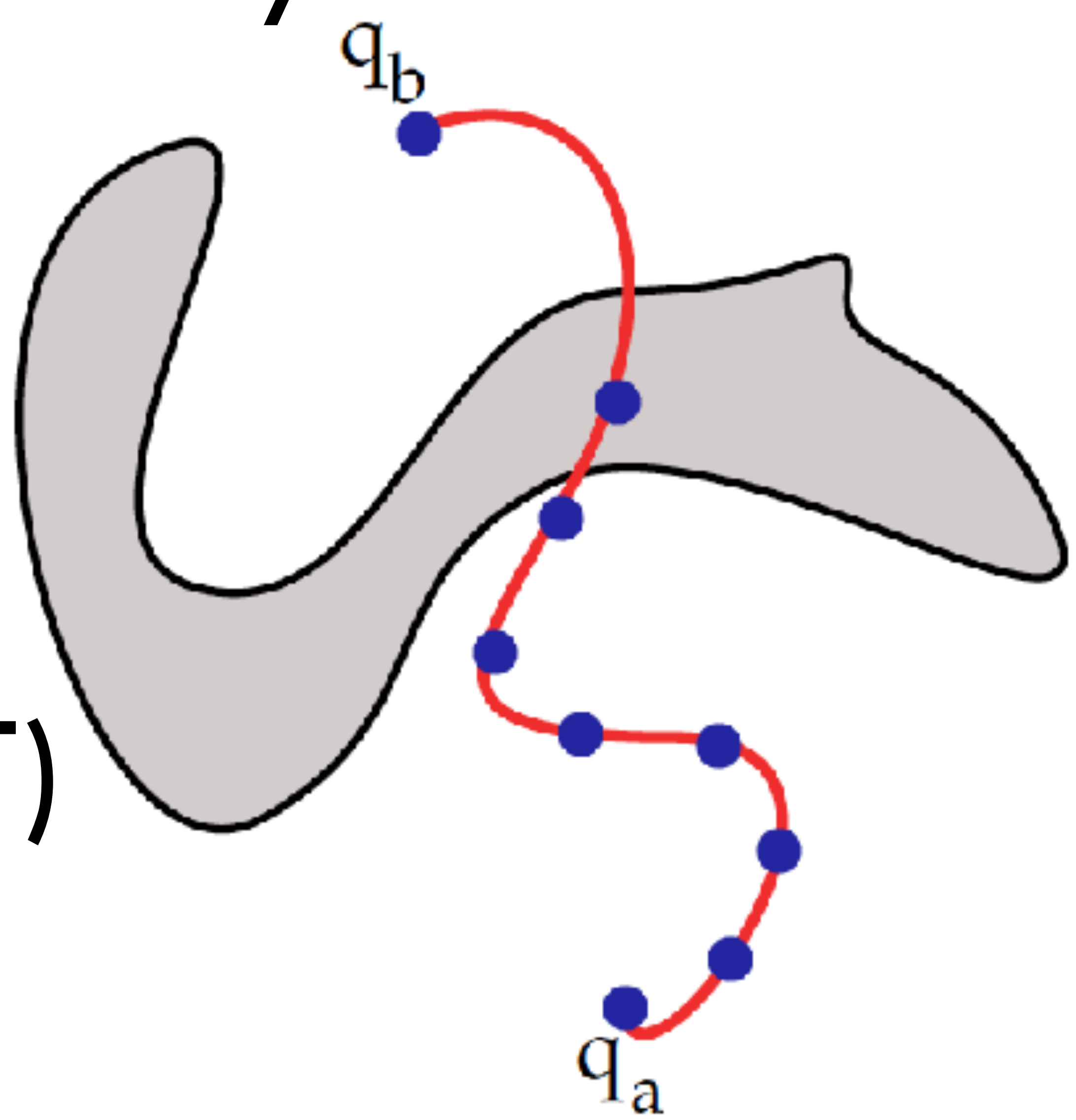
Review: Motion Planning (10/29/19)

- Plan a **path** for a robot from an initial configuration to a goal configuration that **avoids obstacles**
  - Sequence of <u>**continuous**</u> configurations
  - Configurations often are **high-dimensional**
    - Example: 7 DOFs

- High-level approaches:
  - Geometric decomposition
  - **Sampling-based**
  - Optimization-based

Sampling-Based Motion Planning

- **Discretize** configuration space by **sampling**
  - Sampling be deterministic or **random**
- **Implicitly** represent the collision-free configuration space using an blackbox **collision checker**
  - **Abstracts away** complex robot geometry

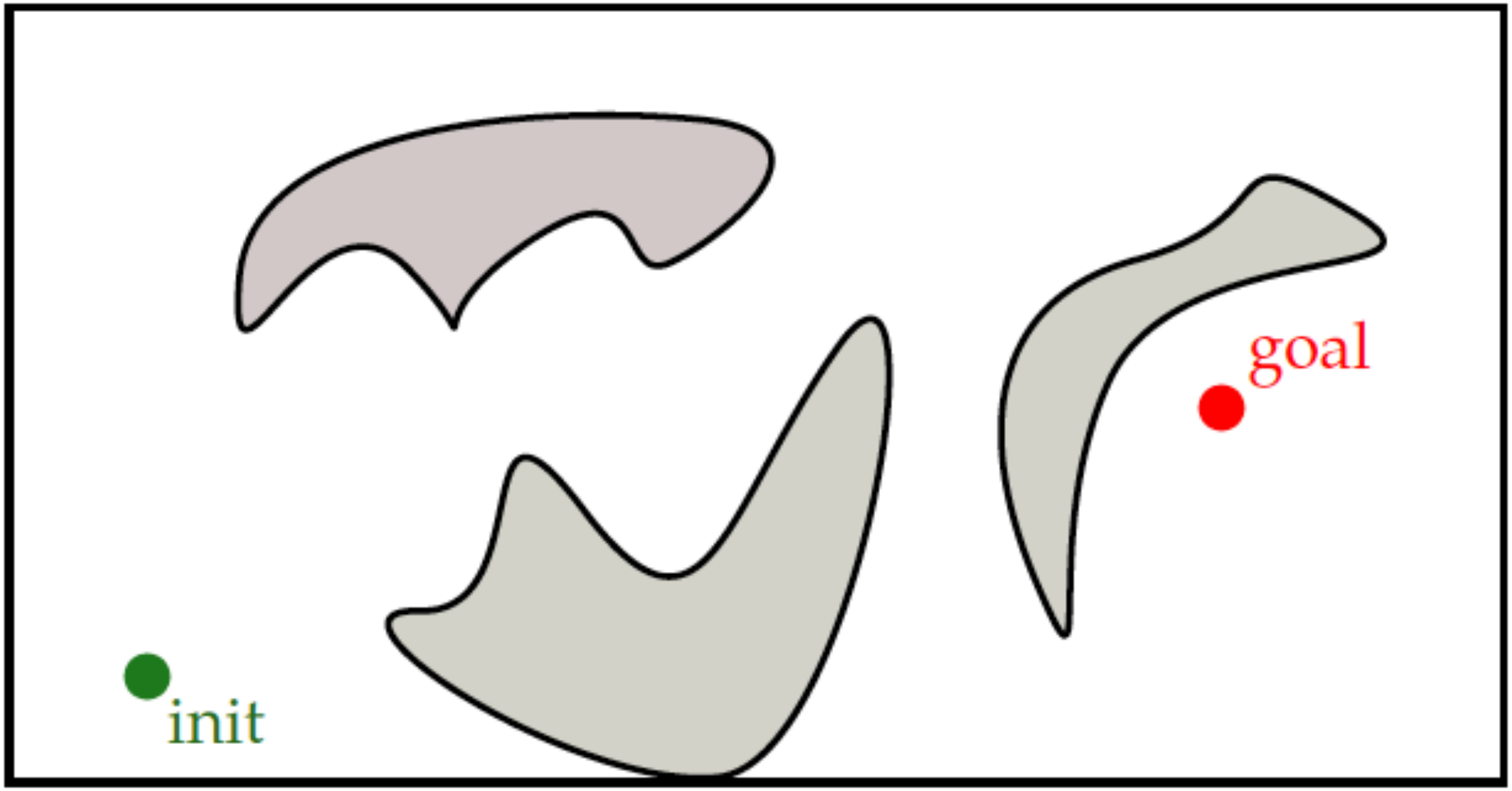


- Algorithms
  - **Probabilistic Roadmap (PRM)**
  - Rapidly-Exploring Random Tree (RRT)
  - Bidirectional RRT (BiRRT)

[Kavraki 1994][Kuffner 2000][LaValle 2006]

[Fig from Erion Plaku]

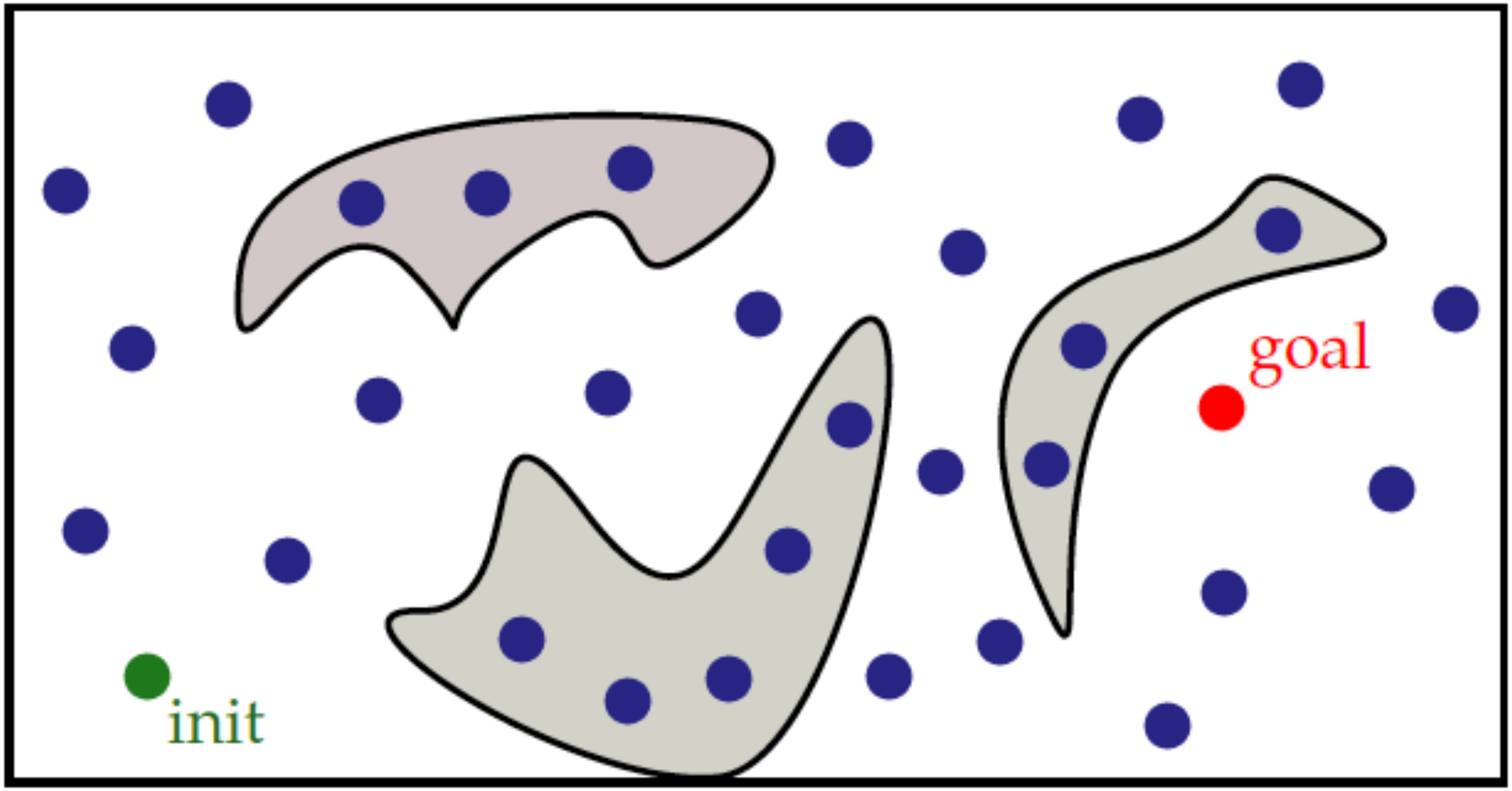
Probabilistic Roadmap (1/7)



[Fig from Erion Plaku]

Find a path from init to goal that avoids the obstacles

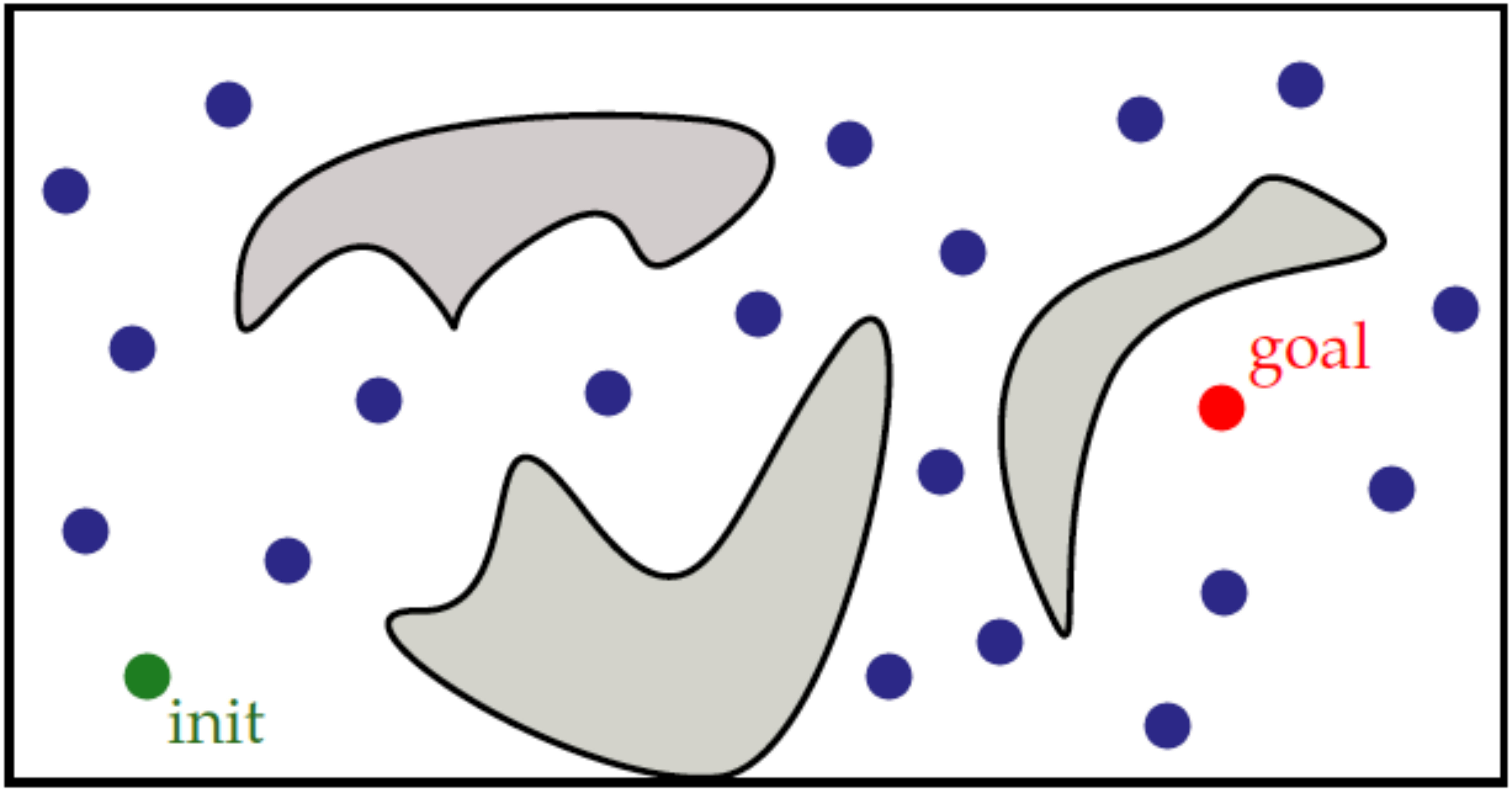
Probabilistic Roadmap (2/7)



[Fig from Erion Plaku]

Sample a set of configurations

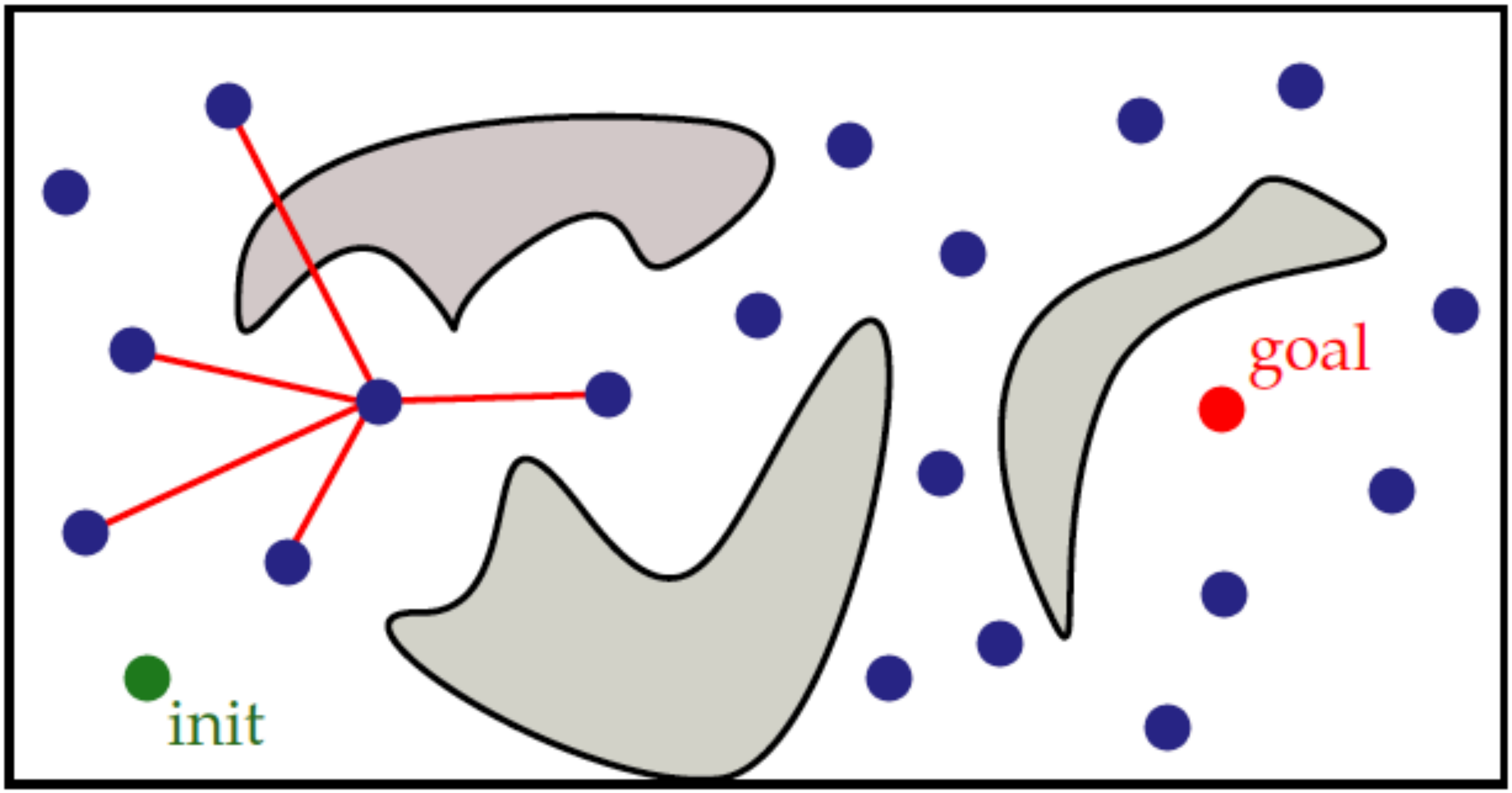
Probabilistic Roadmap (3/7)



[Fig from Erion Plaku]

Remove configurations that collide with the obstacles

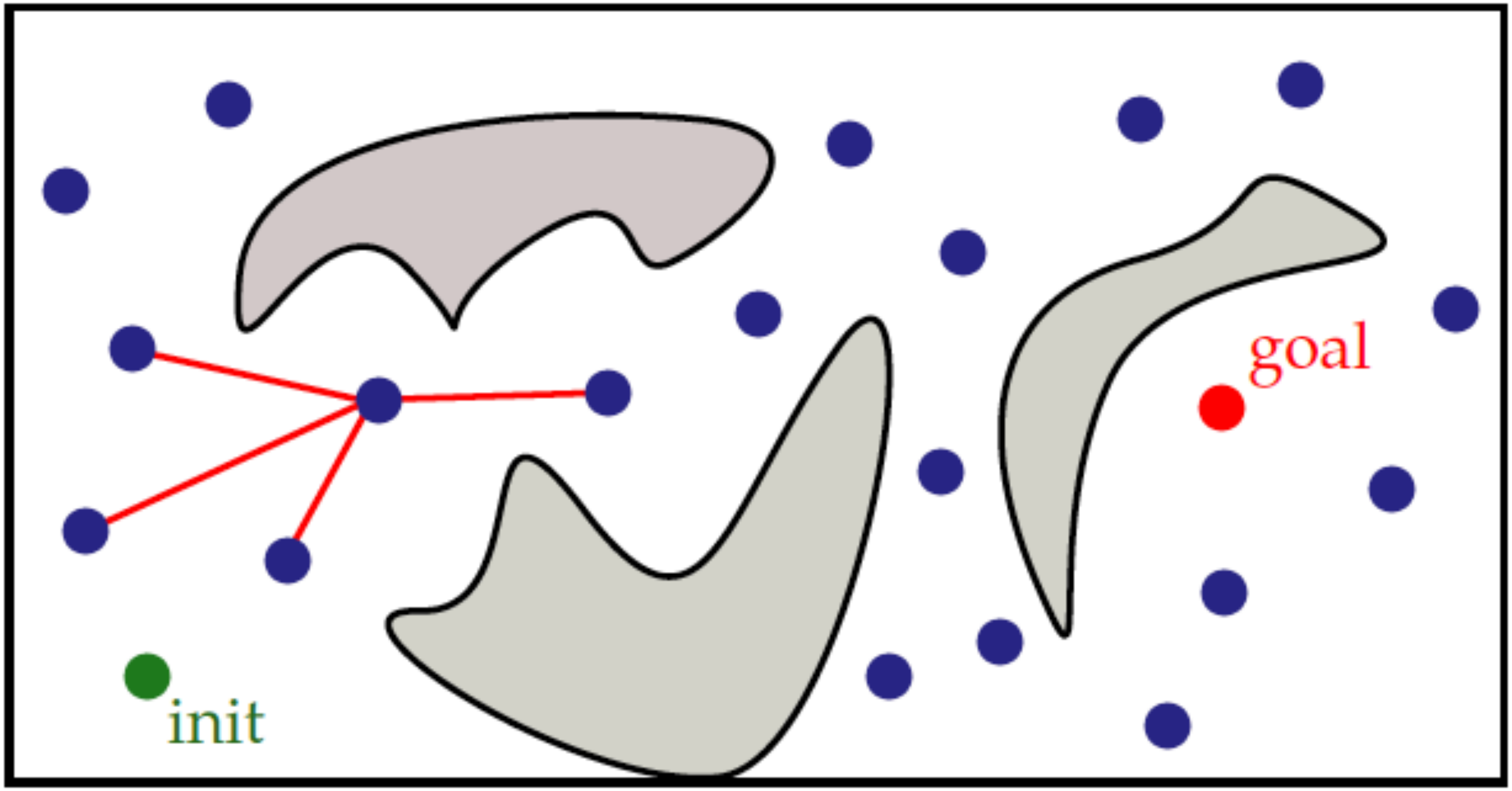
Probabilistic Roadmap (4/7)



[Fig from Erion Plaku]

Connect nearby configurations

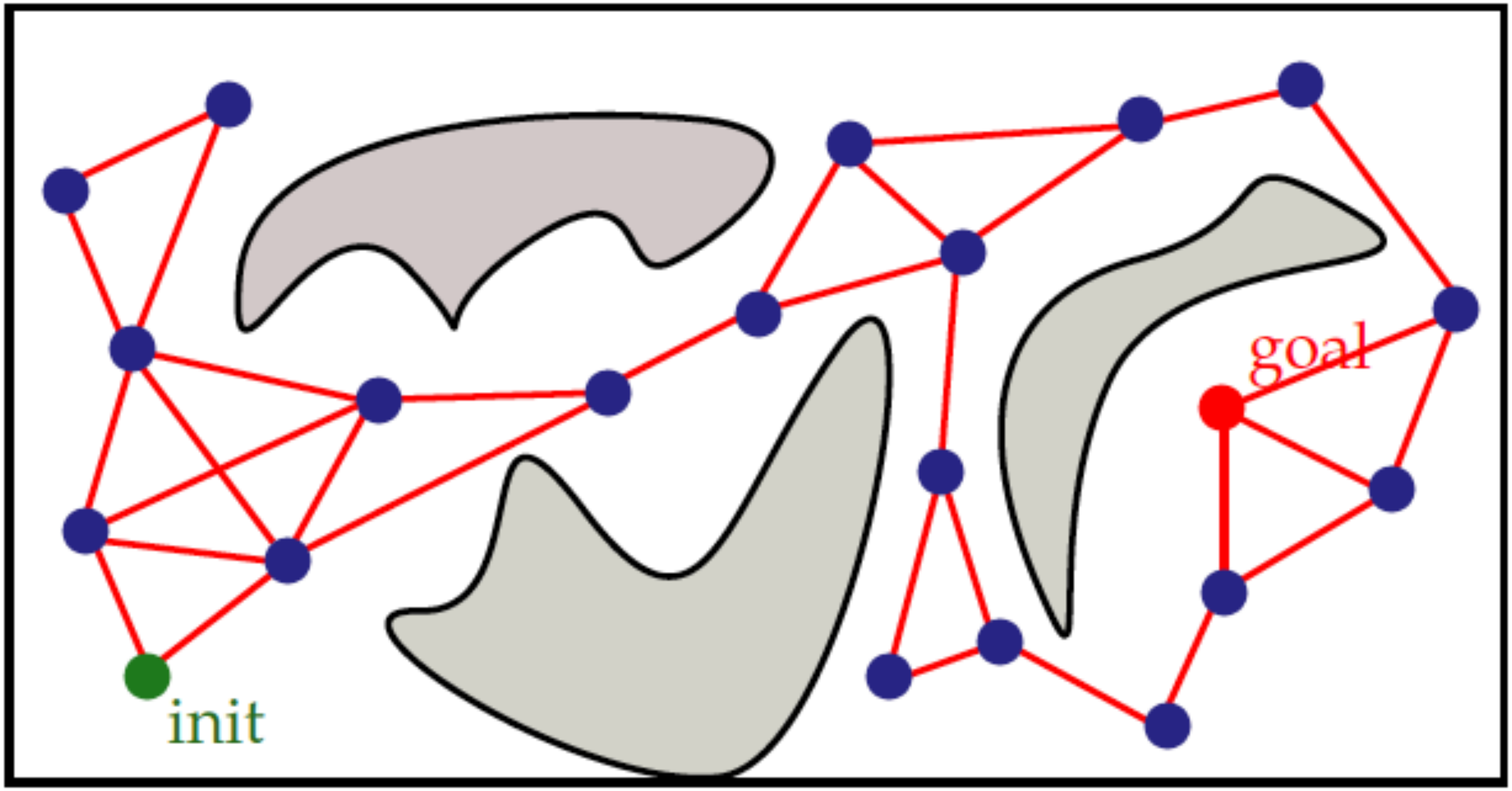
Probabilistic Roadmap (5/7)



[Fig from Erion Plaku]

Prune connections that collide with the obstacles

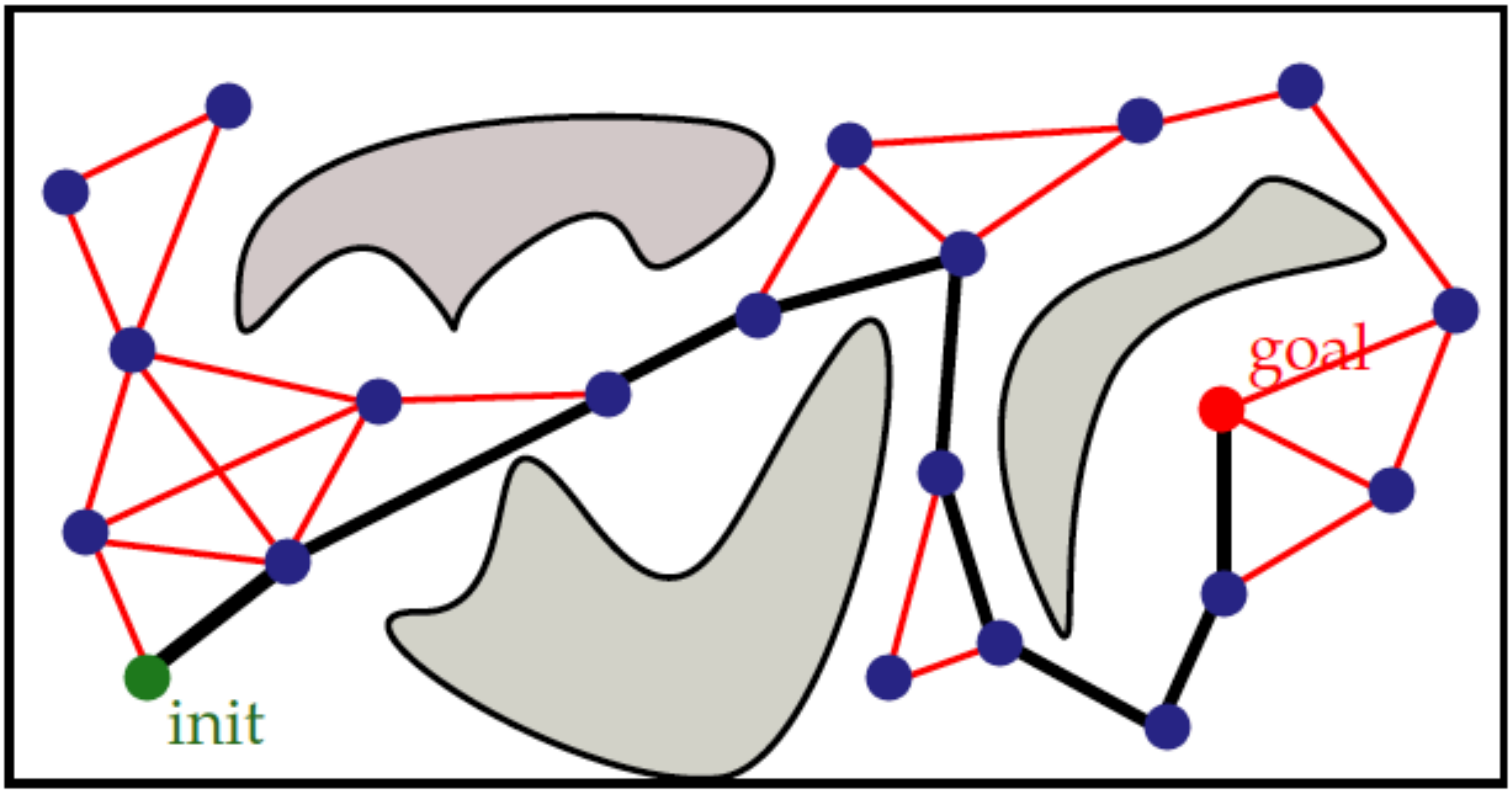
Probabilistic Roadmap (6/7)



[Fig from Erion Plaku]

The resulting structure is a finite roadmap (graph)

Probabilistic Roadmap (7/7)

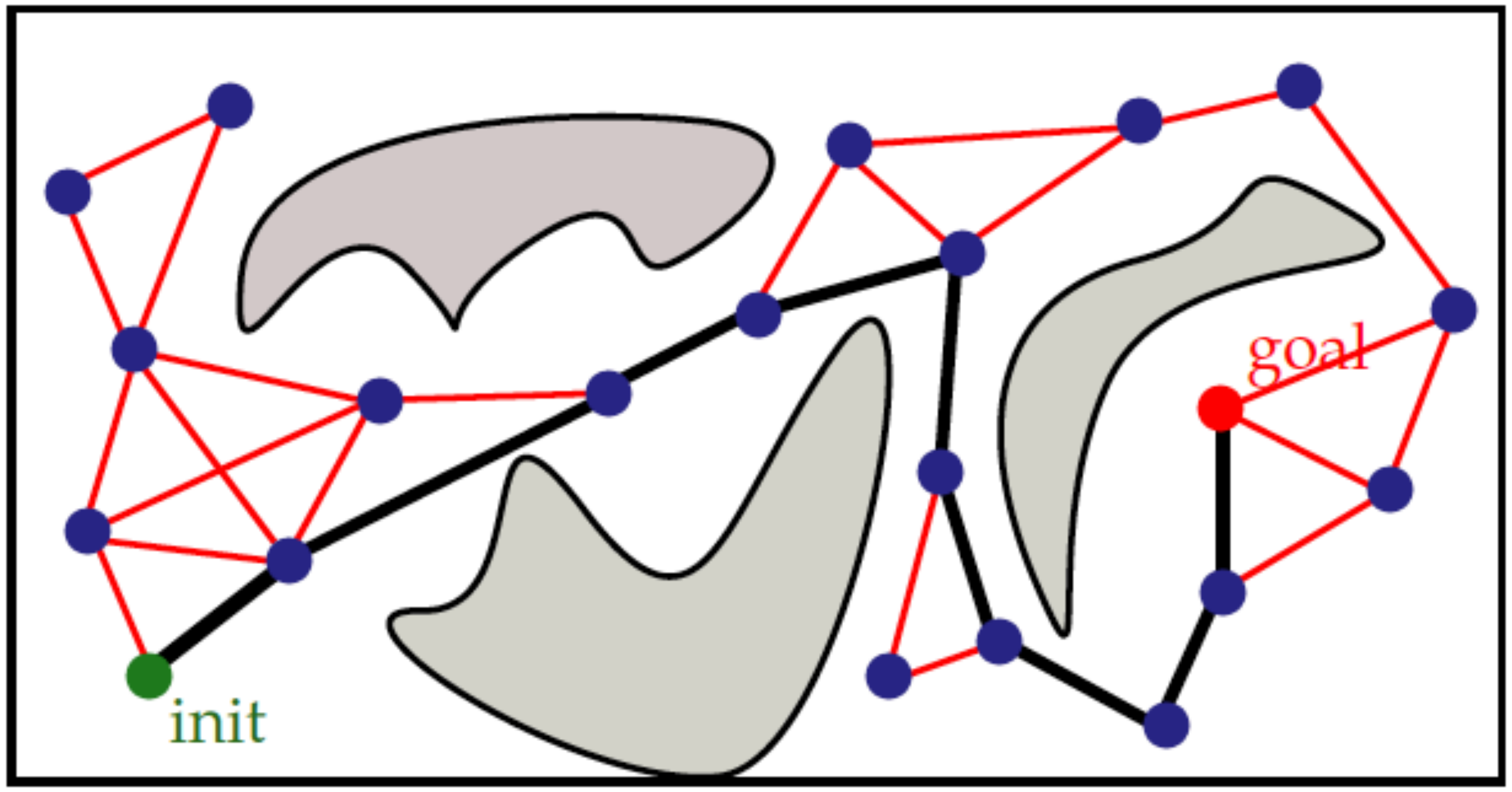


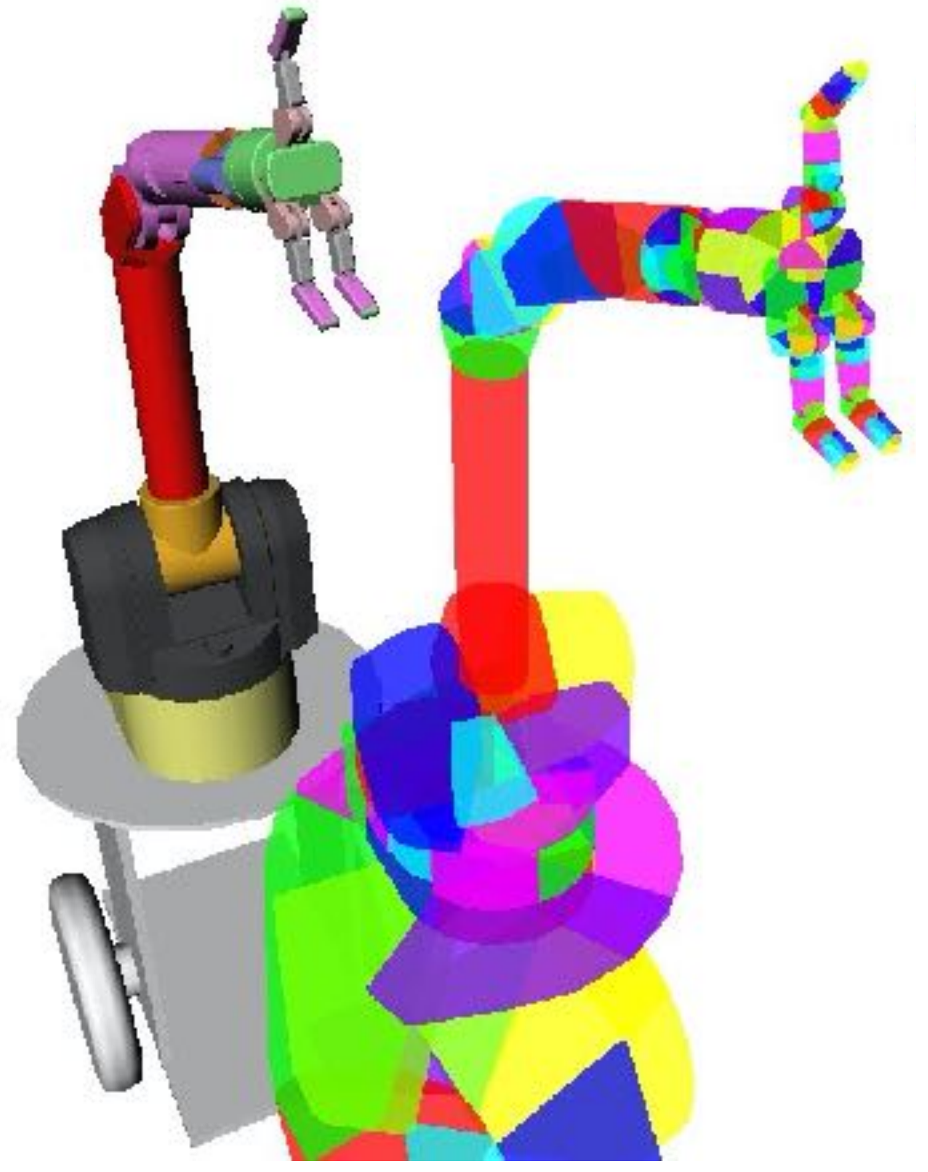
[Fig from Erion Plaku]

Search for the shortest-path on the roadmap

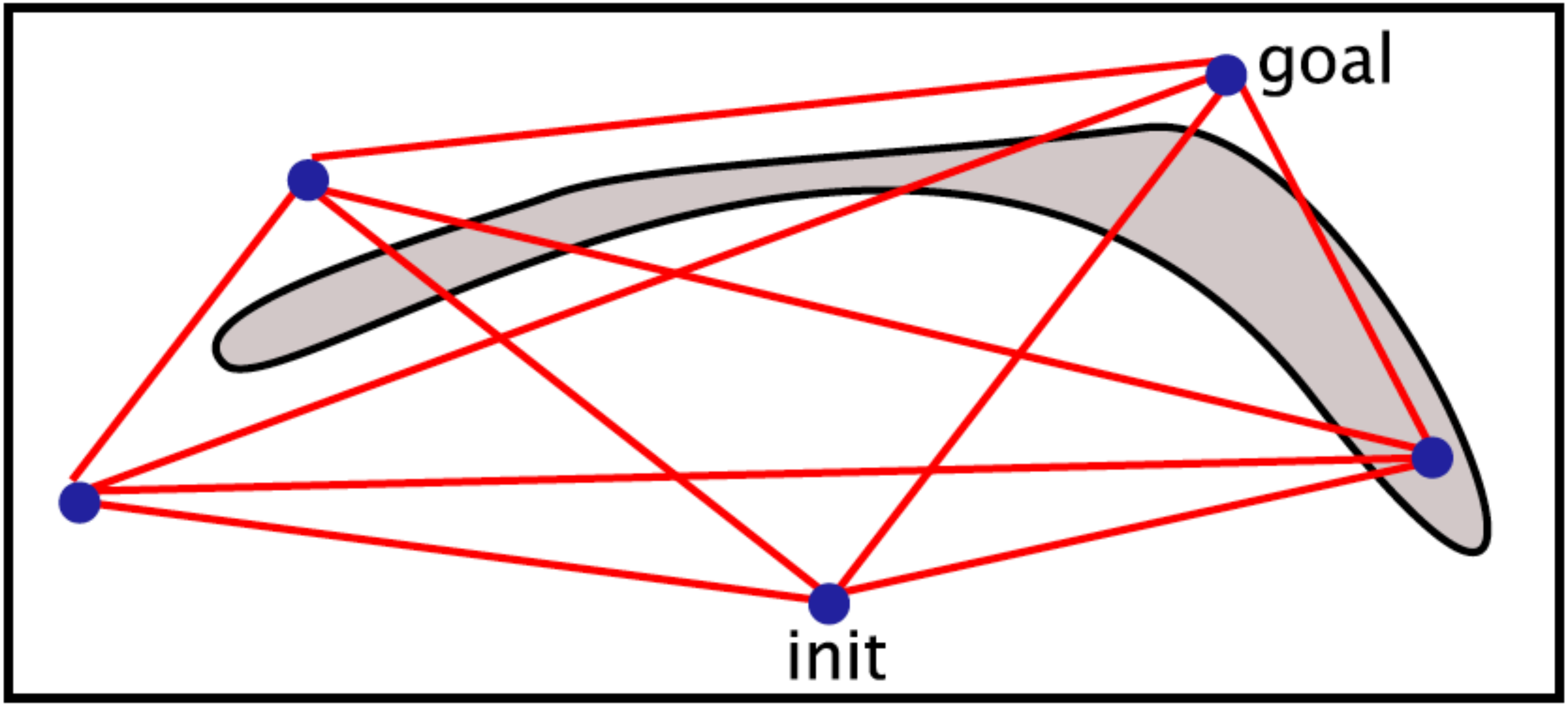
Collision Checking is Expensive

- Collision checking **dominates** runtime
  - **Complex geometries** & **fine resolutions** (for safety)
- Many edges clearly do not lie on a low-cost path
- **Optimistically** plan **without collisions**
- Check collisions **lazily** only by only evaluating **candidate plans**





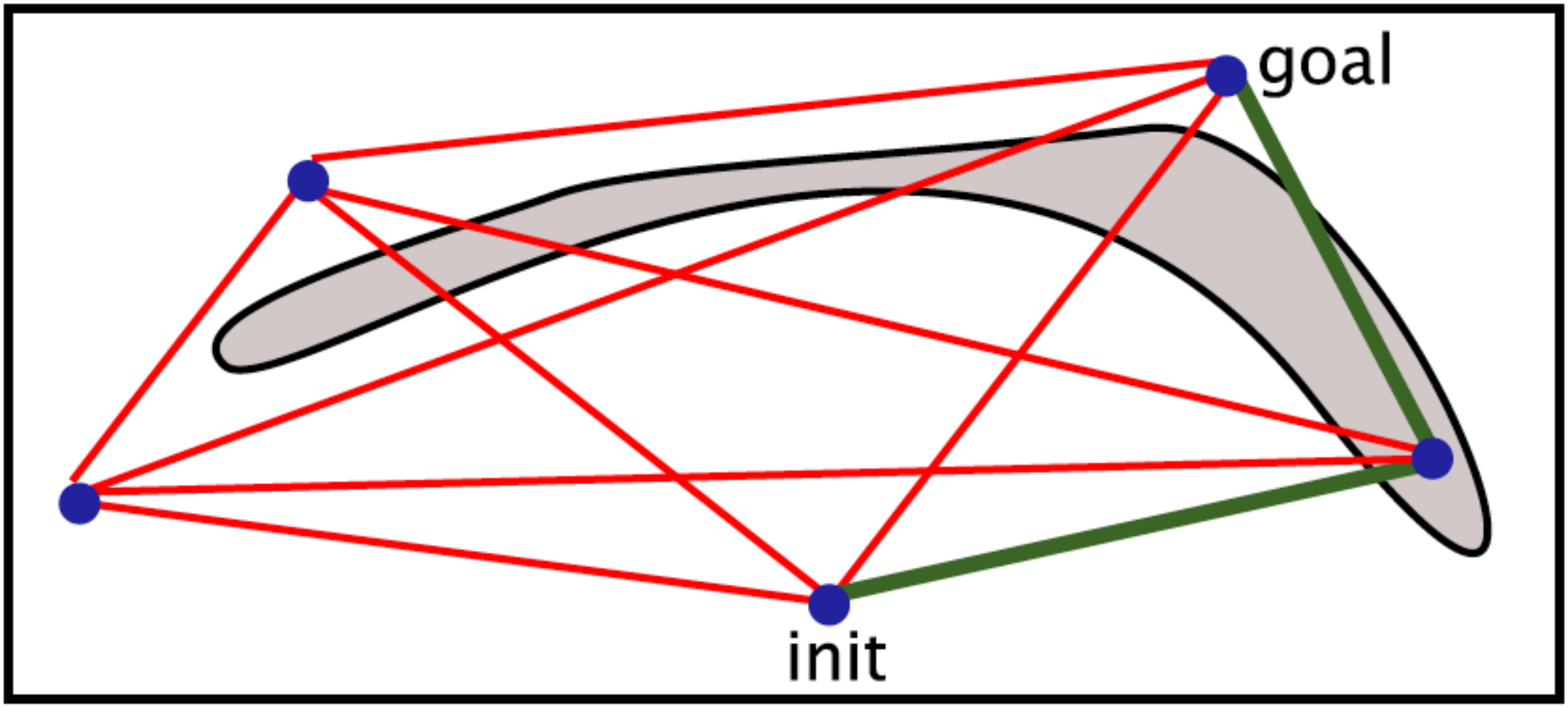
Lazy PRM (1/10)



[Fig from Erion Plaku]

Construct a PRM ignoring collisions

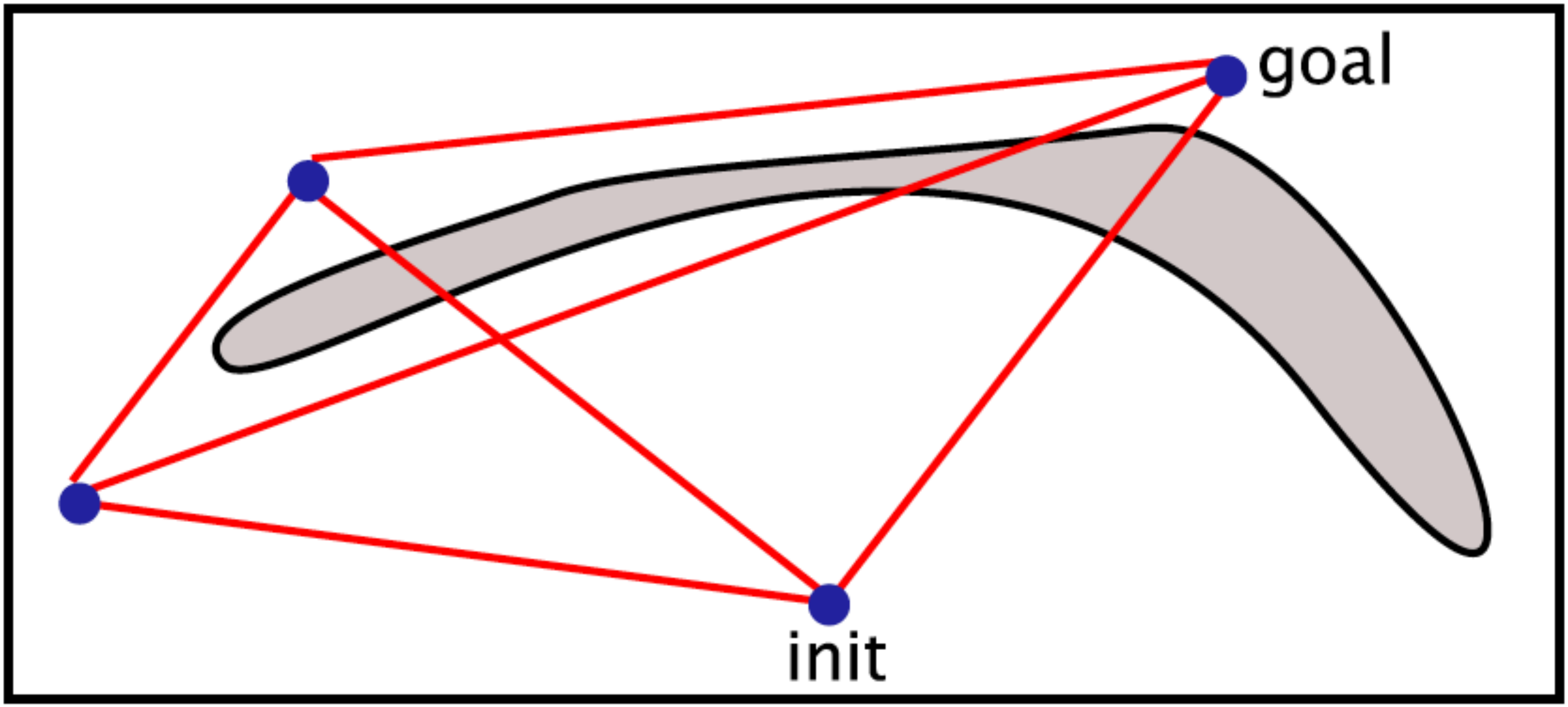
Lazy PRM (2/10)



[Fig from Erion Plaku]

Search for the shortest-path on the roadmap

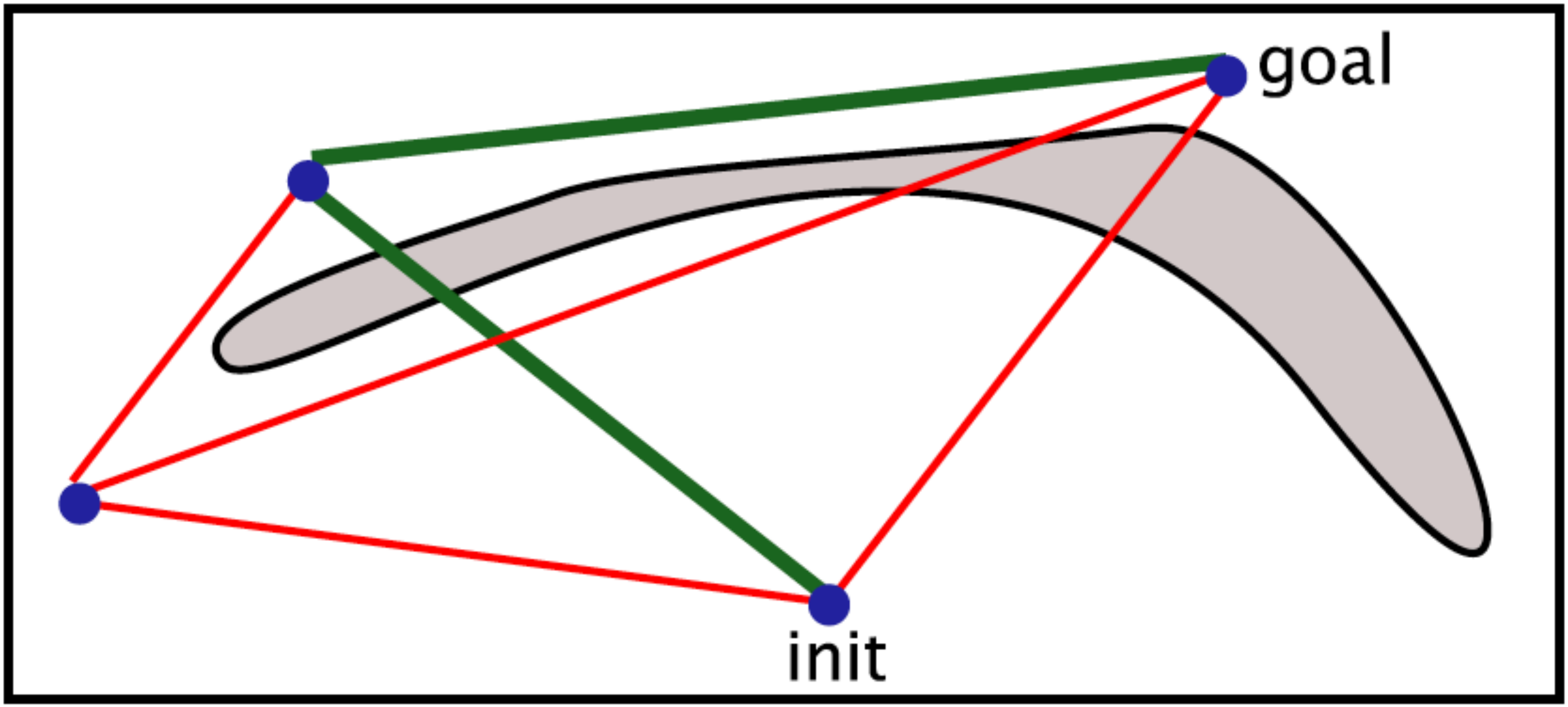
Lazy PRM (3/10)



[Fig from Erion Plaku]

Remove plan edges that collide with obstacles

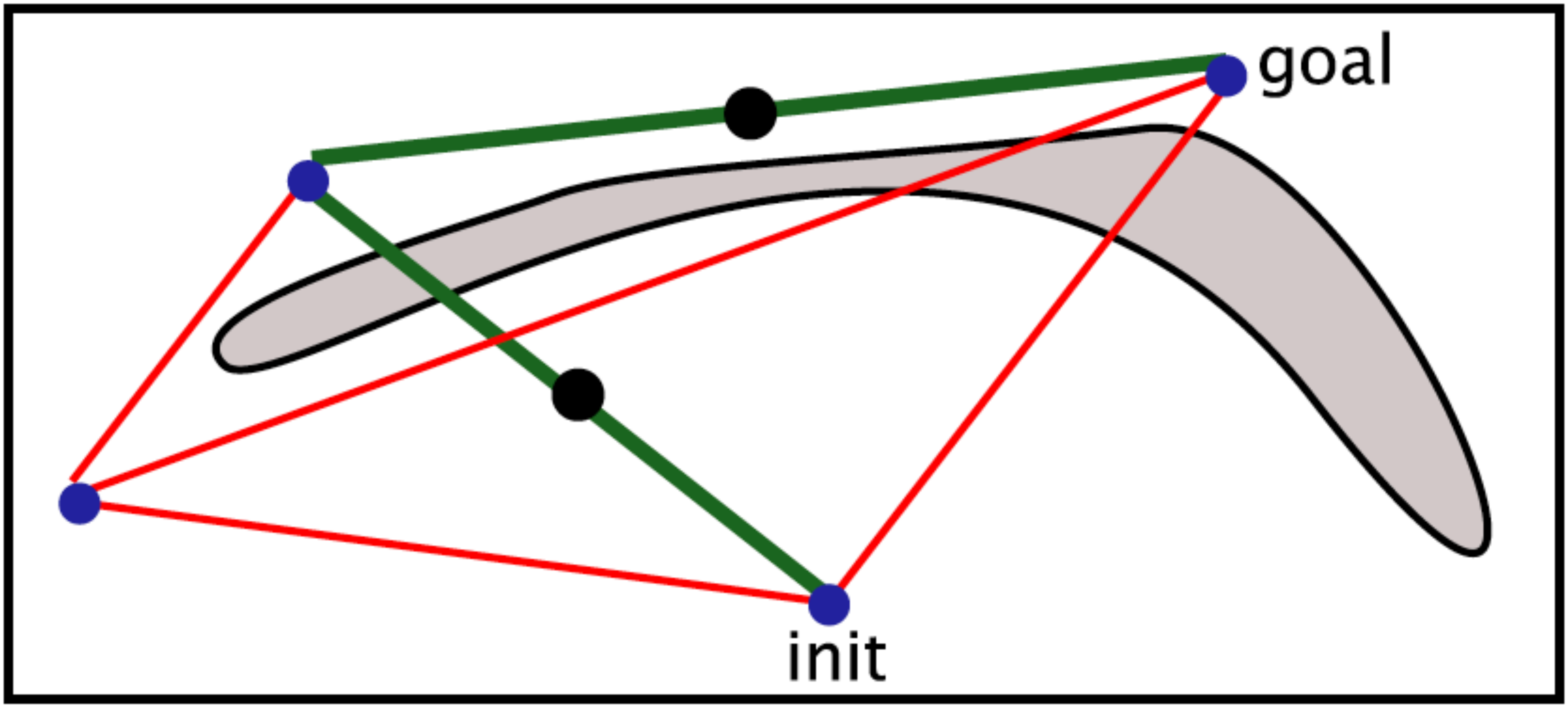
Lazy PRM (4/10)



[Fig from Erion Plaku]

Search for the new shortest-path on the roadmap

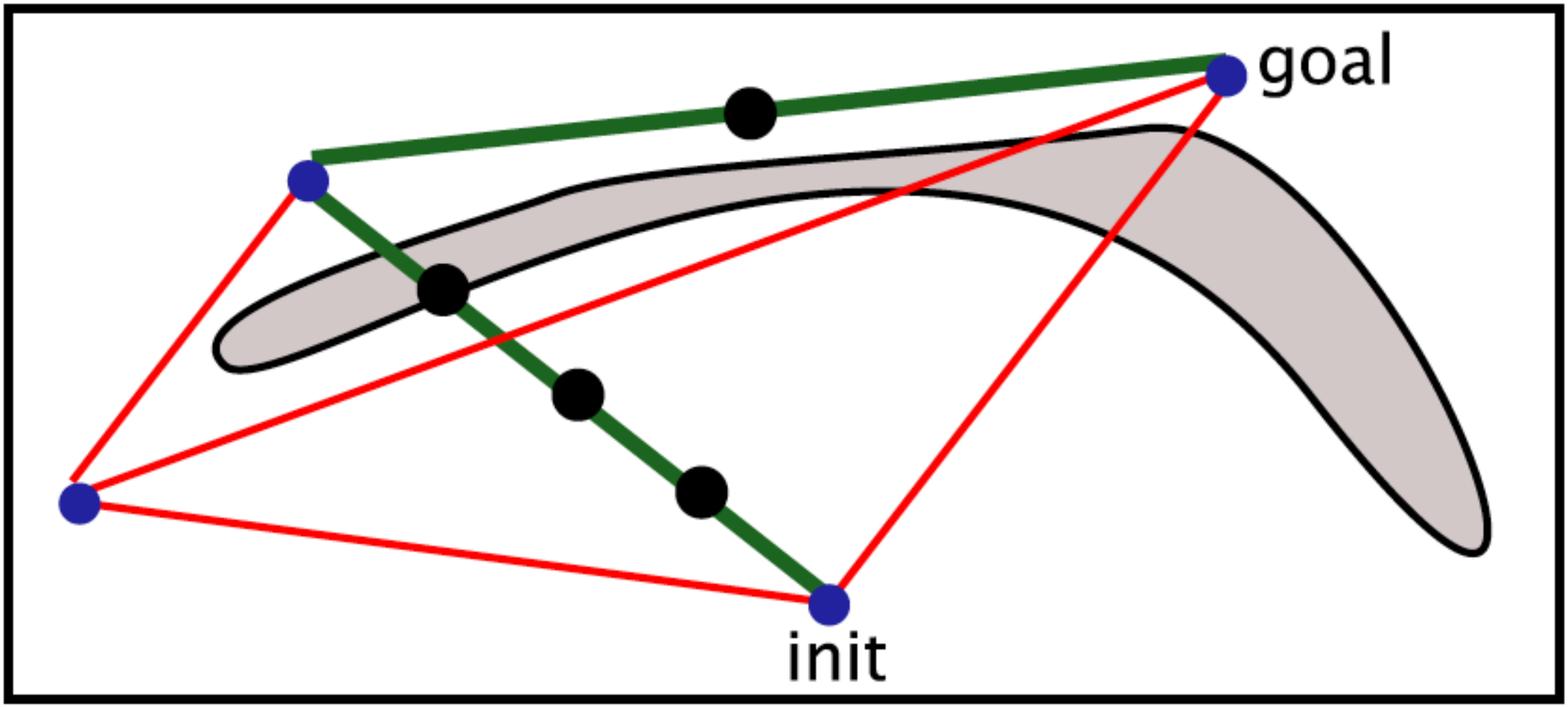
Lazy PRM (5/10)



[Fig from Erion Plaku]

Check the edges on the plan for collisions

Lazy PRM (6/10)

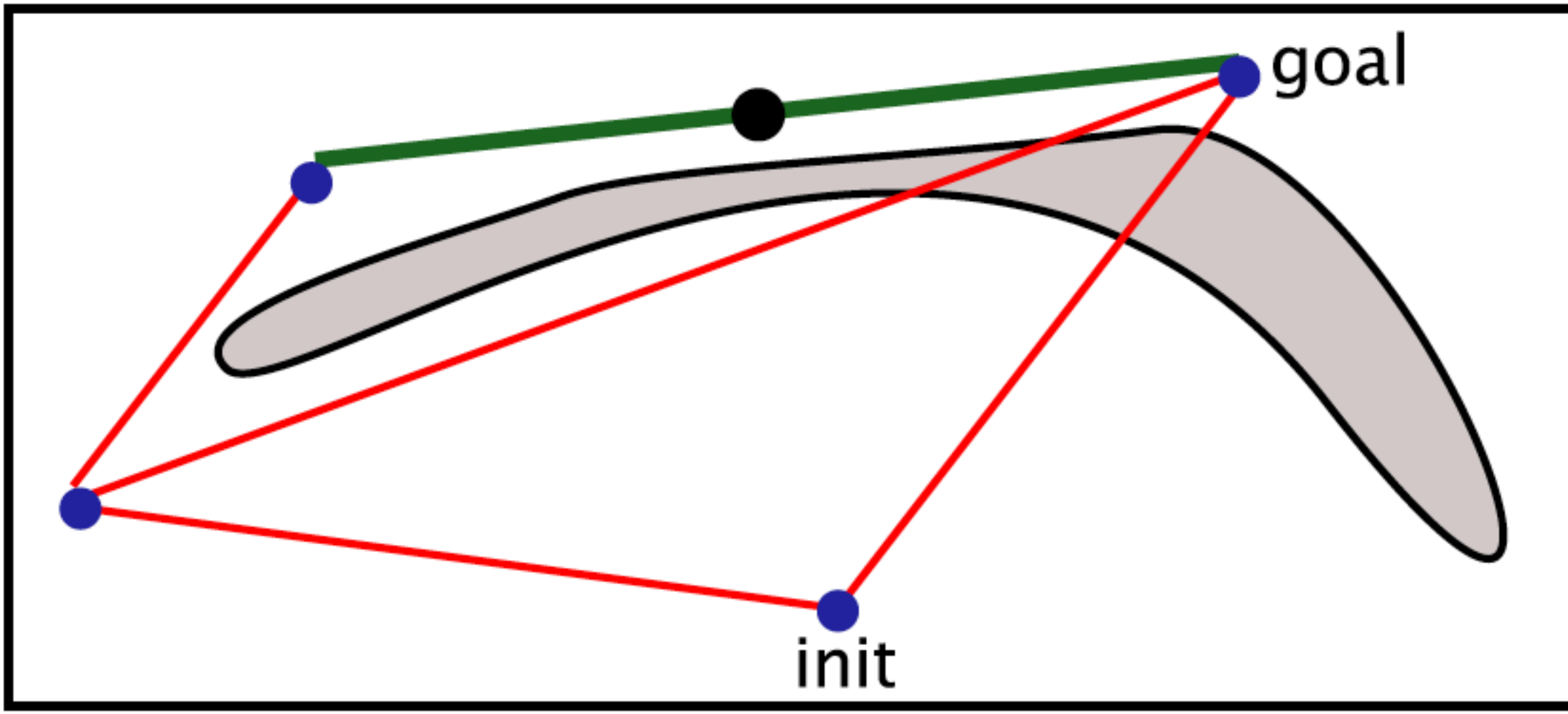


[Fig from Erion Plaku]

Check the edges on the plan for collisions

(with increased resolution)

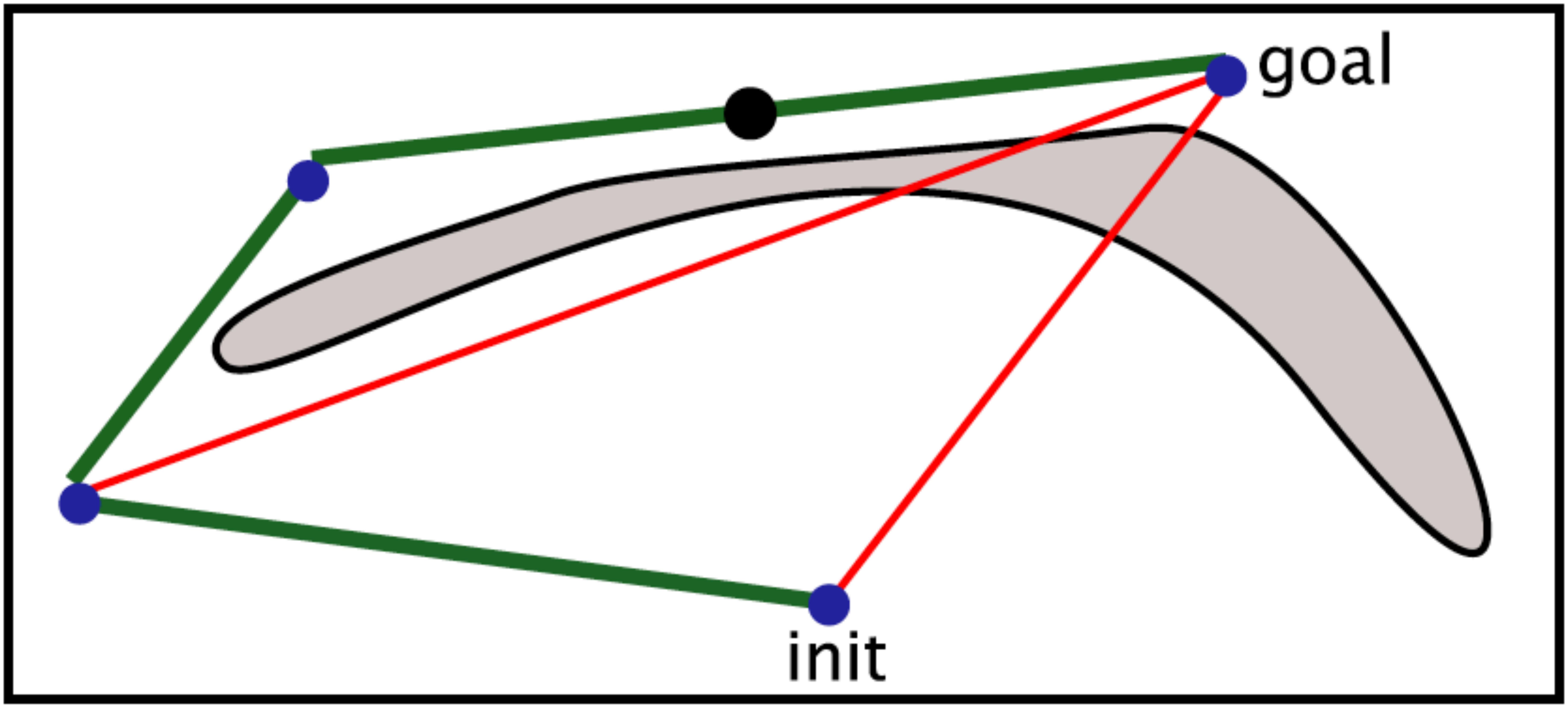
Lazy PRM (7/10)



[Fig from Erion Plaku]

Remove plan edges that collide with obstacles

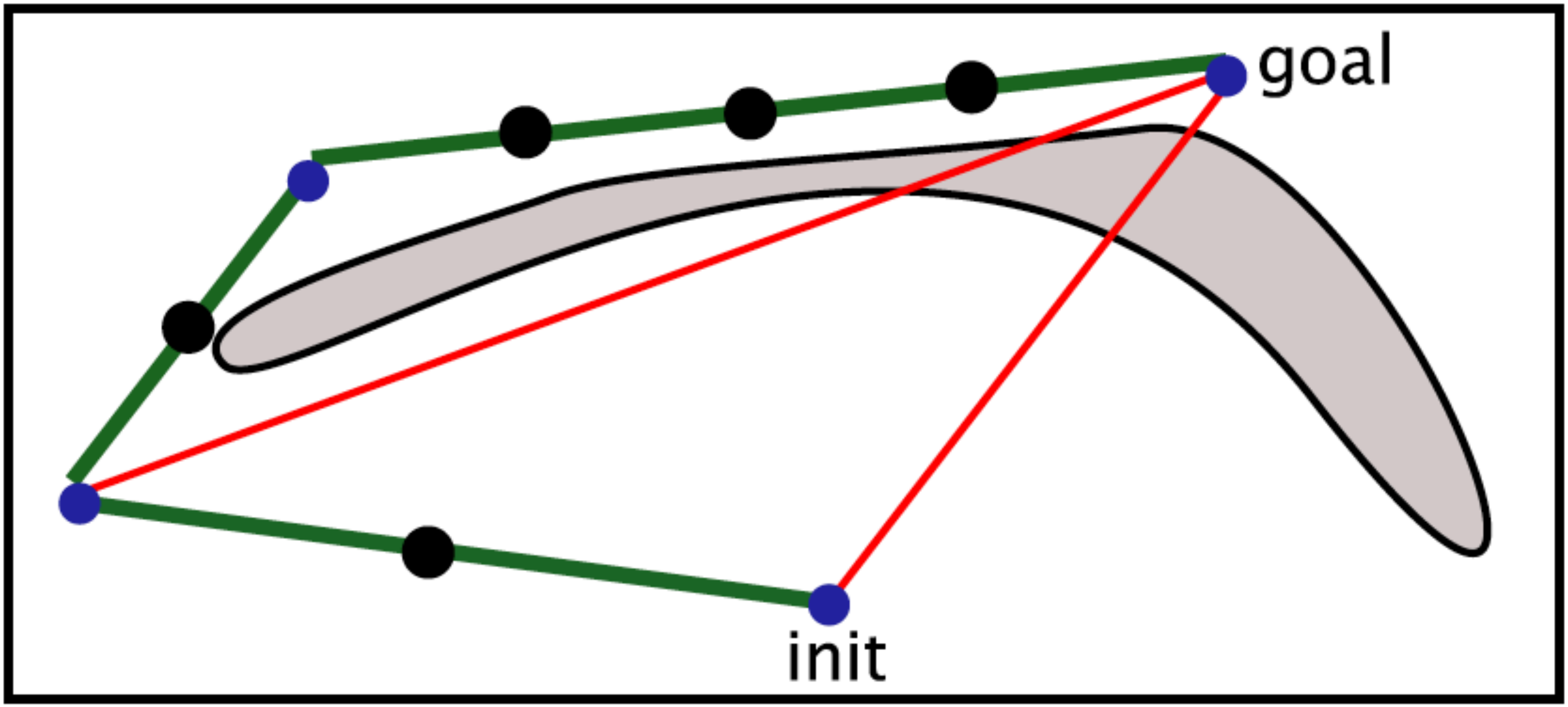
Lazy PRM (8/10)



[Fig from Erion Plaku]

Search for the new shortest-path on the roadmap

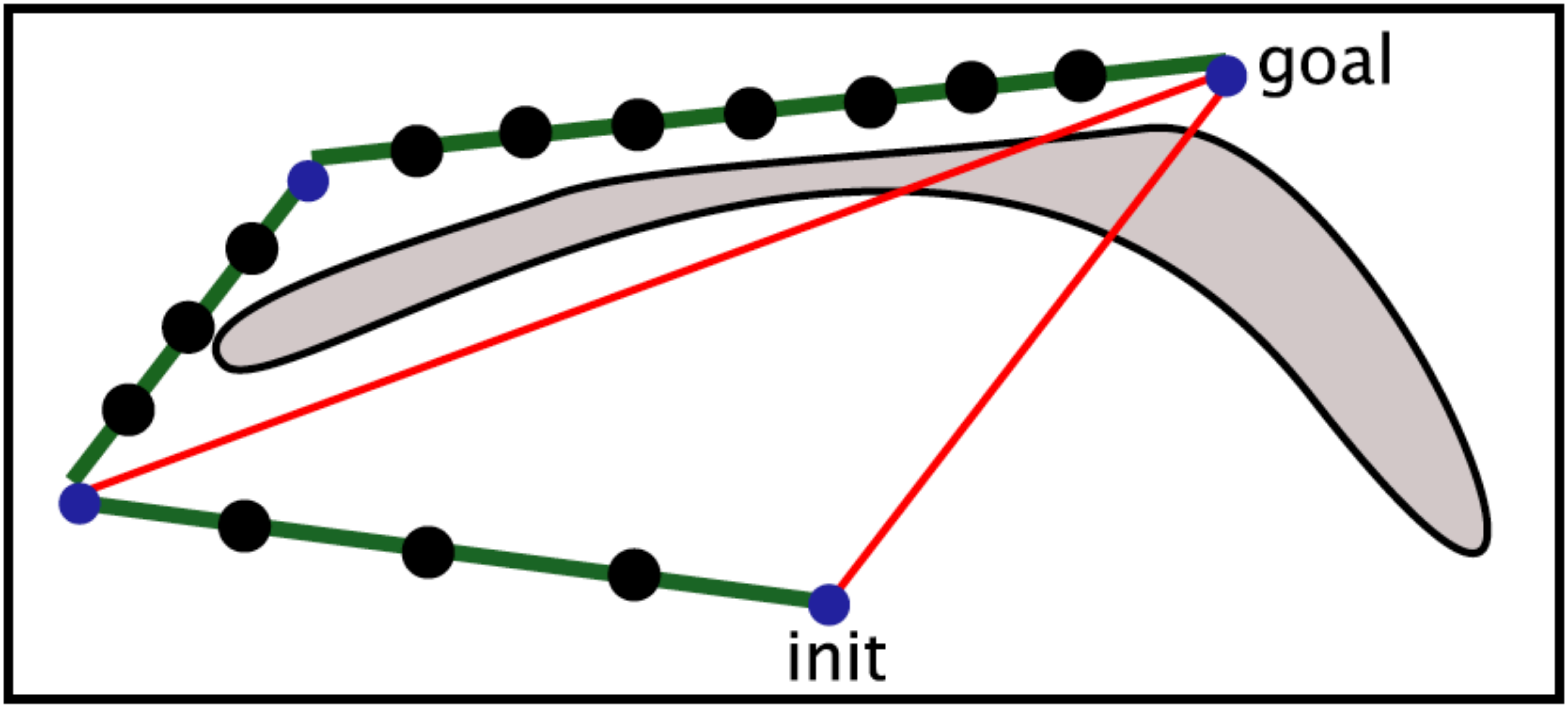
Lazy PRM (9/10)



[Fig from Erion Plaku]

Check the edges on the plan for collisions

Lazy PRM (10/10)



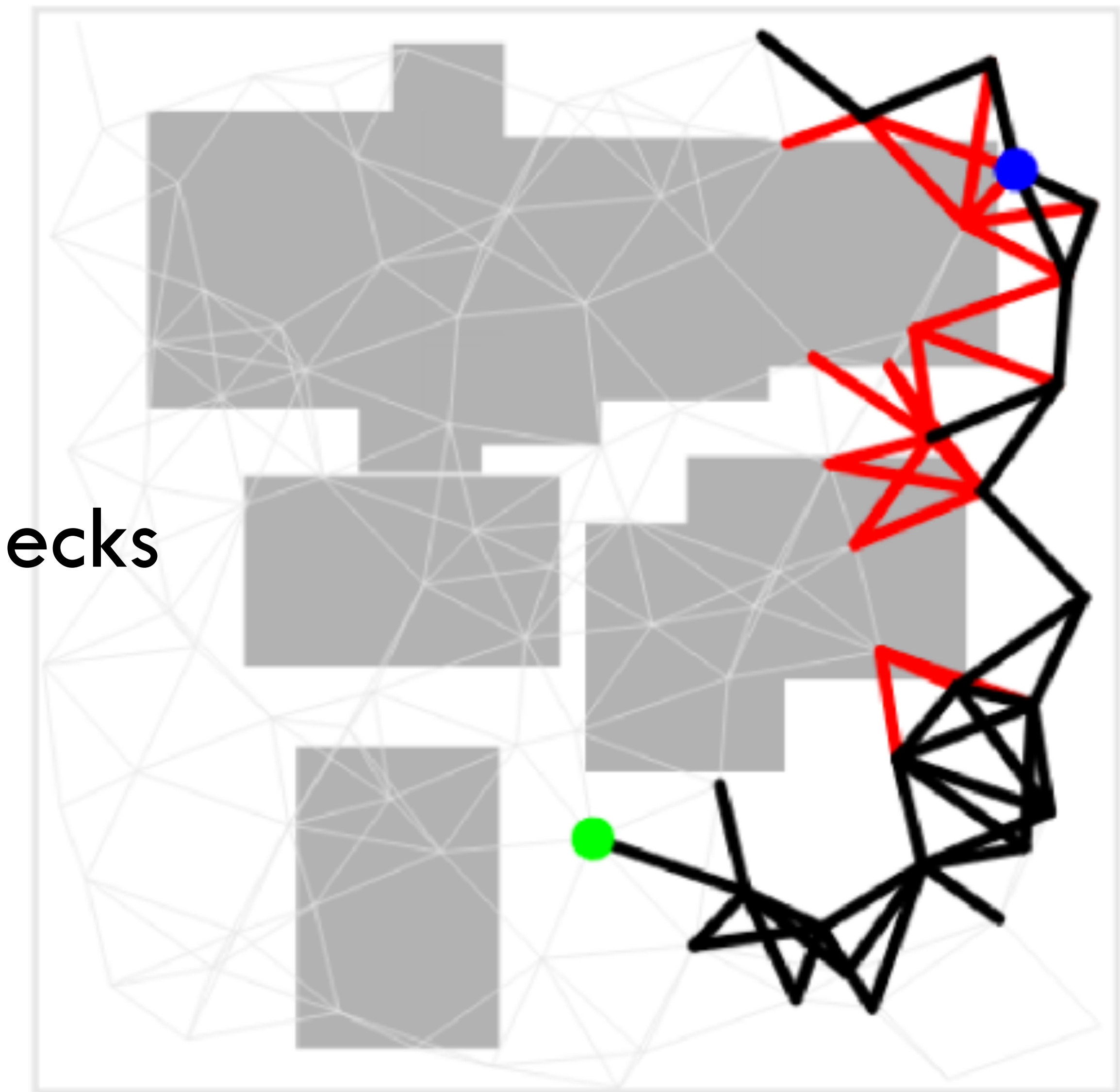
[Fig from Erion Plaku]

Return the current path as a solution

Lazy Motion Planning

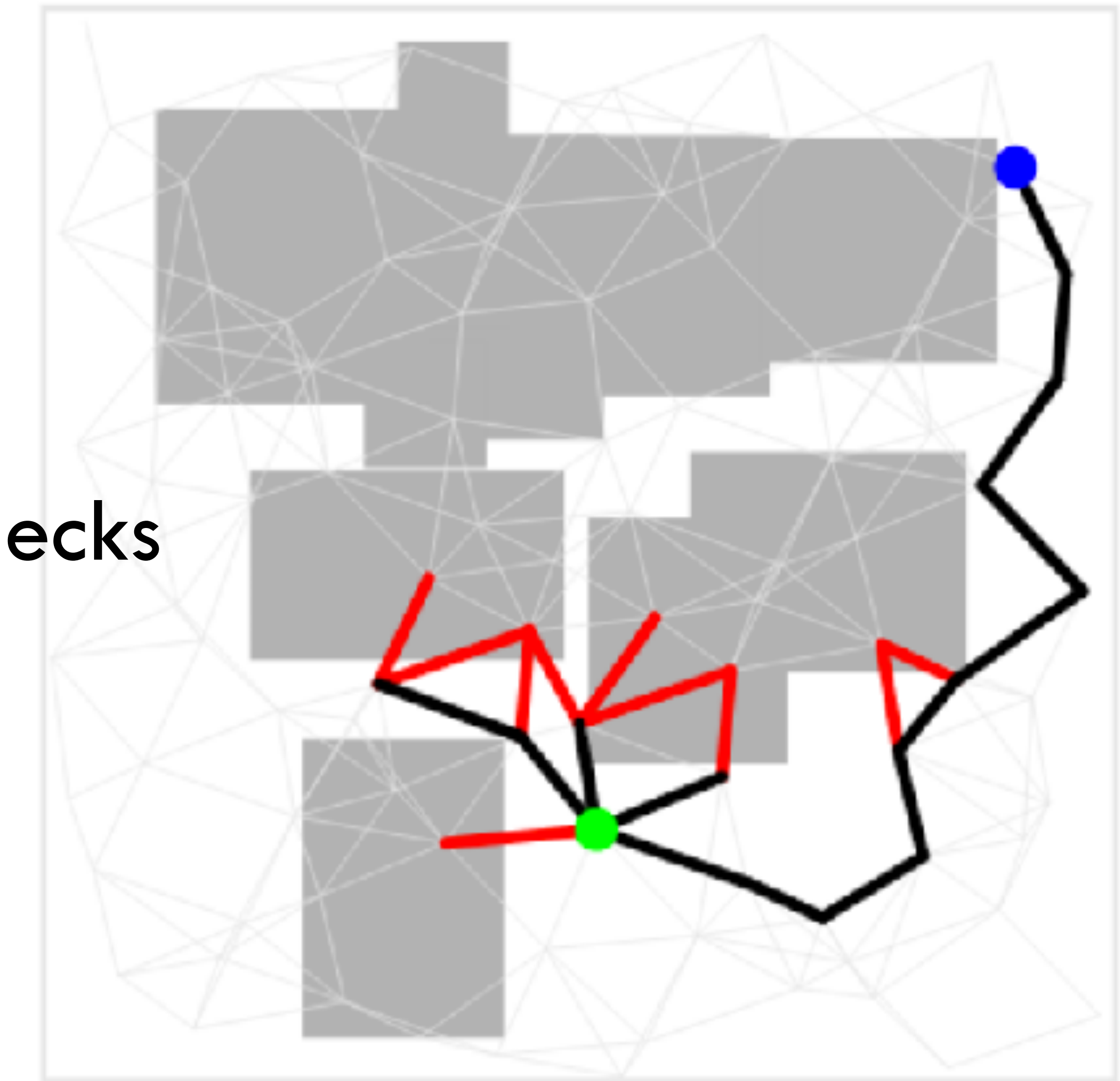
- **Defer** collision checking until a path is found
- **Remove** colliding edges path from the roadmap
- **Repeat** this process with a new path
- **Terminate** when a collision-fee path is found

77 checks

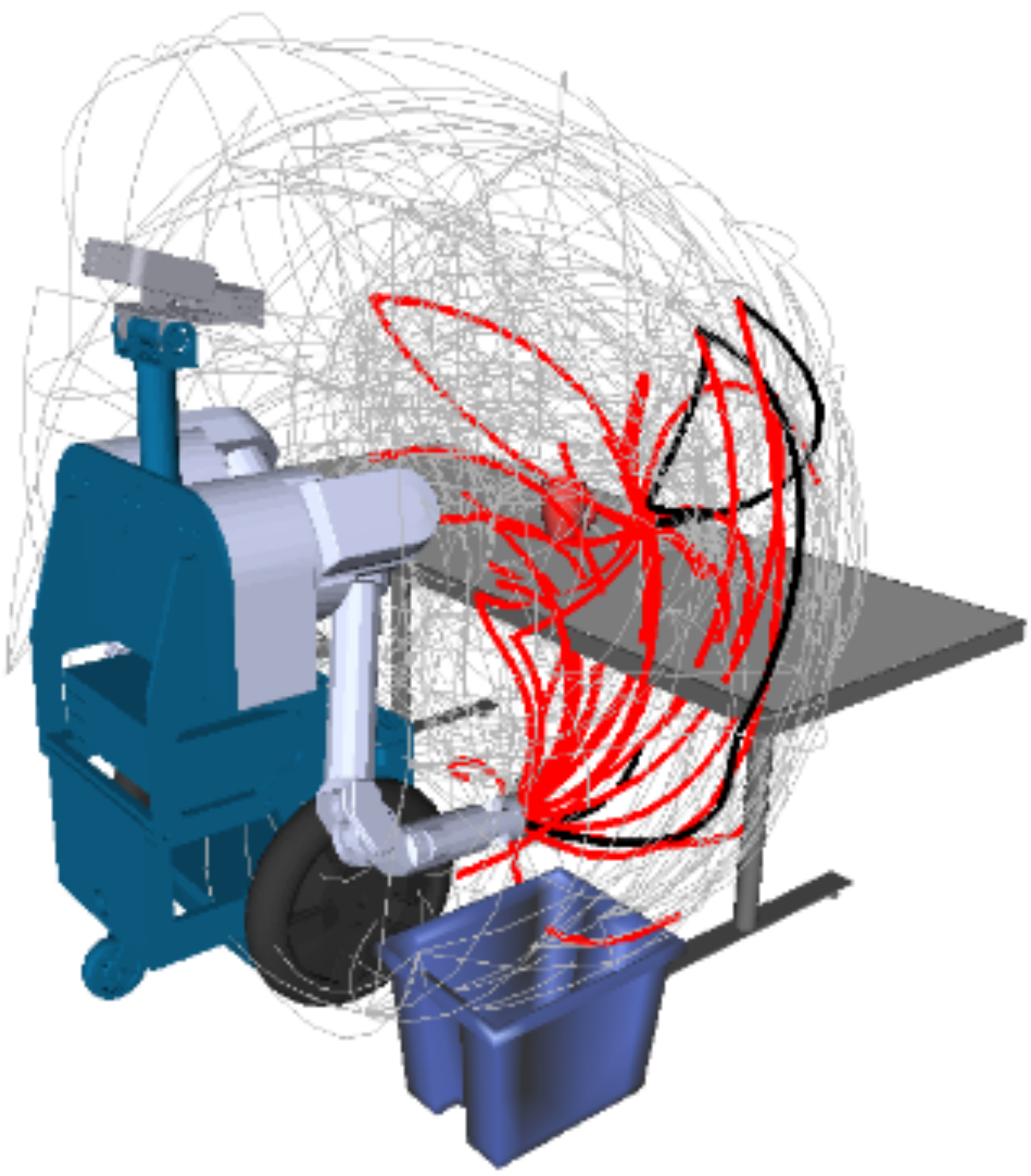


Eager (during search)

23 checks



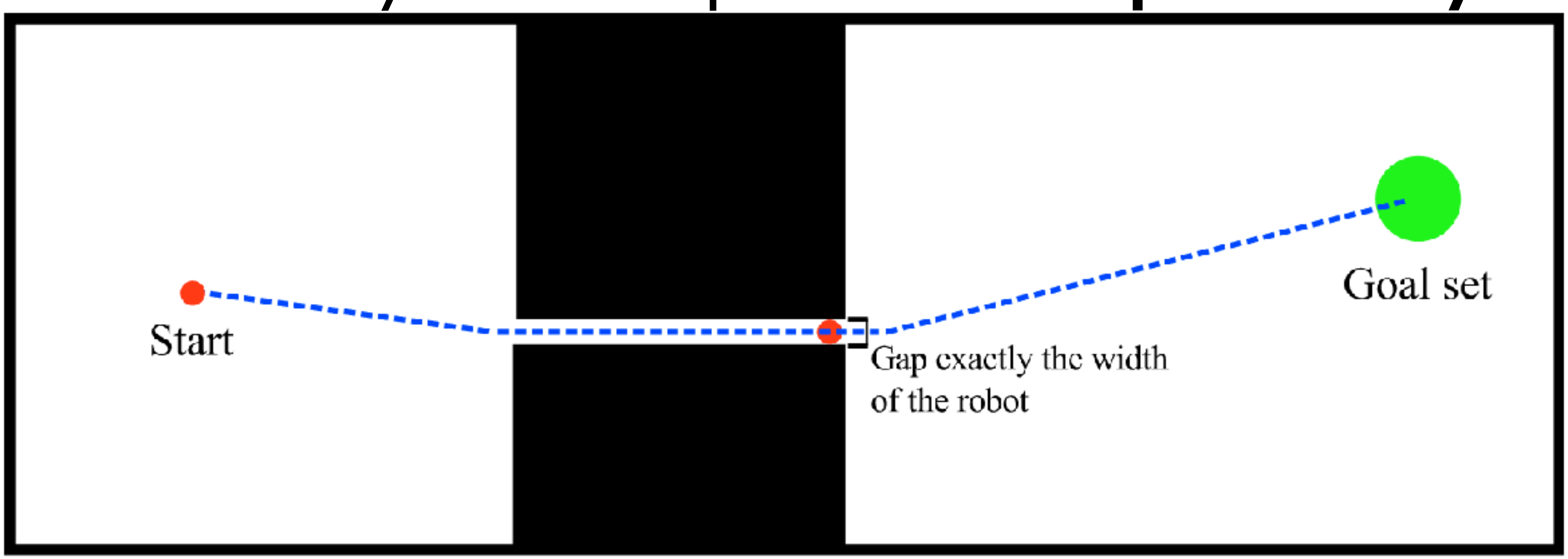
Lazy



[Bohlin 2000][Dellin 2016]

Theoretical Properties

- Sampling-based algorithms cannot prove **infeasibility** nor even solve every **feasible problem**
  - **Robustly feasible:** a problem that admits a solution for which all **local perturbations** are also solutions
- **Probabilistic complete:** an algorithm that solves any robustly feasible problem with **probability 1**



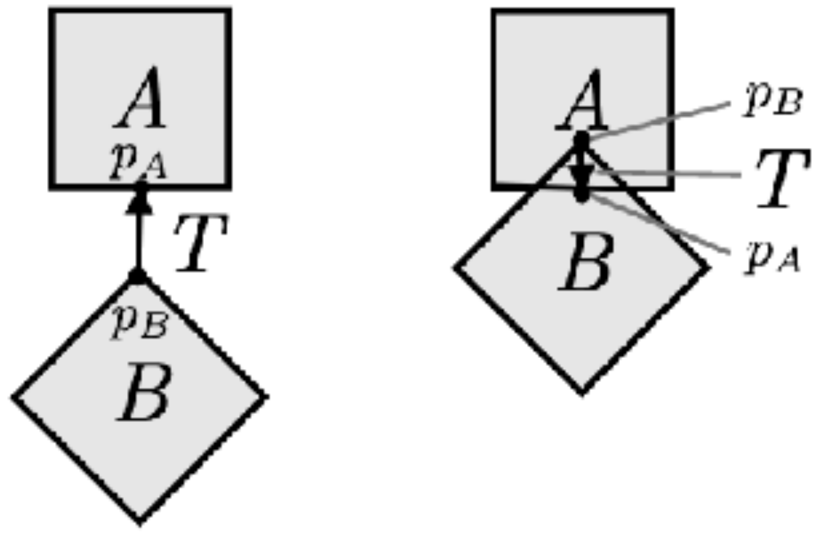
[Fig from Jenny Barry]

Trajectory Optimization

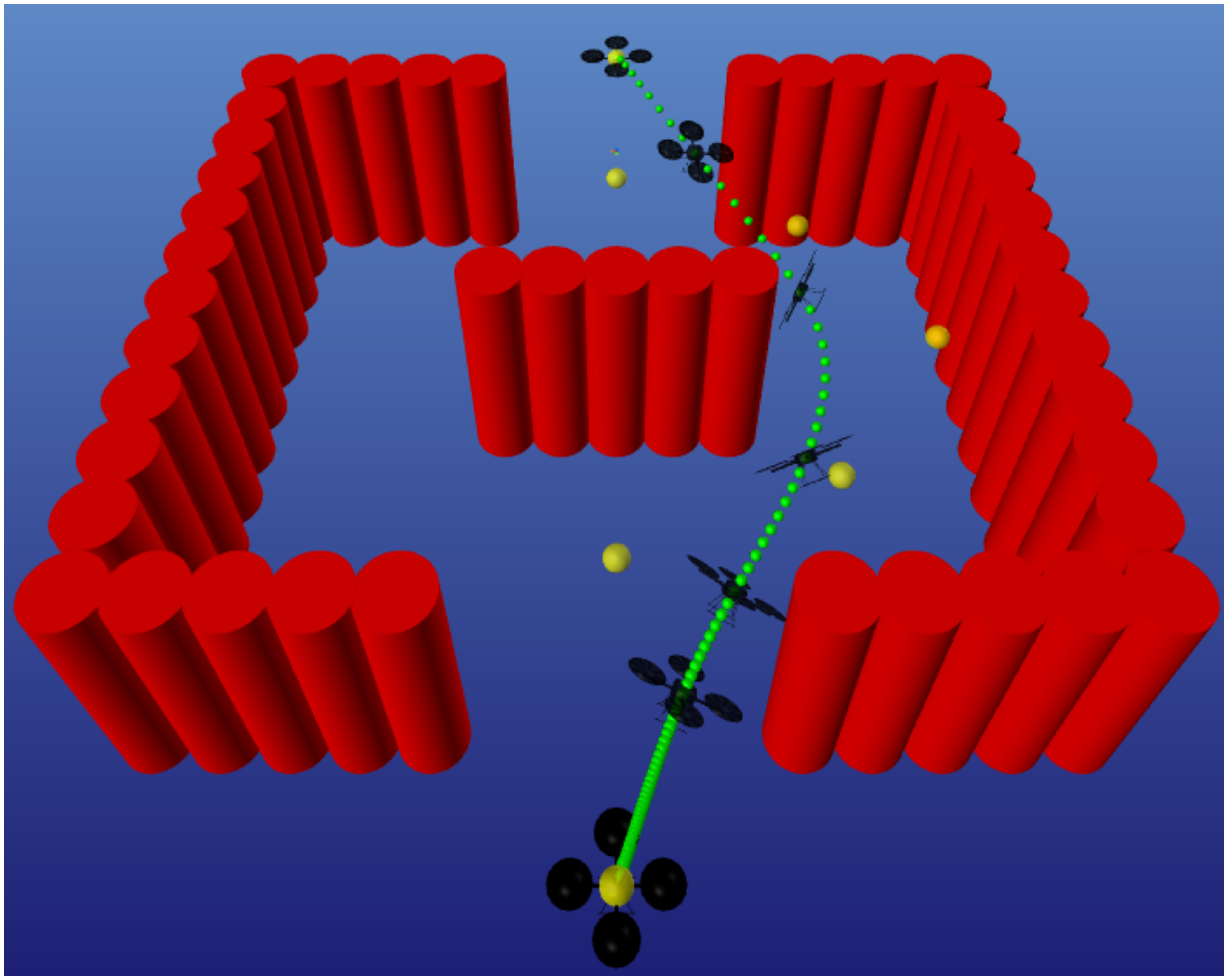
- Frame motion planning as a **non-convex constrained optimization** problem & solve for **local minima**

$$\begin{aligned}&\text{minimize } f(\mathbf{x})\\&\text{subject to}\\&\quad g_i(\mathbf{x}) \le 0, \quad i = 1, 2, \ldots, n_{ineq}\\&\quad h_i(\mathbf{x}) = 0, \quad i = 1, 2, \ldots, n_{eq}\end{aligned}$$

- Collision constraints enforced via **signed distance** (sd)



$sd > 0$ $sd < 0$



[Ratliff 2009][Schulman 2013]

Task and Motion Planning (TAMP)

Shakey the Robot (1969)

- **First autonomous mobile manipulator** (via pushing)
  - Visibility graph, A* search, and STRIPS!
- **Decoupled** task and motion planning
  - Task planning **then** motion planning

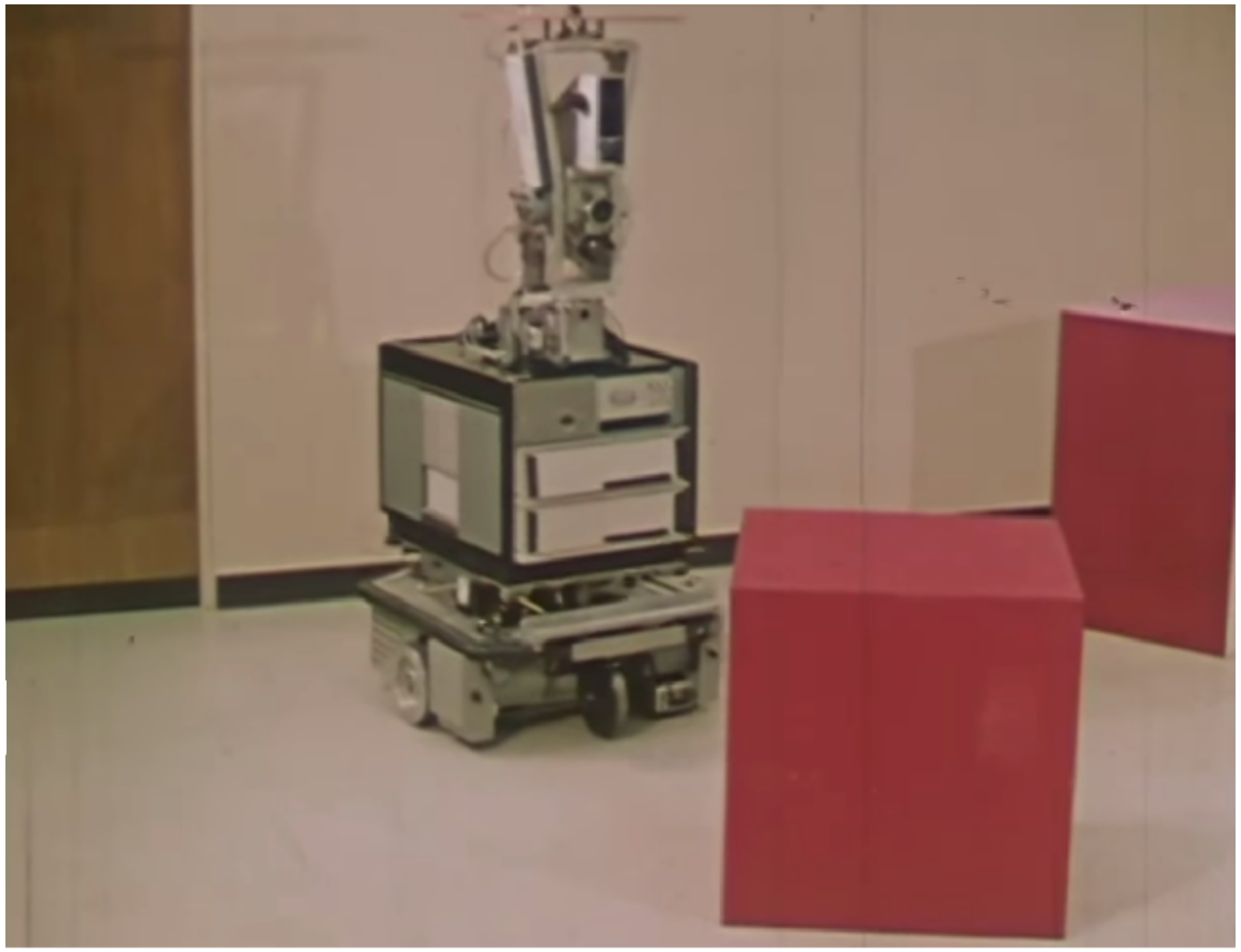
[Fikes 1971]

[Nilsson 1984]

```
type(robot robot)        type(o1 object)
name(robot shakey)       name(o1 box1)
at(robot 4.1 7.2)        at(o1 3.1 5.2)
theta(robot 90.1)        inroom(o1 r1)
                         shape(o1 wedge)
                         radius(o1 3.1)
```

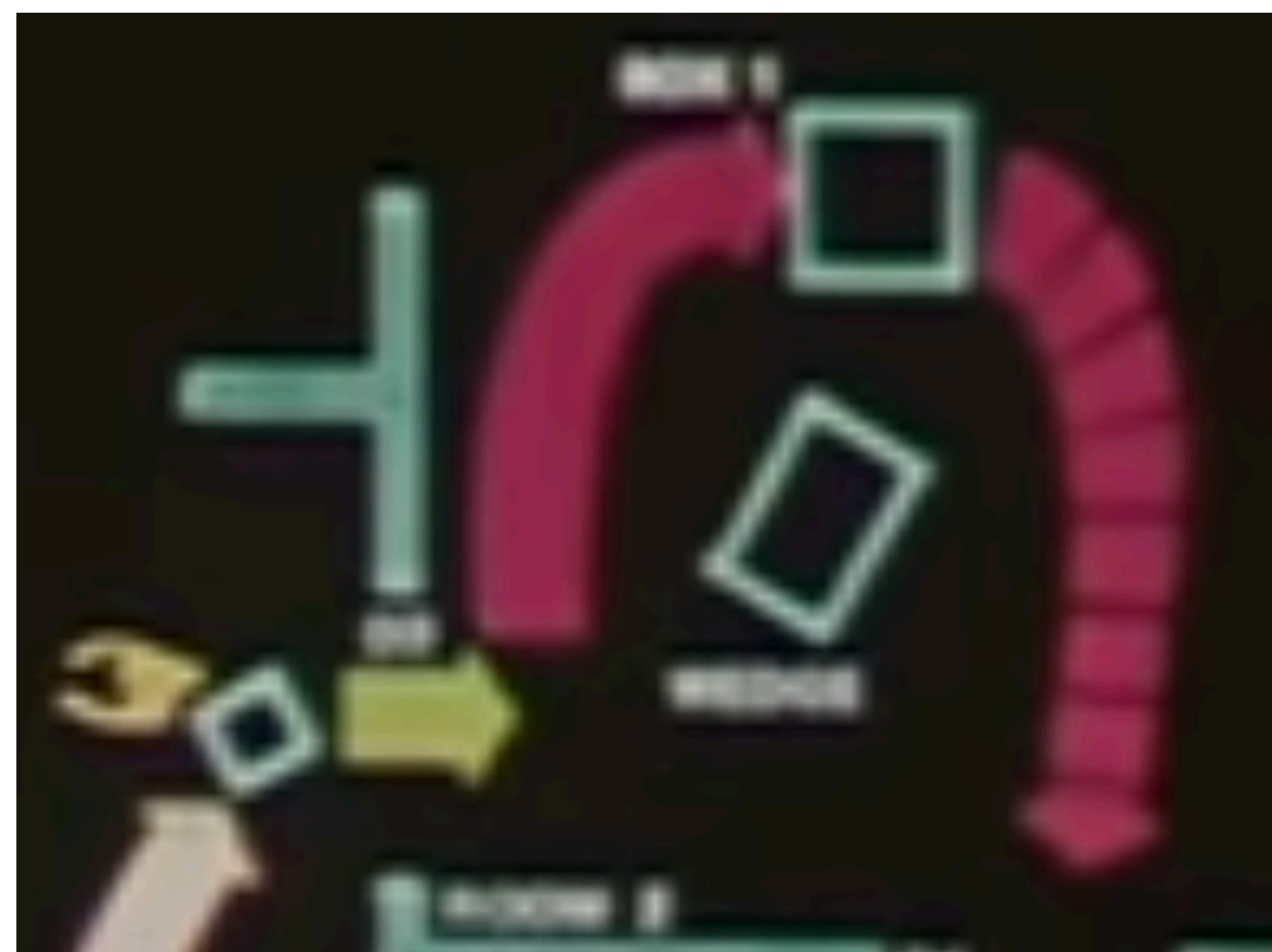
GOTHRU(d,r1,r2)

Precondition	INROOM(ROBOT,r1) ∧ CONNECTS(d,r1,r2)
Delete List	INROOM(ROBOT,$)
Add List	INROOM(ROBOT,r2)



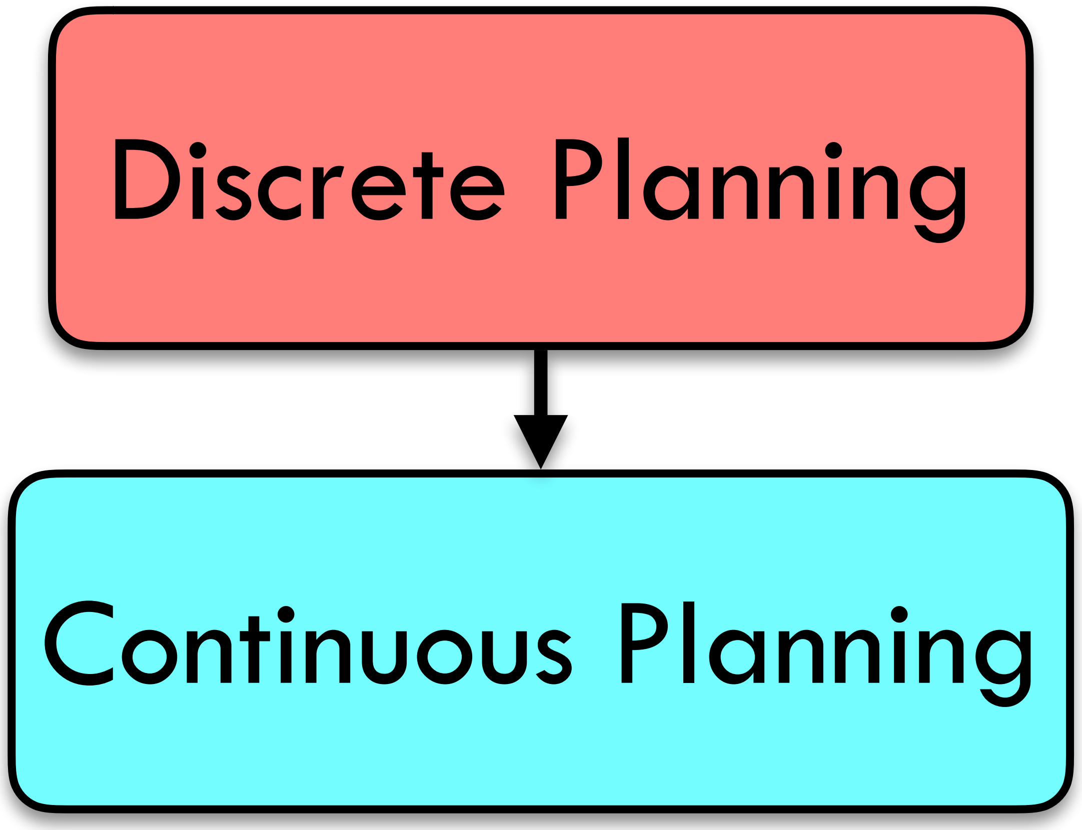
Obstacle Blocks Shakey's Path

- What if a movable block **prevented** Shakey from safely moving into the adjacent room?
- Shakey could **push** it out of the way or **go around** it
  - What's more efficient? How to push it? …

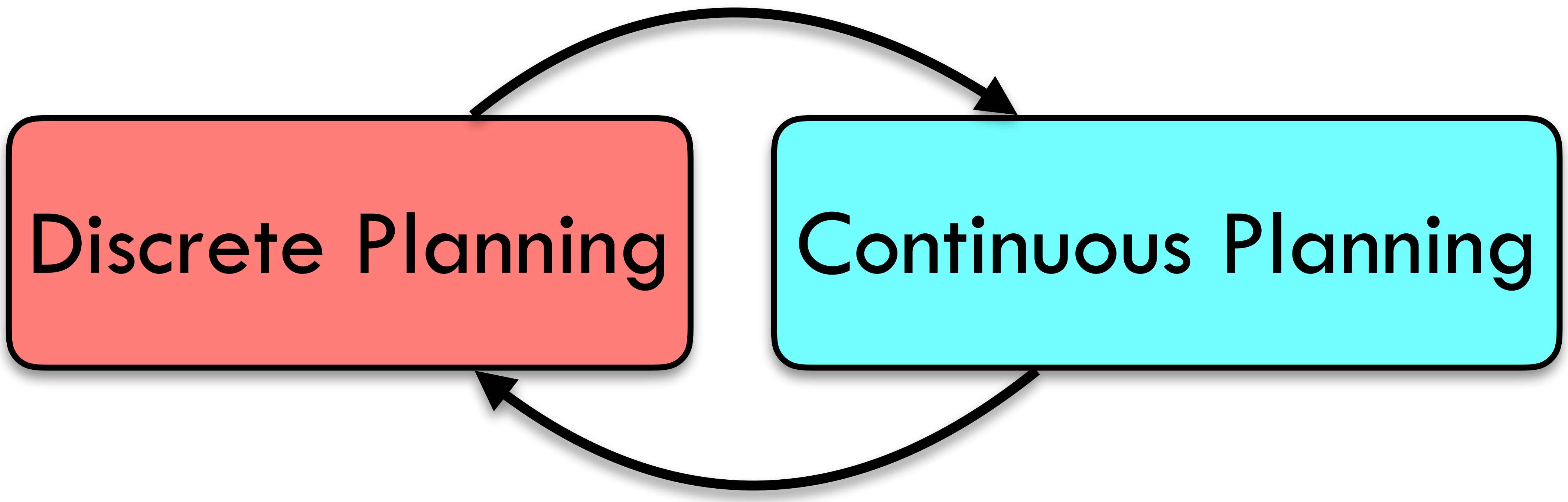


Decoupled vs Integrated TAMP

- **Decoupled:** discrete (task) planning **then** continuous (motion) planning
- Requires a strong **downward refinement** assumption
  - **<u>Every</u>** correct discrete plan can be **refined** into a correct continuous plan (from hierarchal planning)
- **Integrated:** **<u>simultaneous</u>** discrete & continuous planning



Decoupled



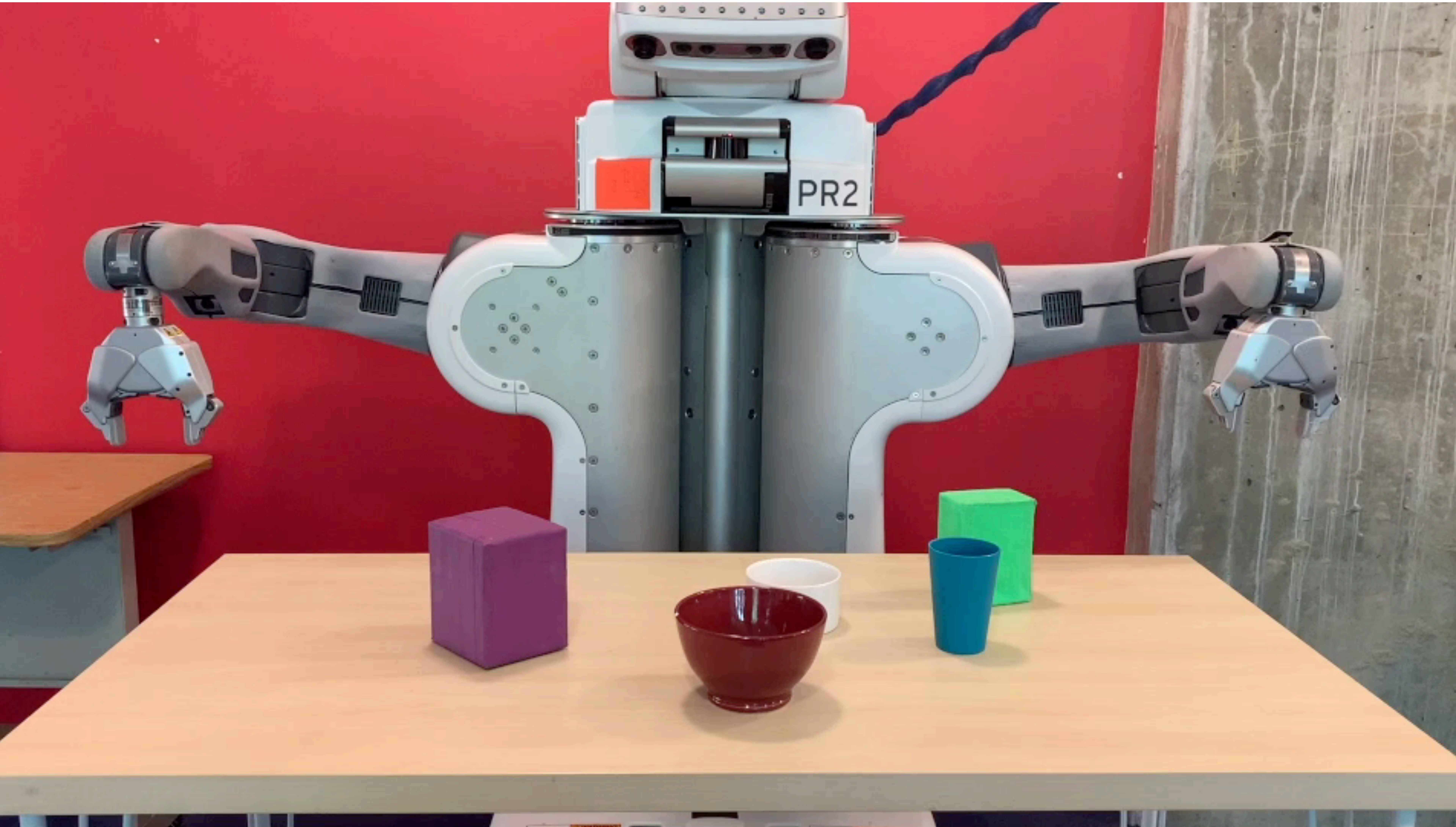
Integrated

Geometric Constraints Affect Plan

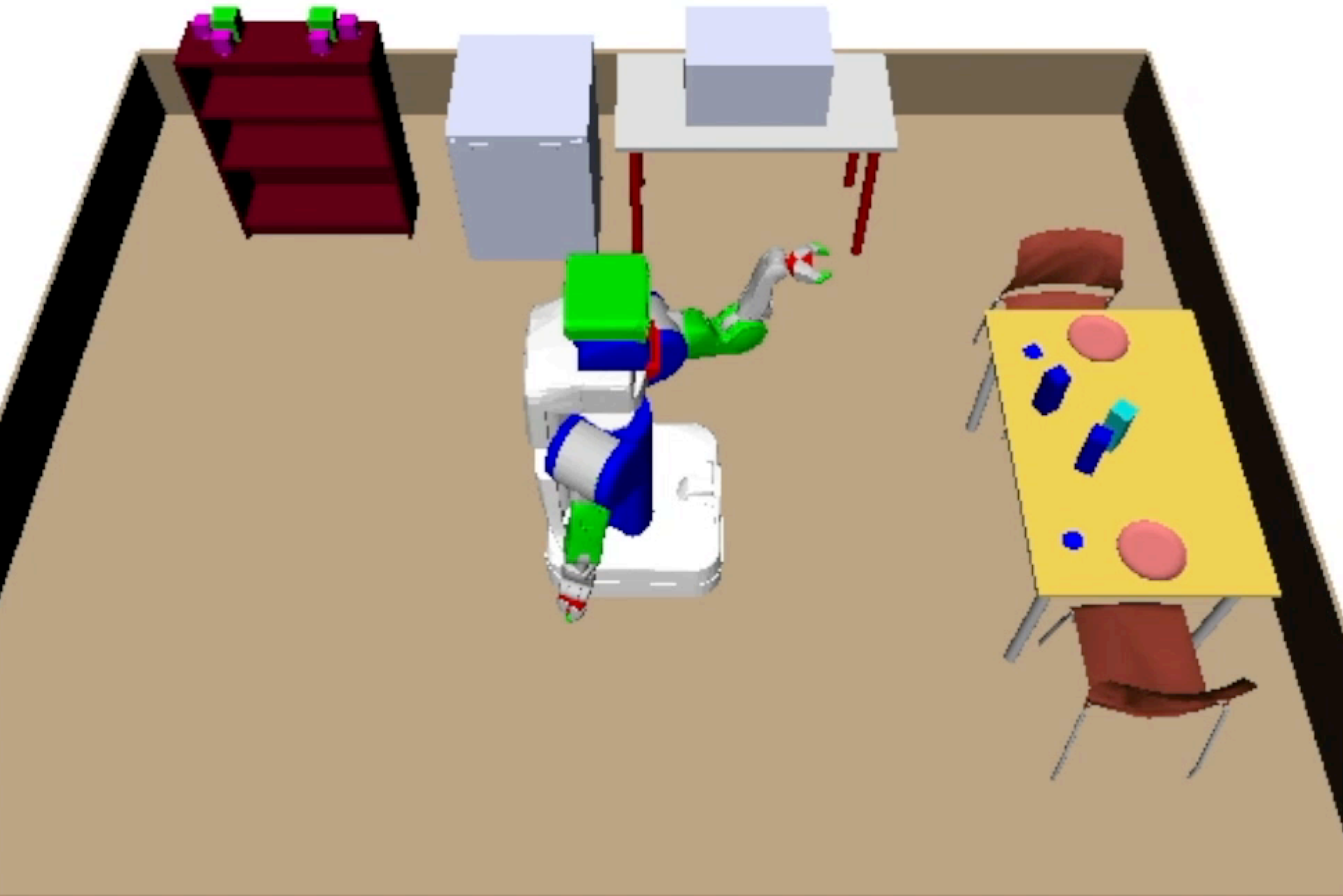
- **Inherits challenges** of both motion & classical planning
  - **High-dimensional, continuous** state-spaces
  - State-space **exponential** in number of variables
  - **Long horizons**

- Continuous constraints **limit high-level strategies**
  - Kinematics, reachability, joint limits, collisions grasp, visibility, stability, stiffness, torque limits, …

Pouring Among Obstacles



Preparing a Meal for Two

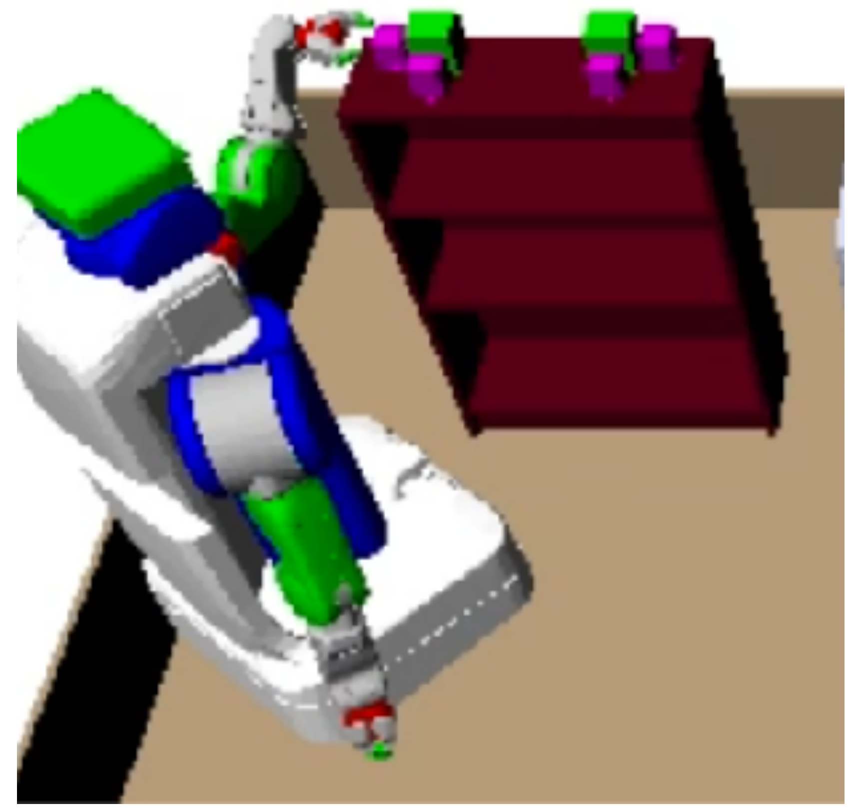


Breaking Down "Preparing a Meal"

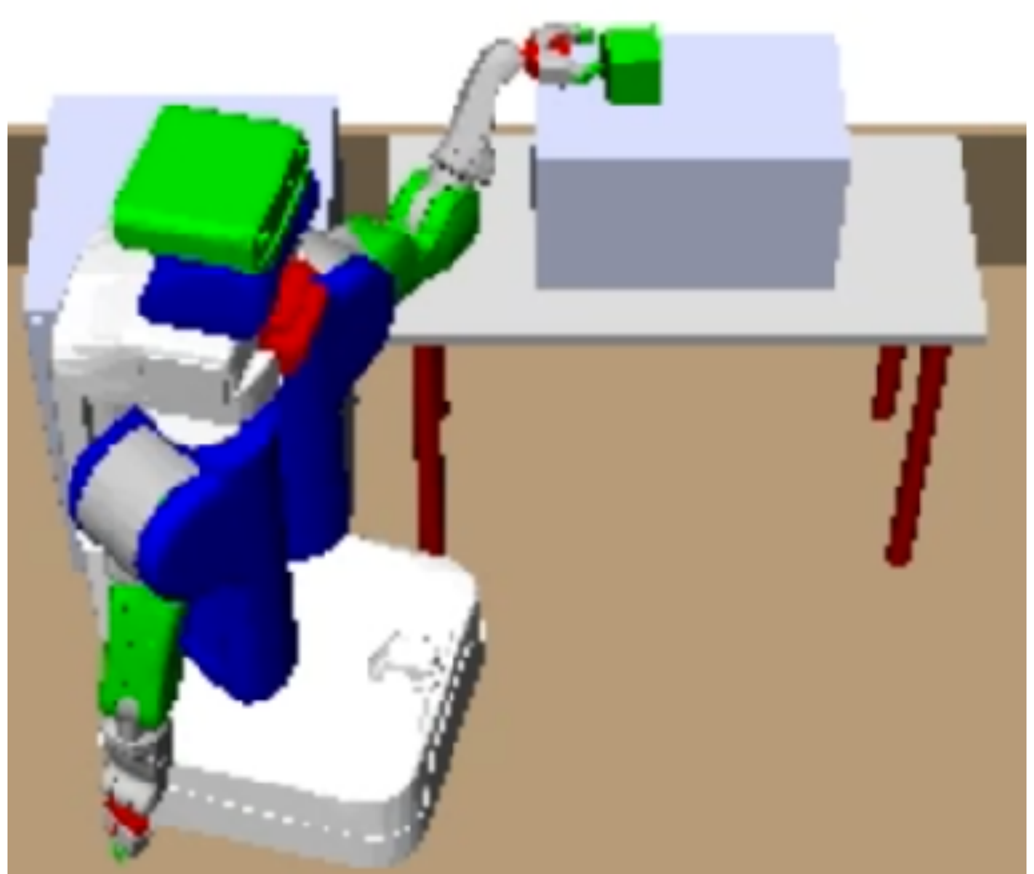
- Clean 3 blue cups and clean/cook 2 green cabbages
- 64 continuous and 10 discrete variables

1. High-dimensional
2. Long horizon
3. Discrete state
4. Geometric constraints

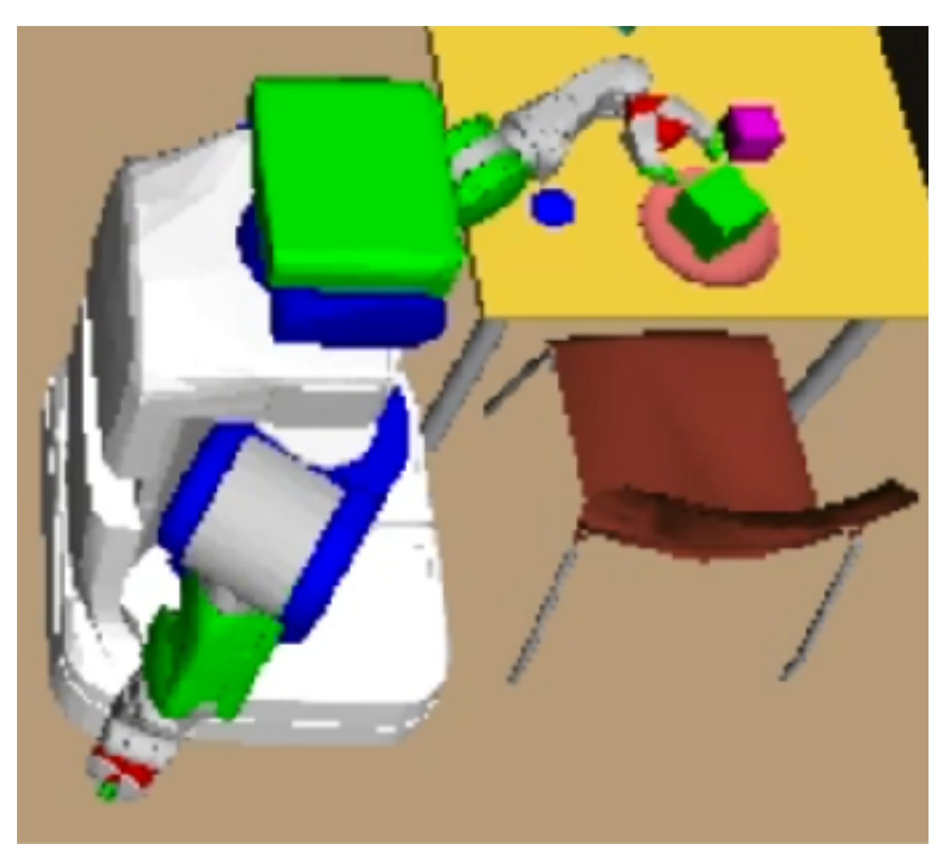
Remove obstructing radishes



Clean each cabbage



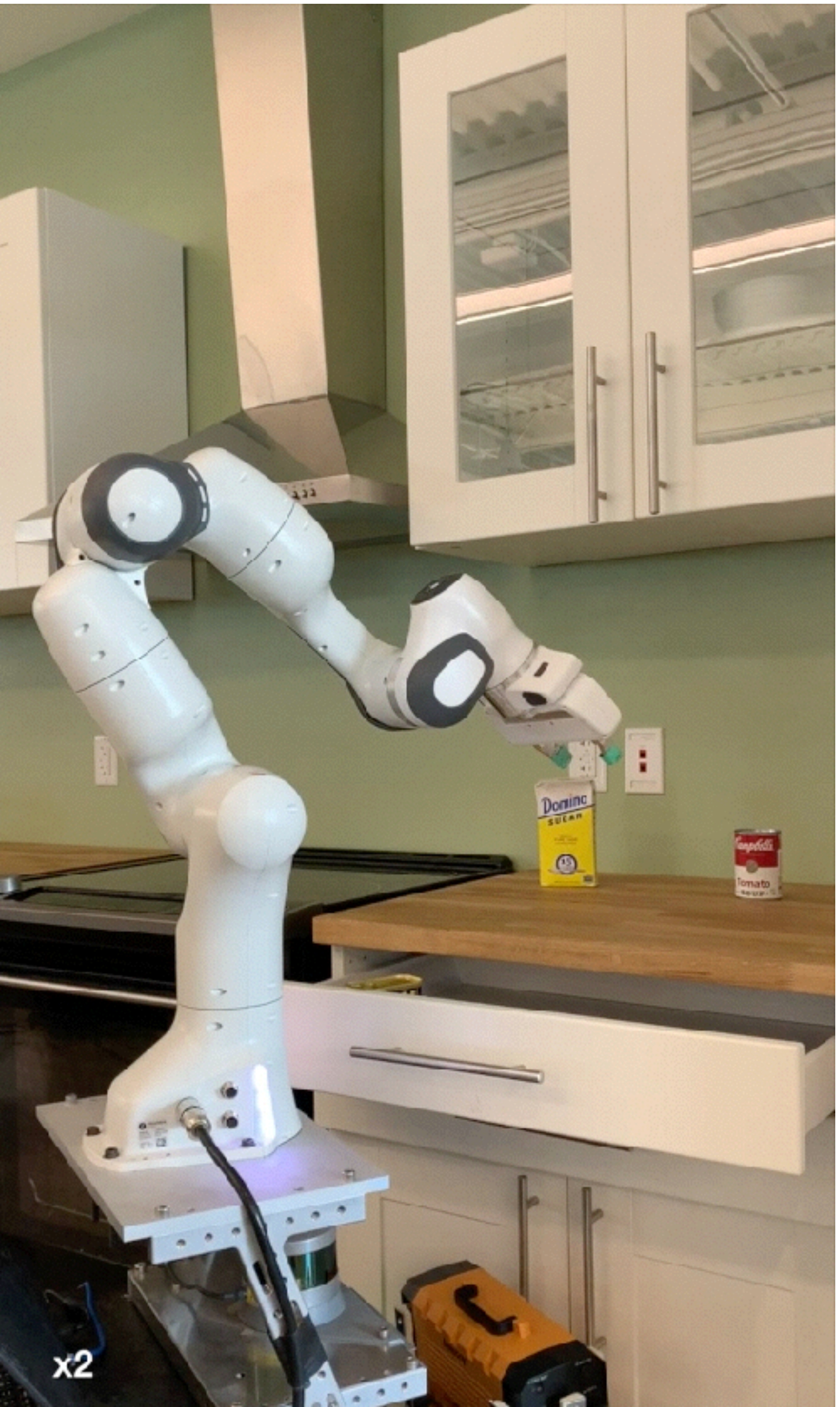
Cook each cabbage



Serve the cabbage

Replace the radishes

Block in Left Cabinet & Doors Closed

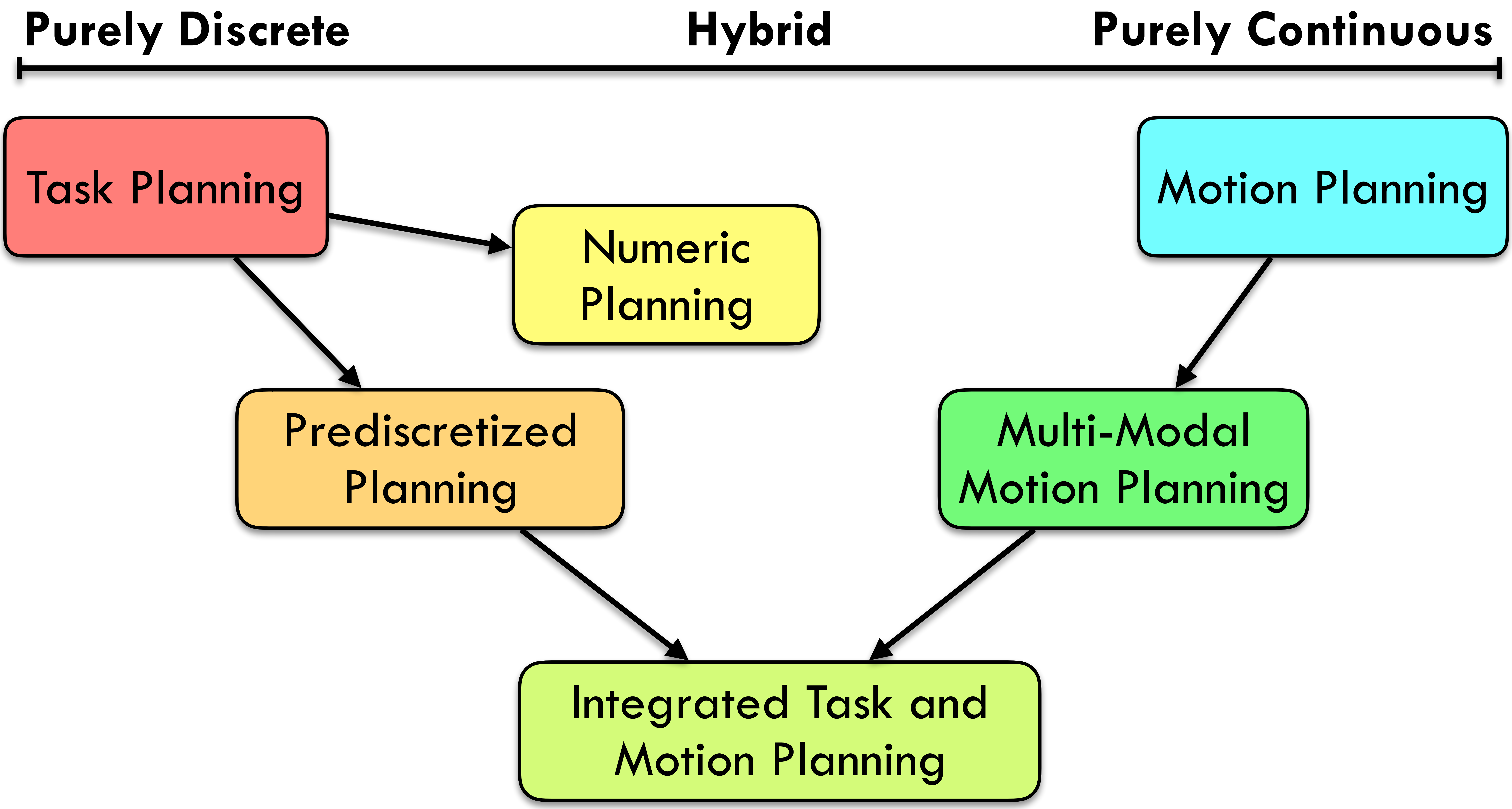


- Robot forced to **regrasp** the object
  - Change from a **top** grasp to a **side** grasp

- **Non-monotonic** problem
  - Plan must **undo goals** to solve
  - **Open** then **close** the cabinet door

- Physical constraints can be subtle!

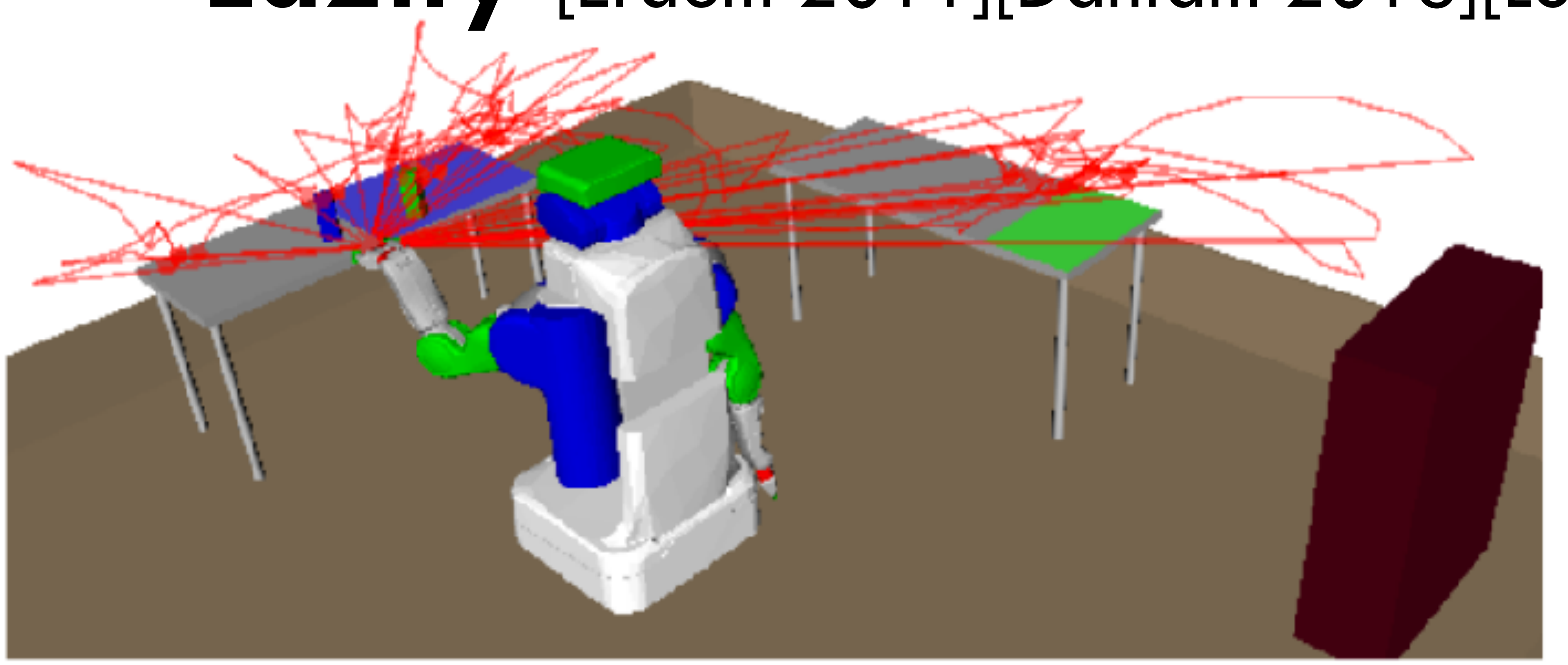
Hybrid Planning Spectrum

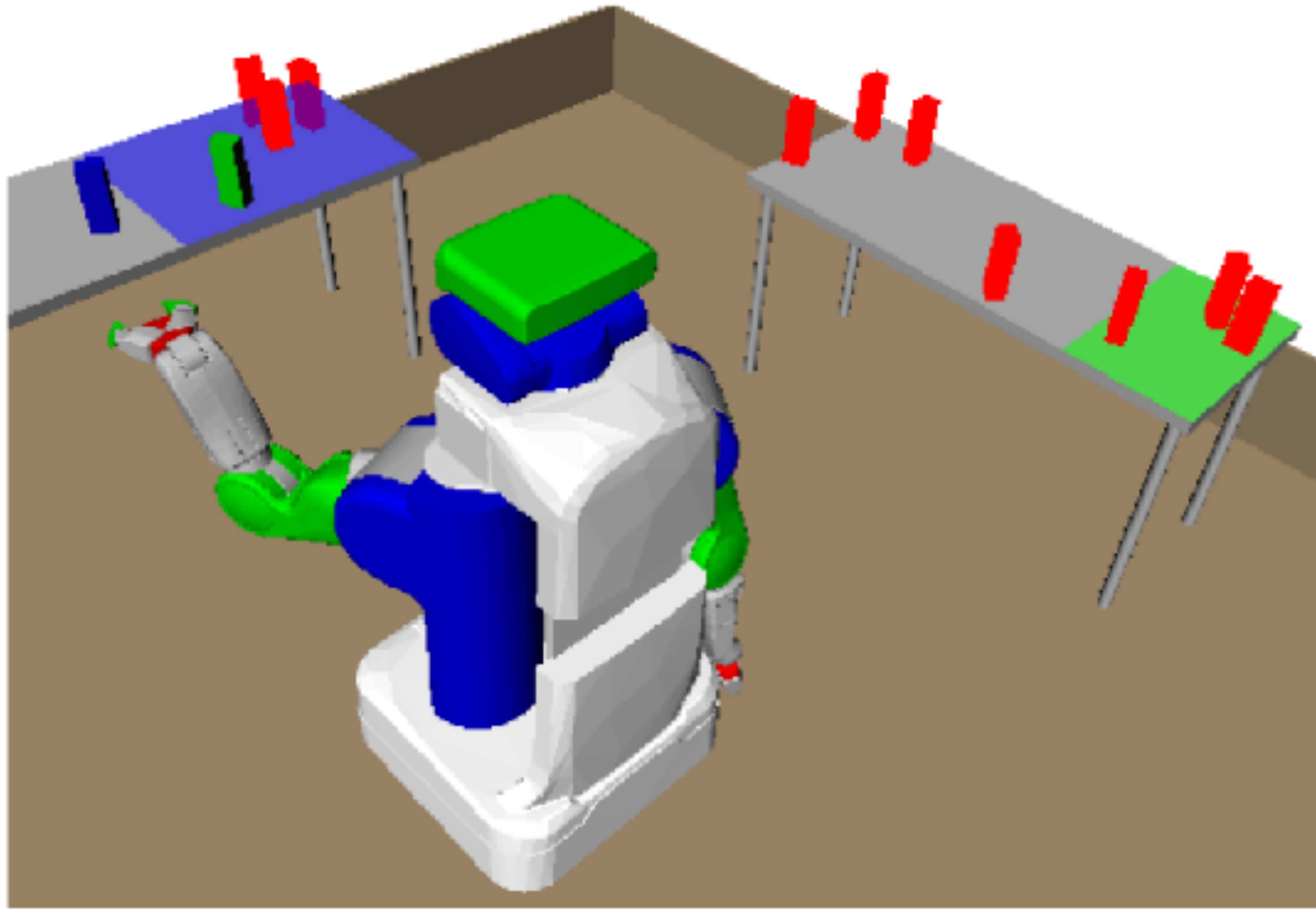


Prediscretized & Numeric Planning

Prediscretized Planning

- Assumes that a **finite set** of object placements, object grasps, and (sometimes) robot configurations are **given**
- Can **directly** perform discrete task planning
- Still need to evaluate **reachability**
  - Eagerly in **batch** [Lozano-Pérez 2014][Garrett 2017][Ferrer-Mestres 2017]
  - Eagerly during **search** [Dornhege 2009]
  - **Lazily** [Erdem 2011][Dantam 2018][Lo 2018]





Discrete-Control Numeric Planning

- Classical planning with **real-valued variables** and **durative** actions
  - **Examples**: time and energy
- Most planners only support **linear**/polynomial dynamics
- **Non-linear** dynamics addressed by **discretizing time**
- **Example:** battery domain

$$\frac{d\delta}{dt} = \frac{i(t)}{c} - k'\delta$$

load

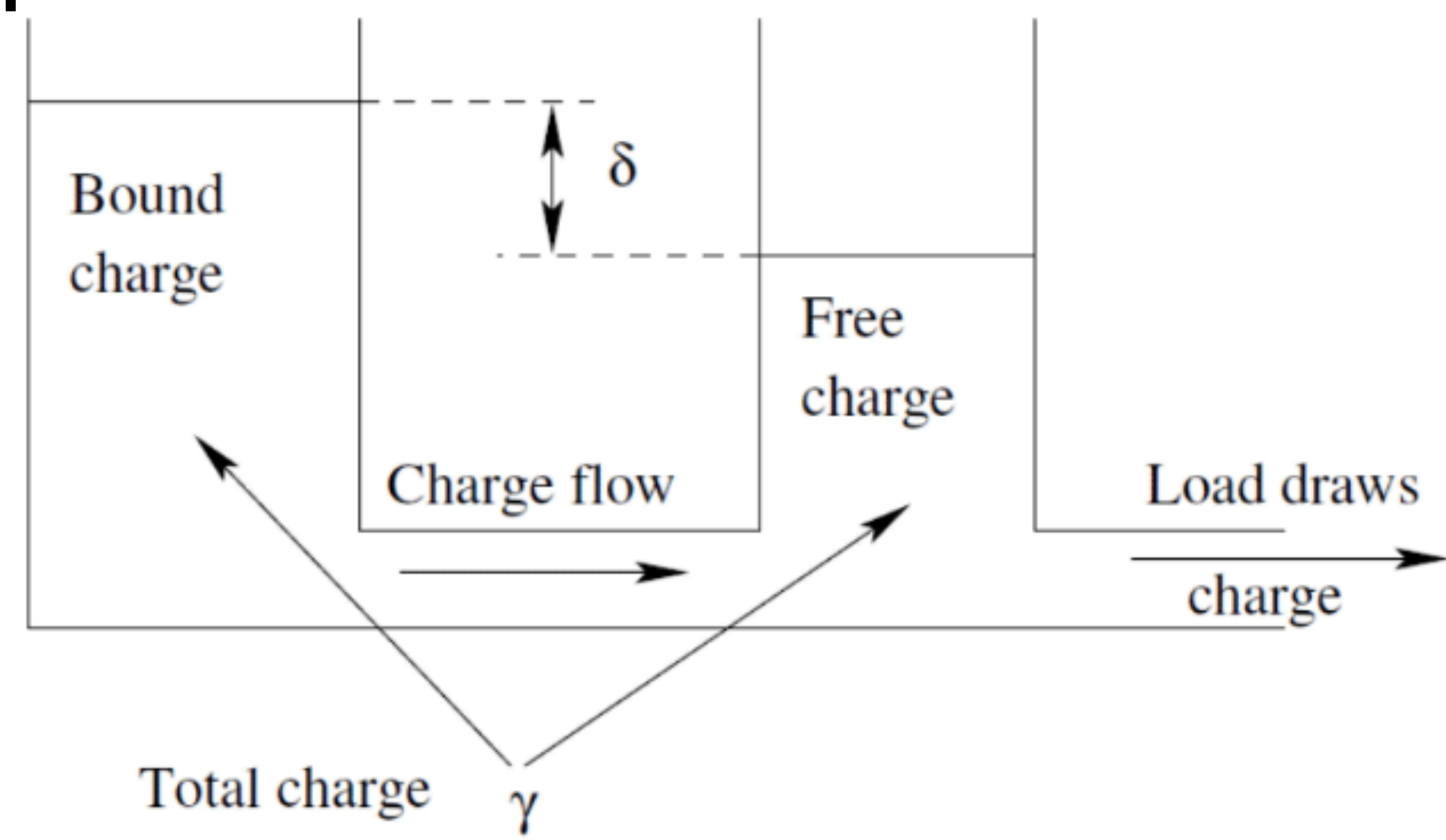
Fixed conductan

$$\frac{d\gamma}{dt} = -i(t)$$

battery capacity

$$\delta(t) = \frac{I}{c} \cdot \frac{1-e^{-k't}}{k'}$$

$$\gamma(t) = C - It$$

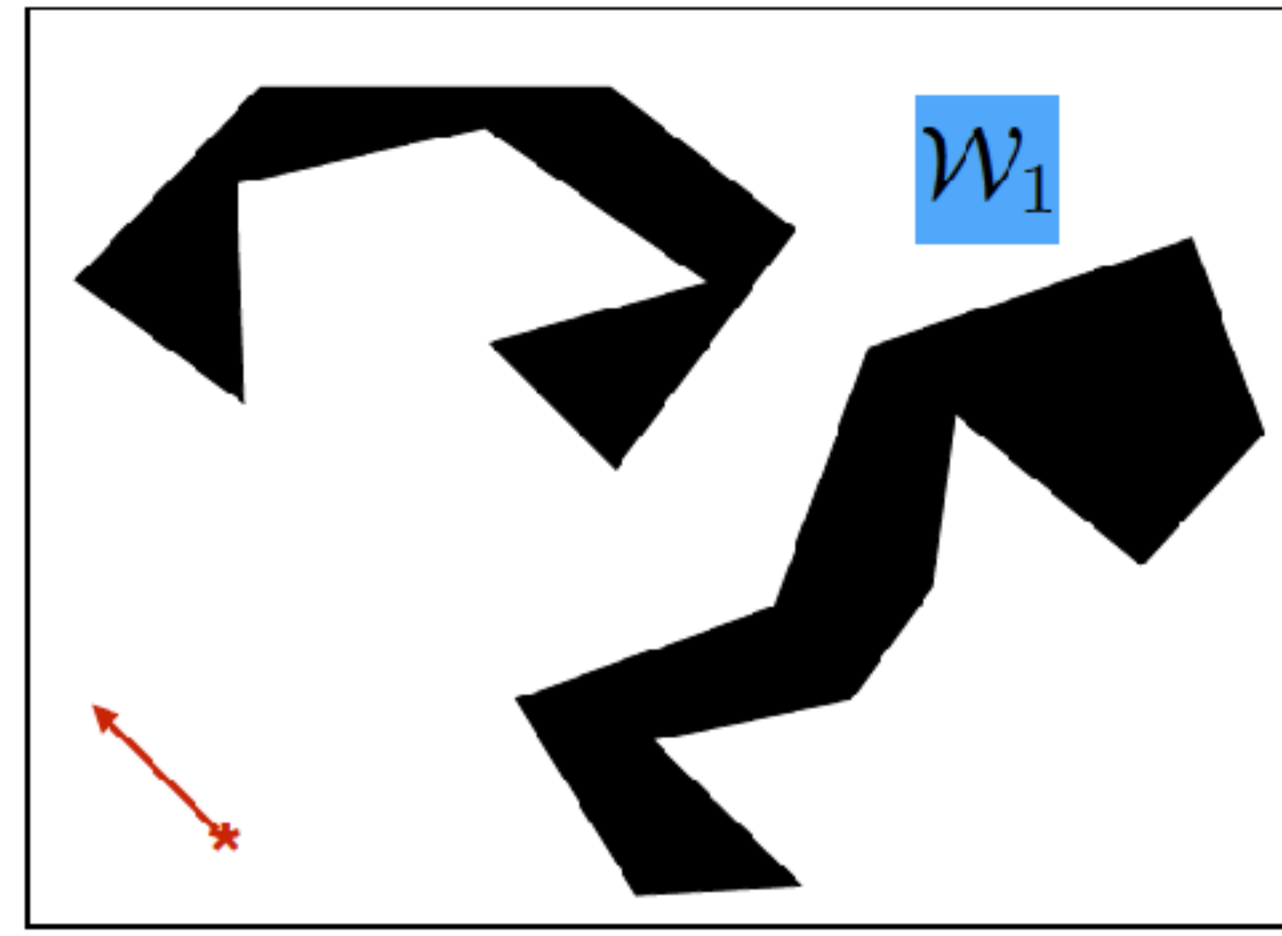


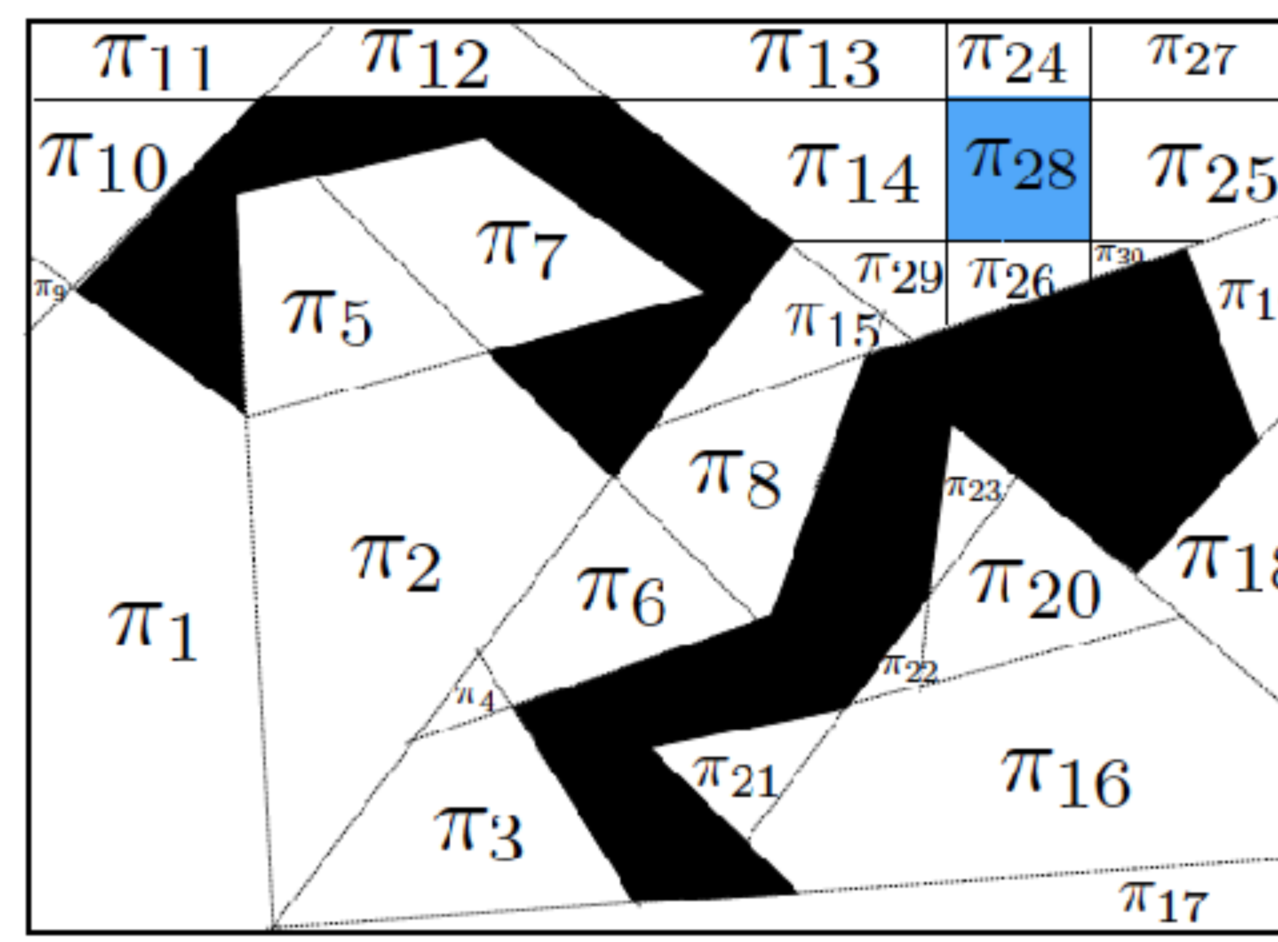
[Fox 2003][Hoffmann 2003][Eyerich 2009]

Continuous-Control Numeric Planning

- **Continuous control** parameters
- Tackle **convex dynamics** using **cone programming**
- Non-convexity handled by **partitioning** the state-space

- **In contrast,** TAMP is often:
  - **High-dimensional**
  - **Non-convex**
    - 3D collision constraints
  - Less sophisticated dynamically



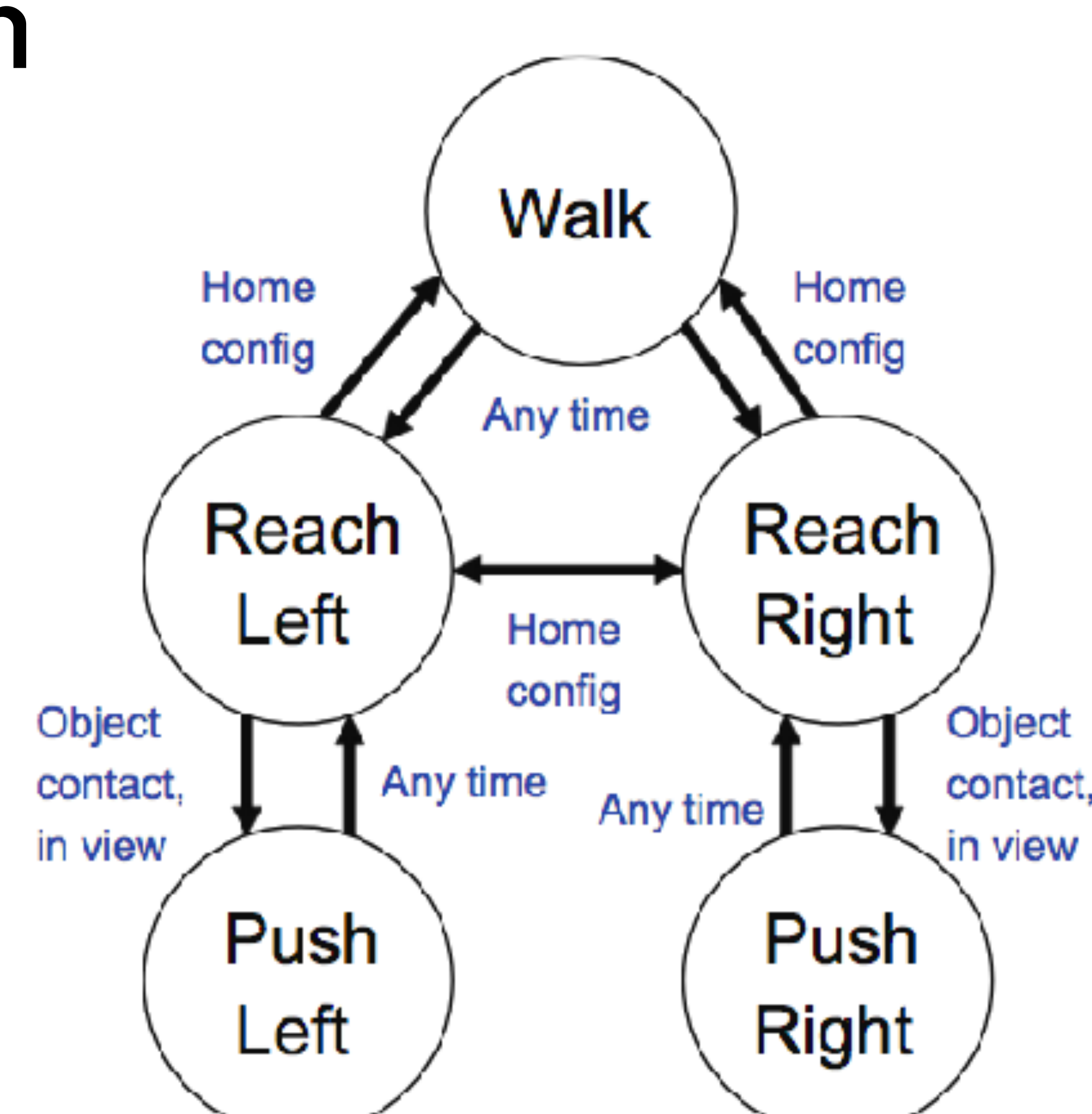


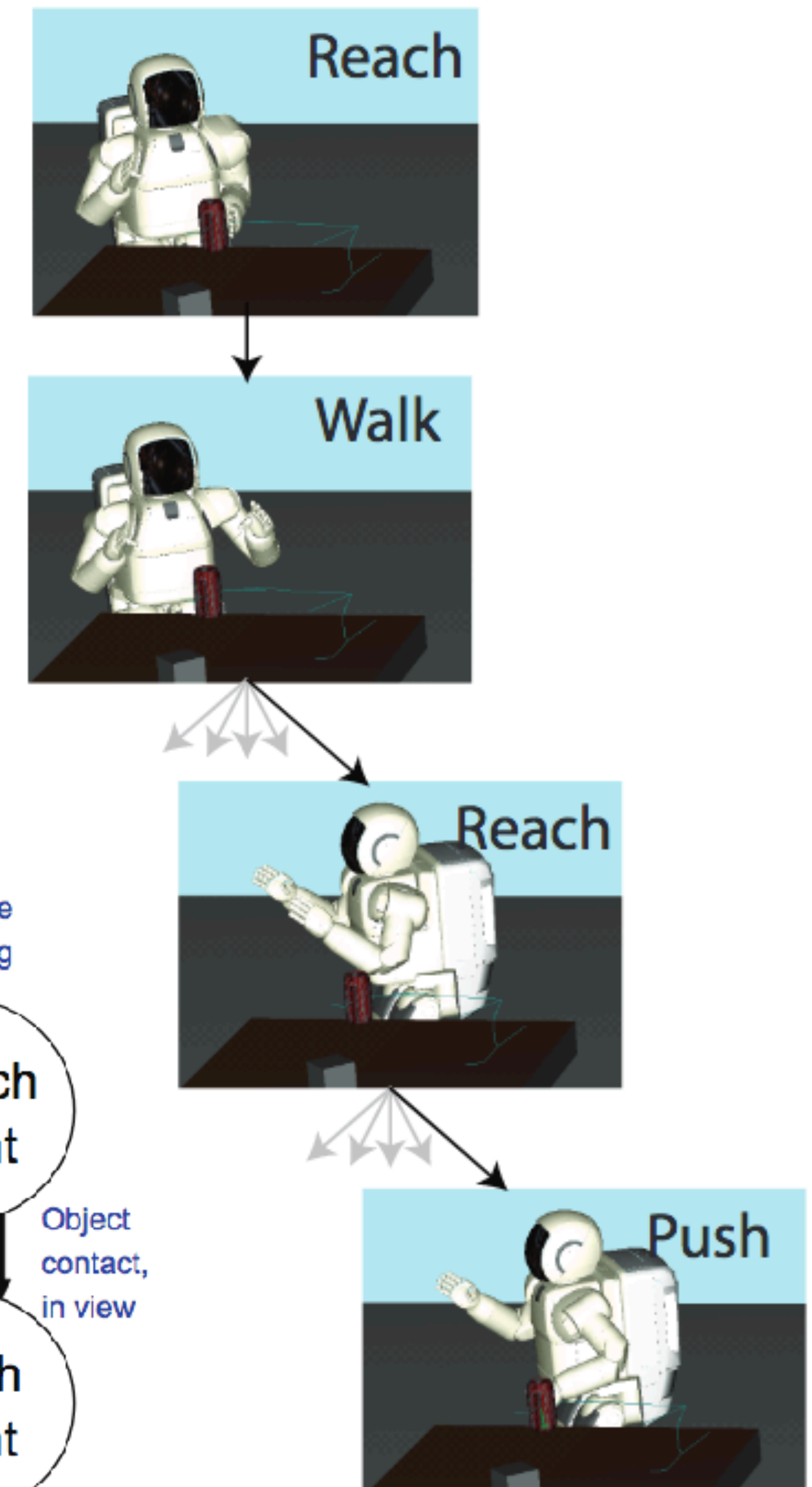
[Deits 2015][Shoukry 2016]
[Fernandez-Gonzalez 2018]

Multi-Modal Motion Planning

Multi-Modal Motion Planning

- Collision-free configuration space **changes** when objects are manipulated
- Use a **sequence** of motion planning problems each defined by a **mode**
- **Mode:** a set of motion constraints
  - Gripper is empty
  - Relative object pose remains **constant**

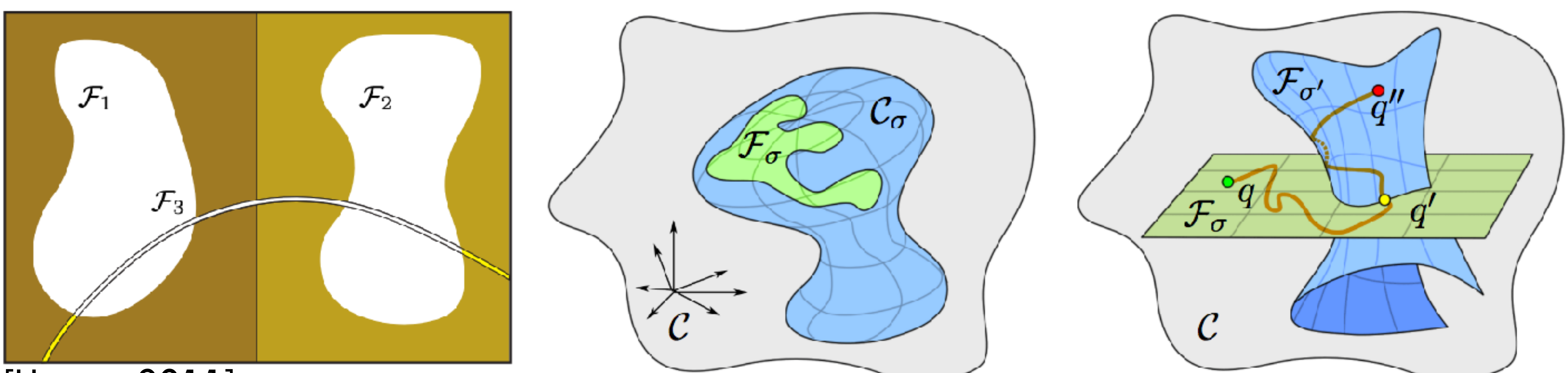




[Alami 1994][Siméon 2004][Hauser 2011]
[Barry 2013][Vega-Brown 2016]

Low-dimensional Intersections

- Need samples that **connect** adjacent modes
- Intersection of two modes is often **low-dimensional**
  - **Special-purpose** samplers are needed
- **Example:** transition from gripper **empty** to **holding**
- Configurations at the **intersection** obtained using **inverse kinematics** (IK)

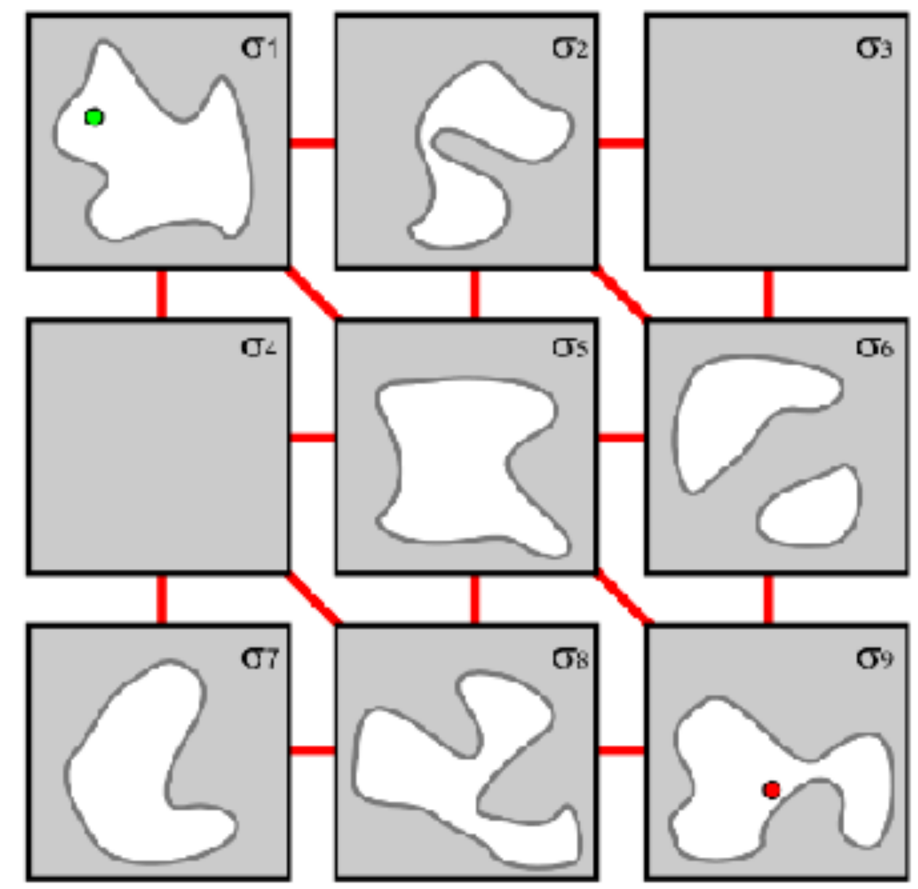


[Hauser 2011]

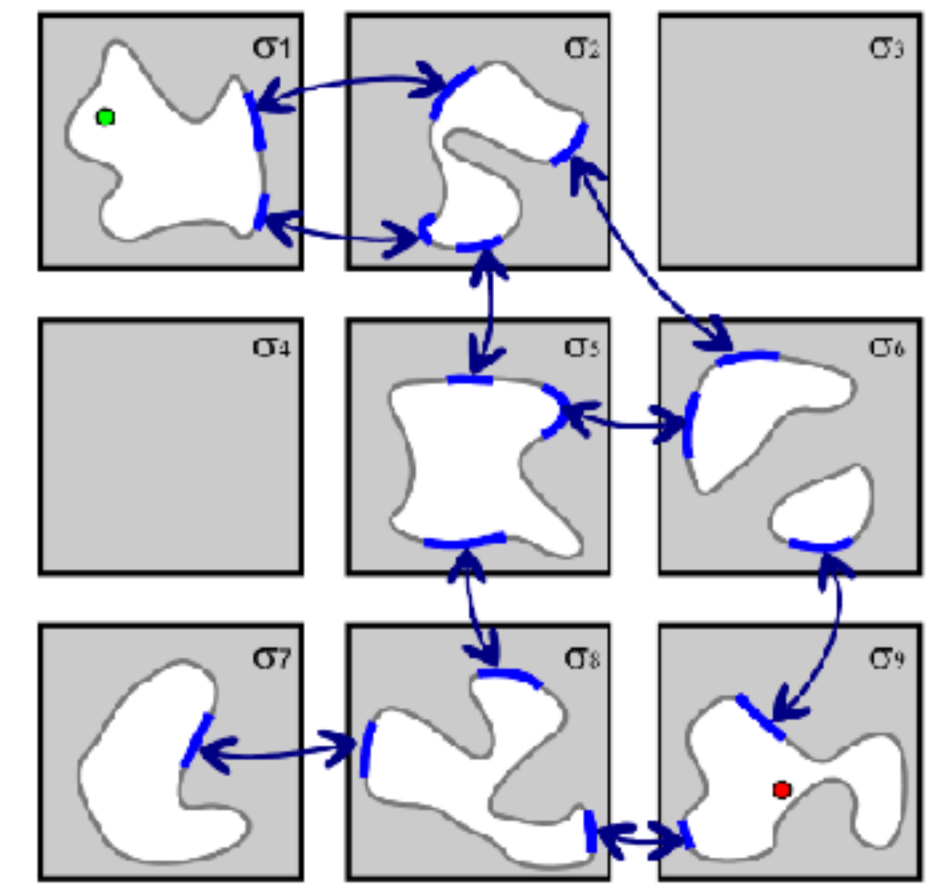
Sampling-Based Multi-Modal Planning

1. Sample from the set of **modes**
2. Sample at the **low-dimensional intersection** of adjacent modes
3. Sample a roadmap **within** each mode
4. Discrete search on the multi-modal **roadmap**

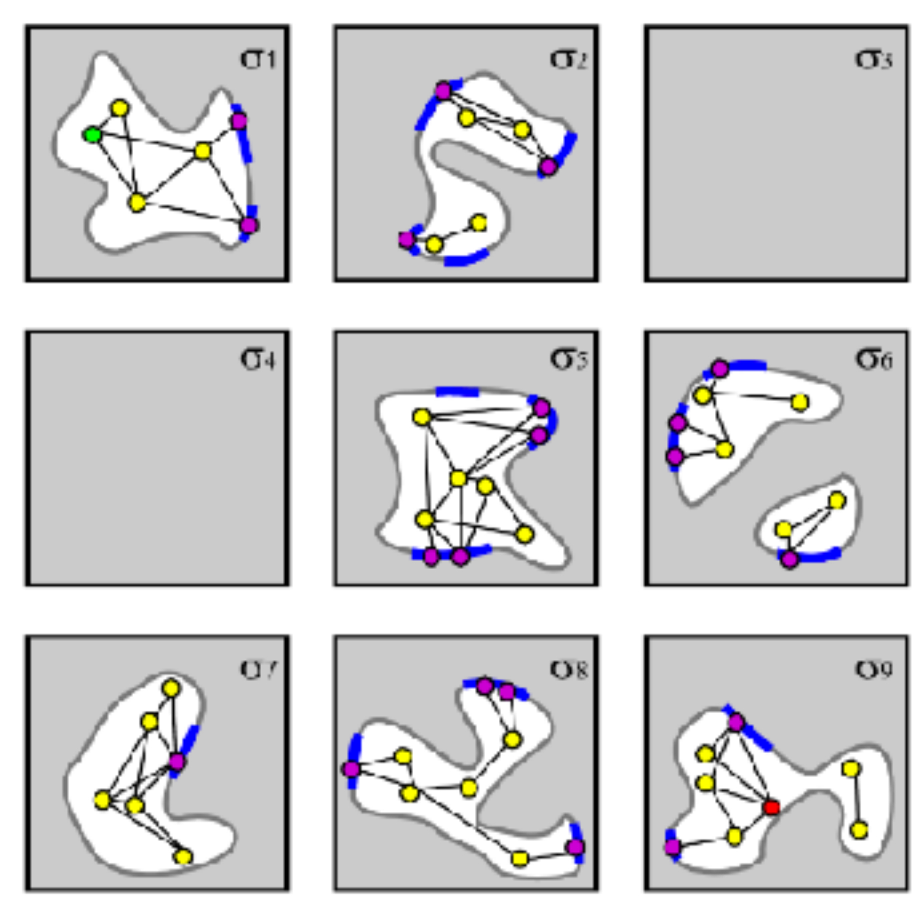
[Hauser 2011]



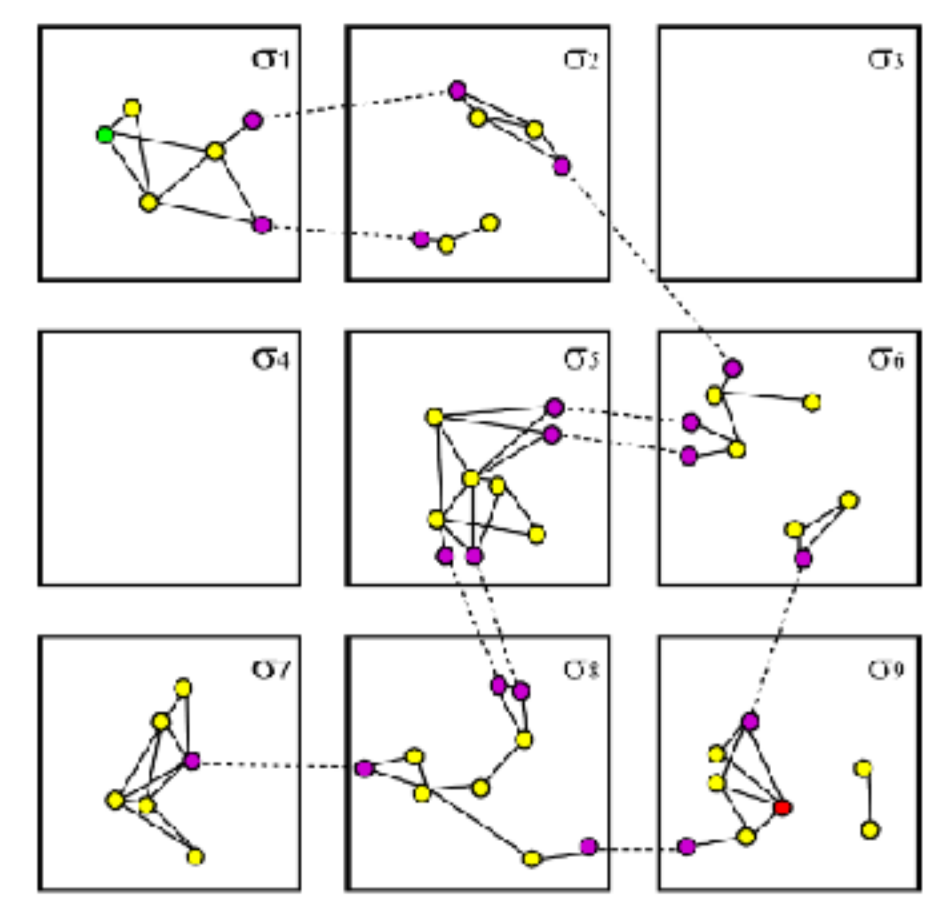
Adjacent modes



Intersections



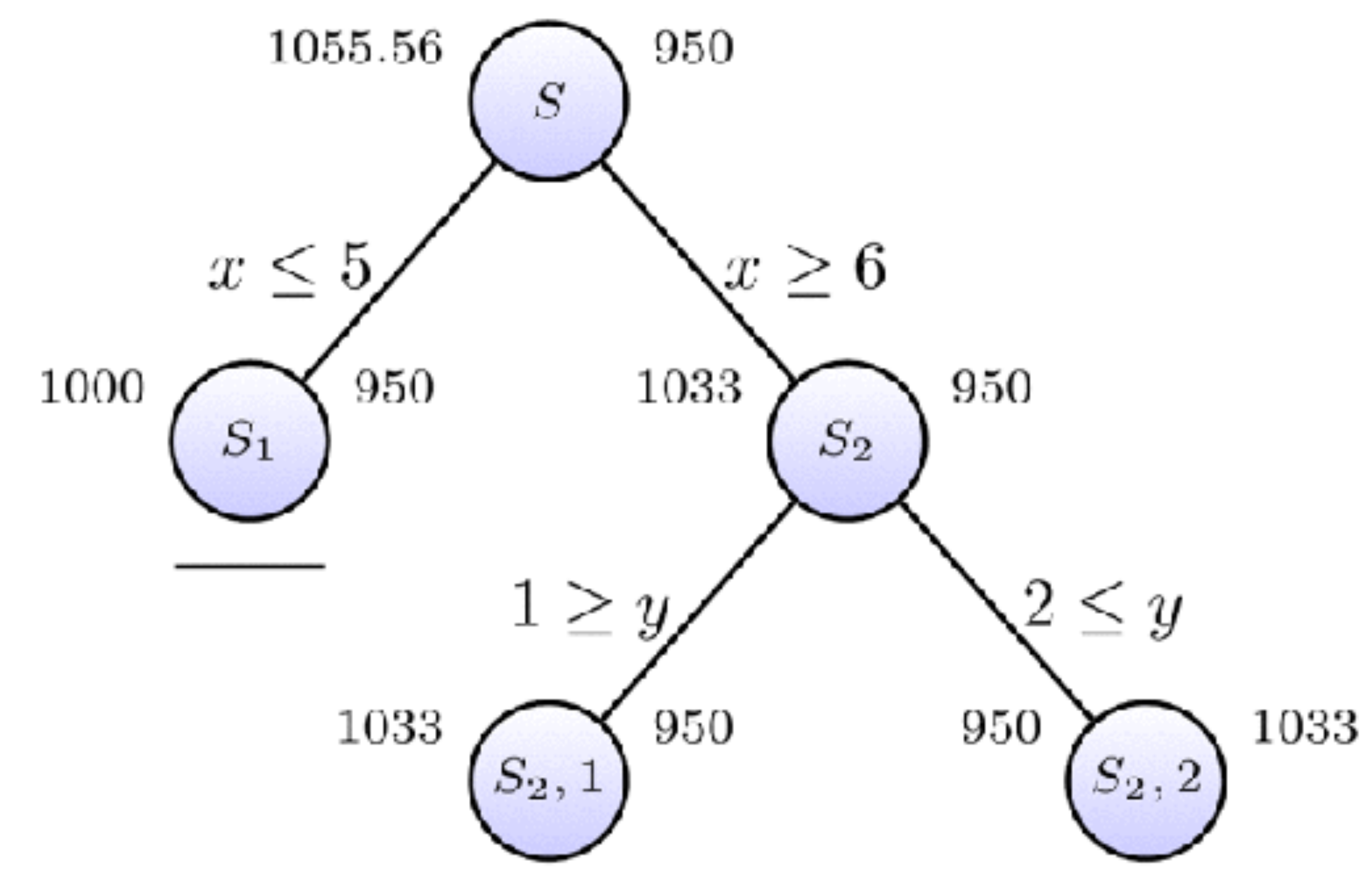
Individual mode roadmaps

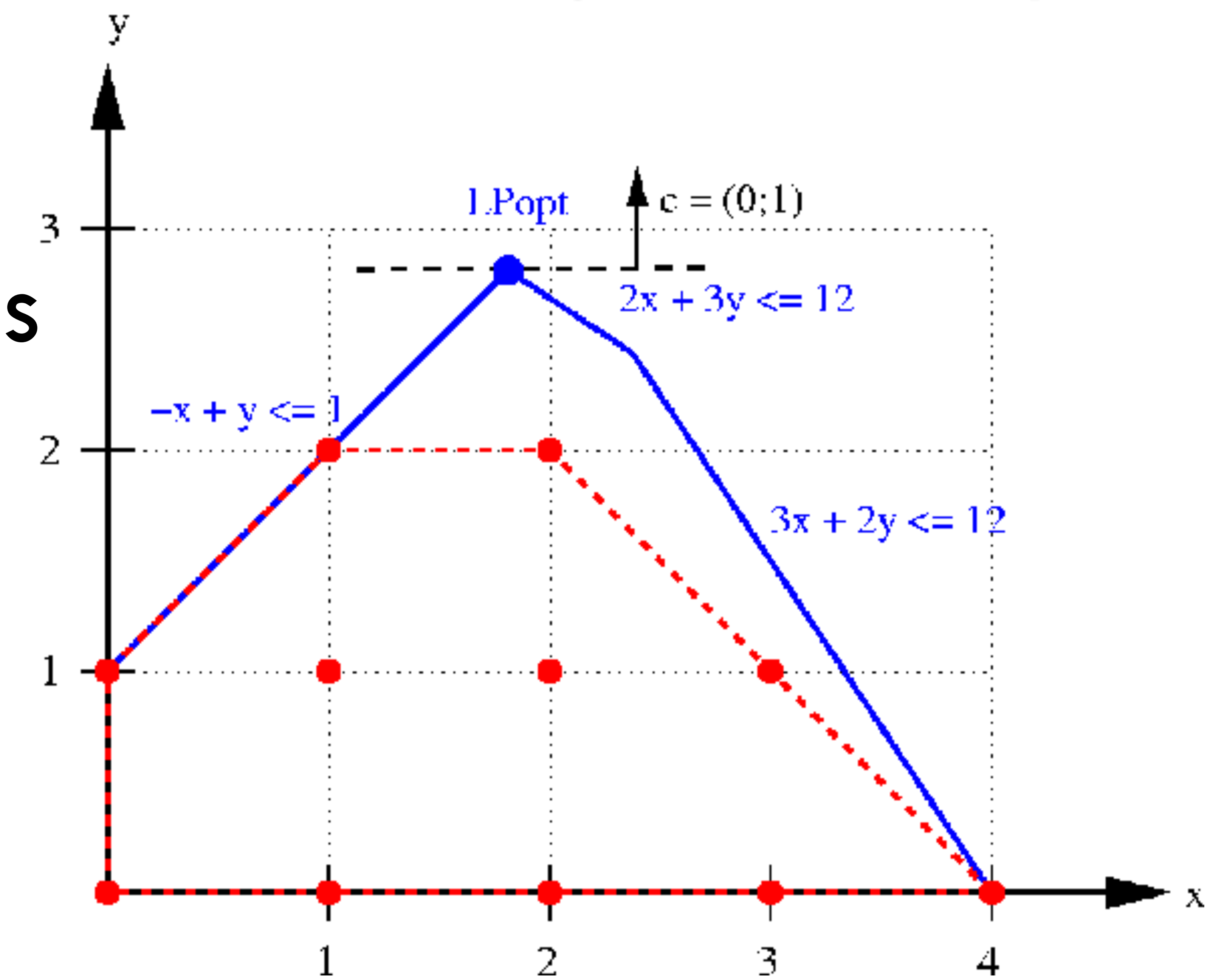


Combined Roadmap

Mixed Integer Programming (MIP)

- Continuous and integer variables
- Convex constraints and costs
- **Branch-and-bound**
  - Split on integer variables
- **Integrality relaxation**
  - Lower bound on cost
  - Loose when **logical** operations



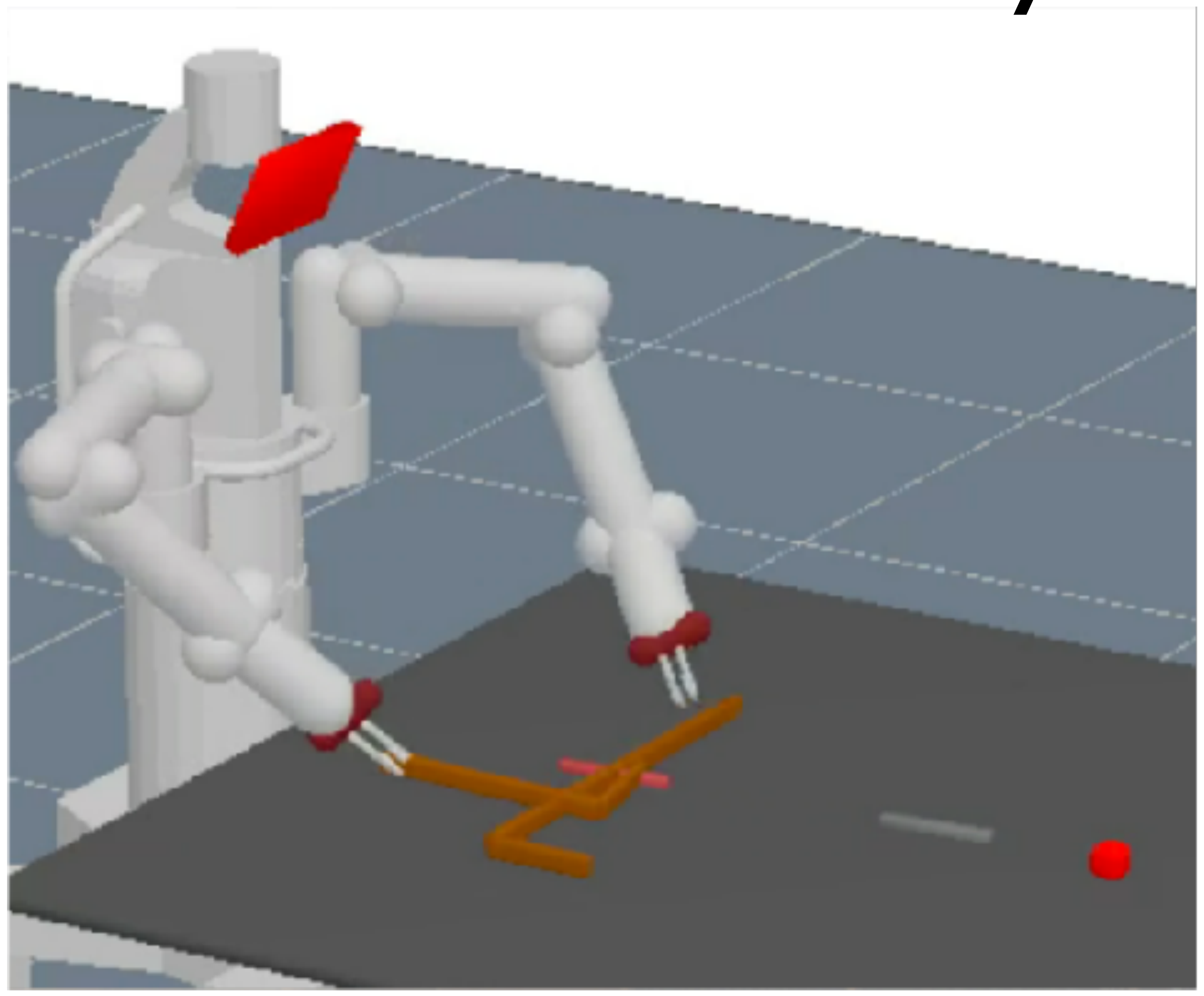


- Planning limitation
  - # of variables may be **exponential** in problem size

Optimization-Based Multi-Modal Motion Planning

- Discrete search over sequences of **mode switches**
  - Sequences have **varying length**
  - Each sequence induces a **non-convex constrained optimization problem**
- Sequences can be pruned using **lower bounds** obtained by **relaxing** some constraints

[Lagriffoul 2014]



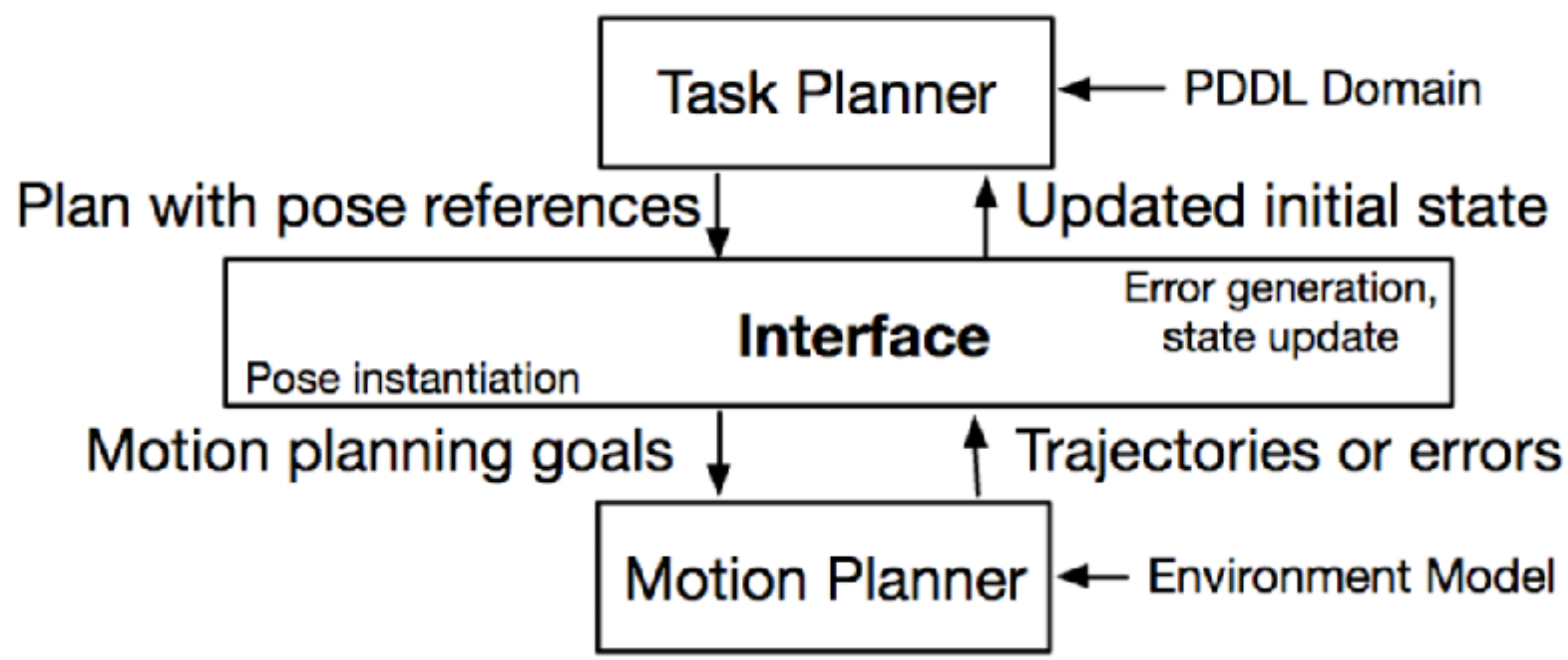
[Toussaint 2015]
[Toussaint 2018]

$$
\begin{aligned}
\min_{x, a_{1:K}, s_{1:K}} \quad & \int_0^T f_{\text{path}}(\bar{x}(t))\, dt + f_{\text{goal}}(x(T)) \\
\text{s.t.} \quad & x(0) = x_0,\ h_{\text{goal}}(x(T)) = 0,\ g_{\text{goal}}(x(T)) \le 0, \\
& \forall t \in [0, T]:\ h_{\text{path}}(\bar{x}(t), s_{k(t)}) = 0, \\
& \qquad\qquad\quad g_{\text{path}}(\bar{x}(t), s_{k(t)}) \le 0 \\
& \forall k \in \{1, .., K\}:\ h_{\text{switch}}(\hat{x}(t_k), a_k) = 0, \\
& \qquad\qquad\qquad g_{\text{switch}}(\hat{x}(t_k), a_k) \le 0, \\
& \qquad\qquad\qquad s_k \in \text{succ}(s_{k\text{-}1}, a_k)\ .
\end{aligned}
$$

Integrated TAMP

- Geometric search **guided** by classical planning
  - Both heuristic and sampling guidance [Gravot 2005][Plaku 2010]
- Task and motion planning **interface**
  - Maintain **separate** discrete and continuous descriptions
  - Custom interface to communicate between the two
  - How are failures **diagnosed?**

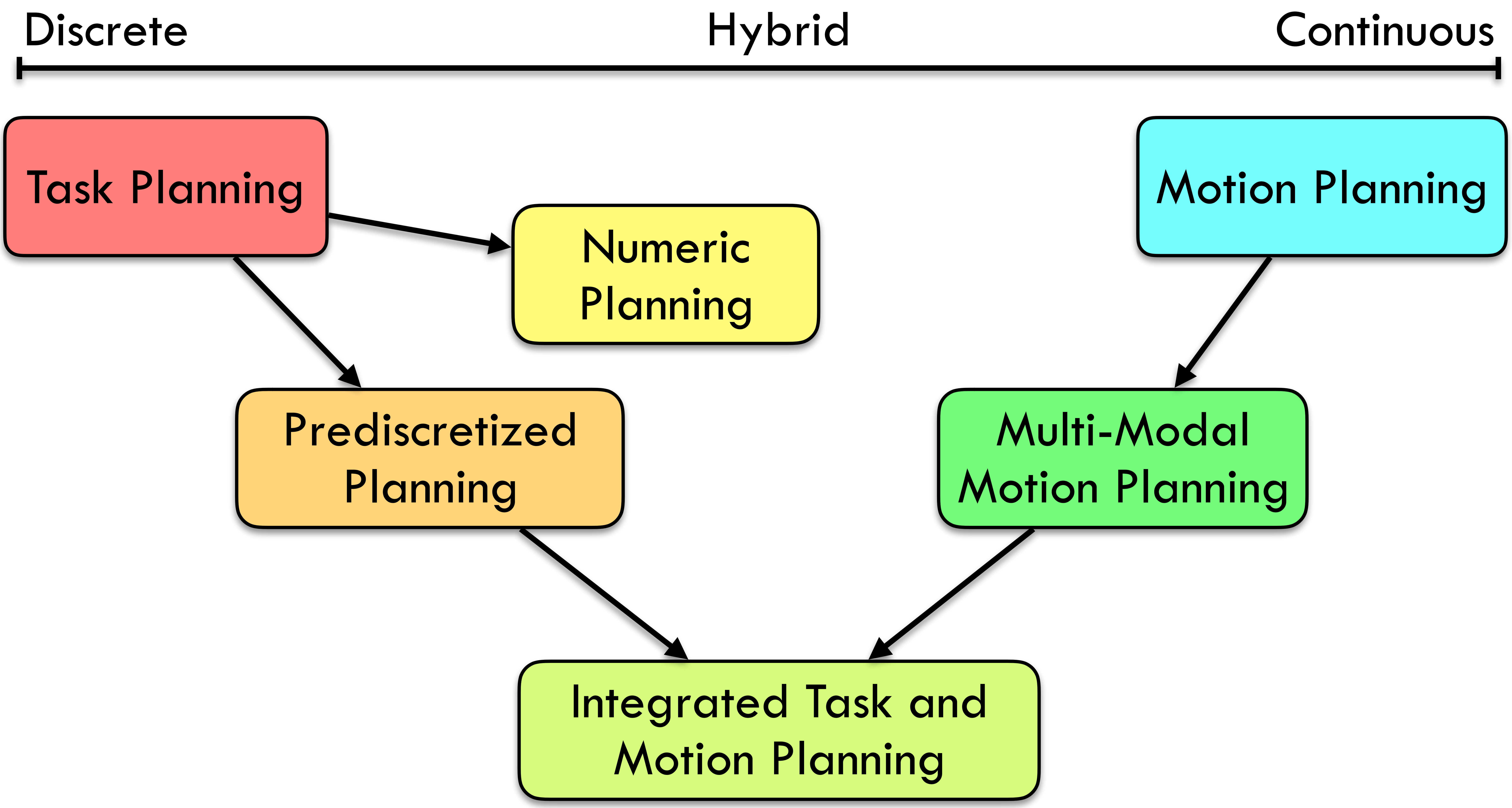
[Erdem 2011][De Silva 2013]
[Srivastava 2014][Dantam 2018]



- Direct search in **combined** state-space

[Kaelbling 2011] [Garrett 2018a] [Garrett 2018b]

Hybrid Planning Spectrum Revisited



Our Approach: STRIPStream

- **No general-purpose, flexible framework** for planning in a variety of TAMP domains
- Extends **PDDL** to incorporate **sampling procedures**
  - Can model domains with **infinitely-many** actions

- Develop **domain-independent** algorithms that treat the samplers as **blackbox inputs**
- Algorithms solve a **sequence of finite** PDDL problems
  - Leverage existing **classical planners** as subroutines
- Algorithms are particularly **fast when downward refinement holds** while remaining **complete**

STRIPStream Language

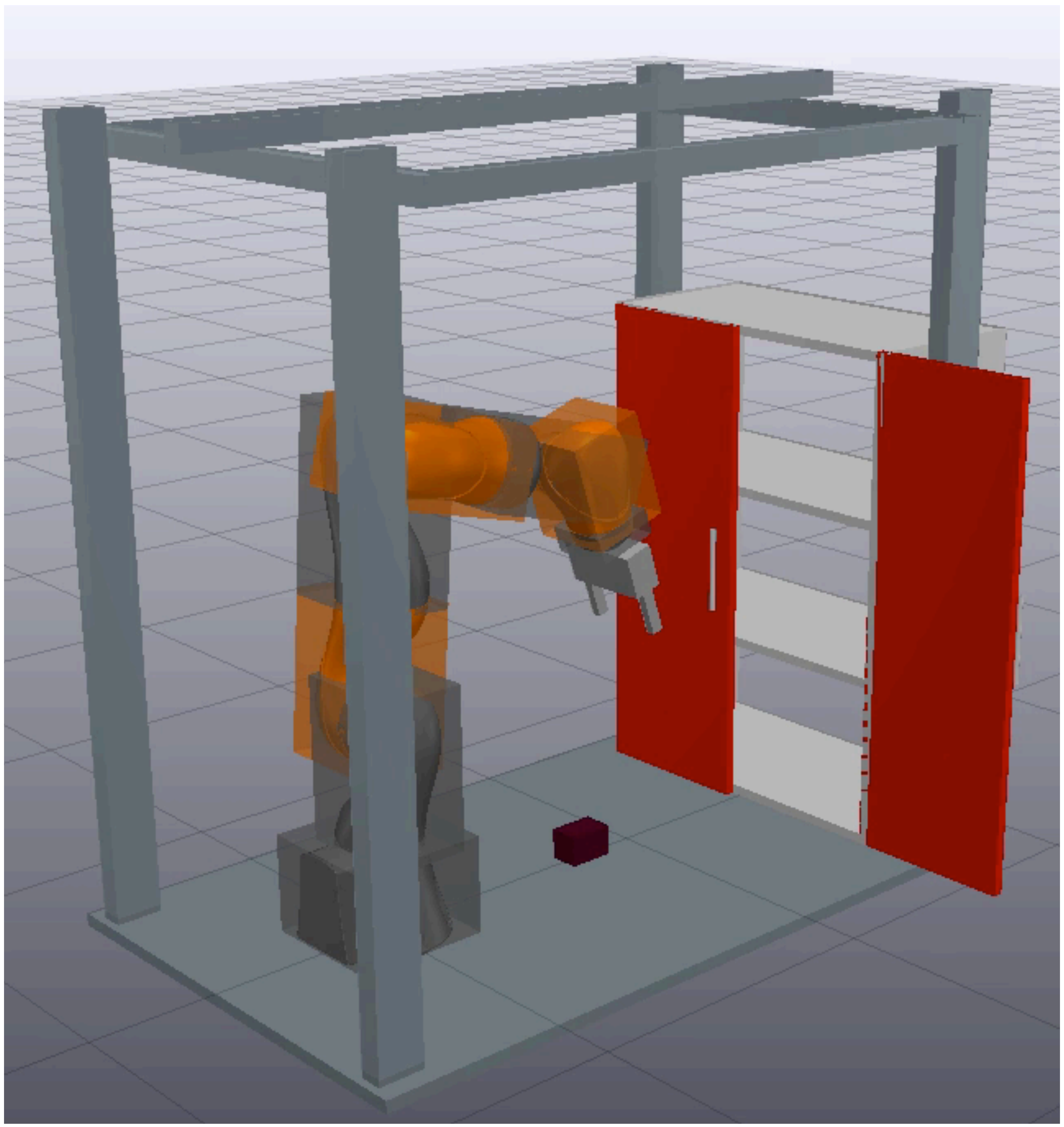
Benefits of Extending PDDL

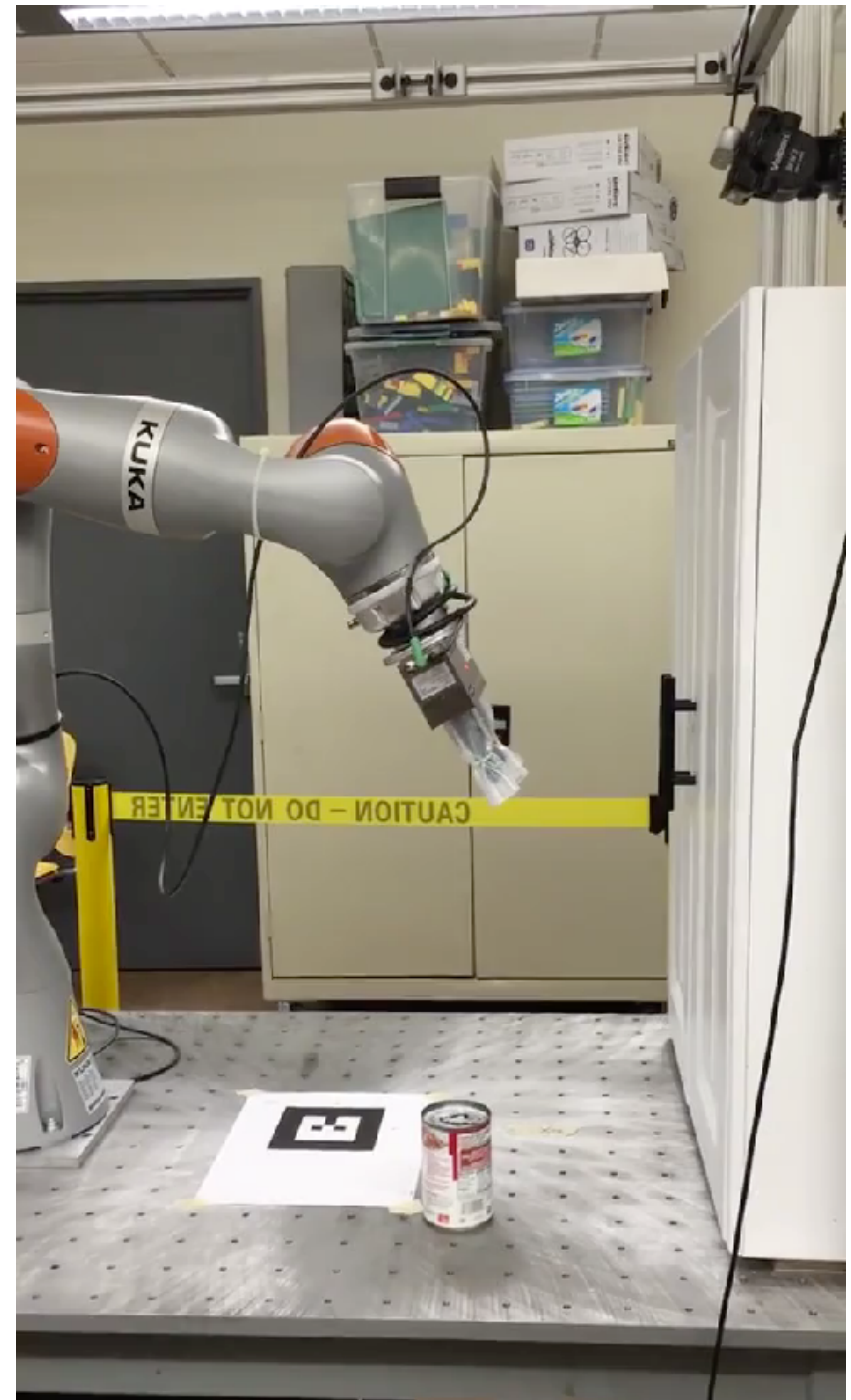
- **Standardized** action description language
- Emphasis on describing and solving problems in a **domain-independent** way

- Large wealth of efficient, **existing algorithms** that exploit **factored** state & action structure

- Encodes the **difference** between two states using preconditions & effects
  - Most variables are **unchanged**
  - Actions can be described using **few parameters**

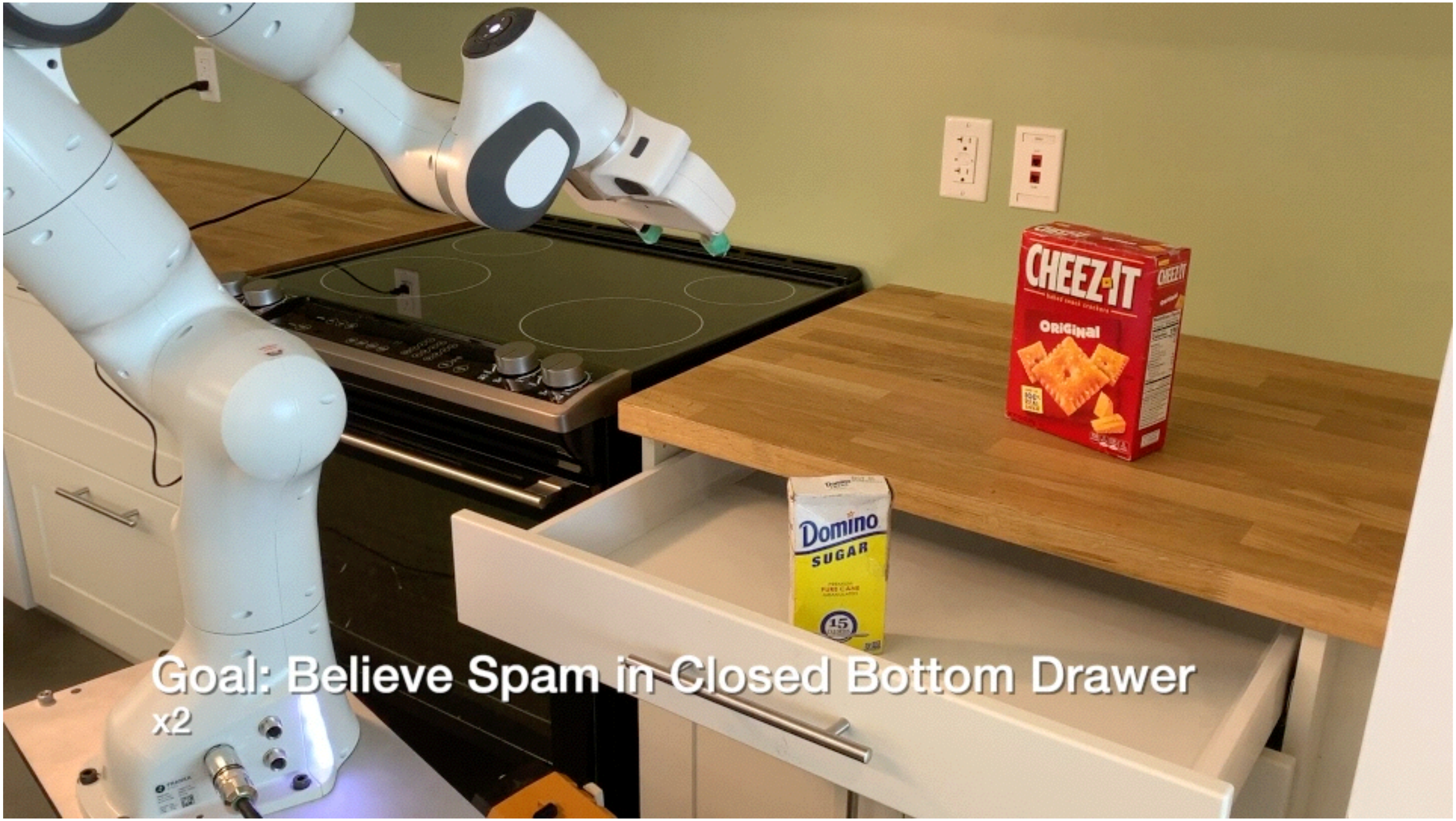
STRIPStream + Drake





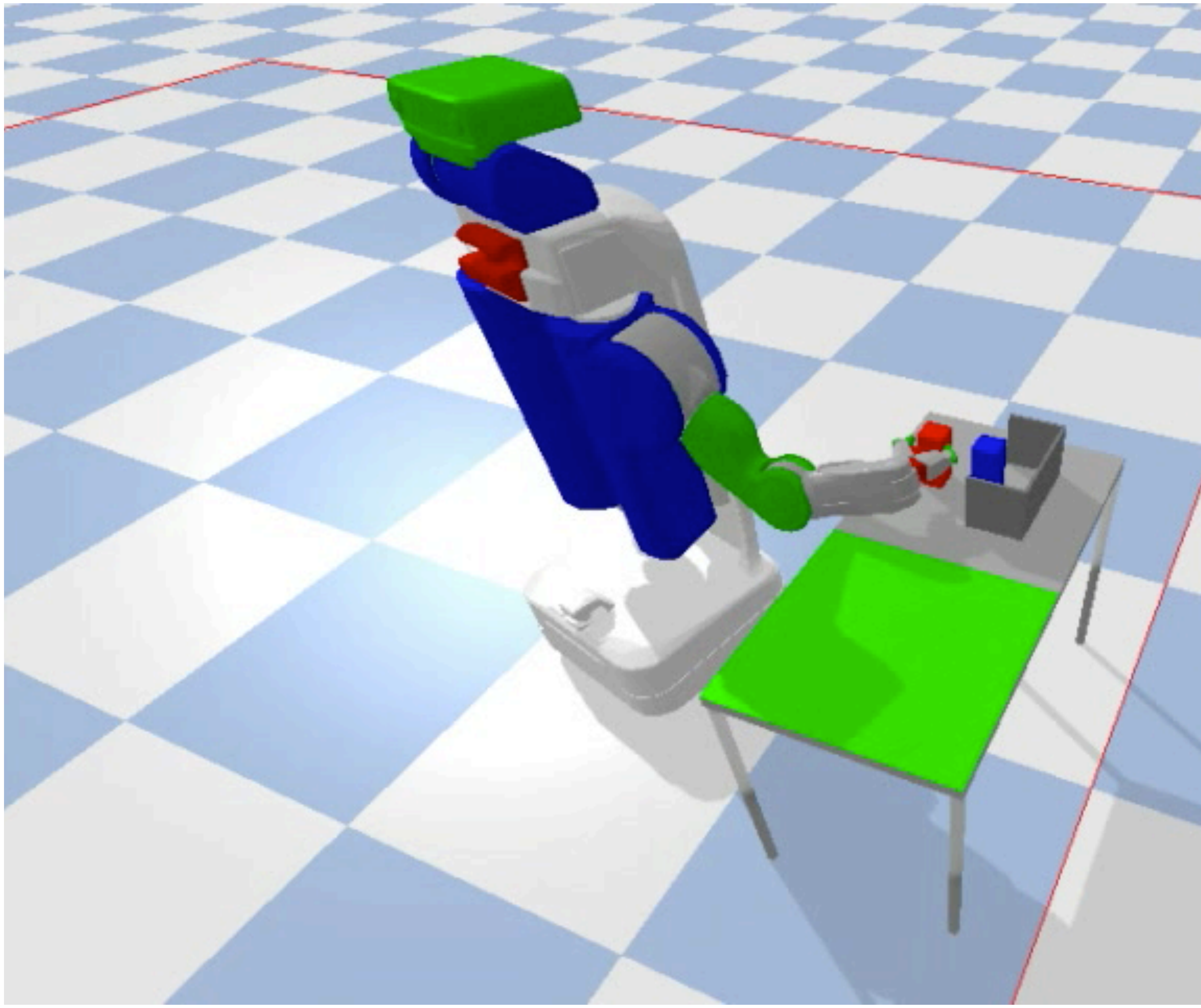
Solved Using the Same Algorithm

Framework not specific to a single robot or robotics at all!



Motivating Pick & Place Example

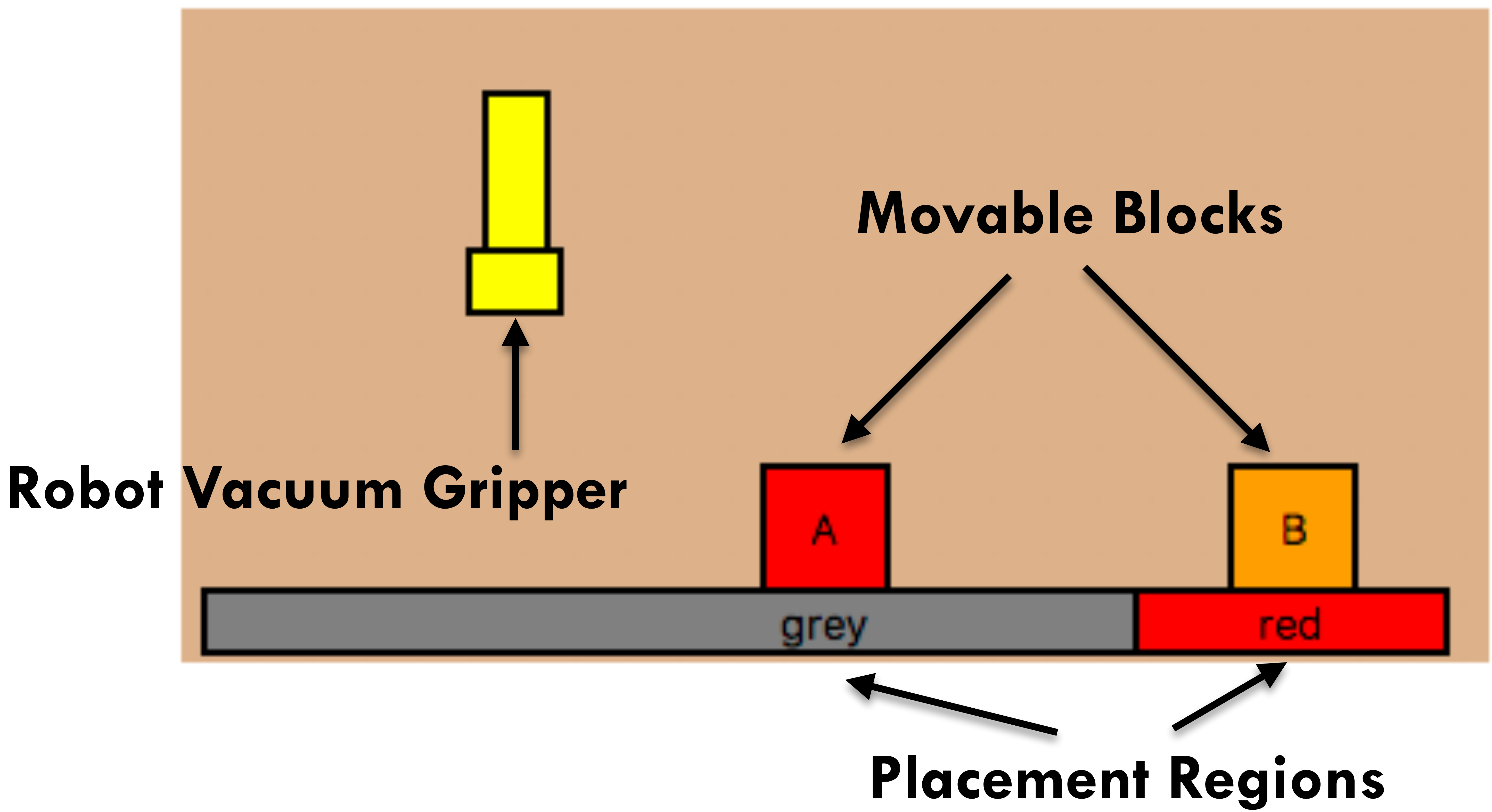
- Single object **prevents** a goal object from being reachable



- Focus on a compact 2D version
- Formulation almost the same for 3D
- Algorithms agnostic to number of DOFs

2D Pick-and-Place Example

- **Goal**: block **A** within the **red** region
- Robot and block poses are continuous (x, y) pairs
- Block **B** obstructs the placement of **A**



2D Pick-and-Place Solution

- One (of infinitely many) possible solutions
  - move, pick **B**, move, place **B**,
    move, pick **A**, move, place **A**

2D Pick-and-Place Initial & Goal

- Some constants are **numpy arrays**
- **Static initial facts** - value is **constant** over time
  - (Block, A), (Block, B), (Region, red), (Region, grey), (Conf, **[-7.5 5.]**), (Pose, A, **[0. 0.]**), (Pose, B, **[7.5 0.]**), (Grasp, A, **[0. -2.5]**), (Grasp, B, **[0. -2.5]**)
- **Fluent initial facts** - value **changes** over time
  - (AtConf, **[-7.5 5.]**), (HandEmpty), (AtPose, A, **[0. 0.]**), (AtPose, B, **[7.5 0.]**)
- **Goal formula:** `(`**`exists`**` (?p) (`**`and`**` (Contained `**A**` ?p `**red**`)`
  `(AtPose `**A**` ?p)))`

2D Pick-and-Place Actions

- Typical PDDL action description except that arguments are **high-dimensional** & **continuous**!
- To use the actions, must **prove** the following **static facts:**

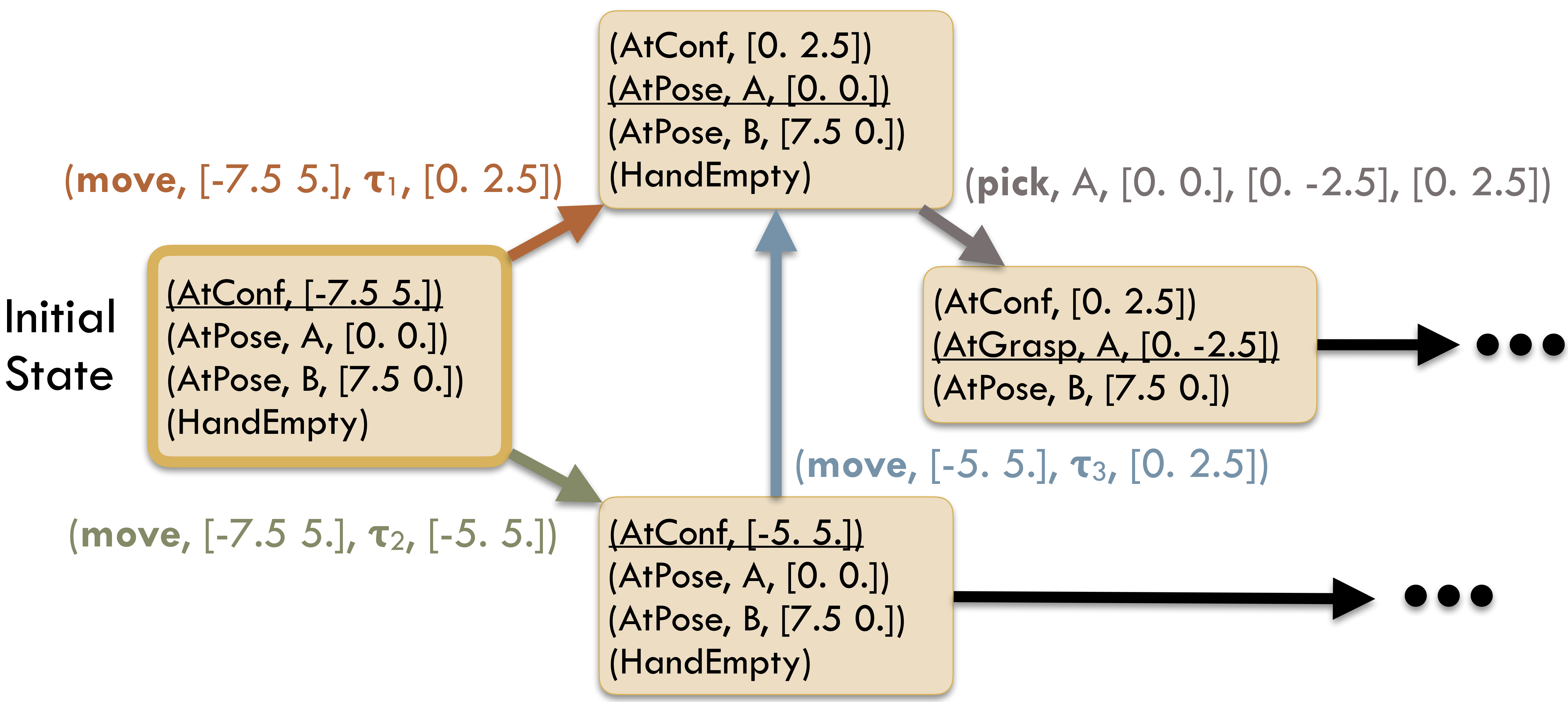
```
(Motion ?q1 ?t ?q2), (Kin ?b ?p ?g ?q)
```

```
(:action move
  :parameters (?q1 ?t ?q2)
  :precondition (and (Motion ?q1 ?t ?q2) (AtConf ?q1))
  :effect (and (AtConf ?q2) (not (AtConf ?q1))))

(:action pick
  :parameters (?b ?p ?g ?q)
  :precondition (and (Kin ?b ?p ?g ?q)
                     (AtConf ?q) (AtPose ?b ?p) (HandEmpty))
  :effect (and (AtGrasp ?b ?g)
               (not (AtPose ?b ?p)) (not (HandEmpty))))
```

BFS in Discretized State-Space

- Suppose we were **given** the following additional static facts:
  - (Motion, [-7.5 5.], τ_1, [0. 2.5]), (Motion, [-7.5 5.], τ_2, [-5. 5.]), (Motion, [-5. 5.], τ_3, [0. 2.5]), (Kin, A, [0. 0.], [0. -2.5], [0. 2.5]), …



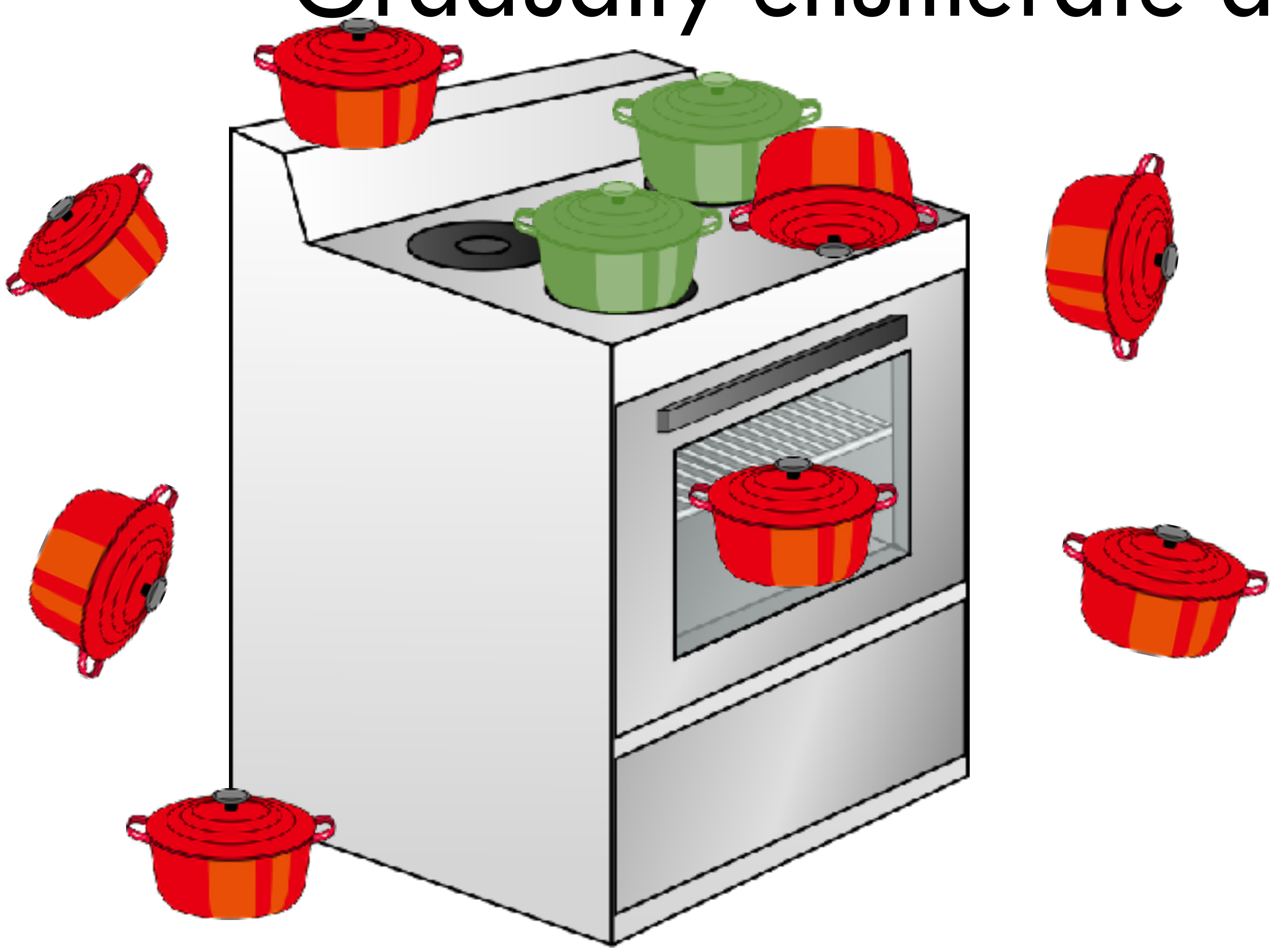
No a Priori Discretization

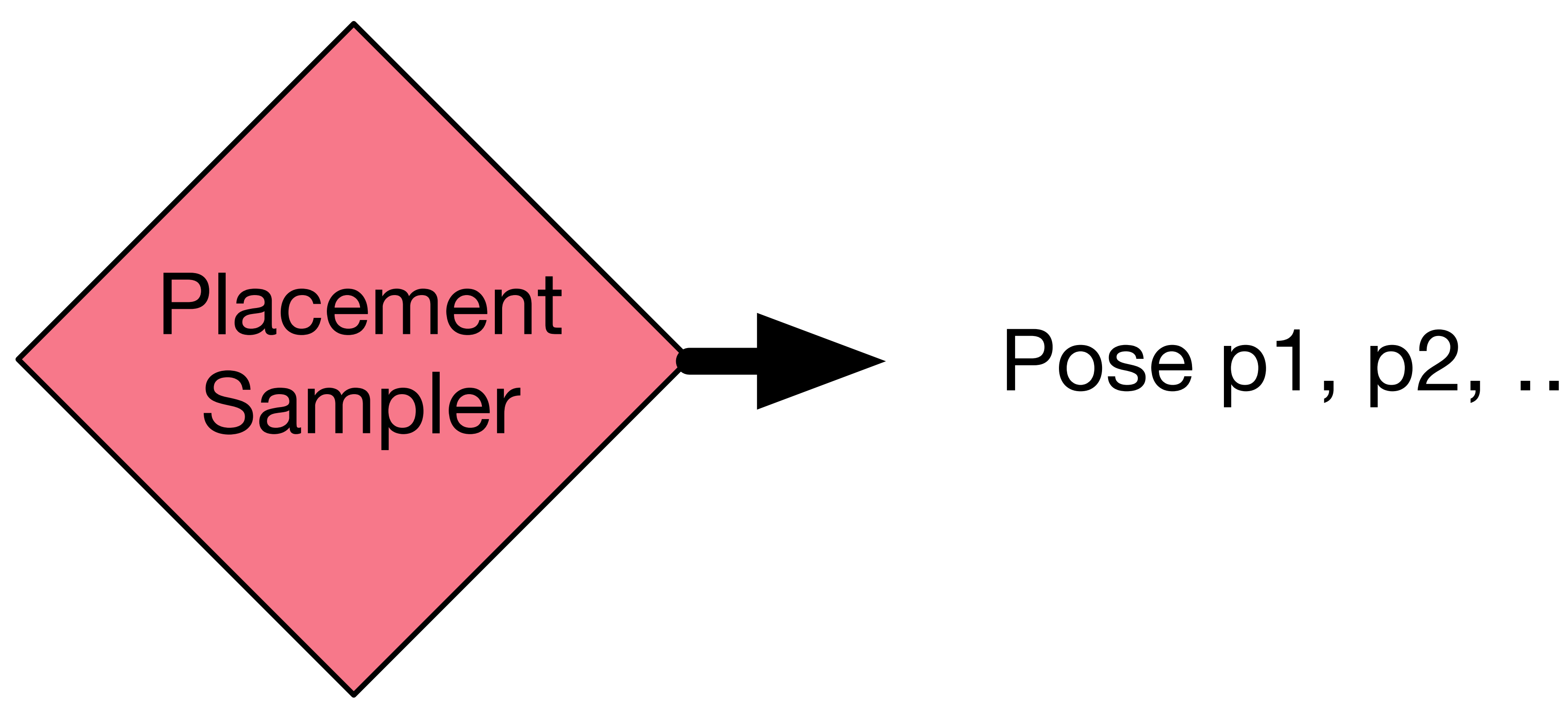
- **Values given at start:**
  - 1 initial configuration: (Conf, **[-7.5 5.]**)
  - 2 initial poses: (Pose, A, **[0. 0.]**), (Pose, B, **[7.5 0.]**)
  - 2 grasps: (Grasp, A, **[0. -2.5]**), (Grasp, B, **[0. -2.5]**)

- **Planner needs to find:**
  - 1 pose within a region: `(Contain` A `?p` red`)`
  - 1 collision-free pose: `(CFree` A `?p ?` B `?p2)`
  - 4 grasping configurations: `(Kin ?b ?p ?g ?q)`
  - 4 robot trajectories: `(Motion ?q1 ?t ?q2)`

What Samplers Do We Need?

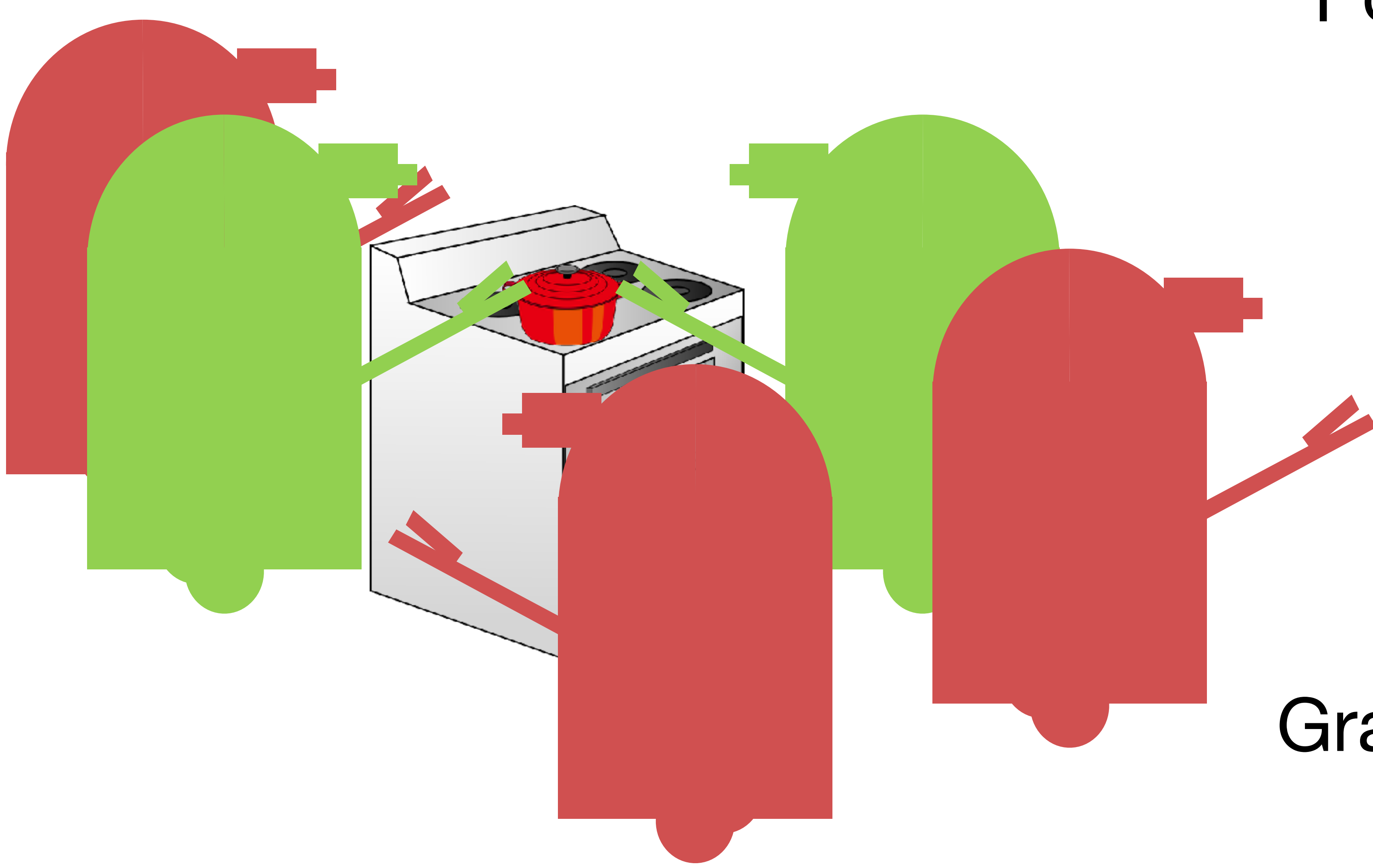
- **Low-dimensional** placement stability constraint (`Contain`)
  - *i.e.* 1D manifold embedded in 2D pose space
- Directly **sample values that satisfy the constraint**
- May need **arbitrarily many** samples
  - Gradually enumerate an **infinite sequence**

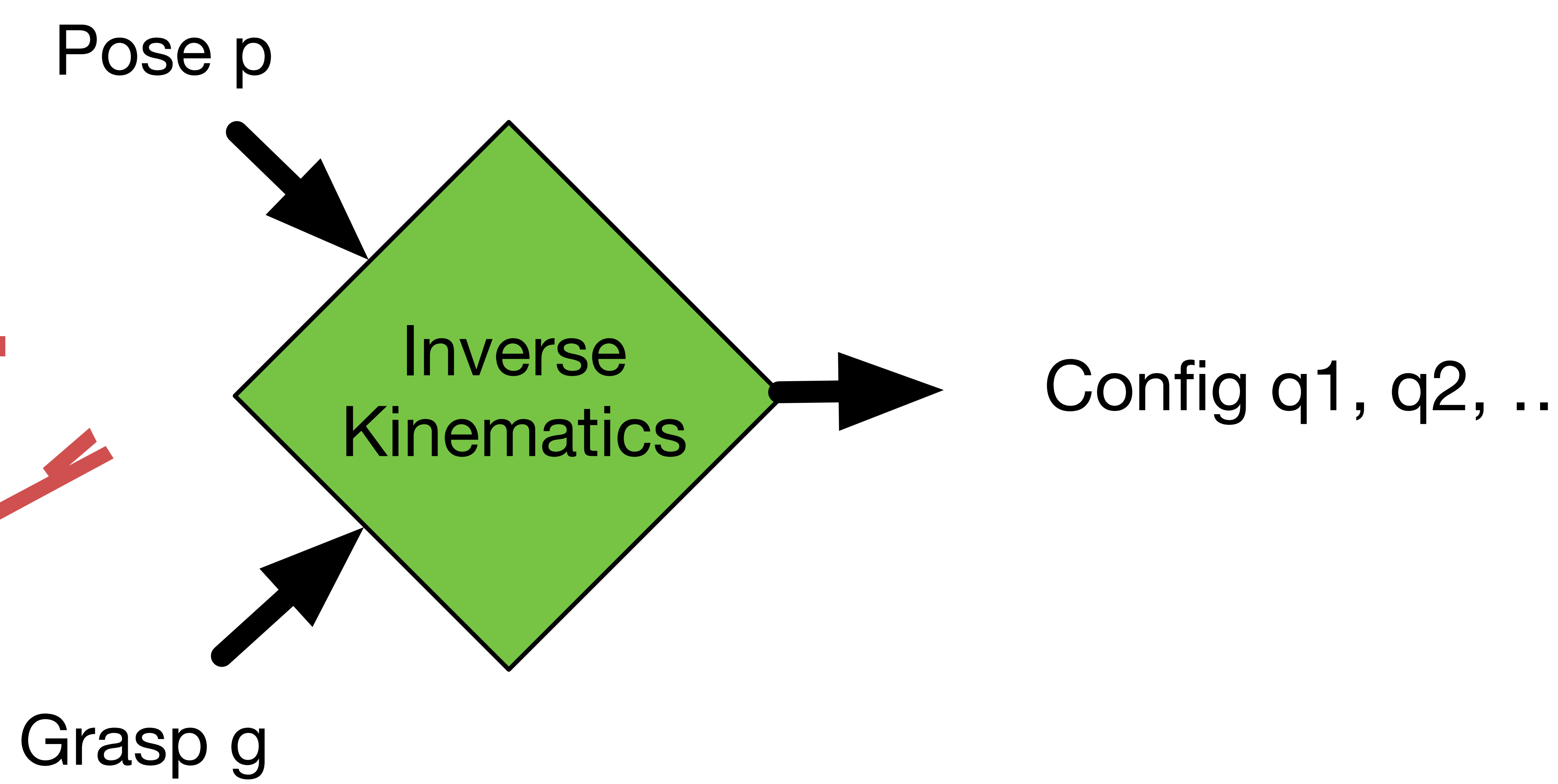




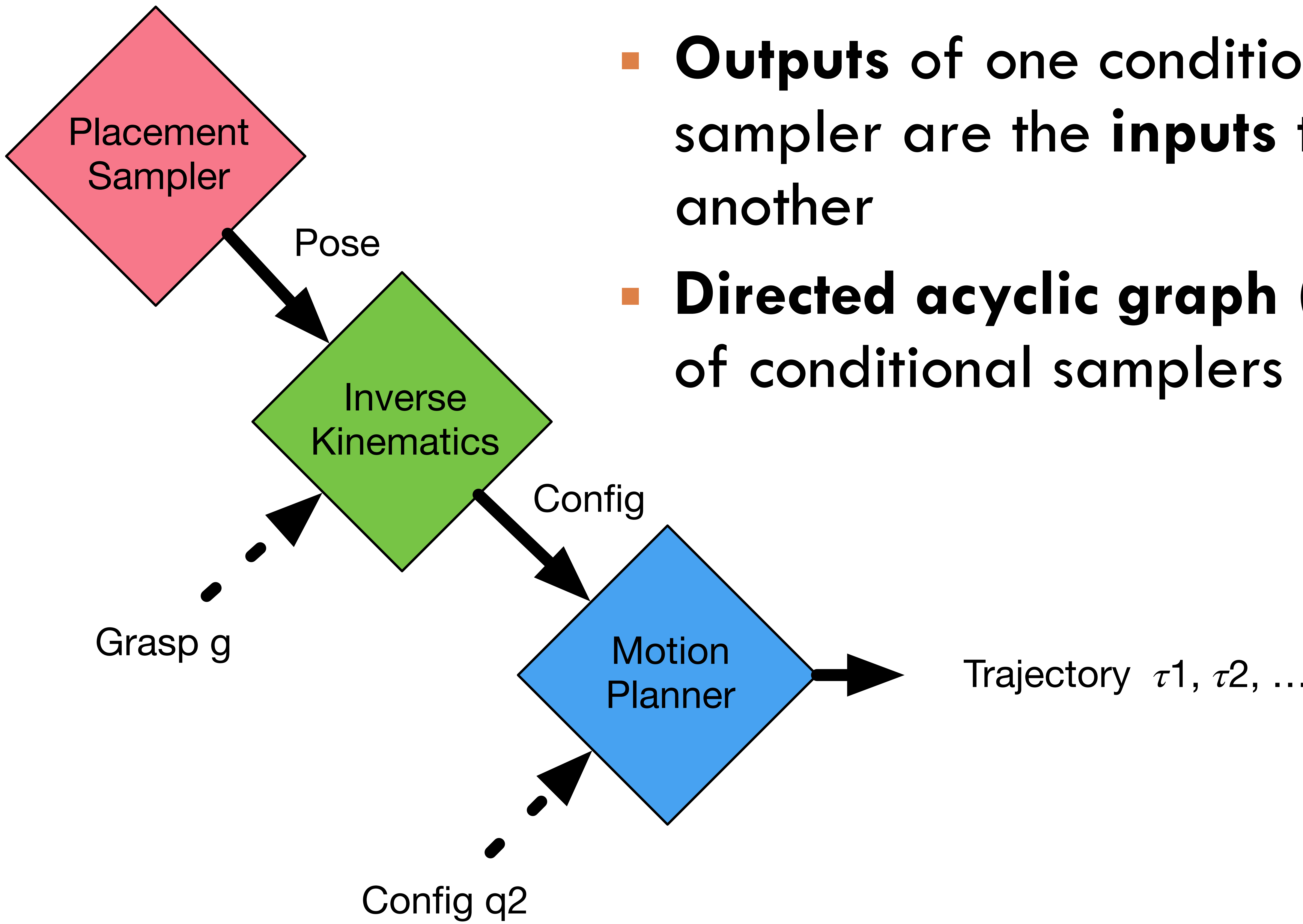
Intersection of Constraints

- **Kinematic constraint** (`Kin`) involves poses, grasps, and configurations
- **Conditional samplers** - samplers with inputs





Composing Conditional Samplers



- **Outputs** of one conditional sampler are the **inputs** to another
- **Directed acyclic graph (DAG)** of conditional samplers

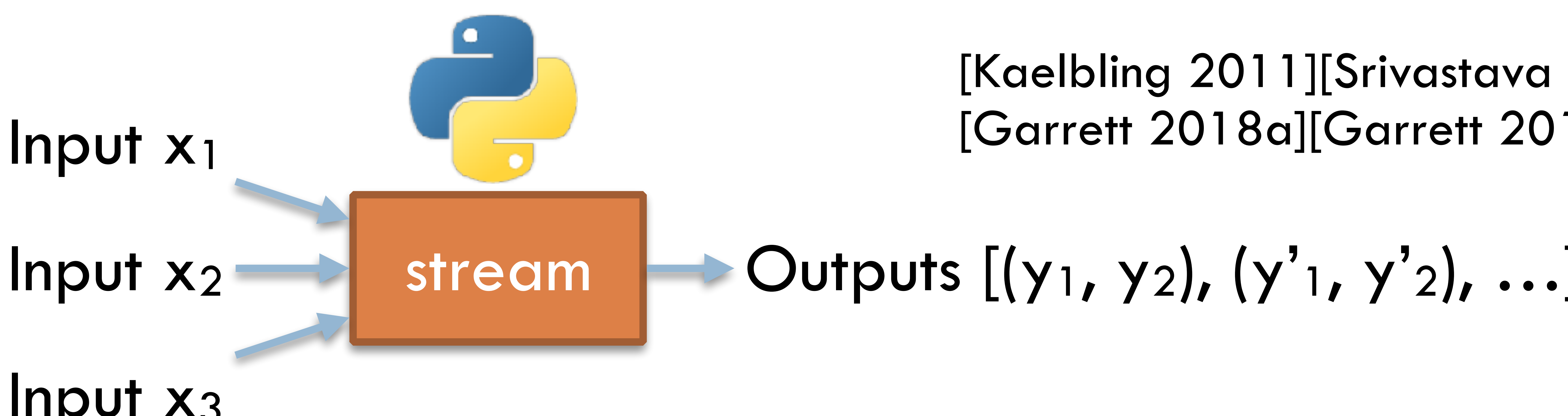
Stream: a function to a generator

- **Advantages**
  - Programmatic implementation
  - Compositional
  - Supports infinite sequences

```python
def stream(x1, x2, x3):
    i = 0
    while True:
        y1 = i*(x1 + x2)
        y2 = i*(x2 + x3)
        yield (y1, y2)
        i += 1
```

- **Stream** - function from an **input object tuple** (x_1, x_2, x_3) to a (potentially infinite) sequence of **output object tuples** $[(y_1, y_2), (y'_1, y'_2), \ldots]$

[Kaelbling 2011][Srivastava 2014]
[Garrett 2018a][Garrett 2018b]



Stream Certified Facts

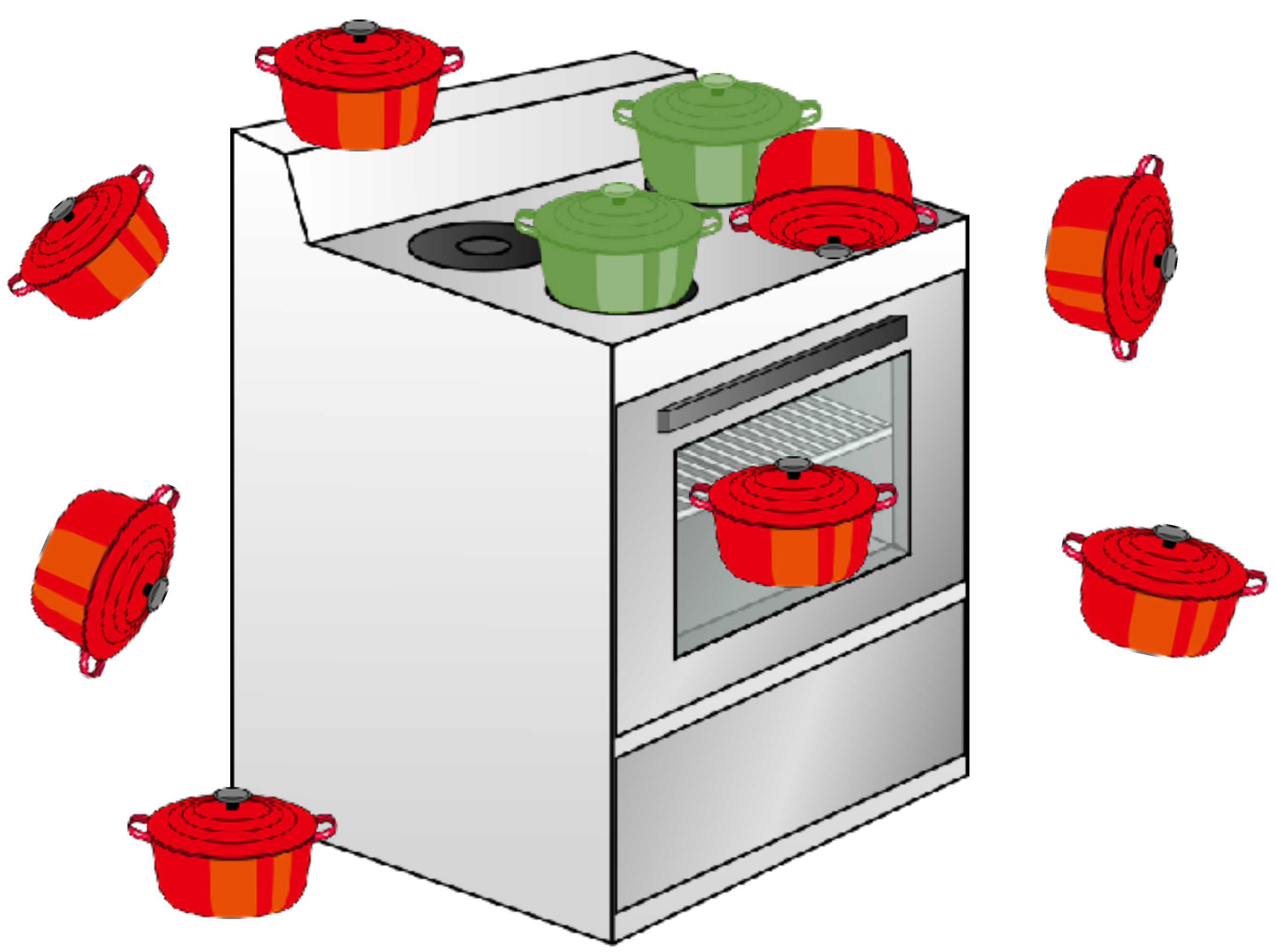
- Objects alone aren't helpful: **what do they represent?**
  - Communicate semantics using **predicates**!

- Augment stream specification with:
  - **Domain facts** - static facts declaring legal **inputs**
    - e.g. only configurations can be motion inputs

  - **Certified facts** - static facts that all **outputs** satisfy with their corresponding **inputs**
    - e.g. poses sampled from a region are within it

Sampling Contained Poses


```
(:stream sample-region
  :inputs (?b ?r)
  :domain (and (Block ?b) (Region ?r))
  :outputs (?p)
  :certified (and (Pose ?b ?p) (Contain ?b ?p ?r)))
```



```
def sample_region(b, r):
  x_min, x_max = REGIONS[r]
  w = BLOCKS[b].width
  while True:
      x = random.uniform(x_min + w/2,
                         x_max - w/2)
      p = np.array([x, 0.])
      yield (p,)
```

Block b

Region r

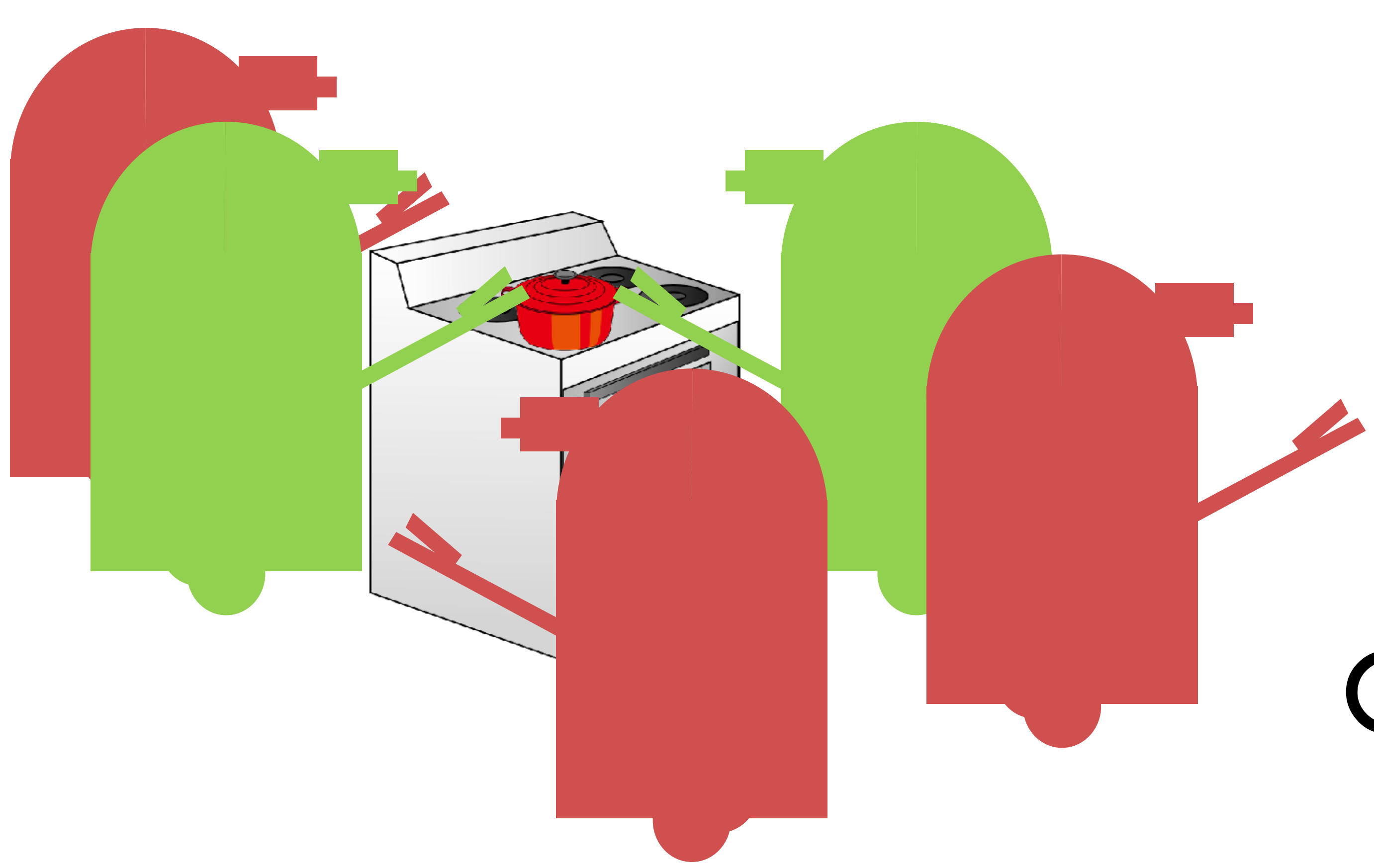
sample-region

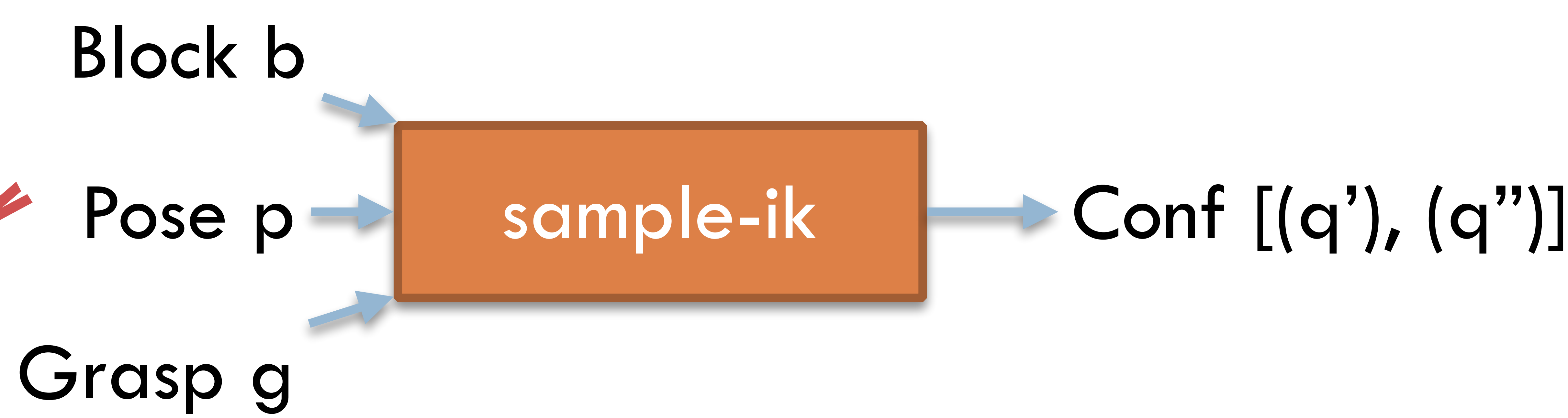
Pose [(p), (p'), (p"), ...]

Sampling IK Solutions

- **Inverse kinematics** (IK) to produce robot grasping configuration
  - Trivial in 2D, non-trial in general (e.g. 7 DOF arm)

```
(:stream sample-ik
  :inputs (?b ?p ?g)
  :domain (and (Pose ?b ?p) (Grasp ?b ?g))
  :outputs (?q)
  :certified (and (Conf ?q) (Kin ?b ?p ?g ?q)))
```





Calling a Motion Planner

- "Sample" (e.g. via a PRM) **multi-waypoint trajectories**
- Include **joint limits & fixed obstacle collisions**, but not movable object collisions

```
(:stream sample-motion
   :inputs (?q1 ?q2)
   :domain (and (Conf ?q1) (Conf ?q2))
   :outputs (?t)
   :certified (and (Traj ?t) (Motion ?q1 ?t ?q2)))
```

2D Place Collisions

- Add parameters for the pose of each block - **bad!**
- Use a **derived predicate** for whether currently **unsafe**
  - Predicate defined by **logical formula** [Fox 2003] [Thiébaux 2005]
  - Enables lightweight **logical inference**
  - Decomposes collision checking into a logical **AND**

```
(:action place
  :parameters (?b ?p ?g ?q)
  :precondition (and ... (not (UnsafePose ?b ?p)))
  :effect (and ...)

(:derived (UnsafePose ?b1 ?p1)
  (exists (?b2 ?p2) (and (Pose ?b1 ?p1) (Pose ?b2 ?p2)
                          (not (= ?b1 ?b2)) (AtPose ?b2 ?p2)
                          (not (CFree ?b1 ?p1 ?b2 ?p2)))))
```

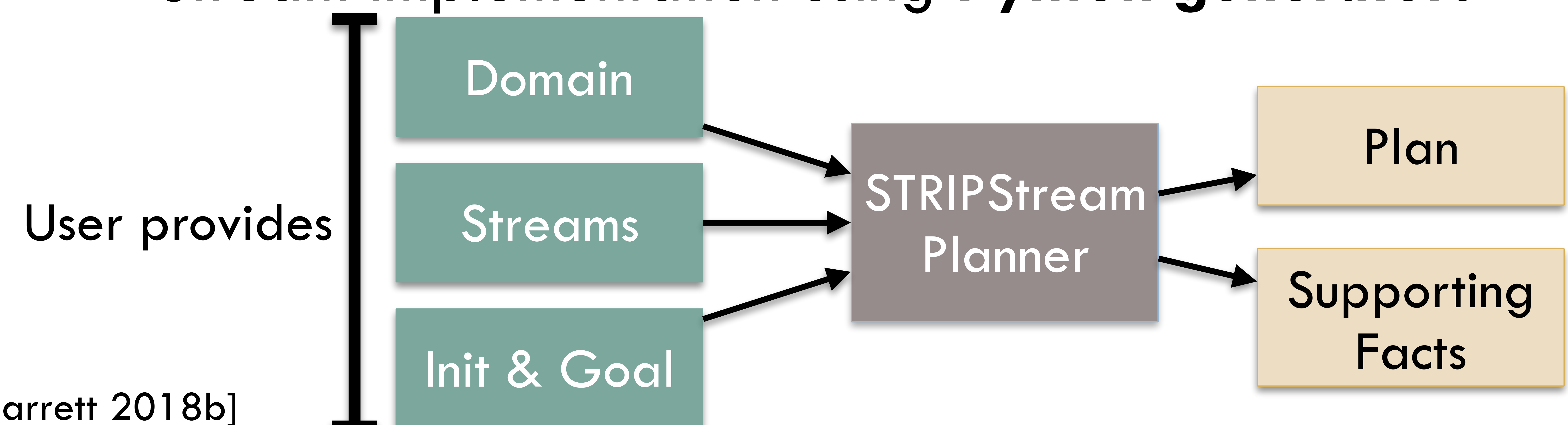
Check Block Collisions

- **Test stream:** stream without output objects
- Return True if **collision-free** placement (e.g. via querying a collision checker)

```
(:stream test-cfree
  :inputs (?b1 ?p1 ?b2 ?p2)
  :domain (and (Pose ?b1 ?p1) (Pose ?b2 ?p2))
  :outputs ()
  :certified (CFree ?b1 ?p1 ?b2 ?p2))
```

STRIPStream = STRIPS + Streams

- **Domain dynamics** (*domain.pddl*): *declares* actions
- **Stream properties** (*stream.pddl*)
  - Declares stream inputs, outputs, and certified facts
- **Problem** and **stream implementation** (*problem.py*)
  - Initial state, **Python constants**, & goal formula
  - Stream implementation using **Python generators**



[Garrett 2018b]

STRIPStream Algorithms

Two STRIPStream Algorithms

- **STRIPStream planners decide** which streams to use
- Algorithms alternate between **searching & sampling:**

1. **Search** a finite PDDL problem for plan
2. **Modify** the PDDL problem (depending on the plan)

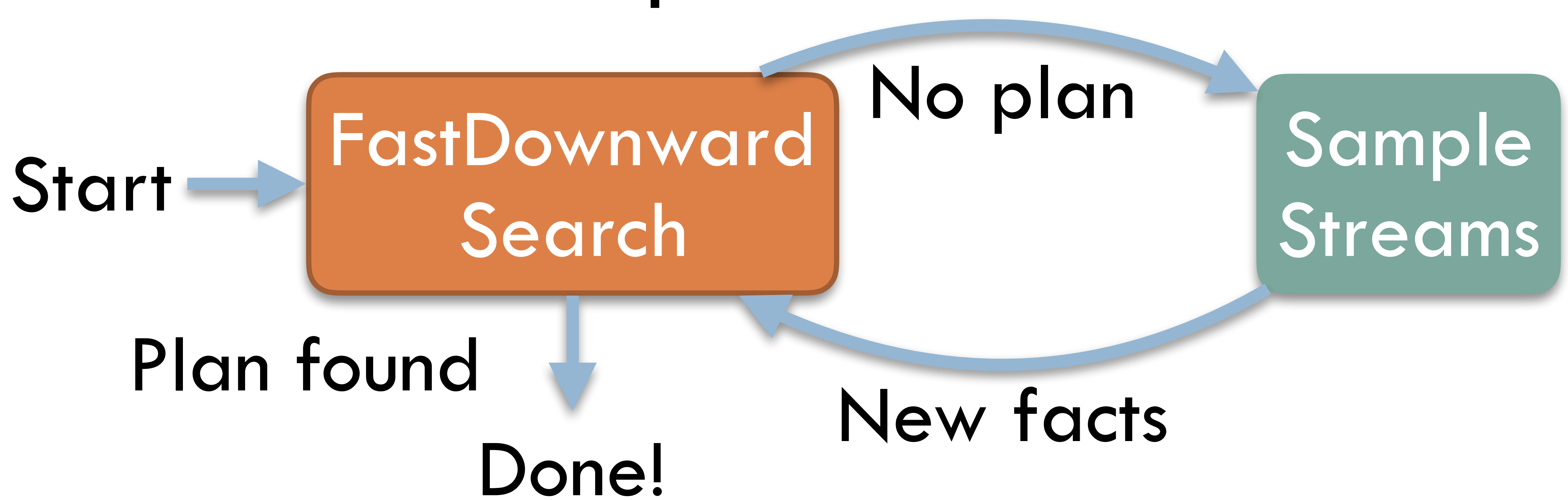
- Search implemented using **off-the-shelf algorithms**
  - **Off-the-shelf AI planner** - FastDownward
    - Exploits factoring in its search heuristics (e.*g*. h_{FF})
    - http://www.fast-downward.org/
  - **Probabilistically complete** given *sufficient* samplers

[Garrett 2018a]
[Garrett 2018b]

Incremental Algorithm

- Incrementally construct all possible initial facts
- Periodically check if a solution exists
- Repeat:

1. **Compose** and **evaluate** a finite number of streams to unveil more facts in the initial state
2. **Search** the current PDDL problem for plan
3. **Terminate** when a plan is found

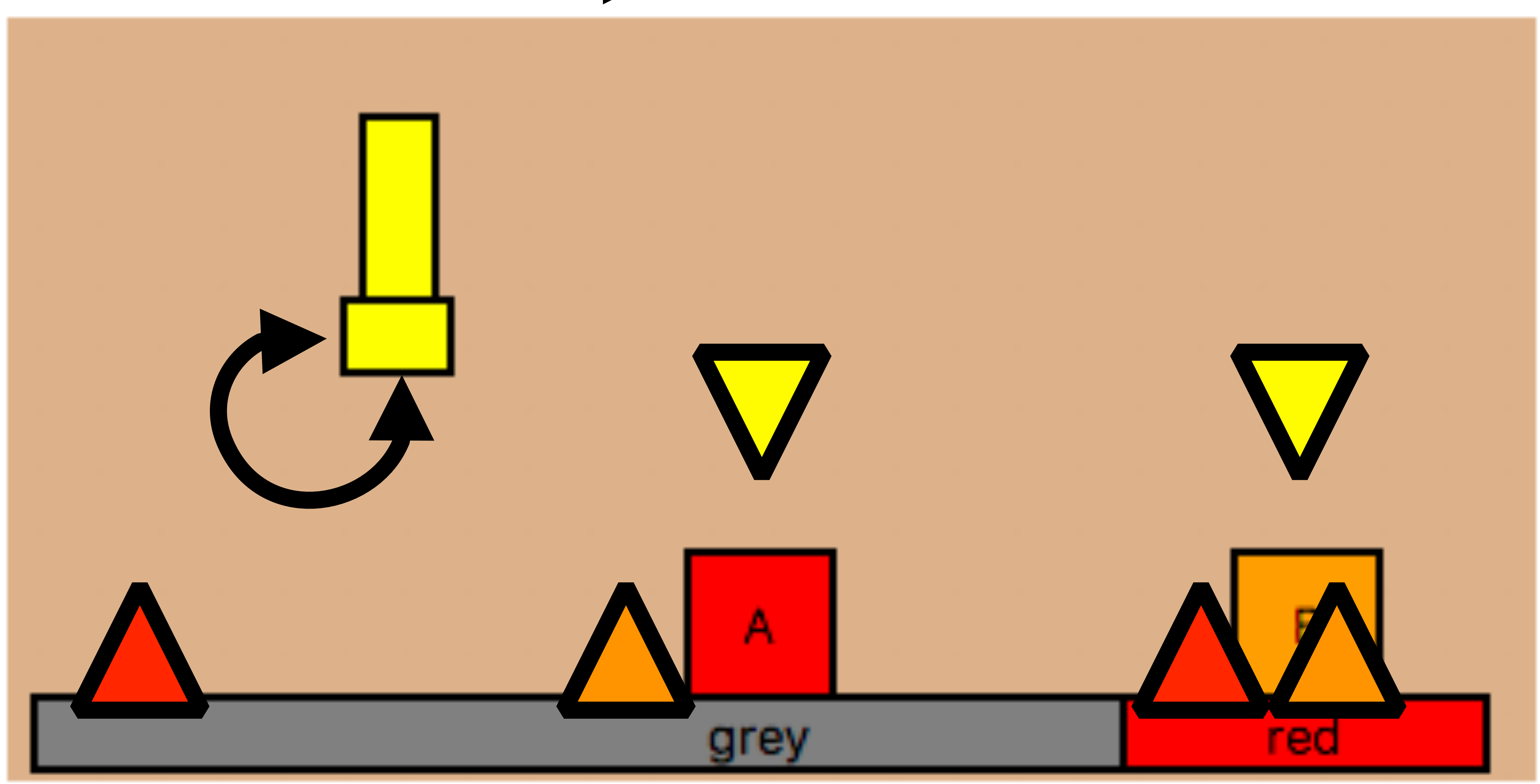


[Garrett 2018a]
[Garrett 2018b]

Incremental: Sampling Iteration 1

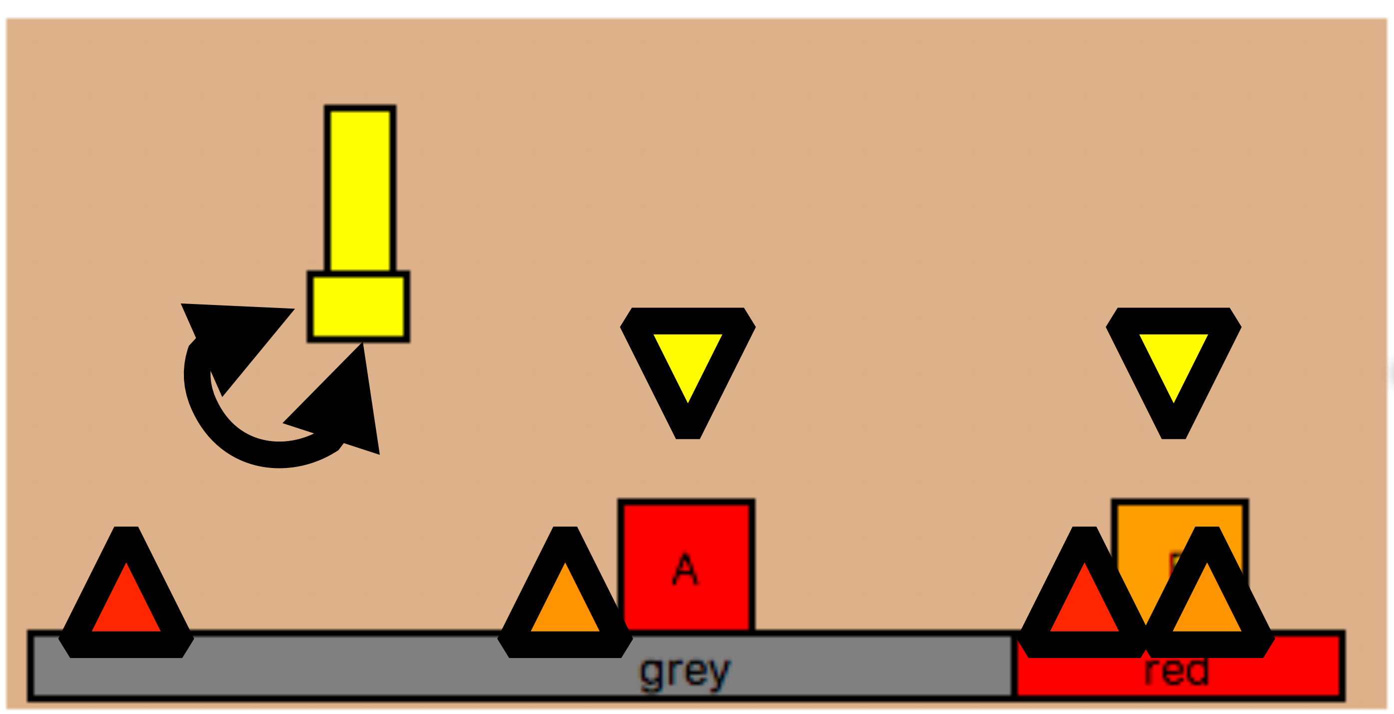
Iteration 1 - 14 stream evaluations

- **Sampled:**
  - 2 new robot configurations:
  - 4 new block poses:
  - 2 new trajectories:



Incremental: Search Iteration 1

- Pass current discretization to FastDownward
- If **infeasible**, the current set of samples is insufficient

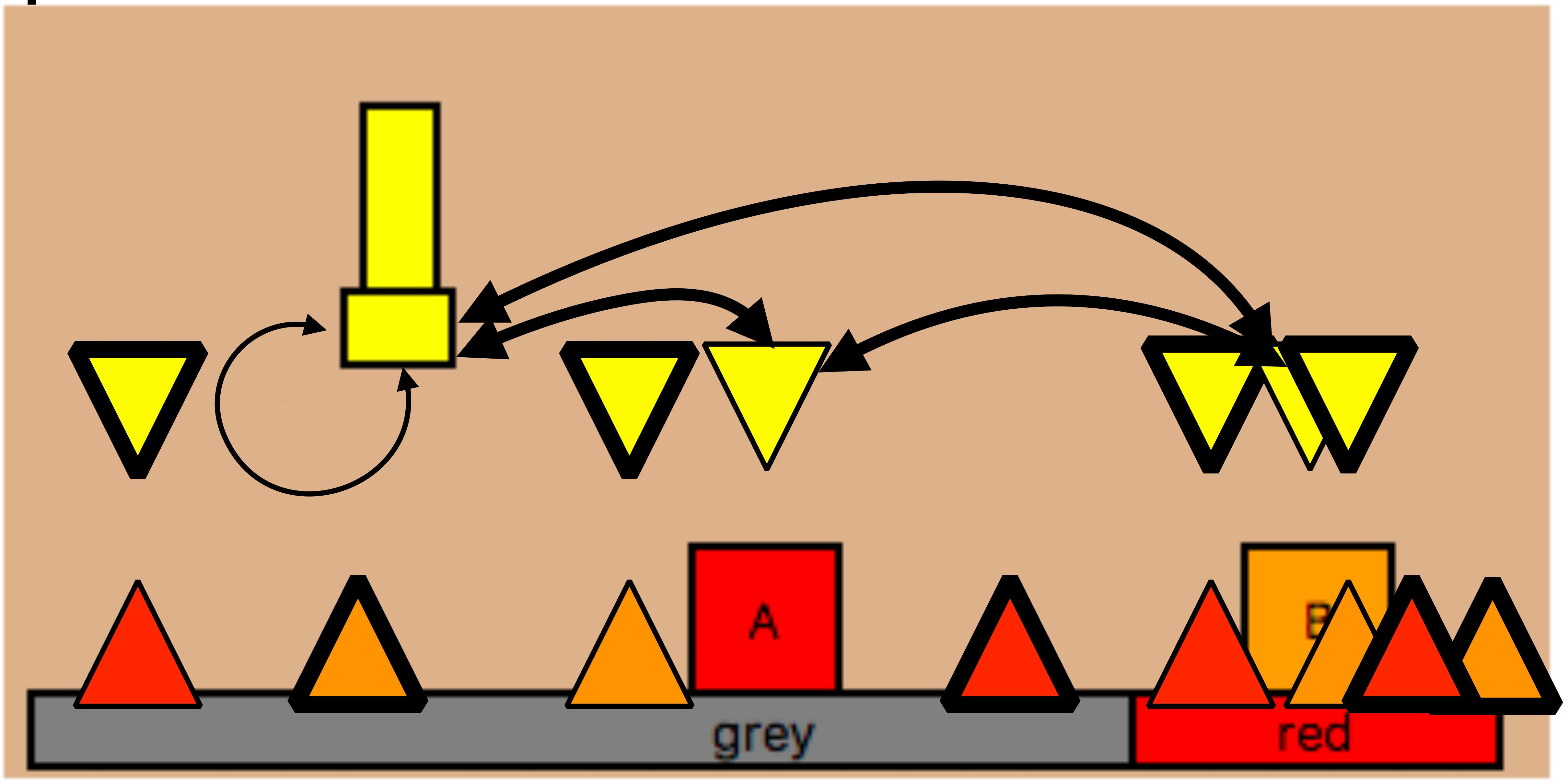


→ FastDownward Search → Infeasible!

Incremental: Sampling Iteration 2

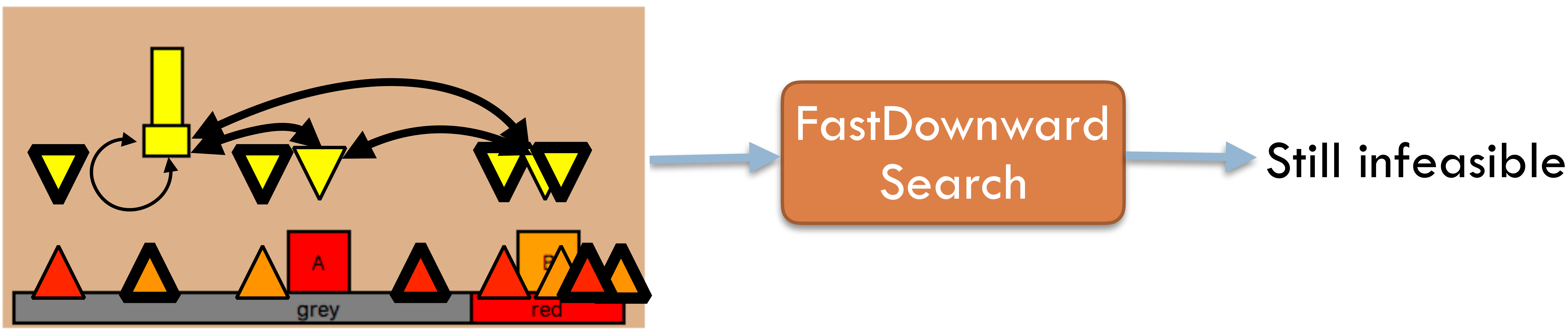
Iteration 2 - 54 stream evaluations

- **Sampled:**
  - 4 new robot configurations:
  - 4 new block poses:
  - 10 new trajectories:



Incremental: Search Iteration 2

- Pass current discretization to FastDownward
- If **infeasible**, the current set of samples is insufficient



Incremental Example: Iterations 3-4

Iteration 3 - 118 stream evaluations
Iteration 4 - 182 stream evaluations

Solution:
1) **move** [-7.5 5.] [[-7.5 5.], [-7.5 5.], [7.5 5.], [7.5 2.5]] [7.5 2.5]
2) **pick B** [7.5 0.] [0. -2.5] [7.5 2.5]
3) **move** [7.5 2.5] [[7.5 2.5], [7.5 5.], [10.97 5.], [10.97 2.5]] [10.97 2.5]
4) **place B** [10.97 0.] [0. -2.5] [10.97 2.5]
5) **move** [10.97 2.5] [[10.97 2.5], [10.97 5.], [0. 5.], [0. 2.5]] [0. 2.5]
6) **pick A** [0. 0.] [0. -2.5] [0. 2.5]
7) **move** [0. 2.5] [[0. 2.5], [0. 5.], [7.65 5.], [7.65 2.5]] [7.65 2.5]
8) **place A** [7.65 0.] [0. -2.5] [7.65 2.5]

- **Drawback** - many unnecessary samples produced
  - **Computationally expensive** to generate
  - Induces **large discrete-planning problems**

Optimistic Stream Outputs

- Many TAMP streams are exceptionally **expensive**
  - Inverse kinematics, motion planning, collision checking
- **Only** query streams that are **identified** as useful
  - Plan with **optimistic hypothetical** outputs [Srivastava 2014]
- Inductively create **unique placeholder** output objects for each stream instance (has **#** as its prefix)

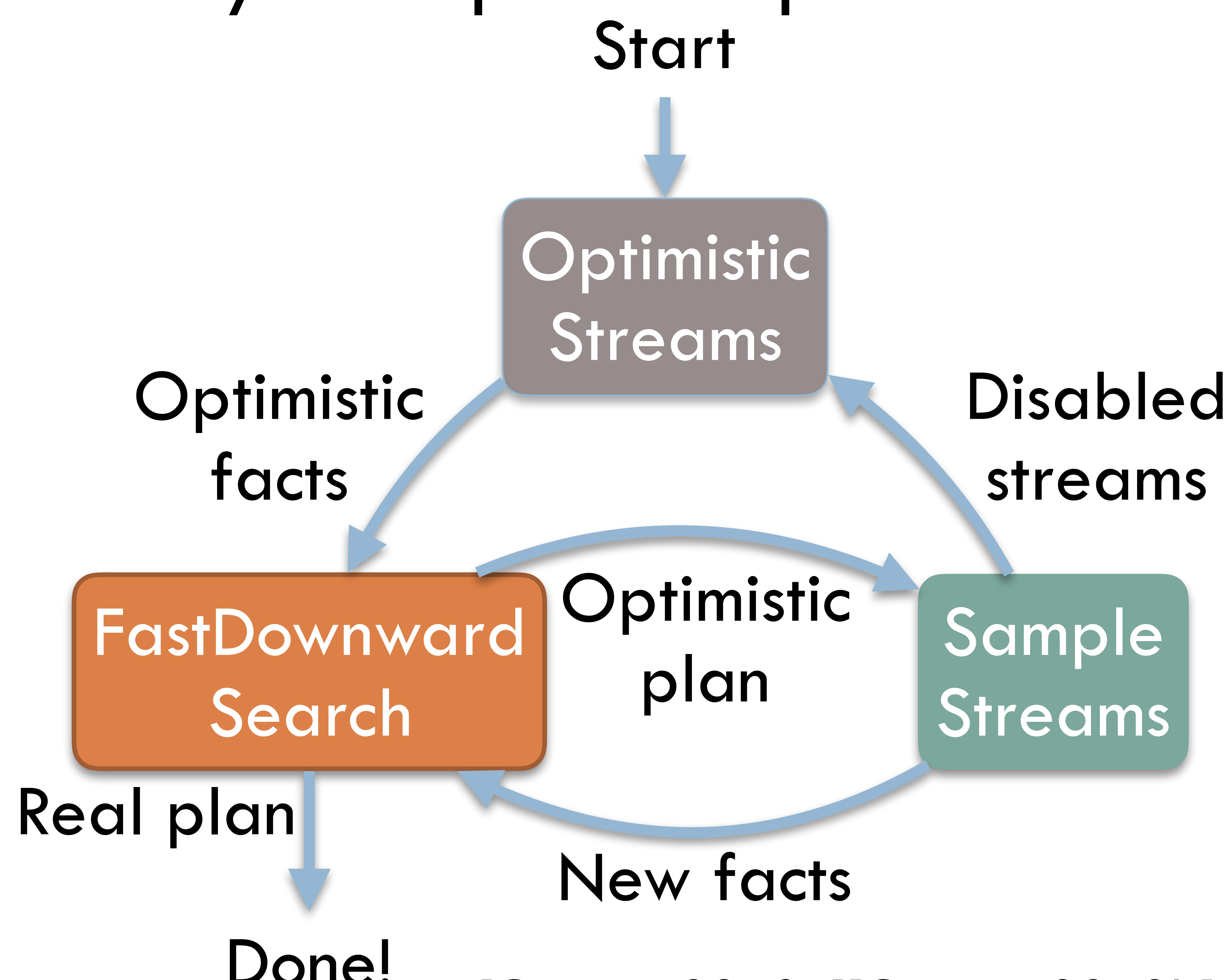
Optimistic evaluations:

1. **s-region:**(b0, red)->(**#p0**)
2. **s-ik:**(b0, [0. 0.], [0. -2.5])->(**#q0**),
3. **s-ik:**(b0, **#p0**, [0. -2.5]) ->(**#q2**)

[Garrett 2018a]
[Garrett 2018b]

Focused Algorithm

- **Lazily** plan using optimistic outputs **before** real outputs
- **Recover** set of streams used by the optimistic plan
- Repeat:
  1. Construct active **optimistic** objects
  2. **Search** with **real & optimistic** objects
  3. If **only real objects** used, **return plan**
  4. **Sample** used streams
  5. **Disable** used streams

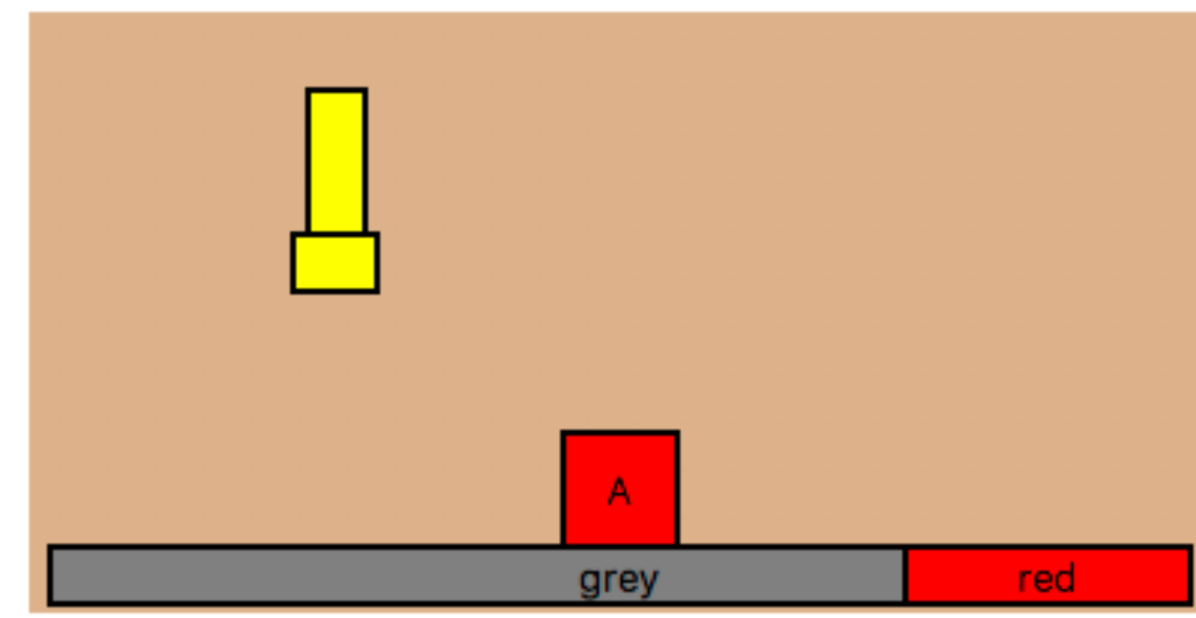


[Garrett 2018a][Garrett 2018b]

Focused Example 1

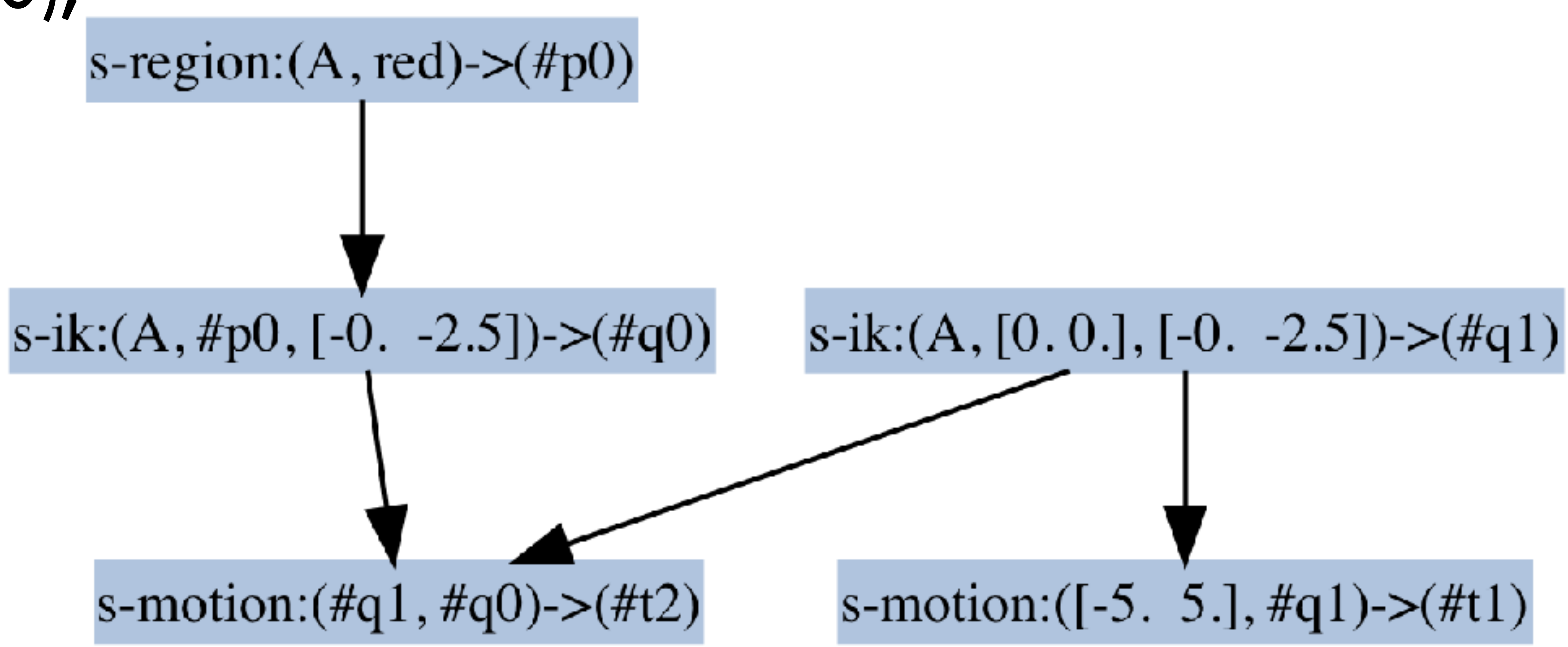
Optimistic Plan:

move([-5. 5.], #t0, #q0), **pick**(A, [0. 0.], [-0. -2.5], #q0), **move**(#q0, #t2, #q1), **place**(A, #p0, [-0. -2.5], #q1)



Constraints:

(kin, A, #q0, #p0, [-0. -2.5]),
(kin, A, #q1, [0. 0.], [-0. -2.5]),
(motion, [-5. 5.], #t1, #q1),
(motion, #q1, #t2, #q0),
(contain, A, #p0, red),



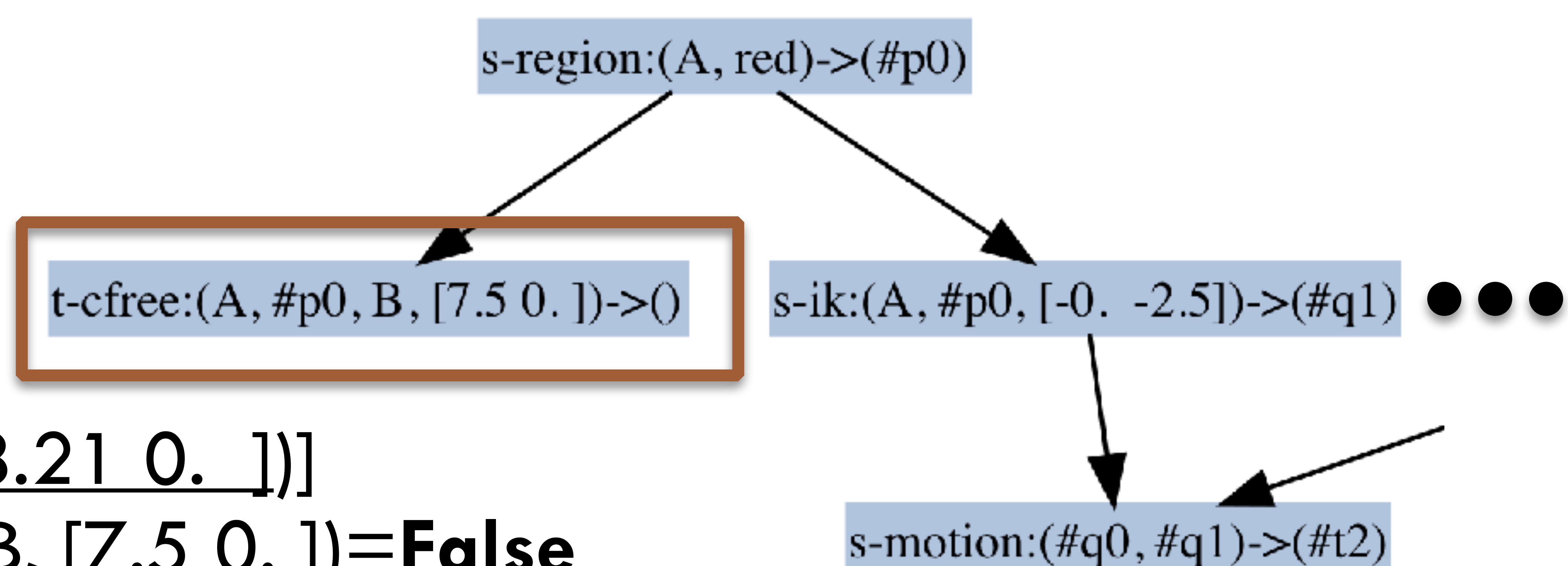
Focused Example 2: Iteration 1

Optimistic Plan:

move([-5. 5.], #t0, #q0), **pick**(A, [0. 0.], [-0. -2.5], #q0), **move**(#q0, #t2, #q1), **place**(A, #p0, [-0. -2.5], #q1)

Constraints:

(cfree, A, #p0, B, [7.5 0.]), (contain, A, #p0, red), (kin, A, #q0, [0. 0.], [-0. -2.5]), (kin, A, #q1, #p0, [-0. -2.5]), (motion, #q0, #t2, #q1), (motion, [-5. 5.], #t0, #q0)



Stream evaluations:

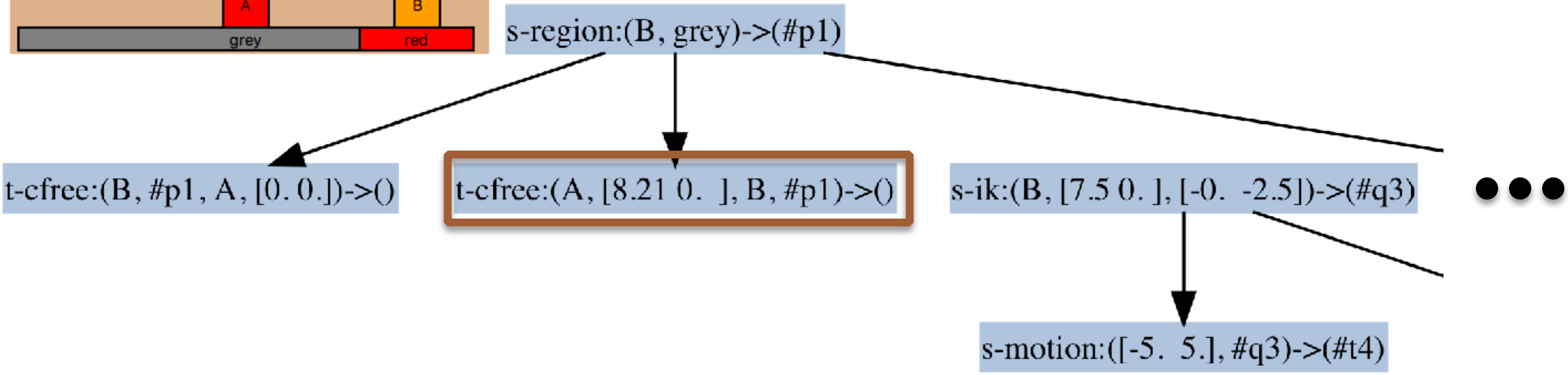
1. **s-region:**(A, red)->[([8.21 0.])]
2. **t-cfree:**(A, [8.21 0.], B, [7.5 0.])=**False**

These stream instances are **removed** from subsequent searches

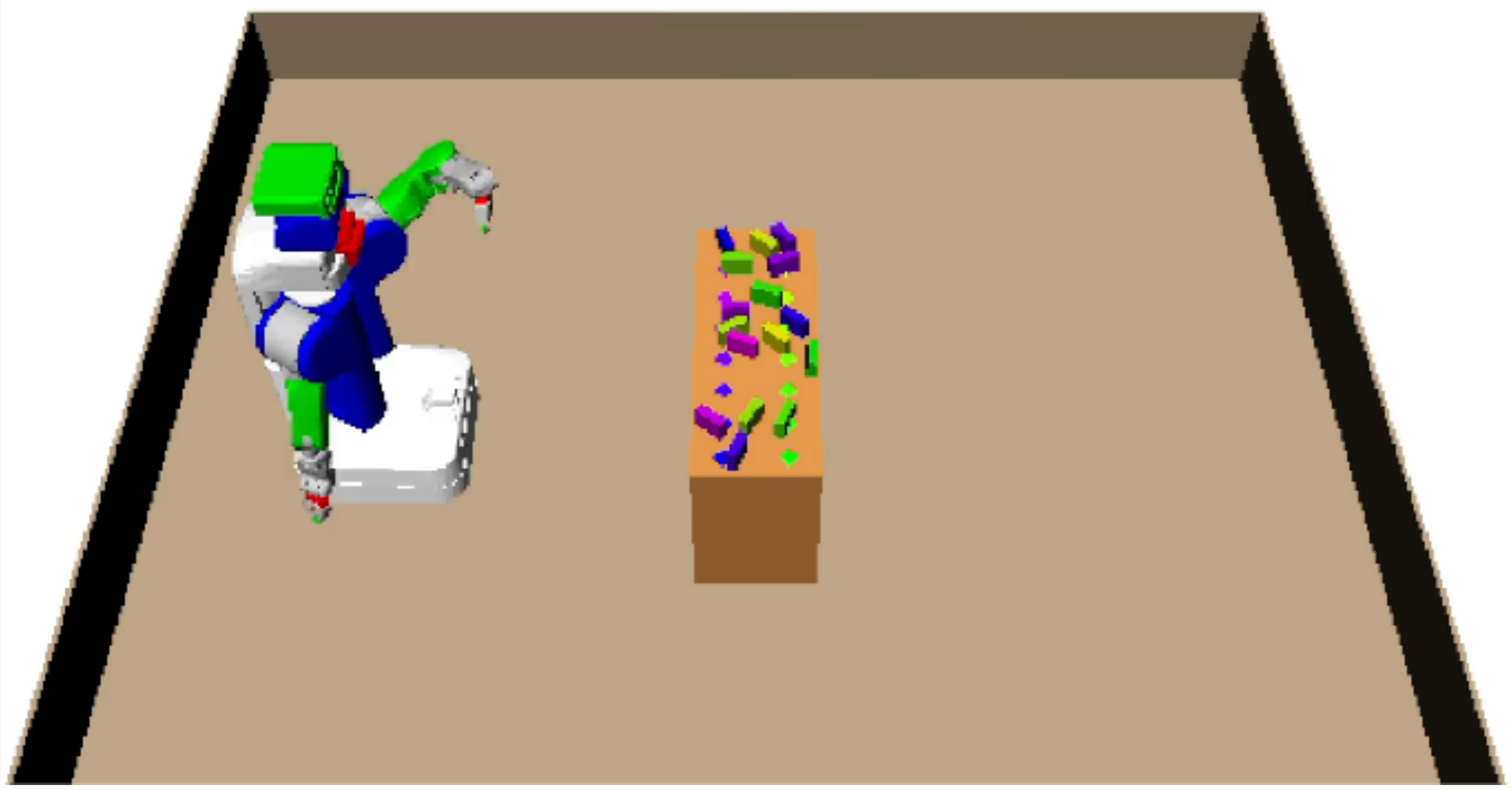
Focused Example: Iteration 2

Optimistic Plan:
move([-5. 5.], #t4, #q2), **pick**(B, [7.5 0.], [-0. -2.5], #q2), **move**(#q2, #t9, #q3), **place**(B, #p1, [-0. -2.5], #q3), **move**(#q3, #t6, #q0), **pick**(A, [0. 0.], [-0. -2.5], #q0), **move**(#q0, #t8, #q4), **place**(A, [8.21 0.], [-0. -2.5], #q4)

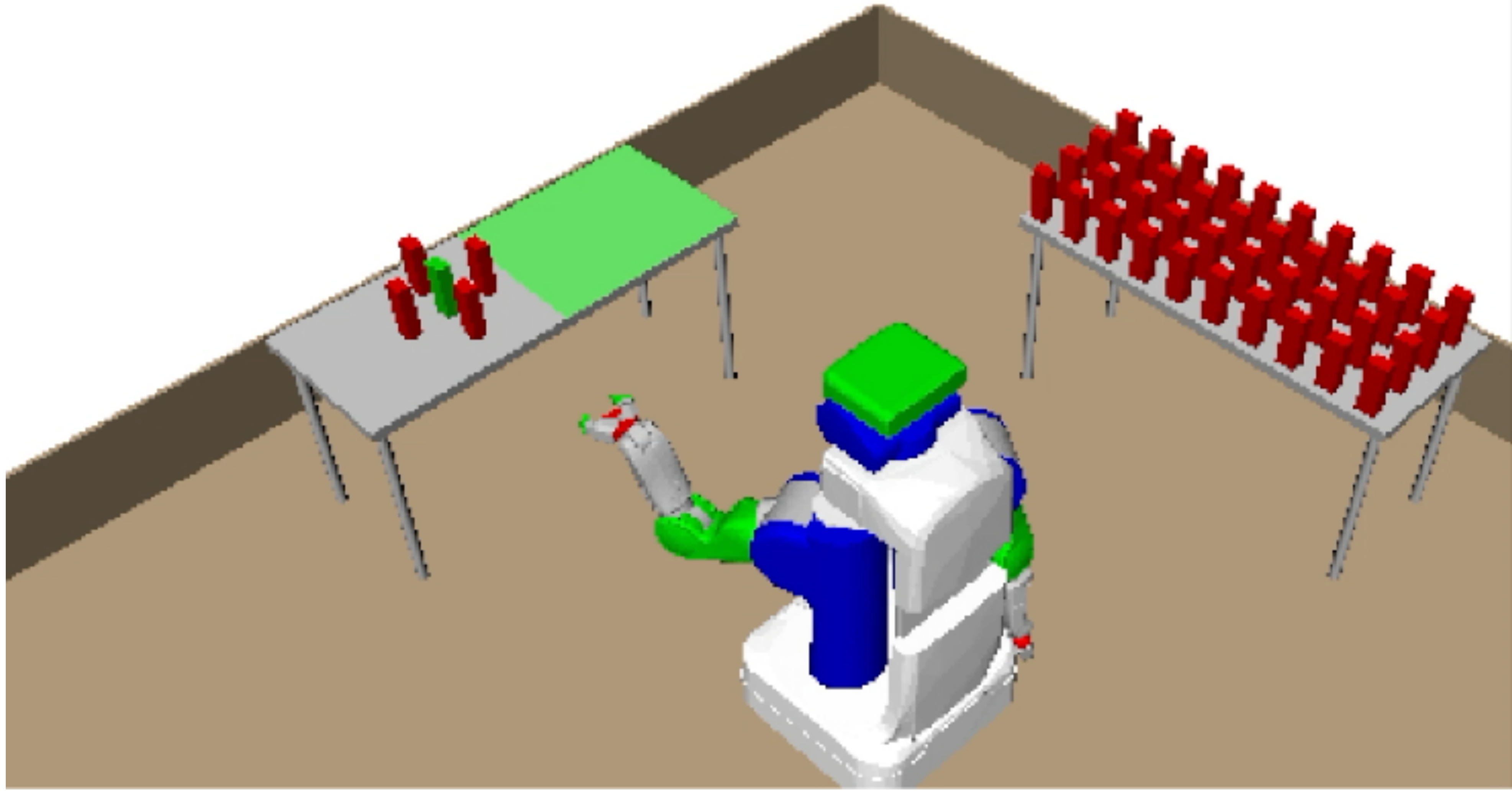
t-cfree:(A, [8.21 0.], B, [7.5 0.]) previously **failed**
t-cfree:(A, [8.21 0.], B, #p1) might **succeed**



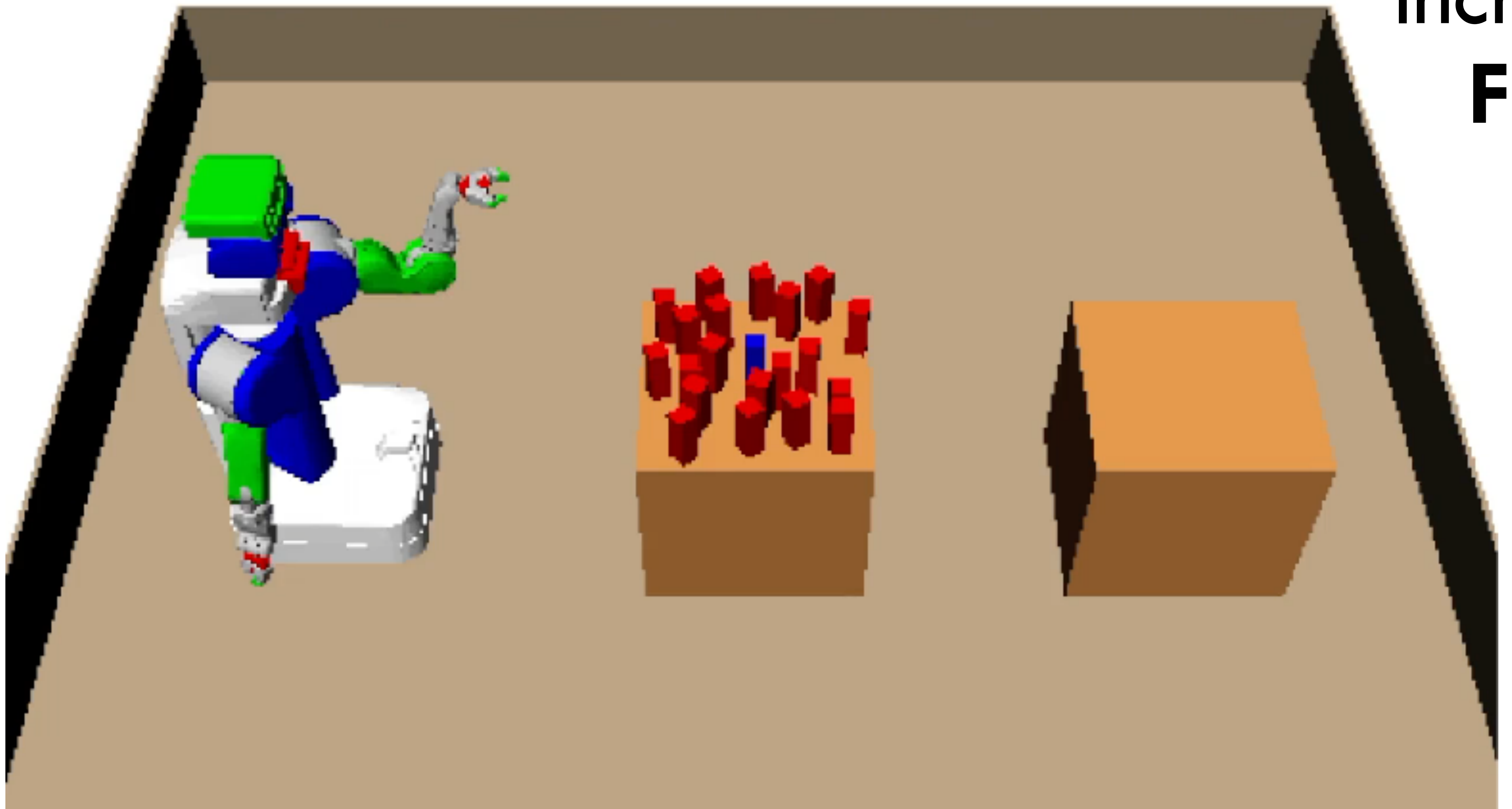
Focused Outperforms Incremental



Incremental ~20 s
Focused ~10 s



Incremental N/A
Focused ~25s



Incremental N/A
Focused ~20s

[Garrett 2018a]

Cost-Minimizing Planning

- Actions costs specified as **nonnegative functions**

```
(:action move
  :parameters (?q1 ?t ?q2)
  :precondition (and (Motion ?q1 ?t ?q2)
                     (AtConf ?q1))
  :effect (and (AtConf ?q2)
               (not (AtConf ?q1)))
               (increase (total-cost) (Length ?t)))
```

```
(:function (Length ?t)
   (Traj ?t))
```

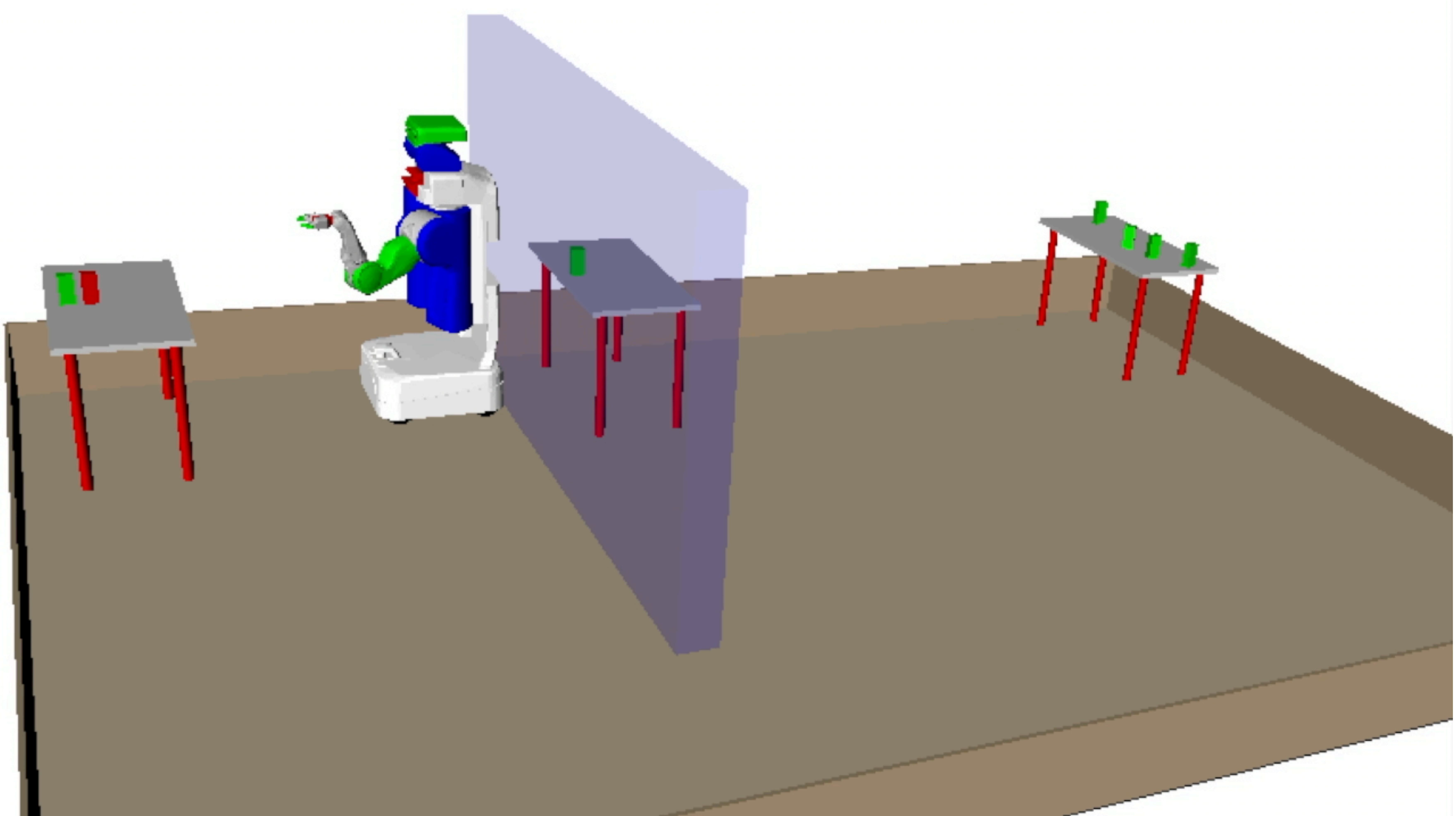
- Function specification similar to derived predicates

```python
def Length(t):
    return sum(np.linalg.norm(q2 - q1)
               for q1, q2 in zip(t[:-1], t[1:]))
```

- **Asymptotically optimal** algorithms

Goal: Hold Any Green Block

- **Lower bounds on costs** improve focused performance

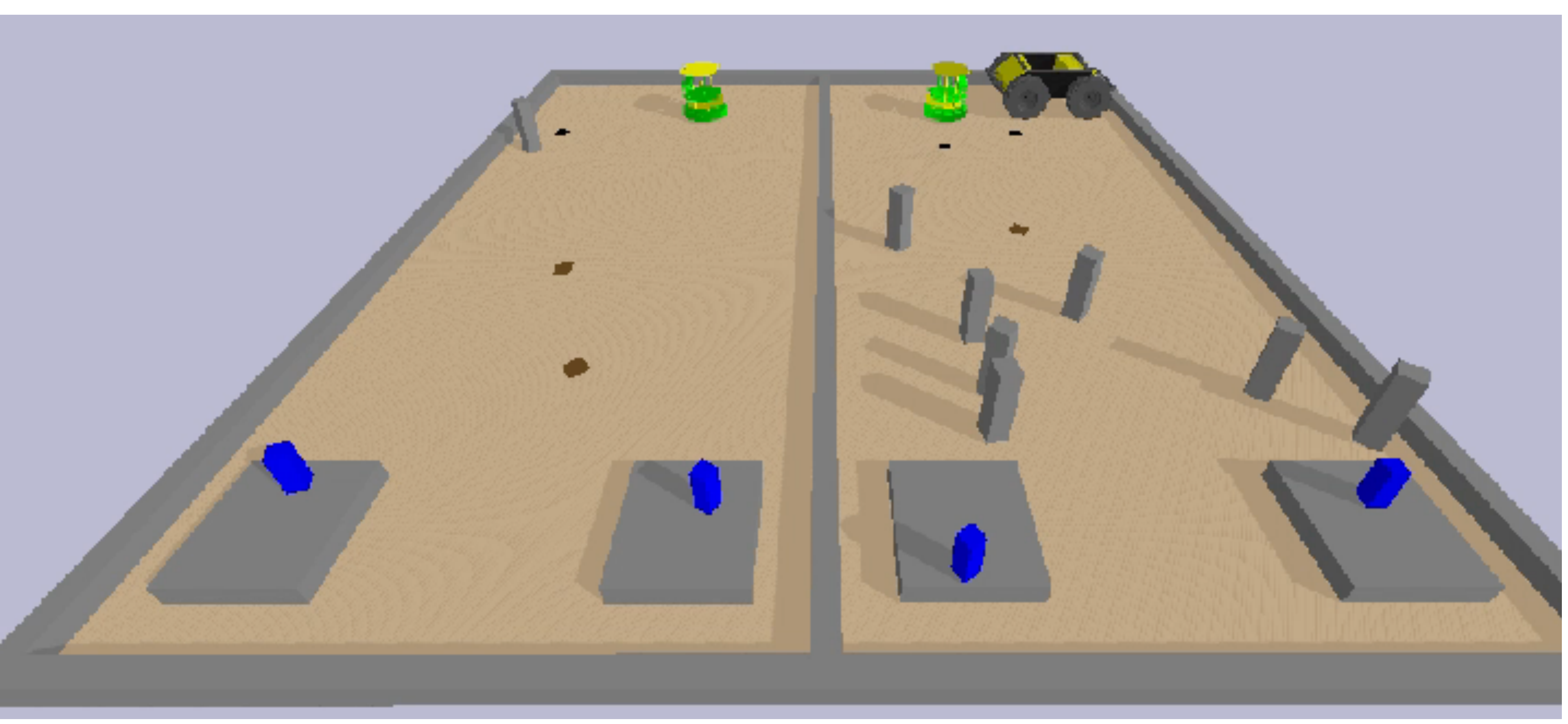


Multi-Robot TAMP

Centralized Scheduling of Robots

- PDDL rovers domain with **visibility** and **reachability**
- How to plan for **simultaneous** execution?
- Use a **temporal planner** as search subroutine (e.g. **Temporal FastDownward**)

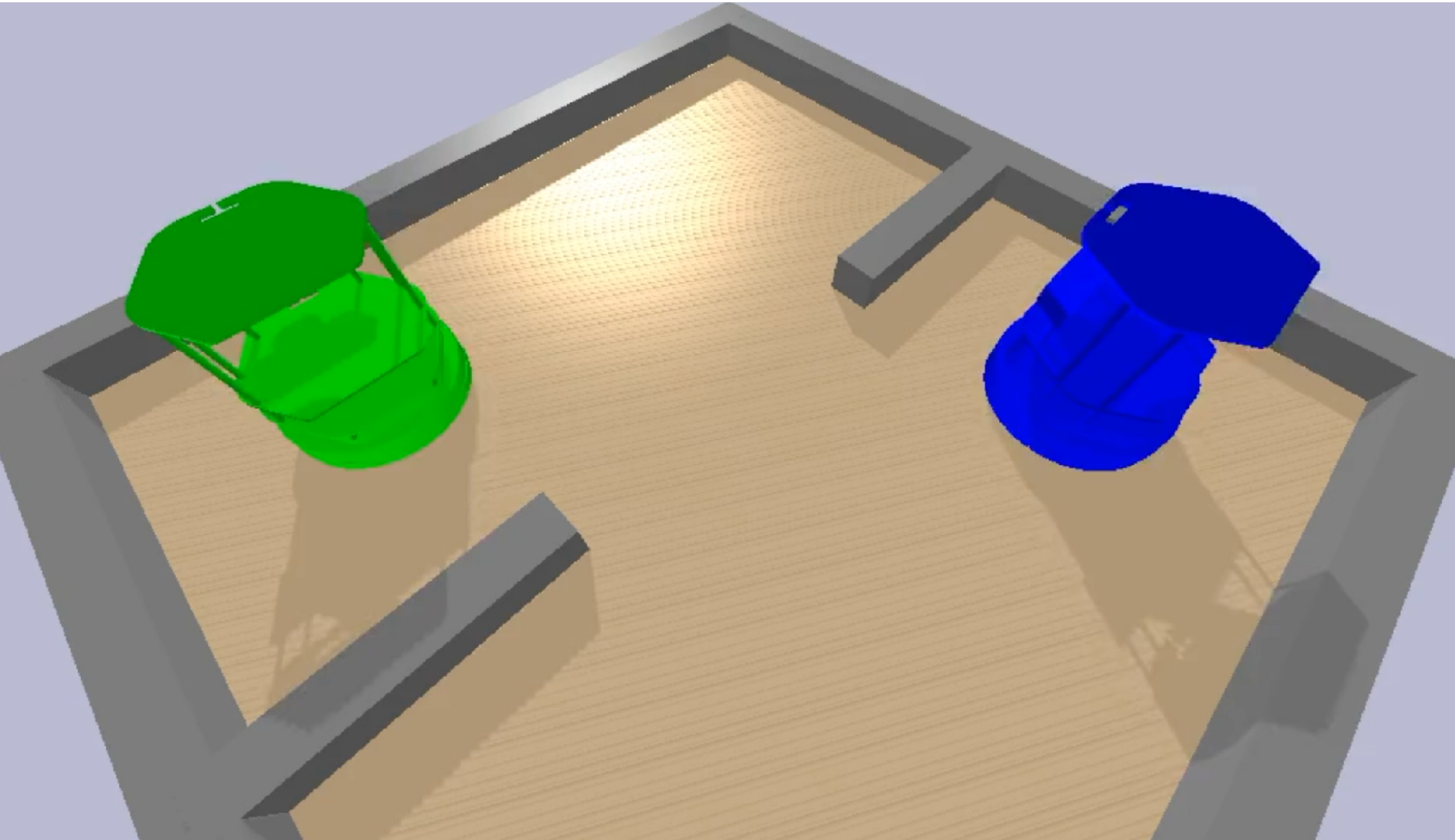
[Eyerich 2009]



BULLET PHYSICS LIBRARY

OpenRAVE

Swap Initial Configurations



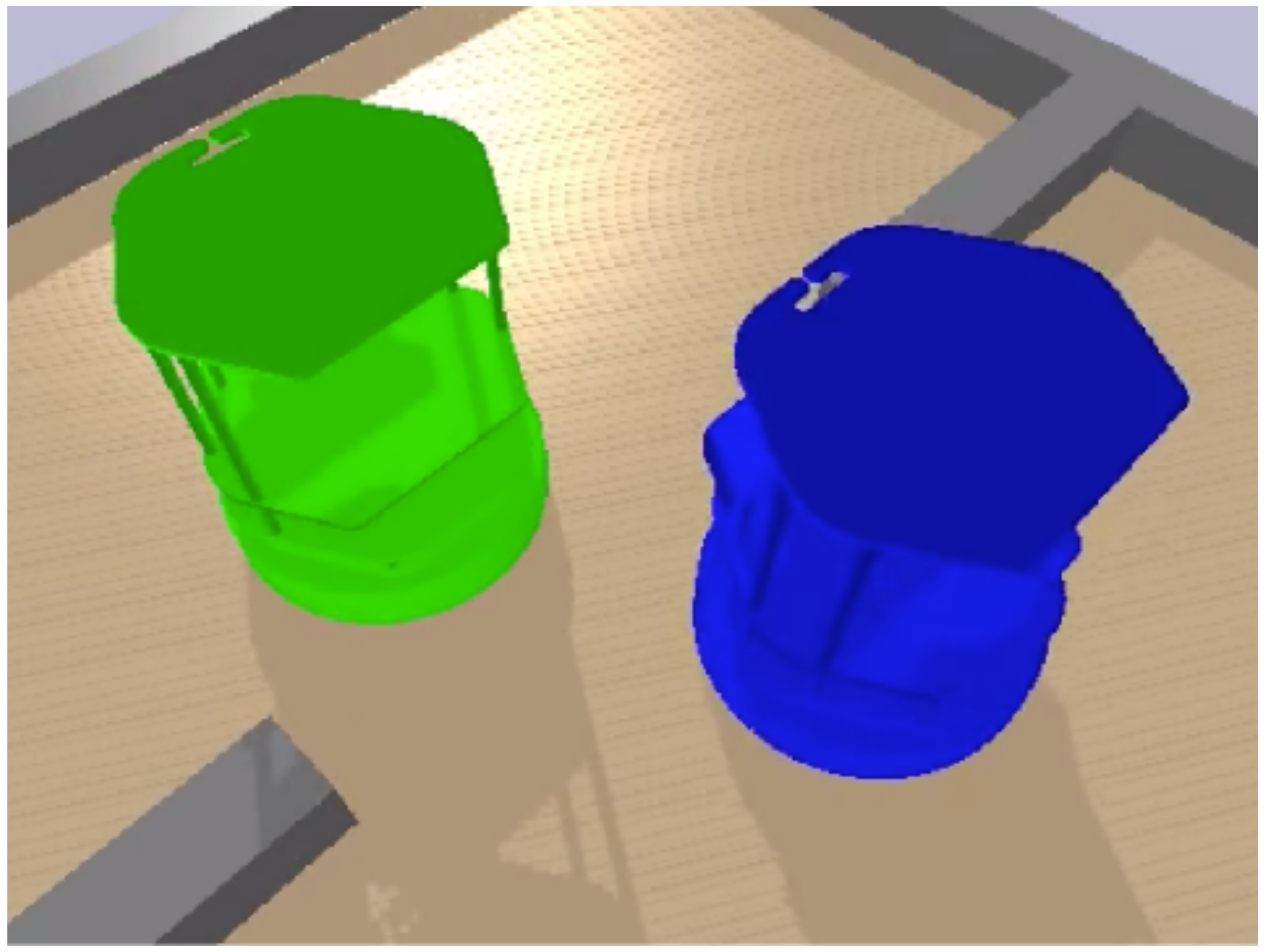
Temporal Task & Motion Planning

- **Temporally annotated** preconditions and effects
  - "at start", "over all", and "at end" (PDDL2.1) [Fox 2003]

```
(:durative-action move
 :parameters (?r ?q1 ?t ?q2)
 :duration (= ?duration (/ (Distance ?t) (Speed ?r)))

:condition (and
   (at start (Robot ?r))
   (at start (Motion ?q1 ?t ?q2))
   (at start (AtConf ?r ?q1))
   (over all (not (UnsafeTraj ?r ?t)))

 :effect (and
   (at start (not (AtConf ?r ?q1)))
   (at start (OnTraj ?r ?t))
   (at end (not (OnTraj ?r ?t)))
   (at end (AtConf ?r ?q2))))
```



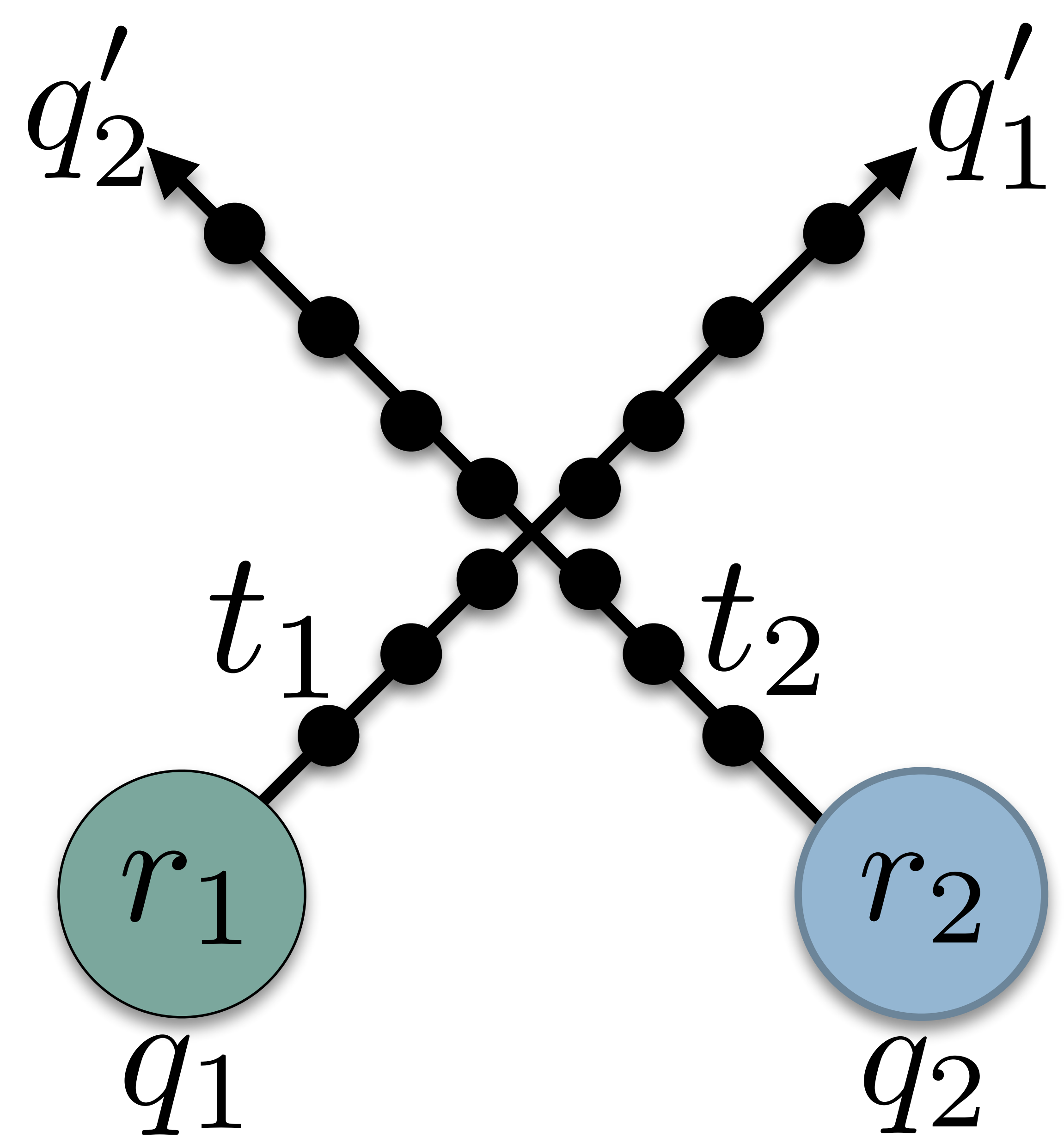
Enforcing Collision Constraints

- Robots might collide **during** the execution of their trajectories
  - Planner doesn't know exact position along trajectory
  - Conservatively, **check all configuration pairs** per segment

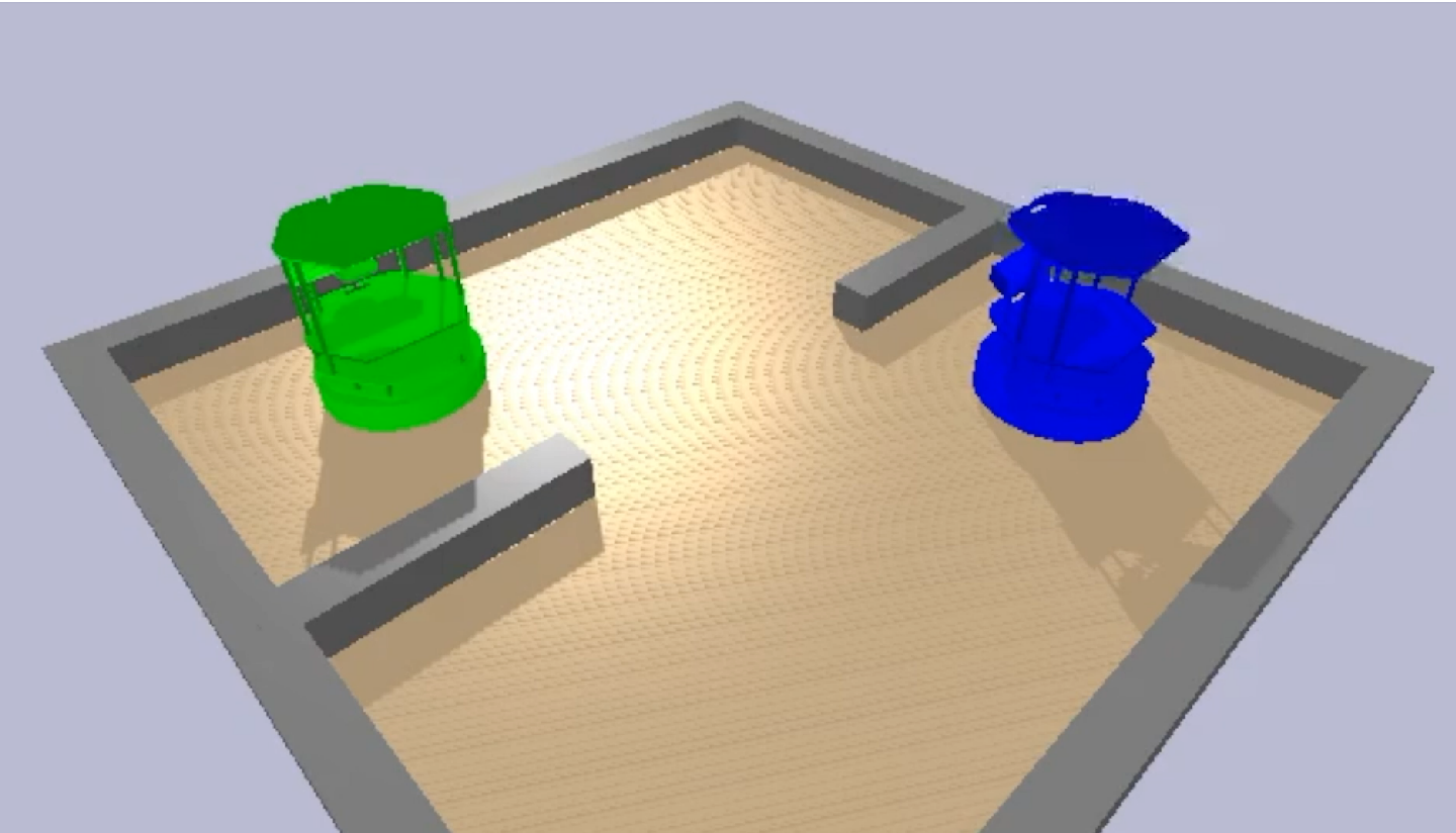
```
(over all (not (UnsafeTraj ?r ?t)))
```

- **Derived predicate** evaluated at each time event

```
(:derived (UnsafeTraj ?r1 ?t1)
  (exists (?r2 ?t2) (and (Robot ?r1) (Robot ?r2)
                         (not (= ?r1 ?r2))
                         (TrajTrajCollision ?t1 ?t2)
                         (OnTraj ?r2 ?t2))))
```



Swap with Rechargeable Battery



Numeric Task & Motion Planning

- Robot movement **depletes battery charge** proportional to distance traversed
- **Infinitely-many** possible move action instances

```
(:durative-action move
 :parameters (?r ?q1 ?t ?q2)
 :duration (= ?duration (/ (Distance ?t) (Speed ?r)))

 :condition (and ...
   (at start (<= (* (ConsumeRate ?r) ?duration)
                    (Energy ?r))))

 :effect (and ...
   (at start (decrease (Energy ?r)
                       (* (ConsumeRate ?r) ?duration))))
```

Numeric Task & Motion Planning

- Robots can recharge battery via **solar power**
- Can perform **3D robotic planning** while benefiting from state-of-the art **numeric heuristics**

```
(:durative-action recharge
 :parameters (?r ?q)
 :duration (= ?duration (/ (- (Capacity ?r) (Energy ?r))
                              (RechargeRate ?r)))

 :condition (...)

 :effect (and ...
   (at end (increase (Energy ?r)
                     (* (RechargeRate ?r) ?duration)))))
```

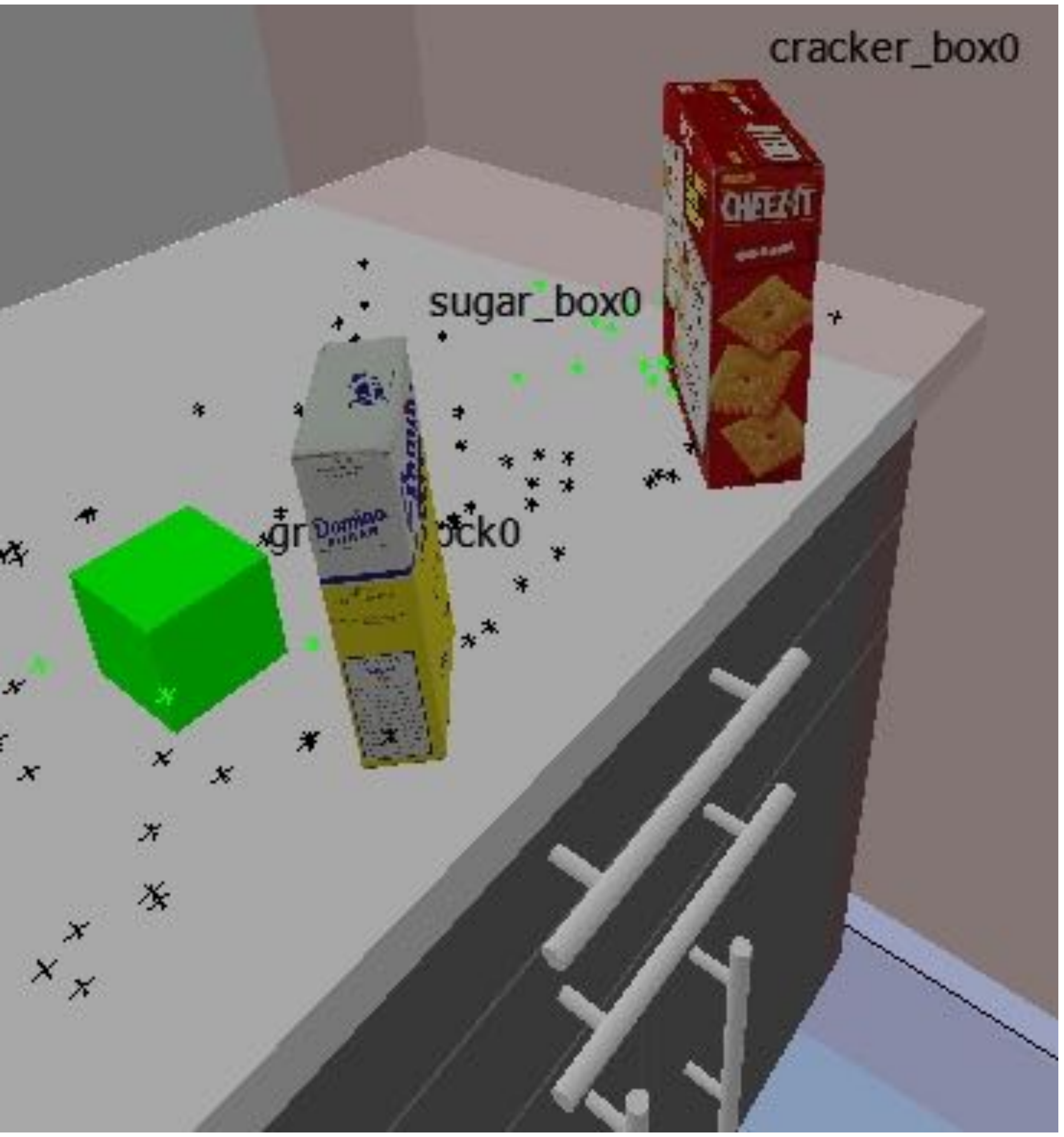
TAMP Under Uncertainty

MDP: Stochastic Action Effects

- Approximate as cost-sensitive **deterministic** problem
- **Policy** computed online via **replanning**

POMDP: Partially-Observable State

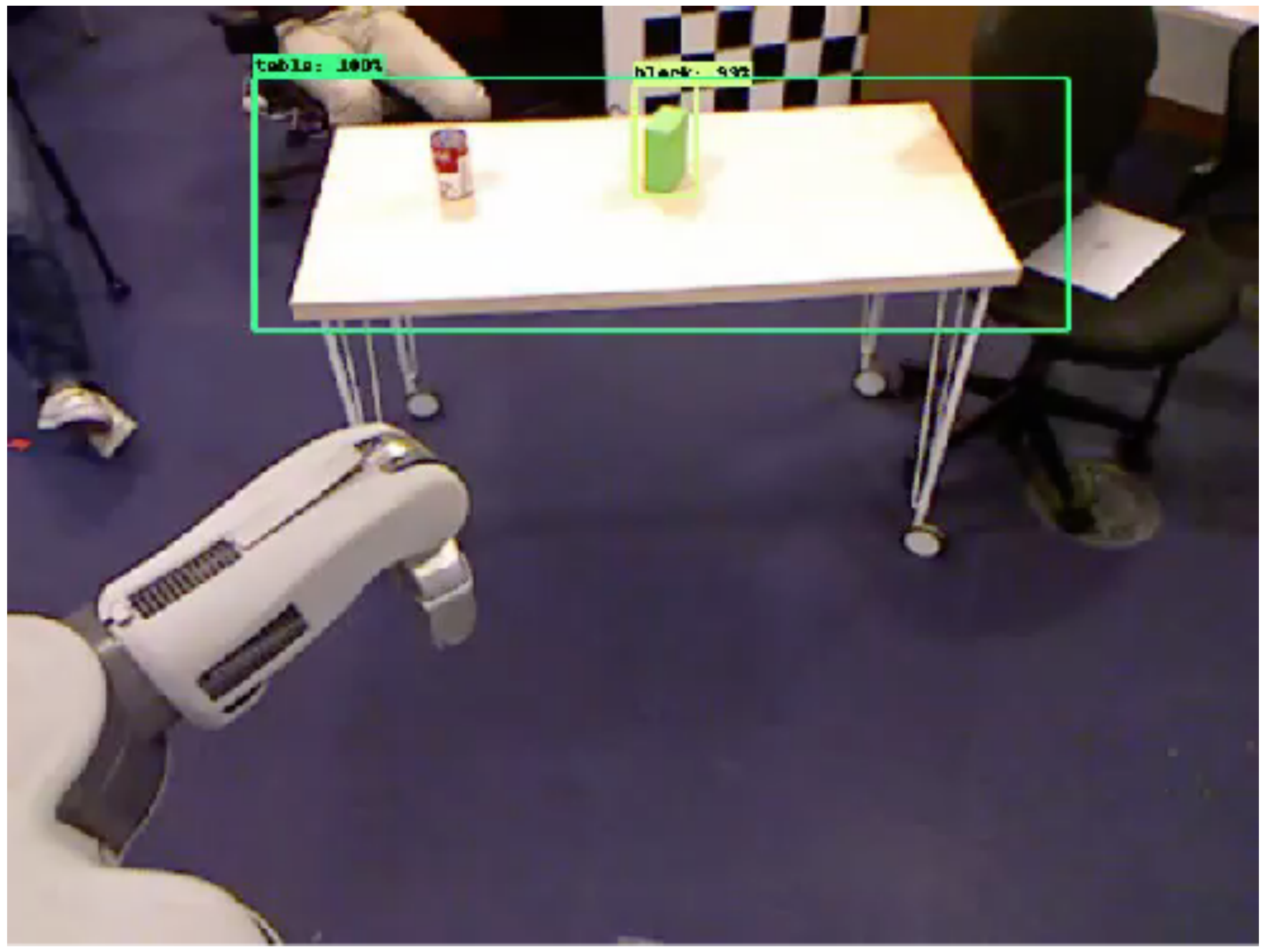
- Update a **belief** (probability distribution) over states
- Plan in the **space of beliefs** (belief space planning)
  - Intentionally take observation actions

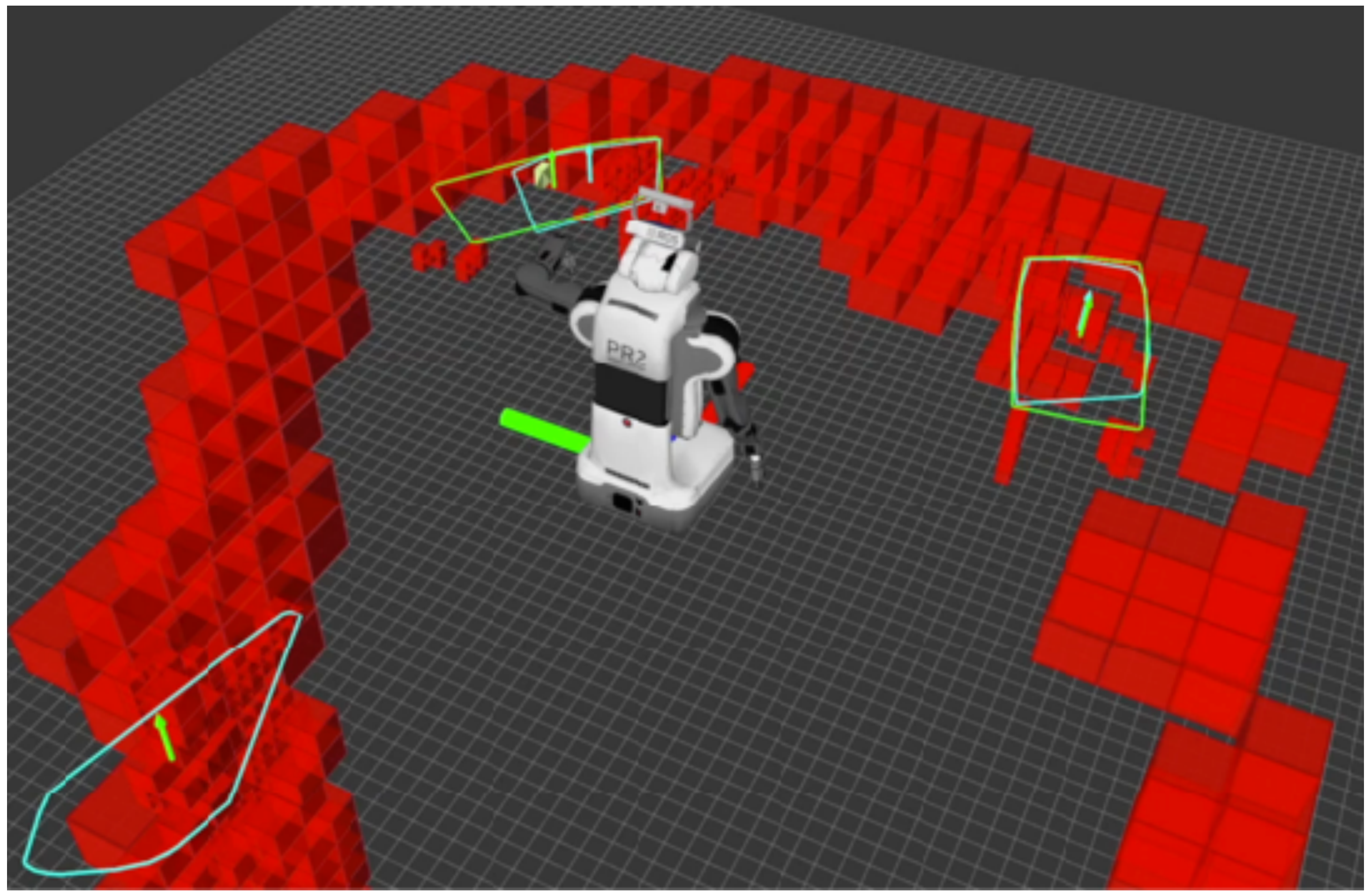


Geometric & Probabilistic Constraints

Belief-Space TAMP System

- Convolutional Neural Network (**CNN**) Object Detector
- Point cloud **plane estimation** to identify surfaces
- Point cloud **pose estimation** for objects
- **Occupancy grid** for non-manipulable
- Plan, execute, & observe in **real time**

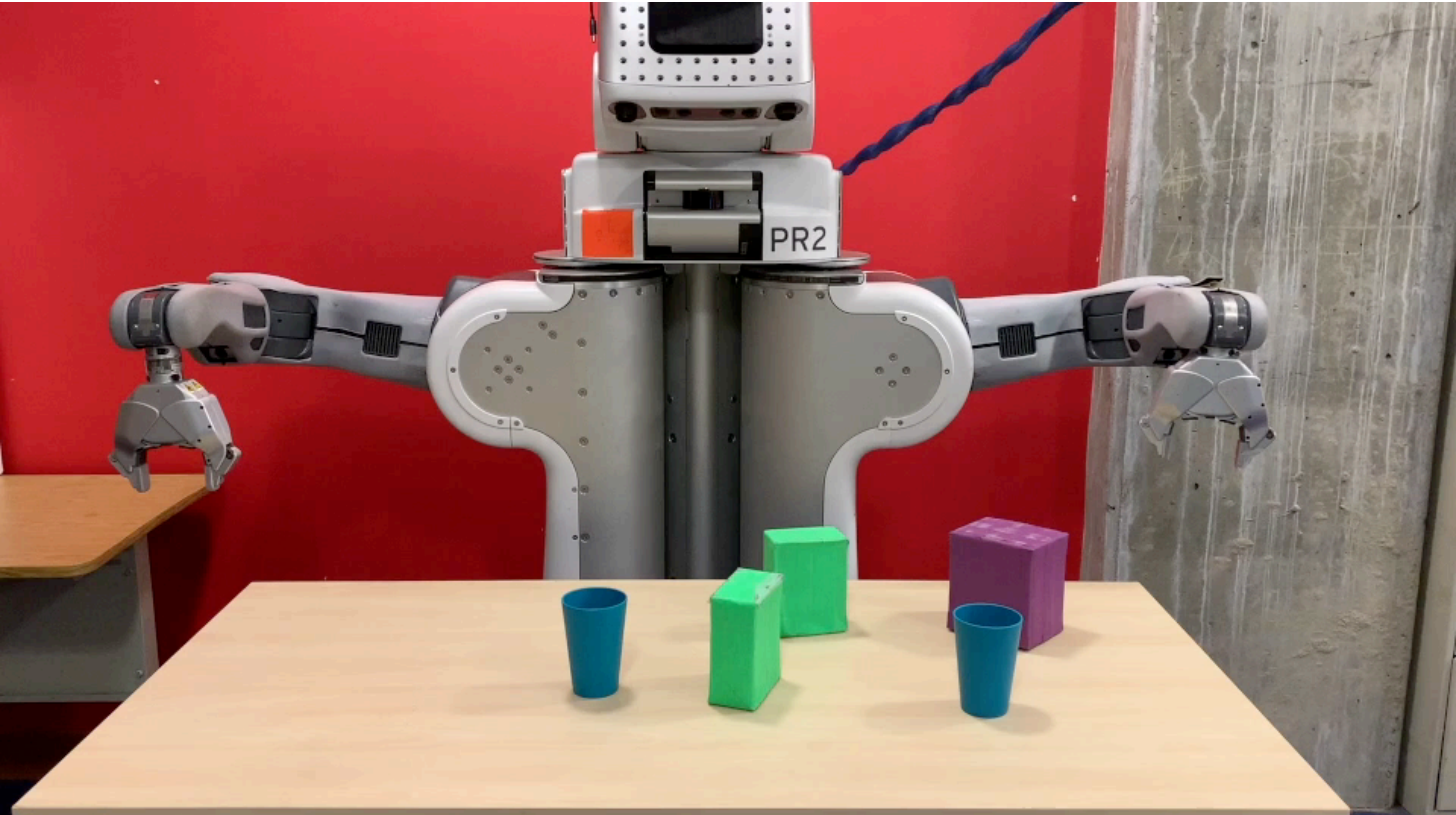




Takeaways

- **Task and Motion Planning (TAMP):** hybrid planning where <u>continuous constraints affect discrete decisions</u>
- **Sampling** is powerful for exploring continuous spaces
- **STRIPStream:** planning language that supports **sampling procedures** as blackbox streams
  - **Domain-independent** algorithms
  - **Lazy/optimistic** planning intelligently queries only a small number of samplers (focused algorithm)
- Ongoing work involving **cost-sensitive, multi-agent, probabilistic & partially observable** TAMP

Questions? (and Outtakes!)



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