

## **2.29 Course Project**

# **Modeling of Ion Transport Membrane Reactors: A Review and Practice**

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# Outline

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## 1. Literature review

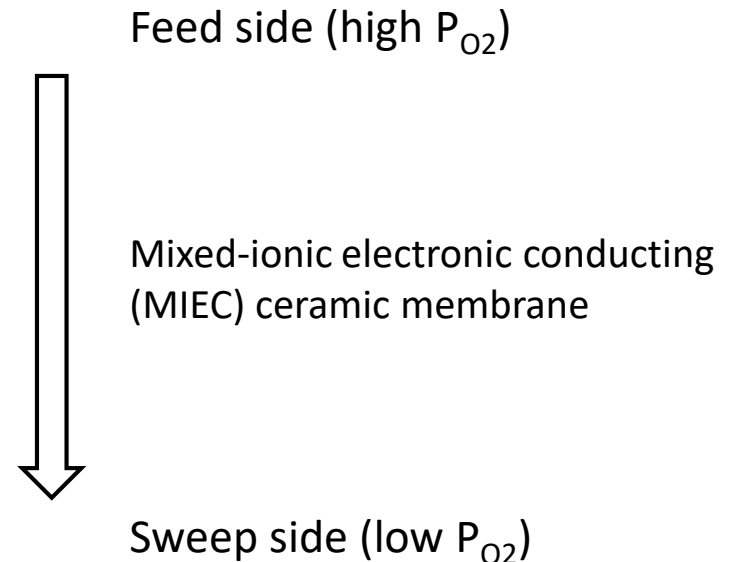
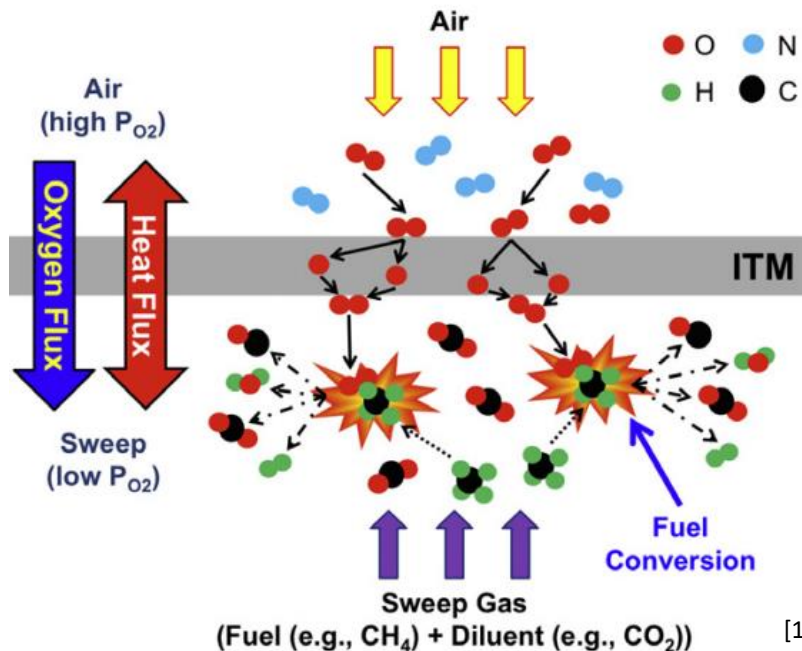
- ITM reactor
- ITM models
- An Intermediate-fidelity model

## 2. Modeling practice

- A monolith reactor with LCF91 membrane
- FLUENT simulation for permeation channel

# ITM Reactor

**Ion transport membrane (ITM)** technology is a novel approach providing an alternative solution to separate oxygen from air.



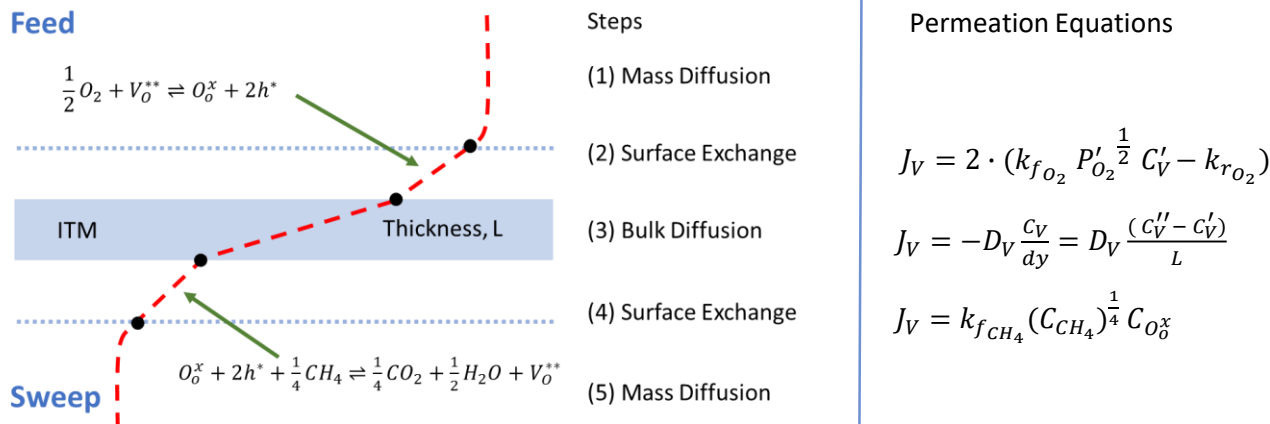
Advantages:

1. Potentially achieve **100%  $CO_2$  capture**
2. Reducing **70% power consumption** compared with conventional  $O_2$  production methods
3. Increase power generation efficiency by **4%**

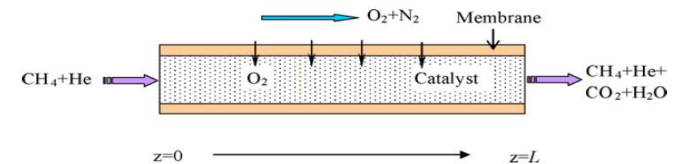
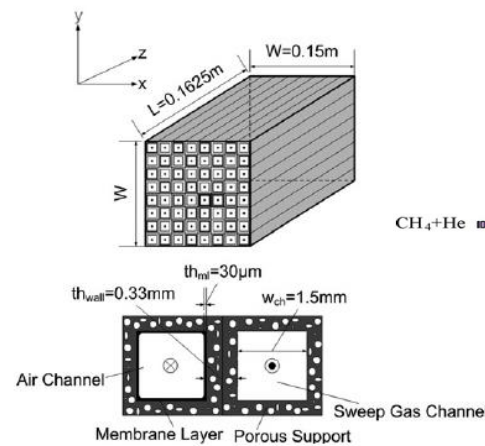
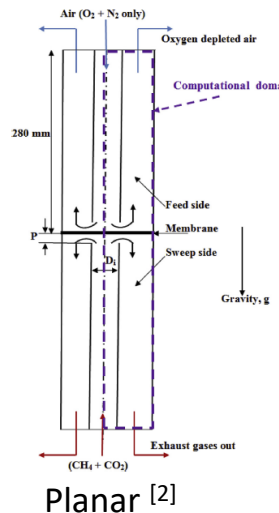
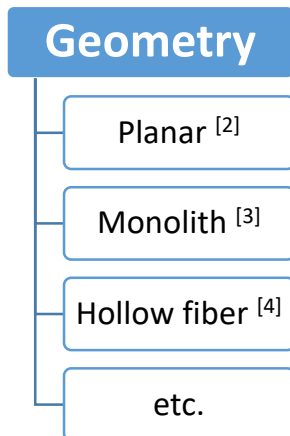
# ITM models

## Purpose of different levels of ITM models:

### 1. Material-level analysis → Transport phenomena



### 2. System-level analysis → Reactor Design and operating conditions



[2] Nemitalah MA, Habib MA, Mezghani K. Experimental and numerical study of oxygen separation and oxy-combustion characteristics inside a button-cell LNO-ITM reactor. Energy 2015;84:600–11.

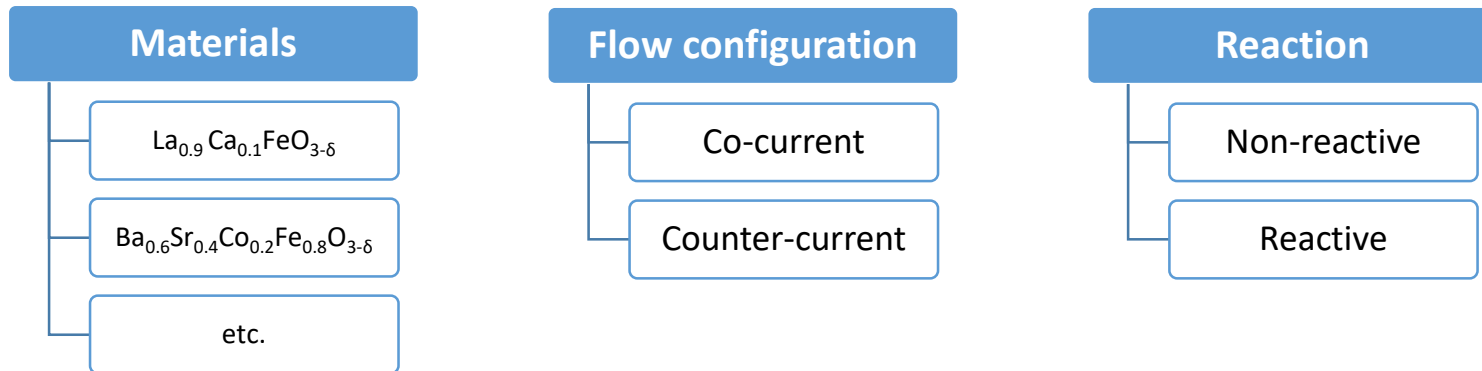
[3] Colombo K. E., Kharton, V. V., and Bolland, O., 2010, "Simulation of an Oxygen Membrane-Based Gas Turbine Power Plant: Dynamic Regimes With Operational and Material Constraints," Energy Fuels, 24, pp. 590–608

[4] X. Tan, K. Li, A. Thursfield, I.S. Metcalfe, Oxyfuel combustion using a catalytic ceramic membrane reactor, Catalysis Today 131 (1–4) (2008) 292–304.

# ITM models

## Purpose of different levels of ITM models:

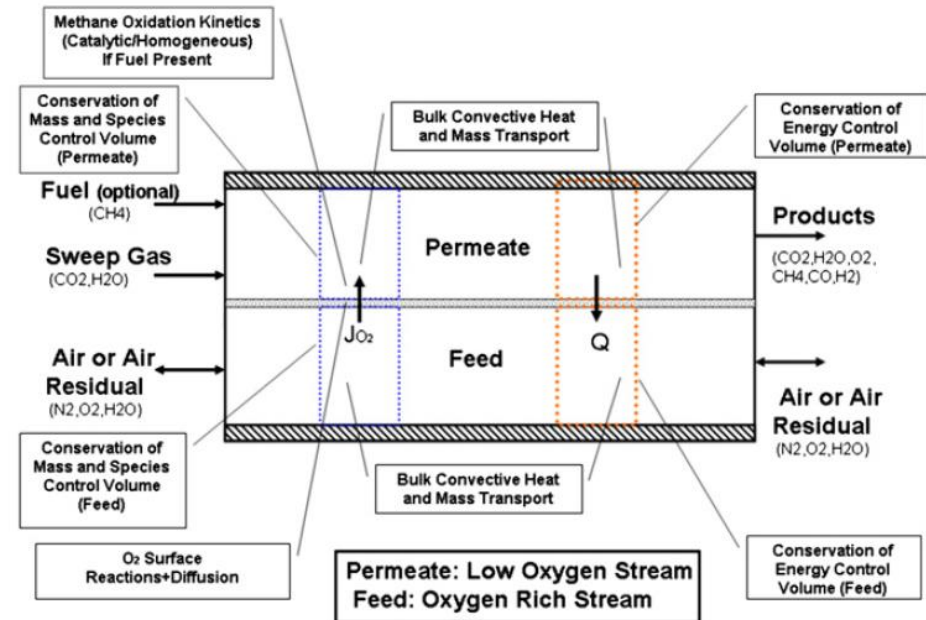
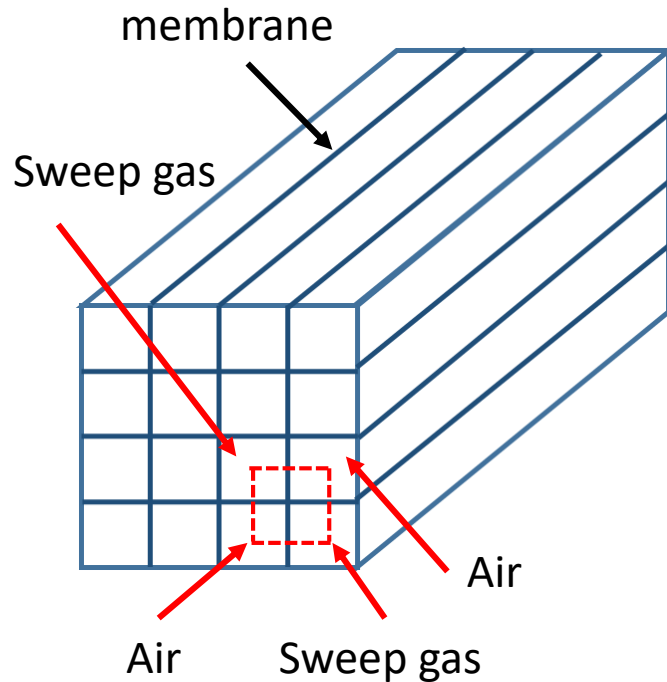
2. System-level analysis → Reactor Design and operating conditions



## Requirements of a good ITM models:

- 1) Capture important physical relationships
  - Conservation of mass and species
  - Thermodynamics
  - Oxygen permeation phenomena
  - Heat transfer
  - Chemical reactions
  
- 2) Without extreme computational time
  - Highly-coupled nonlinear system
  - Combustion process could be complicated

# An Intermediate-fidelity model [5]



The model simplifies the monolith reactor into a **1-D problem** due to symmetry

- Split the geometry into discrete elements
- Steady-state conservation equations are written for each discrete element

# Conservation equations [5]

## Conservation of mass and species:

$$\dot{n}_{i+1,O_2} = \dot{n}_{i,O_2} + \phi A_i J_{i,O_2} + \phi V_i R''_{i,O_2}$$

$\dot{n}$  is the molar flow-rate of O<sub>2</sub> mol/s,

$J_{i,O_2}$  is the local oxygen flux [mol/m<sup>2</sup>]

$R''_{i,O_2}$  is the local rate of production of oxygen due to chemical reaction [mol/m<sup>3</sup>]

## First law of thermodynamics:

$$\sum_j \dot{n}_{i+1,j} \bar{h}_j(T_{i+1}) = \sum_j \dot{n}_{i,j} \bar{h}_j(T_i) - \dot{Q}_i + \dot{H}_{i,O_2,ext}$$

$\dot{Q}_i$  represents the convective heat transfer between streams, where the overall heat transfer coefficient  $U_i$

$$\dot{Q}_i = \phi \bar{U}_i A_i (T_i'' - T_i')$$

$\dot{H}_{i,O_2,ext}$  represents the enthalpy stream transported from the feed to the permeate side

## Second law of thermodynamics:

$$\dot{S}_{gen} = \sum_{outlet} \dot{n}_j \bar{s}_j(T, P_j) - \sum_{inlet} \dot{n}_j \bar{s}_j(T, P_j)$$

# Transport equations

## Heat and mass transfer consideration:

Gnielinski correlation is used for forced convection in turbulent pipe flow.

$$Nu_{D_{h,i}} = \frac{f_i/8 \cdot (Re_{D_{h,i}} - 1000)Pr}{1 + 12.7 \sqrt{\frac{f_i}{8}} (Pr^{\frac{2}{3}} - 1)}$$

Due to the small channel sizes of the reactor, the author assumes that the **forced convection** dominates the heat transfer.

## Oxygen permeation mechanisms:

The semi-empirical form:  $J_{O_2} = A \exp\left(-\frac{B}{T_M}\right) [(P'_{O_2})^n - (P''_{O_2})^n]$

A stands for pre-exponential factor; B represents the effective activation energy.

## Things become complicated when we have reactive ITM:

Methane oxidation kinetics:

- 1) Fast kinetics assumption (products of chemical reaction is only CO<sub>2</sub> and H<sub>2</sub>O)
- 2) Thermodynamic equilibrium assumption (CH<sub>4</sub> CO<sub>2</sub> CO H<sub>2</sub> H<sub>2</sub>O O<sub>2</sub>)
- 3) Additional oxidation kinetics scheme

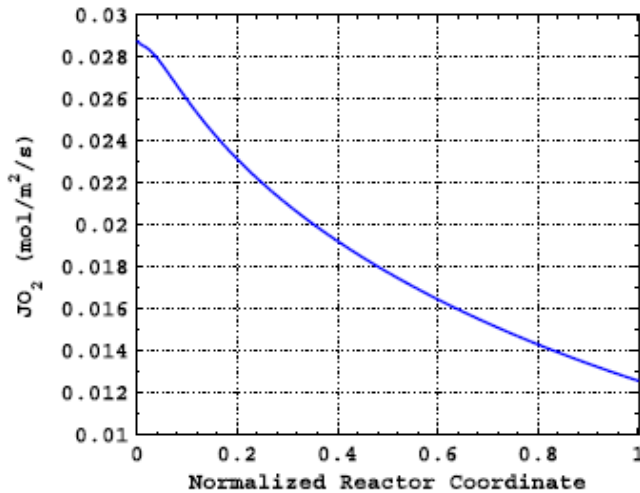
## Approach and solver:

Equation-oriented approach is used to solve the system of non-linear equations with JACOBIAN, a general modeling and simulation program.

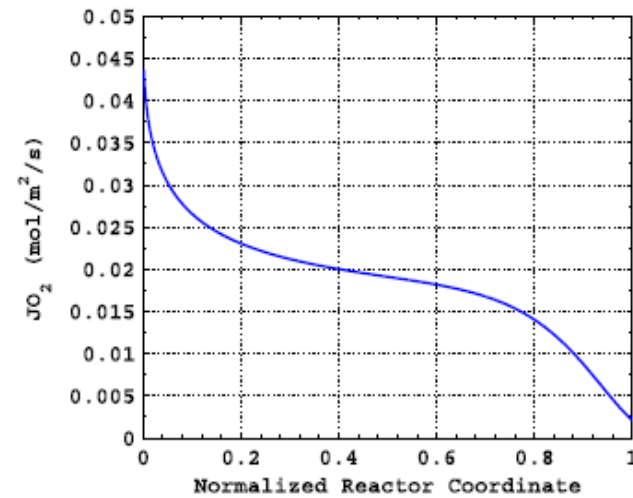


# Sample results [5]

Separation-only Mode

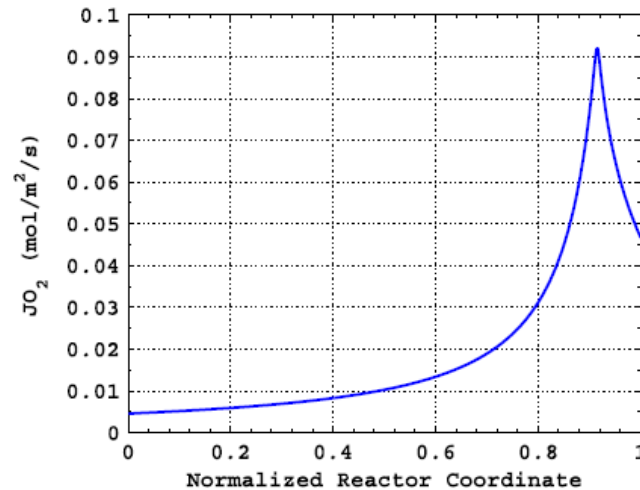


Co-current configuration

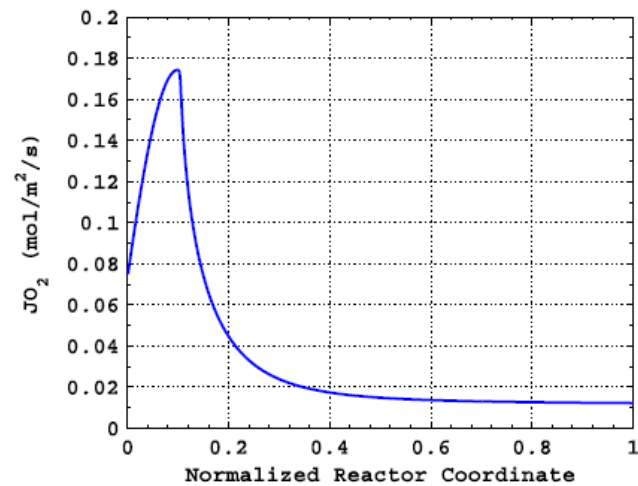


Counter-current configuration

Reactive Mode



Flux  
Co-current configuration



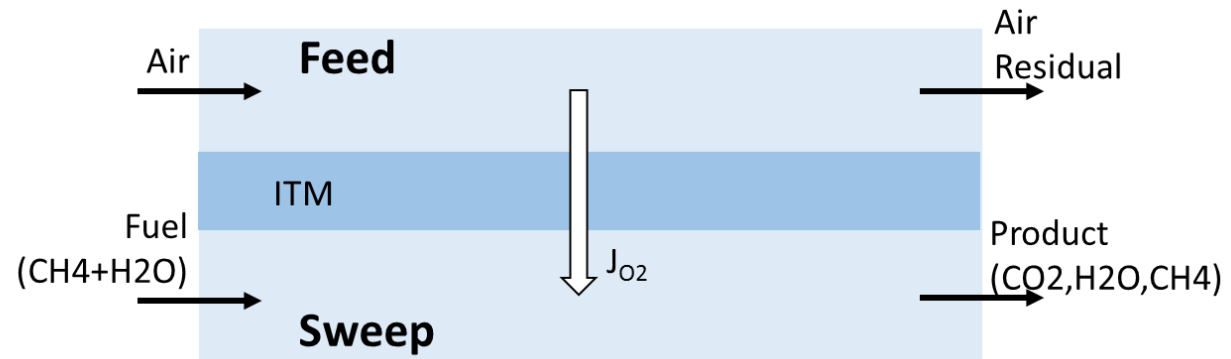
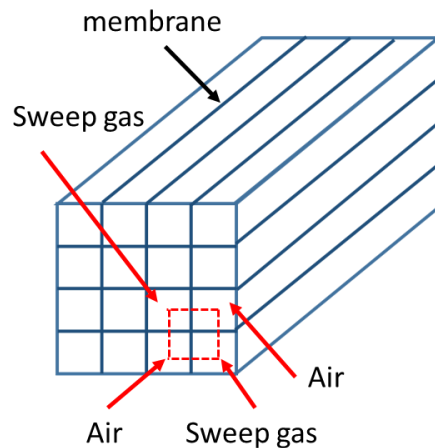
Oxygen Flux  
Counter-current configuration

# Outline

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  - ITM models
  - An Intermediate-fidelity model
  
2. Modeling practice
  - A monolith reactor with LCF91 membrane
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# A co-current monolith reactor



Simplifications made:

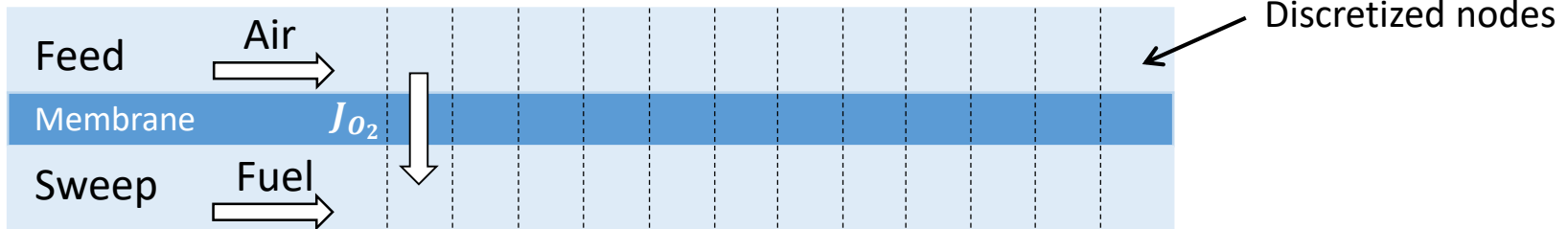
1. Assume temperature constant in the channel
2. Pressure drop neglected
3. Fast kinetics assumptions



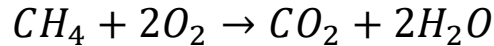
Equations satisfied:

1. Conservation of mass and species
2. First and second laws of thermodynamics
3. Resistance-network oxygen permeation mechanism

# Base case simulation parameters

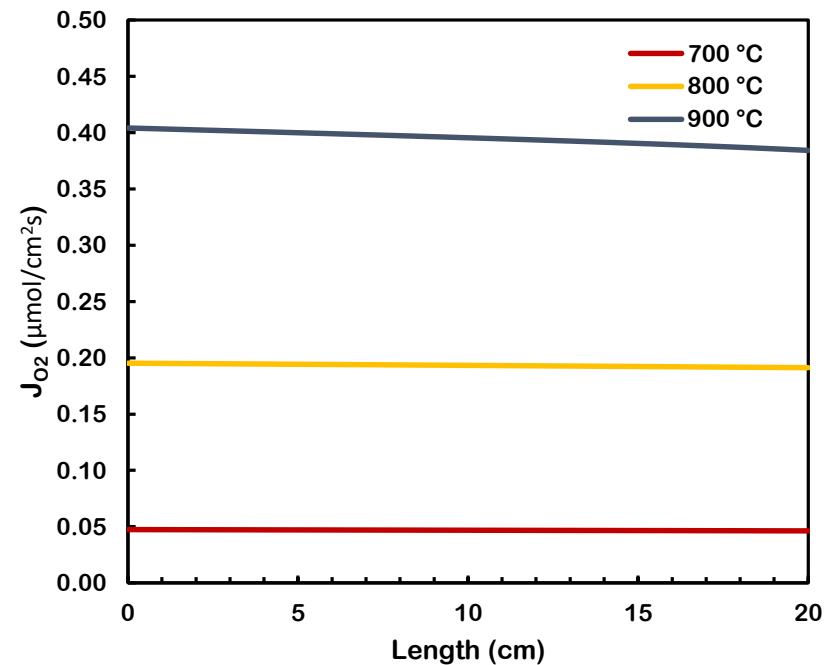


$$J_{O_2} = \frac{1}{2} \cdot \frac{C_o - \frac{k_{rO_2}}{k_{fO_2} P'_{O_2}{}^{\frac{1}{2}}}}{\frac{1}{2k_{fO_2} P'_{O_2}{}^{\frac{1}{2}}} + \frac{L}{D_V} + \frac{1}{k_{fCH_4} (C_{CH_4})^{\frac{1}{4}}}}$$

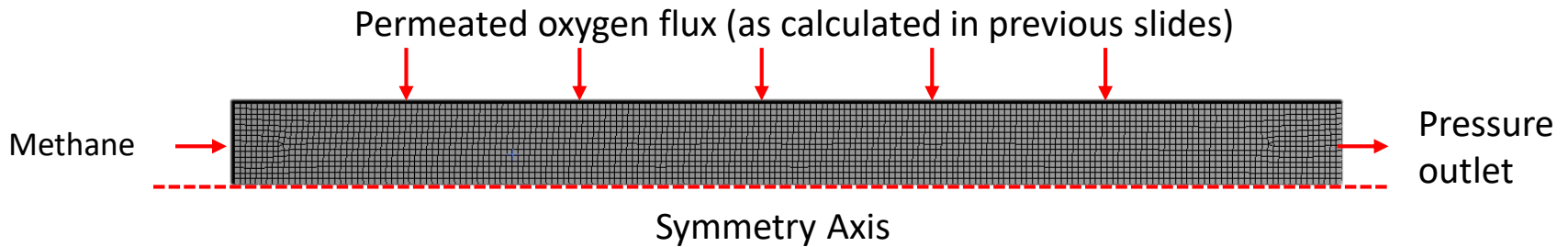
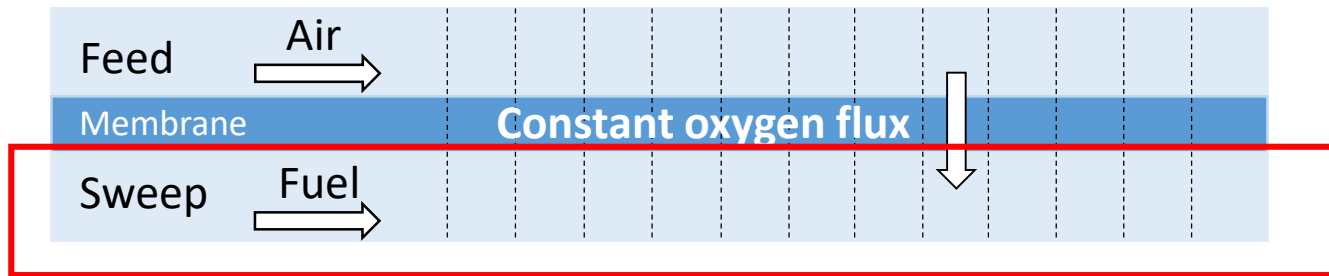


$$\dot{n}_{i+1,O_2} = \dot{n}_{i,O_2} + \Phi A_i J_{i,O_2} + \Phi V_i R'''_{i,O_2}$$

Parameter	Value
Channel Height [cm]	1.5
Channel Length [mm]	200
Membrane material	La <sub>0.9</sub> Ca <sub>0.1</sub> FeO <sub>3-δ</sub>
Membrane Thickness [mm]	1
Sweep side methane concentration	100%
Operation Temperature [°C]	700-9000

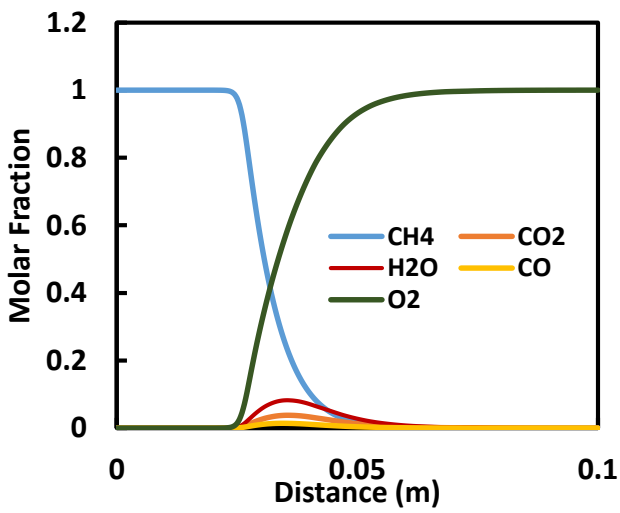
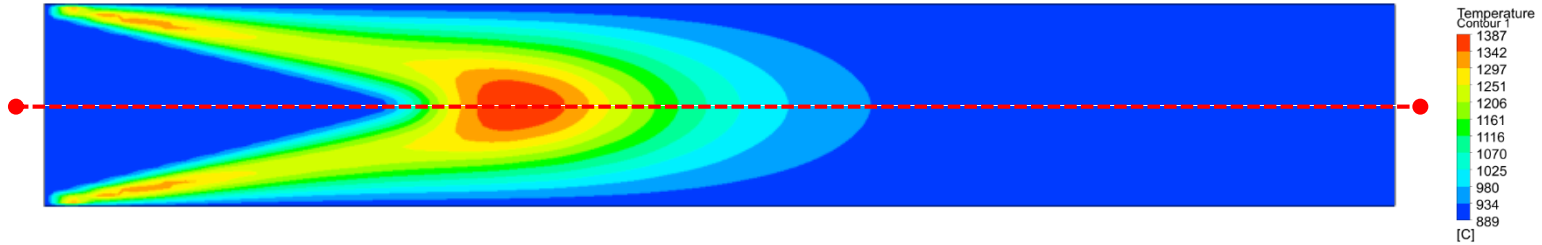


# CFD analysis for sweep side channel

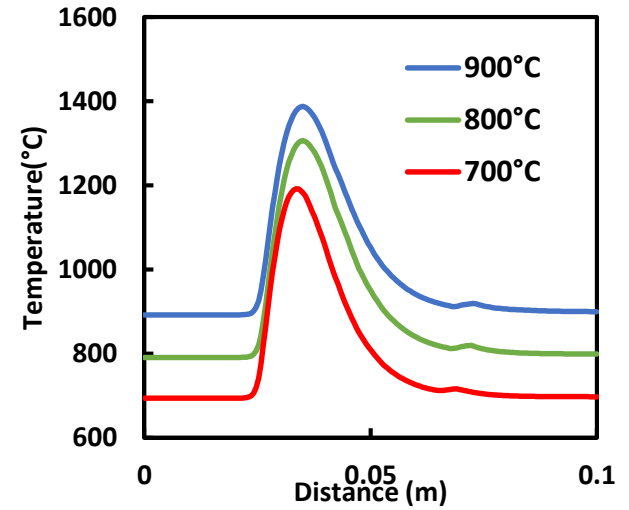
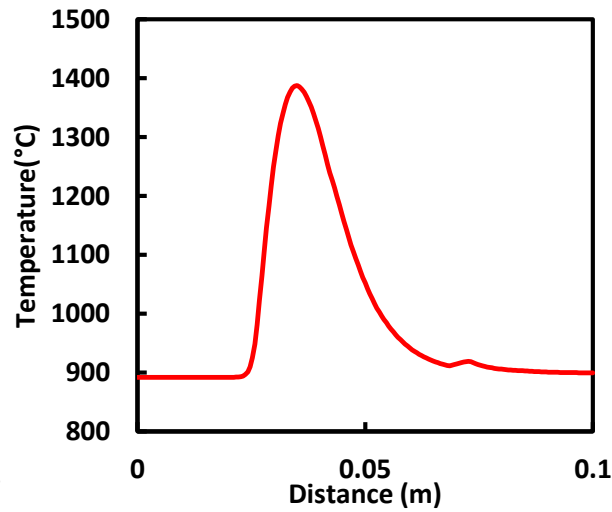


Simplification	2D channel
Solver	ANASYS Fluent
Species reaction model	Non-premixed combustion
Gas Mixture	Methane-air
Inlet	Preheated gas
Outlet	Pressure outlet

# Simulation Results



Base case: 900°C preheated channel and gases



Temperature comparison

# Conclusion and Discussion

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## **Review:**

- ITM technology is a novel approach to separate oxygen from air, which could provide solutions to CCS.
- ITM reactor modeling varies depending on the geometry, materials, flow configuration and whether the model enables reactions.
- ITM reactor is a highly-coupled nonlinear system and an intermediate-fidelity model is introduced.

## **Modeling practice:**

- A monolith reactor was developed enables the oxygen permeation phenomena and fast kinetics reaction
- The simulation shows that the oxygen permeation rate does not decrease much along the reactor
- The 2D sweep channel was simulated for the oxy-combustion process
- The simulated temperature shows the effect of the combustion may not be neglected

# Further Improvement

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- **Monolith reactor:**

1. Enables the temperature variable by adding energy equation
2. Optimize the reactor size

- **CFD modeling**

1. Try different solvers and kinetics databases
2. Revise the definition of boundary conditions

*Thanks!*

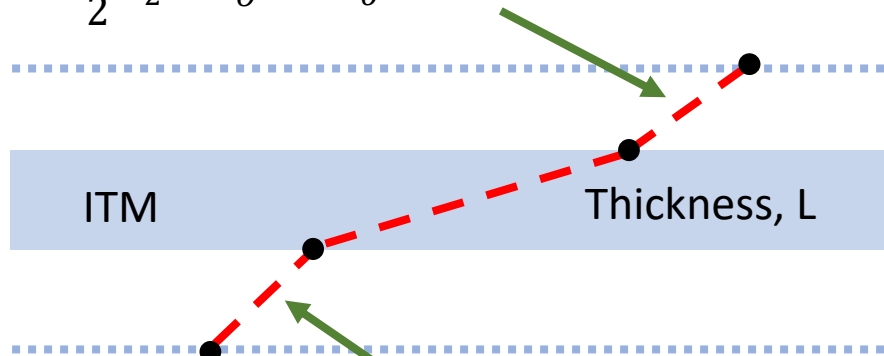
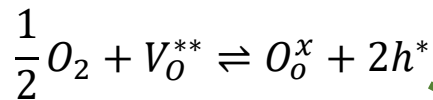


# Backup Slides

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# Resistance-network mechanism

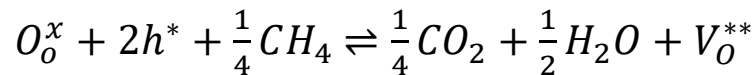
Feed



ITM

Thickness, L

Sweep



$$J_{O_2} = \frac{1}{2} J_V$$

$$J_V = 2 \cdot (k_{f_{O_2}} P'_{O_2}{}^{\frac{1}{2}} C'_V - k_{r_{O_2}})$$

$$J_V = -D_V \frac{C_V}{dy} = D_V \frac{(C''_V - C'_V)}{L}$$

$$J_V = k_{f_{CH_4}} (C_{CH_4})^{\frac{1}{4}} C_{O_0}^x$$

$$C_O = C_{O_0}^x + C_V$$

$$J_V = \frac{C_O - \frac{k_{r_{O_2}}}{k_{f_{O_2}} P'_{O_2}{}^{\frac{1}{2}}}}{\frac{1}{2k_{f_{O_2}} P'_{O_2}{}^{\frac{1}{2}}} + \frac{L}{D_V} + \frac{1}{k_{f_{CH_4}} (C_{CH_4})^{\frac{1}{4}}}}$$