Lateral Nanomechanics of Cartilage Aggrecan Macromolecules

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ABSTRACT To explore the role of the brushlike proteoglycan, aggrecan, in the shear behavior of cartilage tissue, we measured the lateral resistance to deformation of a monolayer of chemically end-attached cartilage aggrecan on a microcontact printed surface in aqueous NaCl solutions via lateral force microscopy. The effects of bath ionic strength (IS, 0.001–1.0 M) and lateral displacement rate (~1–100 μm/s) were studied using probe tips functionalized with neutral hydroxyl-terminated self-assembled alkanethiol monolayers. Probe tips having two different end-radii (R ~ 50 nm and 2.5 μm) enabled access to different length-scales of interactions (nano and micro). The measured lateral force was observed to depend linearly on the applied normal force, and the lateral force to normal force proportionality constant, μ, was calculated. The value μ increased (from 0.03 ± 0.01 to 0.11 ± 0.01) with increasing bath IS (0.001–1.0 M) for experiments using the microsized tip due to the larger compressive strain of aggrecan that resulted from increased IS at constant compressive force. With the nanosized tip, μ also increased with IS but by a smaller amount due to the fewer number of aggrecan involved in shear deformation. The variations in lateral force as a function of applied compressive strain εn and changes in bath IS suggested that both electrostatic and nonelectrostatic interactions contributed significantly to the shear deformational behavior of the aggrecan layers. While lateral force did not vary with lateral displacement rate at low IS, where elasticlike electrostatic interactions between aggrecan dominated, lateral force increased significantly with displacement rate at physiological and higher IS, suggestive of additional viscoelastic and/or poroelastic interactions within the aggrecan layer. These data provide insights into molecular-level deformation of aggrecan macromolecules that are important to the understanding of cartilage behavior.

INTRODUCTION

Articular cartilage is a specialized connective tissue found at the surfaces of bones in synovial joints. Cartilage macromolecular composition and structure (1) is optimized to sustain a complex combination of compressive, shear, and tensile loads that exist during joint motion (2,3). The major extracellular matrix proteoglycan, aggrecan, which comprises 30–35% of the tissue dry weight, is thought to play a critical role in proper biomechanical functioning of cartilage in response to compressive (4) and shear (5) loads. Aggrecan is a polyelectrolyte having a bottle-brush structure (Fig. 1), consisting of a core protein (contour length ~400 nm) with ~100 covalently bound chondroitin sulfate glycosaminoglycan (CS-GAG) chains (contour length ~40 nm) that are closely spaced (2–4 nm) and negatively charged, along with smaller keratan sulfate GAGs and oligosaccharides (6,7). Within cartilage tissue, aggrecan is bound noncovalently at its G1 globular domain to the higher molecular weight GAG chain, hyaluronan (HA), stabilized by link protein (8).

Nanomechanical studies of cartilage and its extracellular matrix components have shown the potential to link molecular structure and interactions to tissue-level biomechanical properties. Recently, we reported the use of atomic force microscope (AFM)-based instruments to quantify the compressive nanoscale deformation between opposing chemically endgrafted monolayers of CS-GAGs (9,10) and aggrecan (11,12).

These biomimetic model systems demonstrated highly nonlinear nanomechanical behavior, with the aggrecan layer stiffness increasing more rapidly with strain than that of CS-GAG layer. The contribution of electrostatic interactions to the compressive stiffness of the CS-GAG (10) and aggrecan (12) layers was well described by a Poisson-Boltzmann-based model representing GAG chains as finite length charged rods (13). In other related studies, nanoindentation of intact porcine cartilage was performed using microsized colloidal probe tips to measure the tissue’s aggregate dynamic compressive modulus (~2.6 MPa), while the use of sharp pyramidal nanosized probe tips gave values ~100-fold lower (~0.02 MPa) and were thought to be more indicative of molecular fine structure (14,15). Nanoindentation was also used to detect changes in tissue-level properties after enzymatic digestion of collagen and proteoglycan moieties (14), during the process of osteoarthritis degradation (16), and cartilage tissue repair (14,15). Single molecule force-extension measurements on HA (17,18) and CS-GAG (18) have been performed using optical tweezers (17) and AFM (18), respectively, giving estimates of the persistence length in near-physiological aqueous solution conditions. With the goal of providing insights into joint lubrication mechanisms (19), the frictional properties of HA have been quantified using the surface force apparatus (SFA) via covalent attachment of HA to lipid bilayers on mica (20) and electrostatic adsorption of HA on quaternized poly(4-vinylpyridine) (21) or lipid bilayers (22) on mica. AFM using microscale probe tips has also been used to measure the frictional coefficient of the surface of bovine...
articular cartilage in the presence and absence of the superficial zone (23), and found that it was similar to macroscale results (23,24).

While the compressive and tensile stiffness of cartilage extracellular matrix constituents have been studied at the molecular level, the molecular contributions to cartilage shear properties have received less attention. It is recognized from tissue-level biomechanical studies that aggrecan and GAG intermolecular interactions play an important role in resisting shear deformation of cartilage (5,25,26), given the high density of aggrecan within the tissue (20–80 mg/mL (27)). In addition, the known ionic strength dependence of the torsional shear modulus of cartilage disks was well predicted by a Poisson-Boltzmann-based unit cell model of GAG-GAG electrostatic interactions (5). Hence, the objective of this study was to quantify the nanoscale lateral deformation behavior of chemically end-grafted aggrecan monolayers to better understand the origins of tissue-level shear behavior (as opposed to surface lubrication).

Toward this end, lateral force microscopy (LFM) was carried out on microcontact printed planar substrates (28) of chemically end-grafted fetal bovine cartilage aggrecan prepared at high physiological densities with surface molecular separation distances ~25 nm (12). Nanosized (end-radius, \( R \approx 50 \) nm) and microsized (\( R \approx 2.5 \mu m \)) probe tips functionalized with neutral hydroxyl-terminated self-assembled monolayers (OH-SAMs) were employed to study lateral nanomechanics at different length scales where the interactions involved either a few or a large ensemble (~10^3) of aggrecan molecules (12). Lateral force was measured as a function of normal compressive force (0–80 nN), enabling the determination of the lateral proportionality constant, \( m \), in NaCl solutions of varied ionic strength (0.001–1.0 M, pH ~5.6). The use of microcontact printed surfaces enabled the simultaneous measurement of aggrecan height (and hence, conformation and compressive normal strain) with lateral and normal force. Results using probe tips having differing surface chemistries suggested that the contribution of interfacial adhesion between the aggrecan layer and probe tip to the measured lateral force were very small compared to the effects of aggrecan deformation. To help isolate the effects of electrostatic and nonelectrostatic interactions on the resistance of aggrecan to lateral deformation, lateral forces were measured as a function of aggrecan height at different bath ionic strengths. Height was then converted to effective normal strain, \( e_n \), and the measured lateral force was estimated as a function of the ratio of the average GAG-GAG spacing to the characteristic electrical Debye length at each ionic strength. (Electrostatic interactions become relatively more important as this ratio becomes smaller.) The underlying time-independent (elasticlike) and time-dependent (e.g., visco/poroelastic) deformation mechanisms were also explored by comparing the lateral forces measured at different probe tip displacement rates.

**METHODS**

**Sample and probe tip preparation and characterization**

Purified fetal bovine epiphyseal A1A1D1D1 aggrecan, MW ~3 MDa (7) was chemically functionalized with thiol-groups, as described previously (11). Microcontact printed (28) samples were prepared where aggrecan was chemically end-grafted within hexagonal patterns (10-μm side length), and a hydroxyl-terminated self-assembled monolayer (OH-SAM, 11-mercaptoundecanol, HS(CH\(_2\)\(_n\))\(_{11}\)OH, Aldrich, St. Louis, MO), was functionalized outside the hexagonal patterns, as described previously (11). The aggrecan packing density was one monomer per ~25 nm \(^2\) (measured using the dimethylmethylene blue dye binding assay (29)). Samples were characterized using contact mode AFM imaging in NaCl solutions at different ionic strengths to visualize the height differences between the aggrecan-OH-SAM pattern using both the OH-SAM functionalized nanosized and microsized probe tips (11,12). Patterned control substrates of carboxyl- and amine-terminated SAMs (COOH-SAM and NH\(_2\)-SAM) were prepared in a similar
fashion via microcontact printing using 3 mM 11-mercaptoundecanoic acid, HS(CH$_2$)$_{10}$COOH (Aldrich), and 2-aminoethanethiol hydrochloride, HS(CH$_2$)$_2$NH$_2$HCl (Aldrich, 24 h incubation), both in ethanol. These control samples were imaged by lateral force microscopy in 0.01 M NaCl at pH 4.7 and 10.3 (pH values were adjusted using HCl and NaOH) to measure the lateral forces between the probe tip and the samples (for reviews of measuring friction forces on SAMs via LFM, see (30–33)).

Both standard nanosized AFM probe tips ($R \sim 50$ nm as measured by scanning electron microscopy, NP tip D, silicon nitride, V-shaped cantilever, nominal spring constant $k \sim 0.06$ N/m, Veeco, Santa Barbara, CA) and nanosized colloidal probe tips ($R \sim 2.5$ $\mu$m, silicon nitride, V-shaped cantilever, nominal spring constant $k \sim 0.12$ N/m, Bioforce Nanosciences, Ames, IA) were used. Both were coated with 2 nm of Cr and 50 nm of Au, and then functionalized with neutral OH-SAMs by immersion for 24 h in 3 mM HS(CH$_2$)$_2$OH ethanol solution, to minimize the electrostatic and hydrophobic interactions between the tip and aggrecan layer. A hydrophobic methyl-functionalized microsized probe tip was also prepared by immersion for 24 h in 3mM ethanethiol, HSCH$_2$CH$_3$ (Aldrich), ethanol solution. Based on the surface interaction area calculated from the measured probe tip radii and the known aggrecan packing density, the nanosized tips (Fig. 2a) were estimated to interact directly with $<10$ aggrecan on the surface, while the microsized tips (Fig. 2b) interacted with $\sim 10^3$ aggrecan (12).

Shear nanomechanics of aggrecan via lateral force microscopy

A Multimode Nanoscope IV AFM (Veeco) was used with a PicoForce piezo for the lateral force microscopy experiments. The scan direction was parallel to the base of the V-shaped cantilever, i.e., a 90° scan angle. As the cantilever scans across the surface under a constant applied normal force (Fig. 2c), it twists in the scanning (lateral) direction, resulting in a horizontal deflection of the laser spot on a quadrant position-sensitive photodiode that outputs a lateral deflection signal (Volts). Simultaneously, the cantilever bends in the normal direction and results in a separate output as the normal deflection signal (Volts) on the same photodiode. The normal deflection signal is of a greater magnitude and the cross talk, or interference of the normal to the lateral signal, is typically an order-of-magnitude larger than the actual lateral deflection signal caused by the cantilever twisting (34). To account for this, both forward (trace) and reverse (retrace) line scans (lateral signal loops) were performed. The magnitude of the lateral force was calculated from the average of the lateral deflection signal (i.e., one-half the trace minus retrace signal, or half-width, Fig. 2c). Calibration of the lateral sensitivity $\alpha$ (nN/V) was conducted using an extension of the "wedge method" (34,35), thus enabling quantification of the lateral force in nN (see Appendix). The normal deflection sensitivity $\beta$ (nN/V) was determined by calibrating the normal cantilever spring constant via the thermal oscillation method (36).

Based on these methods, lateral force scans were measured at eight locations on each hexagon as a function of the applied normal force, probe tip displacement rate, and bath ionic strength ($0.001$–$1.0$ M NaCl solutions, pH $\sim 5.6$). The proportionality coefficient between lateral force and applied normal force, $\mu$, which characterizes the resistance of the aggrecan layer to lateral deformation at given applied normal forces, was estimated via linear regression on the data pooled from all eight scan lines at any given ionic strength (IS) or pH, suggesting that the properties of the aggrecan across the hexagon were relatively homogeneous.

During lateral force microscopy scans, the height difference between the aggrecan and OH-SAM regions was recorded simultaneously (Fig. 2, a and b), which equals the aggrecan layer height as the height of OH-SAM layer is negligibly small ($\sim 2$ nm) (11). Hence, simultaneous assessment of aggrecan height (and hence, conformation and compressive normal strain) with lateral and normal force was obtained, as previously described (11,12). Lateral force was plotted versus aggrecan height and compressive normal strain, $\epsilon_n$, which was calculated as the aggrecan height normalized by the equilibrium aggrecan height at 0 applied normal force (12). A 30-$\mu$m scan size and 1-Hz scan frequency were employed at a lateral scan rate 60 $\mu$m/s. In an additional series of experiments, a range of lateral scan rates from
increased to 0.03 at 0.001, 0.01, and 0.1 M IS, respectively. The SAM \( \frac{1}{2} \cdot \) was found to be 2 \( \cdot \) \( \cdot \) 0.02 to 0.03 and \( \cdot \) \( \cdot \) \( \cdot \) \( \cdot \) \( \cdot \) \( \cdot \) 2 \( \cdot \) \( \cdot \) 0.02, as the pH was decreased from 10.3 to 2.4 (Fig. 4). Control experiments—friction between nanosized OH-SAM probe tip versus COOH-NH\(_2\) SAM microcontact printed surface

A hexagonal microcontact printed COOH- and NH\(_2\)-SAM functionalized substrate (where the COOH-SAM was outside and the NH\(_2\)-SAM was inside the hexagons) was imaged with an OH-SAM nanosized probe tip in 0.01 M NaCl at pH \( \sim 10.3 \) and 2.4, with an applied normal force \( \sim 5 \text{ nN} \). Thirty-micrometer lateral force-scan images (Fig. 3) were constructed from the half-width of the lateral signal loop (Fig. 2 c). At pH \( \sim 10.3 \), the negatively charged COO\(^-\)SAM exhibited a higher lateral force than the NH\(_2\)-SAM, corresponding to the brighter area outside of the hexagon in Fig. 3 a, and the larger half-width in the lateral signal loop (Fig. 2 c) compared to that of the NH\(_2\)-SAM. The COO\(^-\)SAM also exhibited larger lateral signal fluctuations due to stick-slip phenomena (Fig. 2 c) (37). In contrast, the NH\(_2\)-SAM showed higher lateral force at pH \( \sim 2.4 \) (Fig. 3 b). Lateral forces showed a positive linear dependence with increasing normal force for both the NH\(_2\)-SAM and COOH-SAM versus the OH-SAM functionalized probe tip at pH \( \sim 10.3 \) and 2.4 (Fig. 4). The lateral proportionality coefficient, \( \mu \), between carboxyl and hydroxyl, markedly decreased from 0.67 \( \pm \) 0.03 to 0.23 \( \pm \) 0.02, while that between amino and hydroxyl increased from 0.32 \( \pm \) 0.02 to 0.47 \( \pm \) 0.02, as the pH was decreased from 10.3 to 2.4 (Fig. 4). Visualization of the pattern reversal at different pH (Fig. 3) and the linear dependence of lateral on applied normal force (Fig. 4) verified the lateral force microscopy methodology by reproducing results reported previously in the literature (38).

RESULTS

Aggrecan shear using a nanosized probe tip

Lateral force images for a microcontact printed surface of chemically end-grafted aggrecan (inside the hexagon) and an OH-SAM (outside the hexagon) were taken with a nanosized OH-SAM functionalized probe tip in 0.1 M NaCl at pH \( \sim 5.6 \) (Fig. 5 a). Lateral force data from this experiment were obtained at low \( (\sim 3 \text{ nN}) \) and high \( (\sim 15 \text{ nN}) \) normal imaging forces, as seen in two typical signal loops of Fig. 5 b, with a 30-\( \mu \text{m} \) line scan. The half-width of the lateral signal and, hence, the magnitude of the lateral resistance, was much smaller for the aggrecan compared to the OH-SAM at the low applied normal force (Fig. 5 a), and increased with increasing normal force (Fig. 6) (34). (Note that a shift in the baseline of the lateral signal loop was observed at the edge of the hexagonal pattern due to the increase in aggrecan height, but this did not affect the magnitude of the measured lateral force given the linear response of the position-sensitive photo diode. This cross talk came from the interference of cantilever normal deformation with the lateral deflection signal, which was deconvoluted by analyzing the trace-retrace scan loop, as mentioned in Methods.)

Fig. 6 illustrates the dependence of lateral force on normal force for this same sample; each data point represents eight line-scans at different sample locations for a 30-\( \mu \text{m} \) scan size. Data in the OH-SAM region (Fig. 6 a) yielded a linear dependence of lateral force on normal force with \( \mu = 0.16 \pm 0.01 \), which was independent of ionic strength in the range of 0.001–0.1 M, as expected for neutral SAMs. For the aggrecan-functionalized region, two linear regimes were observed: one at lower forces (region I) and one at higher forces (region II, Fig. 6, b and c). In region I, \( \mu \) was found to be \( \mu_1 = 0.10 \pm 0.01 \) at 0.001 and 0.1 M IS and \( \mu_1 = 0.15 \pm 0.04 \) at 0.1 M IS. In region II, \( \mu \) increased to \( \mu_2 = 0.44 \pm 0.03, 0.35 \pm 0.03 \) and 0.37 \( \pm \) 0.03 at 0.001, 0.01, and 0.1 M IS, respectively. The applied normal force at which this transition occurred was found to decrease with increasing ionic strength (e.g., Fig. 6, b and c). It should be noted that scanning under high force in region II produced damage to the aggrecan layer causing irreversible changes in the measured height and lateral force. Lateral force also depended markedly on aggrecan height (Fig. 7). In the low force region of constant lateral linearity (region I), the aggrecan layer was not fully compressed (Fig. 7 a);
in the higher force region II, the aggrecan layer was compressed to <5 nm. The lateral force in both regimes depended on ionic strength (Fig. 7b): at any given aggrecan layer height, the lateral force increased with decreasing ionic strength.

**Aggrecan shear using a microsized probe tip**

Lateral forces between aggrecan and an OH-SAM microsized probe tip ($R \approx 2.5 \mu m$) were measured over a range of applied normal force between 0 and 80 nN. It is known that in this force range, the aggrecan layer is never fully compressed (12). Lateral force was observed to vary linearly with normal force throughout the entire range of applied normal force (Fig. 8). The value $\mu$ was found to be independent of loading history for several loading and unloading cycles in the range of applied normal force (data not shown), indicating a lack of damage to the aggrecan layer during scanning. A marked increase of $\mu$ with increasing ionic strength was observed at higher normal forces.
strength was observed, ranging from $\mu = 0.03 \pm 0.01$ at 0.001 M to $0.11 \pm 0.01$ at 1.0 M (Fig. 8). The same sample was tested using the $\text{CH}_3$-SAM tip at 0.1 M and 1.0 M, and no significant differences in the values of $\mu$ were observed compared to the OH-SAM tip (data not shown). As shown in Fig. 9a, the initial aggrecan layer height was greater at lower ionic strength; at any measured height, the lateral force was larger at lower ionic strength. When these same data were plotted as a function of compressive strain $e_n$ (aggrecan height normalized to initial height at $0$ normal force), the lateral force was found to decrease with increasing ionic strength at constant strain (Fig. 9b). To aid in the interpretation of these results (see Discussion), the lateral force data of Fig. 9b were replotted versus the estimated ratio of the GAG spacing divided by Debye length, the characteristic electrostatic interaction length, at different ionic strengths, to distinguish between electrostatic and nonelectrostatic interactions (Fig. 9c). The estimated average GAG spacing corresponding to varying amounts of aggrecan compression was calculated as

$$\text{GAG spacing under compression} = \frac{\text{GAG spacing along core protein} \times \text{measured aggrecan height}}{\text{aggrecan contour length}},$$

where the GAG spacing along core protein is $3.2 \pm 0.8$ nm, and the contour length is $398 \pm 57$ nm for fetal epiphyseal aggrecan, as measured via tapping mode AFM imaging (7). The value of GAG spacing under compression divided by Debye length is $<1$ at lower IS (0.001 and 0.01 M) and $>1$ at higher IS (0.1 and 1.0 M) in the range of measured lateral forces.

![FIGURE 6 Lateral force versus applied normal load for an aggrecan-OH SAM patterned surface with an OH-SAM functionalized nanosized probe tip ($R \sim 50$ nm) in NaCl solutions, pH $\sim 5.6$. (a) OH versus OH. (b) OH versus aggrecan under lower normal force region, corresponding to region (I) of Fig. 6a. (c) OH versus aggrecan under higher normal force region, corresponding to region (II). At 0.01 M, lateral linearity ratio $\mu$ is measured to be $\mu_1 = 0.10 \pm 0.02$ and $\mu_2 = 0.35 \pm 0.03$ in region (b) and (II), respectively (data not shown). Each data point represents the mean ($\pm$SD) of at eight different locations across one hexagon pattern at a fixed applied normal force.](image)

![FIGURE 7 Aggrecan lateral force versus height in NaCl solutions, pH $\sim 5.6$ using a nanosized OH-SAM functional tip ($R \sim 50$ nm, nominal cantilever spring constant, $k \sim 0.06$ N/m). (a) IS = 0.001 M; each data point represents one lateral signal loop, and the aggrecan brush height is recorded simultaneously. Region I: lower normal loads ($<20$ nN), where aggrecan molecules are not highly compressed and lateral forces are expected to originate from molecular shear, rotation, and bending. Region II: higher normal forces ($>20$ nN), where aggrecan molecules are highly compressed and stick-slip mechanisms are observed in the lateral signal loops. (b) Averaged aggrecan lateral force versus height curves at different IS; 0.001 M data correspond to that shown in panel a.](image)
The lateral proportionality coefficient $\mu$ varied with the tip displacement rate in the range $\sim 1$–100 $\mu$m/s (Fig. 10) in a manner that depended on ionic strength. At higher IS (0.1 and 1.0 M), $\mu$ increased significantly with tip displacement rate (confirmed by one-way ANOVA test at each ionic strength, Fig. 10). In contrast, at IS = 0.001 M, $\mu$ did not change significantly with tip displacement rate. The trends reported in this study were found to be reproducible using at least three different microcontact-printed samples for each experiment. The variability of the data are most likely associated with the local grafting density of the aggrecan layer within a hexagonal pattern and the previously quantified degree of aggrecan polydispersity (7). Variations between hexagons were found to be less important.

DISCUSSION

Control experiments—friction between nanosized OH-SAM probe tip versus COOH and $\text{NH}_2$-SAM micro contact printed substrates

The inversion of the lateral force image pattern on the COOH-SAM compared to the $\text{NH}_2$-SAM sample (Fig. 3, a and b) is consistent with the ionization state of the end-functional groups at different pH, as previously reported (38). At pH $\sim 2.4$, the COOH-SAM is fully protonated ($pK_{\text{a}}^{\text{surf}} \sim 5.2$) while $\text{NH}_2^+$-SAMs are fully ionized (p$K_{\text{b}}^{\text{surf}}$ $\sim 7$) (40). At this pH, greater lateral force was measured between the OH-SAM tip and $\text{NH}_2^+$-SAM due to intermolecular hydrogen bonds between $-\text{NH}_2^+$ and $-\text{OH}$ that are stronger.
in the lateral force experiments presented here may have two possible origins: through-thickness molecular-molecular interactions and/or surface interactions between the OH-SAM probe tip and the chain segments of the aggrecan in physical contact with the probe tip. Surface interactions are expected to be minimal, since it was observed that there was negligible adhesion between the aggrecan and OH-SAM tip for normal force measurements under the same conditions tested (12). This hypothesis is further supported by the fact that no marked difference was observed between $\mu$ measured with tips having varied surface chemistry. Hence, through-thickness molecular-molecular interactions are expected to dominate and may include electrostatic repulsion, nonelectrostatic repulsion (e.g., entropic, steric, excluded volume, bending, etc.), and/or molecular entanglements.

An electrostatic contribution to the shear resistance is evident in Fig. 9a, where it is observed that at any constant aggrecan layer height, the lateral force increases with decreasing IS. At the same time, clear differences in the lateral force are observed with ionic strength at constant values of the ratio of GAG spacing to Debye length (Fig. 9c), which supports the hypothesis that nonelectrostatic interactions also contribute to aggrecan shear resistance. Theoretical studies on polymer compression have suggested that more compacted configurations have higher nonelectrostatic interactions, e.g., excluded volume effect (42). Hence, the reduction in lateral force at a given strain $\varepsilon_{n}$ with increasing ionic strength (Fig. 9b) is likely due to the decrease in electrostatic repulsion. This finding is also consistent with the observation that at constant normal force, greater lateral force was measured at higher IS (Fig. 8), which would result in higher compaction of the aggrecan layer due to increased screening of electrostatic interactions.

**Aggrecan shear response using the nanosized probe tip**

For the microsized probe tip, a constant proportionality ratio $\mu$ was observed in the range of applied normal force in all tested IS (Fig. 8). By comparison, the nanosized probe tip highlighted the existence of two different regimes of linearity in the response with applied normal force (Fig. 6, b and c). Higher normal force resulted in full compression or penetration of the tip through the aggrecan layer (11), possibly bringing the tip into contact with the underlying gold substrate. The differences in lateral force mechanisms in regions I and II (Fig. 6, b and c) can be interpreted by analyzing the shape of lateral signal loops (Fig. 5) as well as the corresponding aggrecan height and conformation (Fig. 7). When the aggrecan was fully compressed or penetrated at high normal force, the lateral force was likely dominated by surface interactions between the probe tip and gold layer under the aggrecan (shaded, Fig. 5b (II)). At low normal force, lateral signals in the aggrecan region (shaded, Fig. 5b (I)) had much smaller variations compared to those in the OH-SAM region.

Molecular origins of the aggrecan shear response using the microsized tip

The radius of curvature of the microsized tip is an order-of-magnitude larger than aggrecan height, aggrecan-aggrecan surface separation distance, and the interaction distance between the aggrecan layer and the probe tip. Thus, the ensemble of aggrecan molecules located within the tip-substrate contact area are subjected to a more uniform deformation compared to that produced by the nanosized tip, which may penetrate into the aggrecan layer. The finding that the lateral force was independent of loading history over many loading-unloading cycles suggests that the aggrecan(thiol)-gold end-grafting was stable for the experimental conditions used (2 h for each ionic strength condition). The $\mu$-values measured than those between $-\text{COOH}$ and $-\text{OH}$. At pH $\sim$10.3, the NH$_2$-SAM is nearly neutral while the COO$^-$-SAM is completely ionized and, thus, there is a stronger adhesion force between the COO$^-$ and OH functional groups due to stronger hydrogen bonds (38). The stick-slip behavior and linear dependence of lateral force on applied normal force is consistent with previous results on SAM systems (30), and is known to correlate with adhesion of the end-functional groups (37). The magnitude of the lateral proportionality coefficient $\mu$ may depend on many experimental factors including surface roughness, contact area, sliding speed, temperature, etc. (41), but relative trends, such as the effect of pH, are accurately assessed. The greater pH dependence of $\mu$ in the carboxyl SAM region can be attributed to the larger increase of electronegativity of the carboxyl groups by ionization, and hence the larger magnitude change of the hydrogen bonding energy (30), and thus adhesions, between hydroxyl and carboxyl SAMs from the protonated to the charged state.

**FIGURE 10** Lateral proportionality coefficient $\mu$ as a function of lateral tip displacement rate (from 3.16 to 100 $\mu$m/s) in NaCl solutions, pH $\sim$5.6, calculated as the least-squares estimator $\pm$95% confidence interval from eight series of applied normal forces at the same IS and lateral displacement rate. The $\mu$ varied significantly with displacement rate at 0.1 M and 1.0 M IS (one-way ANOVA, $p < 0.0001$); no significant effect of rate was found at 0.001 M. The value $\mu$ was found to vary significantly with IS and rate (two-way ANOVA test, followed by Tukey-Kramer post-hoc multicomparison test, $p < 0.0001$).
where the lateral forces were dominated by stick-slip surface interactions (37). The transition between different lateral force mechanisms also support the hypothesis that surface interactions between aggrecan and the OH-SAM tip were small.

Under the microsized tip, a degree of normal and lateral confinement of aggrecan within the layer is expected, since \( \sim 10^3 \) aggrecan are compressed simultaneously. However, due to the pyramidal geometry of the nanosized tip, only 2–4 aggrecan molecules are directly interacting with the tip and the measured aggrecan height does not necessarily represent the amount of aggrecan compression in the normal direction. Penetration of the nanosized tip into the aggrecan layer could result in both splay deformation (bending) as well as compression even in the absence of tip lateral displacement. Regardless of these geometrical factors, a linear dependence of lateral force on applied normal force was still observed in the normal force region I in Fig. 6, b and c, and Fig. 7. Although \( \mu \) did not markedly vary with IS in this region (Fig. 6, b and c), as was observed using the microsized probe tip (Fig. 8), a strong IS-dependence was observed between lateral force and aggrecan height (Fig. 7 b). Thus, due to stronger electrostatic repulsion at lower IS, larger normal forces were required to reach a given compressed height, and electrostatic repulsion was stronger in the lateral directions as well. The nanosized probe tip has a larger lateral proportionality coefficient in region I at IS = 0.001–0.1 M compared to that with the microsized tip, which is likely due to length scale and/or geometrical effects. Thus, the two lateral linearity regions measured via the nanosized probe tip (Fig. 6, b and c) helped to interpret the underlying molecular origins of aggrecan shear and to assess the lateral deformation mechanisms of a few aggrecan molecules. By comparison, the microsized tip serves to contrast the effects of compressive and lateral deformation of a larger ensemble of aggrecan molecules, and thereby more closely simulates the deformation of aggrecan within cartilage tissue.

### Rate-dependence of aggrecan shear

The significant increase in \( \mu \) with tip lateral displacement rate at 0.1 M and 1.0 M IS (Fig. 10) suggests that time-dependent (e.g., viscoelastic and/or poroelastic) as well as time-independent (elastic) processes are involved in lateral deformation of aggrecan. In contrast, at low IS (0.001 M), as elastic electrostatic interactions become even more dominant, no significant change in \( \mu \) with displacement rate was observed (Fig. 10). Viscoelastic behavior may be associated with interpenetration, entanglements, and macromolecular friction between aggrecan molecules. Poroelastic behavior may result from lateral deformation-induced fluid flow within and through the densely-packed aggrecan layer and the associated local pressure gradients within the layer, which results in hydrodynamic friction between water and end-attached aggrecan (43,44), as is known to occur within cartilage tissue (45,46). Such rate-dependent phenomena become relatively more important as rate-independent electrostatic interactions decrease with increasing IS. From the data presented here, we cannot yet distinguish between viscoelastic and poroelastic contributions, which are the subject of ongoing studies focusing on scaling approaches to the size and rate of interactions (47). Interestingly, previous studies of the compressive nanomechanics of aggrecan, where electrostatic effects were dominant, showed negligible dependence of aggrecan compressive stiffness on normal tip displacement rate in the range of 0.1–10 \( \mu \)m/s (12).

### Comparison to reported polyelectrolyte lateral force studies

While this study has focused on the shear deformation of the end-grafted aggrecan layer, it is still instructive to compare our findings to recent literature on the surface lubrication properties of polyelectrolytes. Feiler et al. (48) recently used LFM to measure surface forces and frictions associated with adsorbed cationic polyelectrolyte layers of very low charge density, using a similar microsized probe tip geometry (\( R \sim 10 \mu m \)) and range of lateral displacement rates (\( \sim 10–100 \mu m/s \)). Their measured values of \( \mu \) in \( 10^{-4} \) M KBr were higher than the largest measured \( \mu \) for aggrecan even at the highest IS of 1.0 M (Fig. 9), at which electrostatic interactions are screened. Values of \( \mu \) reported for negatively charged polyelectrolyte layers measured using the surface forces apparatus (20,22) at the lowest ionic strength comparable to our study were higher than that found here as well, while in some other negatively charged polyelectrolyte systems, extremely low values of the effective lateral coefficient \( \mu_{\text{eff}} \) (the ratio of lateral to normal force) were also observed (19). These differences are likely associated with differences in the molecular structure of the polyelectrolytes of interest, the arrangement of the adsorbed versus end-anchored attachment, the existence of free polyelectrolyte molecules in solution, the geometry of the opposing layers in the SFA versus AFM configuration, the lateral displacement velocity (greater than fivefold higher in the AFM), and the higher applied normal forces used in the SFA experiments. Nevertheless, a similar trend was observed in both AFM and SFA systems demonstrating that the presence of electrostatic interactions between charged polyelectrolytes effectively reduced the lateral forces at constant normal force (19).

### Comparison to macroscopic shear of cartilage tissue

We first note that the observed decrease in the resistance of aggrecan to shear deformation with increasing IS (Fig. 9) is consistent with the previously reported decrease in both the equilibrium and dynamic torsional shear modulus of cartilage disks with increasing IS at constant disk thickness in vitro (5). During macroscopic deformation of cartilage in...
vivo, aggrecan would be expected to deform in both normal and lateral directions enmeshed within the collagen fibrillar network. In this study, end-attached aggrecan molecules undergo both compression and shear simultaneously. However, while the macromolecules are end-attached to the substrate, the lateral displacement of the aggrecan is not measured, as they are not attached to the tip or to each other like a network. Therefore, it is difficult to define a shear strain (or shear modulus) for the layer in the configuration of Fig. 2, a and b. Assuming aggrecan to be a rigid rod, the maximum shear deformation at 0.1 M was estimated to be ~0.95 of the aggrecan contour length; however, aggrecan is more coiled at physiological conditions and the actual deformation is likely much less. In native cartilage tissue, aggrecan is enmeshed within a collagen fibril network. While the configuration of Fig. 2, a and b (without the collagen network), does not replicate the mechanical constraints that regulate aggrecan deformation within native tissue, our goal is to help further establish a molecular-level understanding of cartilage tissue mechanics by isolating the different components of aggrecan deformation. To this end, the magnitudes of both the normal and lateral force as a function of aggrecan layer height using the microsized tip, replotted from the data of Figs. 8 and 9, are compared in Fig. 11 at near physiological IS (0.1 M NaCl). At any given height (normal deformation), the normal force is ~10-fold larger than the shear force. Conversely, aggrecan resistance to shear deformation is ~10% of its resistance to compression in this layer configuration. In native cartilage, the equilibrium shear modulus is typically ~50% that of the compressive modulus (25). Thus, while the experiments presented here delineate the lateral deformation properties of aggrecan layers having molecular packing densities similar to that in tissue, it is clear that interactions between aggrecan and the enveloping collagen network are also critically important for a complete understanding of the tissue-level biomechanical properties of cartilage. Ongoing studies are therefore focused on lateral nanomechanical interactions between aggrecan and collagen, and between aggrecan macromolecules enmeshed within a collagen network.

CONCLUSIONS

In this study, we examined the shear nanomechanics of aggrecan macromolecules using microcontact printing and lateral force microscopy involving deformation of a few aggrecan or a large assembly of them using nanosized or microsized probe tips, respectively. By deforming a large assembly of aggrecan at physiological concentration, the microsized tip more closely mimics deformation of aggrecan within native cartilage tissue. Using this approach, aggrecan shear force was found to depend linearly on normal force. Both electrostatic and nonelectrostatic interactions at the molecular level were identified by using a combination of probe tip geometries, functionalizations, environmental (e.g., IS) conditions, and appropriate normalization of the data. Stronger electrostatic interactions resulted in larger shear resistance at the same layer height and normal strain, accompanied by more elasticlike deformation (i.e., less rate-dependence). At physiological IS, the rate dependence of the lateral force strongly suggested the presence of visco- and/or poroelastic behavior, consistent with tissue-level aggrecan and GAG-GAG interactions that have been identified in the study of intact cartilage shear behavior.

APPENDIX—LATERAL FORCE CALIBRATION

Wedge method for calibration of nanosized probe tips

Lateral deflection signals (V) from a position-sensitive photodiode (PSPD, resolution ~1 mV) were recorded during line scans. To convert these data into forces, the lateral cantilever deflection sensitivity, a (nN/V), had to be determined. Different calibration methods have been used (34,35,49–57) and compared (58) previously to quantify a. Among these, the nondestructive “wedge” method (34,35), which calibrates the ratio of a to the normal deflection sensitivity β (nN/V), has been the most widely accepted. This approach can be performed in combination with lateral force experiments, thereby eliminating uncertainties introduced by a separate calibration of cantilever stiffness and by changes in experimental conditions including the optical geometry of the laser beam path. The wedge method was first developed using standard nanosized silicon AFM probe tips (R < 100 nm) to scan SiTiO$_3$ samples having geometrically well-specified slopes (i.e., the (101) and (103) crystallographic planes) (34). Varenberg et al. (35) extended this approach by replacing the SiTiO$_3$ sample with an etched silicon calibration sample having both planar and tilted regions (TGF-11, Mikromasch, Wilsonville, OR). This technique allowed use of probe tips having an end-radius R < ~1 μm. In this study, we modified the calculation procedure of a by removing the assumption that the applied normal force remains constant on the horizontal and tilted regions during scanning. In addition, we extended the wedge method to calibrate larger probe tips with end-radii R > ~1 μm. In this case, the reported method using the TGF-11 sample cannot be used because the probe tip makes simultaneous contact with both the horizontal and tilted regions when scanning (i.e., the length of the tilted region ~1 μm, the slope 54°44’) resulting in noise that was an order-of-magnitude larger.
than the lateral deflection signal itself. By using two different mica samples, one horizontal and the other tilted at $-20^\circ$, we developed new calibration procedures and analysis for larger probe tips, which is applicable to probe tips with smaller end-radii as well.

To clarify our modifications on the wedge method, we use the approach based on Eqs. 1–12 of Varenberg et al. (35). The tip (height $h$, end-radius $R$, Fig. A1) is subjected to forces applied by the probe tip (i.e., the contact, adhesion, and friction forces $N$, $A$, and $f$, respectively), and the cantilever of thickness $t$ (i.e., the applied normal and lateral force, $L$ and $T$, and the torsion moment $M$). The subscripts $a$ and $d$ correspond to the forces and moments during uphill and downhill motions, respectively. Momentum equilibrium is described for uphill and downhill motions by Eqs. 11 and 12 in (35):

$$M_a + L_a R \sin \theta - T_u \left( R \cos \theta + h - R + \frac{t}{2} \right) = 0, \quad (A1)$$

$$M_d + L_d R \sin \theta - T_d \left( R \cos \theta + h - R + \frac{t}{2} \right) = 0. \quad (A2)$$

For nanosized probe tip $h \gg R$, Eqs. 1 and 2 are simplified as

$$M_a = T_a \left( h + \frac{t}{2} \right), \quad (A3)$$

$$M_d = T_d \left( h + \frac{t}{2} \right). \quad (A4)$$

The nanosized probe tip used in this study was calibrated following the experimental procedures described in Varenberg et al. (35). A series of 1.1 $\mu$m lateral scan loops (256 datapoints each on trace and retrace) were performed on the TGF-11 calibration grid (surface roughness $\sim 13.5$ nm, slope of tilted region $= 54\degree 44\prime$) at varying applied normal force. Each scan loop included both horizontal and tilted regions (Fig. A2) at a 1 Hz scan rate (2.2 mm/s); scanning rates exceeding 3 mm/s on the tilted region resulted in the deflection signals recorded were used to calculate the normal forces exerted from the cantilever.

For the applied normal force can be rewritten as

$$L = (d + s - b_\alpha) \times \beta, \quad (A9)$$

where $d$ is the vertical deflection signal, $s$ the setpoint, $b_v$ the vertical baseline (corresponding to the vertical signal in the unengaged state), and $\beta$ (nN/V) the cantilever’s normal deflection sensitivity, which is the product of its normal spring constant $k$ (nN/nm) and inverse optical lever sensitivity (nm/V) (36). For a given tilted angle $\theta$ and tip scanning rate, $d$ was observed to be independent of $s$ and remained constant during scanning under a series of vertical setpoints. In addition, it was found that for uphill and downhill motion,

$$d_u = -d_d. \quad (A10)$$

The adhesion force $A$ is measured to be negligible and, hence, it can be calculated as a function of applied normal force $L$,

$$W_o \alpha = \frac{(1 + \mu^2) (L_u - L_d) \sin \theta \cos \theta + \mu (L_u + L_d)}{\cos^2 \theta - \mu^2 \sin^2 \theta}, \quad (A7)$$

$$\Delta \alpha = \frac{(1 + \mu^2) (L_u + L_d) \sin \theta \cos \theta + \mu (L_u - L_d)}{\cos^2 \theta - \mu^2 \sin^2 \theta}. \quad (A8)$$

### New modifications of wedge method for calibration of nanosized probe tips

It was observed that scanning on a tilted surface resulted in normal deflection errors that could not be corrected by the AFM instrument and, thus, $L_d \neq L_u$ (Fig. A2). The deflection signals recorded were used to calculate the normal forces exerted from the cantilever.

$$L_u = L_o + \delta, \quad (A11)$$

$$L_d = L_o - \delta, \quad (A12)$$

where $L_o = (s - b_\alpha) \times \beta$ is the normal force on the horizontal surface (the subscript $o$ indicates the force on the horizontal region), and $\delta = d_0 \beta$ is the additional normal force that resulted from scanning on a tilted surface. The value $\delta$ was observed to remain constant for the series of applied...
versus normal load (Fig. A3), where each data point represents the mean of eight lateral
D
m
m
2 nN/V (Fig. A3). Thus, using a
between the tip and substrate in the tilted region was calculated
was calculated as

\[
\Delta_a(\theta-0) = \frac{2\Delta'_a(\theta-0)}{W_a'\sin 2\theta}
\]  \hspace{1cm} (A15)

The lateral sensitivity \( \alpha \) was calculated as

\[
\alpha = \frac{1}{W_a'(\theta)} \frac{\mu}{\cos \theta - \mu \sin \theta},
\]  \hspace{1cm} (A16)

and the lateral proportionality coefficient on the horizontal surface was then calculated as

\[
\mu_a = \alpha W_a'(0).
\]  \hspace{1cm} (A17)

The true physical value of \( \mu \) and \( \mu_a \) may not be equal but should be close to
each other. Hence, the physical solution from the two possible solutions
derived from Eqs. A15 to A17 (\( \mu, \mu_a, \Delta_a(\theta-0) \) and \( \mu_a, \Delta_a(\theta-0) \)) was determined by
comparing the values of \( |\mu - \mu_a| \); the solution corresponding to the smaller
|\( \mu - \mu_a | \) is the real solution (35). The nanosized probe tip used to obtain the
lateral force data for both the control and aggrecan shear experiments was
found to have a lateral sensitivity \( \alpha = 122 \pm 2 \text{nN/V} \) (Fig. A3). Thus, using a
PSPD with \( \sim 1 \text{mV} \) resolution, the minimum detectable amount of lateral
force was \( \sim 100 \text{pN} \), based on the measured lateral sensitivity.

**Modifications of wedge method for calibration of
microsized probe tips**

The lateral sensitivity of the microsized (colloidal) probe tip used in this
study could not be calibrated using the wedge method since the radius of
the colloid is bigger than the length of the tilted region, and scanning on a tilted
region having \( \theta = 54^\circ 44' \) resulted in uncorrectable noise due to the
relatively large tilted angle. We therefore replaced the TGF-11 sample
(Mikromasch) with two mica substrates, one having a horizontal surface and
the other a surface with tilt angle \( \theta \sim 20^\circ \).

A series of 10-μm lateral scan loops (256 datapoints each on trace and
retrace) was performed on both the horizontal and the tilted mica substrates at
varying applied normal force at 1 Hz scan rate (20 μm/s). The half-widths and
the offsets of baseline signals of the lateral signal loops were measured from
both the horizontal (\( W_a(0) \) and \( \Delta_a(0) \)) and the tilted (\( W_a(0) \) and \( \Delta_a(\theta) \))
samples. The jump of the baseline offset \( \Delta_a(\theta-0) \) from the horizontal to the
tilted sample could not be directly measured, for one single scan loop
including scanning on both horizontal and tilted regions could not be obtained
when using two separate samples. However, the lateral baseline offset was
found to be affected only by two factors, the applied normal force \( L_o \) due to the
crosstalk between the normal and the lateral deflection signals, and the tilt

\[
\frac{\mu}{\mu_a} = \frac{\alpha}{\mu_a} = \frac{1}{\alpha W_a'(0)}
\]  \hspace{1cm} (A18)

\[
|\Delta_a(\theta-0)| = \frac{1}{\alpha W_a'(\theta)} \frac{\mu}{\cos \theta - \mu \sin \theta}
\]  \hspace{1cm} (A19)

\[
W_a'(0) = \frac{\mu_a}{\cos \theta - \mu_a \sin \theta},
\]  \hspace{1cm} (A20)

\[
W_a'(\theta) = \frac{\mu_a}{\cos \theta - \mu_a \sin \theta}
\]  \hspace{1cm} (A21)

\[
\Delta_a(\theta-0) = \frac{2\Delta'_a(\theta-0)}{W_a'\sin 2\theta}
\]  \hspace{1cm} (A15)

\[
\alpha = \frac{1}{W_a'(\theta)} \frac{\mu}{\cos \theta - \mu \sin \theta},
\]  \hspace{1cm} (A16)

and the lateral proportionality coefficient on the horizontal surface was then calculated as

\[
\mu_a = \alpha W_a'(\theta).
\]  \hspace{1cm} (A17)

The true physical value of \( \mu \) and \( \mu_a \) may not be equal but should be close to
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samples. The jump of the baseline offset \( \Delta_a(\theta-0) \) from the horizontal to the
tilted sample could not be directly measured, for one single scan loop
including scanning on both horizontal and tilted regions could not be obtained
when using two separate samples. However, the lateral baseline offset was
found to be affected only by two factors, the applied normal force \( L_o \) due to the
crosstalk between the normal and the lateral deflection signals, and the tilt
angle \( \theta \), which causes the lateral projection of the compression force \( N \) (Fig. A4). The crosstalk between normal and lateral deflection signals is determined by the laser path from the AFM head to the PSPD (59) and, hence, the effect of the crosstalk is the same during scanning on the two different samples as long as the optical laser beam path is untouched while changing the samples. In that case, the difference of lateral baseline dependences on normal force measured on these two samples, \( \Delta u/\Delta o \), has the same physical meaning of lateral baseline jump from a horizontal to a tilted region on one single scan on the same sample, \( \Delta u/\Delta o \).

For the microsized probe tip, where \( h = 2R \), Eqs. A1 and A2 are simplified as

\[
M_u = T_u \left[ R(1 + \cos \theta) + \frac{t}{2} \right] - L_o \sin \theta, \tag{A18}
\]

\[
M_o = T_o \left[ R(1 + \cos \theta) + \frac{t}{2} \right] - L_o \sin \theta. \tag{A19}
\]

Hence, with negligible measured adhesion force \( A \), the two calibration parameters are calculated as

\[
\frac{W}{h + t/2} = \frac{W_o}{h} = \frac{M_u - M_o}{2[R(1 + \cos \theta) + t/2]} = \frac{T_u - T_o}{2} - \frac{[L_u - L_o] \sin \theta}{2[R(1 + \cos \theta) + t/2]} \tag{A20}
\]

\[
\frac{\Delta u(\theta) - \Delta o(0)}{h + t/2} = \frac{[\Delta u(\theta) - \Delta o(0)]}{h + t/2} = \frac{M_u + M_o}{2[R(1 + \cos \theta) + t/2]} = \frac{T_u + T_o}{2} - \frac{[L_u + L_o] \sin \theta}{2[R(1 + \cos \theta) + t/2]} \tag{A21}
\]

Equations A20 and A21 can be written as a function of the applied normal force,

\[
W_o/\alpha = \frac{\mu L_o + (1 + \mu^2) L_o \sin \theta \cos \theta}{\cos \theta - \mu^2 \sin \theta} \tag{A22}
\]

\[
\Delta u(\theta) - \Delta o(0) = \frac{1 + \mu^2}{\cos \theta - \mu^2 \sin \theta} L_o R \sin \theta
- \frac{[R(1 + \cos \theta) + t/2] \cos \theta - \mu^2 \sin \theta}{\cos \theta - \mu^2 \sin \theta}, \tag{A23}
\]

and the lateral proportionality \( \mu \) is then calculated as

\[
\frac{(\Delta u(\theta) - \Delta o(0))'}{W_o/(\theta)} = \left( \mu + \frac{1}{\mu} \right) \frac{\sin \theta \cos \theta}{R \sin \theta} - \frac{1}{\mu} \frac{R \sin \theta}{[R(1 + \cos \theta) + t/2]} \tag{A24}
\]

The cantilever lateral sensitivity \( \alpha \) is calculated using Eq. A16 and the same criteria used for the nanosized probe tip was used to determine the true physical solutions of \( \mu \) and \( \alpha \). The microsized probe tip used in this study was calibrated to have a lateral sensitivity \( \alpha = 148 \pm 17 \text{nN/N} \).

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39. Reference deleted in proof.


