

Electrostatics

$$\vec{F} = q\vec{E} \quad (\text{electric force on a particle with charge } q)$$

The electric field at point P due to a small element of charge dq is

$$d\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^2} \hat{r}$$

where \vec{r} ($= r\hat{r}$) is the displacement vector that points from dq to P.

For any closed surface S,

$$\oint_S \vec{E} \cdot d\vec{A} = \frac{1}{\epsilon_0} Q_{\text{enclosed by S}} \quad (\text{Gauss's Law})$$

Known Electric Field Strengths

$$E = \frac{Q}{4\pi\epsilon_0 r^2} \quad (\text{point charge } Q)$$

$$E = \frac{\lambda}{2\pi\epsilon_0 r} \quad (\text{infinite line of uniform charge density } \lambda \text{ C/m})$$

$$E = \frac{\sigma}{2\epsilon_0} \quad (\text{infinite sheet of uniform charge density } \sigma \text{ C/m}^2)$$

Electric Potential

$$U = qV \quad (\text{electrostatic potential energy of a particle with charge } q)$$

$$V_b - V_a = - \int_{\vec{r}_a}^{\vec{r}_b} \vec{E} \cdot d\vec{l} \quad (\text{finding electric potential from electric field})$$

$$\vec{E} = -\nabla V \quad (\text{finding electric field from electric potential})$$

The electrostatic potential at point P due to a small element of charge dq , relative to $V(r = \infty) = 0$, is

$$dV = \frac{1}{4\pi\epsilon_0} \frac{dq}{r}$$

where r is the distance from dq to P.

Capacitance

$$Q = CV \quad (\text{definition of capacitance})$$

$$C = \epsilon_0 \frac{A}{d} \quad (\text{for a vacuum- or air-filled parallel-plate capacitor with area } A \text{ and separation } d)$$

$$U = \frac{1}{2} CV^2 \quad (\text{energy stored in a capacitor})$$

Electric Field Energy

Electric fields store energy with a density (J/m^3) of

$$u = \frac{1}{2}\epsilon_0 E^2$$

Dielectrics

$$E = \frac{E_0}{K} \quad (\text{electric field inside a dielectric material placed in an external field } E_0)$$

$$C = \epsilon \frac{A}{d} = K\epsilon_0 \frac{A}{d} \quad (\text{for a parallel-plate capacitor filled with a dielectric material})$$

Current

$$I = \frac{dq}{dt} = \int \vec{J} \cdot d\vec{A} \quad (\text{definition of current and current density})$$

For any closed surface S,

$$I_{\text{leaving S}} = \oint_S \vec{J} \cdot d\vec{A} = -\frac{d}{dt} Q_{\text{enclosed by S}} \quad (\text{continuity equation})$$

In a non-ideal conductor with conductivity σ (resistivity $\rho = \frac{1}{\sigma}$),

$$\vec{J} = \sigma \vec{E} = \frac{1}{\rho} \vec{E}$$

Resistance

$$V = IR \quad (\text{definition of resistance})$$

$$R = \rho \frac{l}{A} \quad (\text{for a wire with length } l \text{ and cross-sectional area } A)$$

Circuit Elements

Type	Relationship	Series Combination	Parallel Combination
Resistor	$V = IR$	$R_{\text{eq}} = R_1 + R_2$	$\frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2}$
Capacitor	$I = C \frac{dV}{dt}$	$\frac{1}{C_{\text{eq}}} = \frac{1}{C_1} + \frac{1}{C_2}$	$C_{\text{eq}} = C_1 + C_2$

Math Corner

Vector Calculus

$$\vec{\nabla} = \hat{i} \frac{\partial}{\partial x} + \hat{j} \frac{\partial}{\partial y} + \hat{k} \frac{\partial}{\partial z} \quad (\text{the "del" operator})$$

$$\vec{\nabla} f = \hat{i} \frac{\partial f}{\partial x} + \hat{j} \frac{\partial f}{\partial y} + \hat{k} \frac{\partial f}{\partial z} \quad (\text{gradient})$$

Vector Multiplication

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta_{A,B} = AB_{\parallel \text{ to } A} = A_{\parallel \text{ to } B}B$$

$$|\vec{A} \times \vec{B}| = |\vec{A}| |\vec{B}| \sin \theta_{A,B} = AB_{\perp \text{ to } A} = A_{\perp \text{ to } B}B$$

Geometry

A sphere of radius R has volume $\frac{4}{3}\pi R^3$ and surface area $4\pi R^2$.

A cylinder of radius R and height h has volume $\pi R^2 h$ and surface area $2\pi R h + 2\pi R^2$ (the first term is the area around the side, the second term is the area of the top and bottom).

Trigonometry

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\sin(\theta + \phi) = \sin \theta \cos \phi + \cos \theta \sin \phi$$

$$\cos(\theta + \phi) = \cos \theta \cos \phi - \sin \theta \sin \phi$$

$$\sin^2 \theta = \frac{1}{2} - \frac{1}{2} \cos(2\theta)$$

$$\cos^2 \theta = \frac{1}{2} + \frac{1}{2} \cos(2\theta)$$

$$\sin(2\theta) = 2 \sin \theta \cos \theta$$

$$\sin 45^\circ = \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\sin 30^\circ = \cos 60^\circ = \frac{1}{2}$$

$$\sin 60^\circ = \cos 30^\circ = \frac{\sqrt{3}}{2}$$

Quadratic Formula

$$\text{If } ax^2 + bx + c = 0 \text{ then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}.$$